

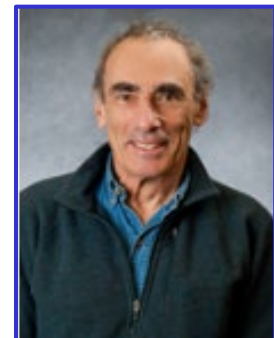
Recent Studies on Relic Neutrinos and Related Topics

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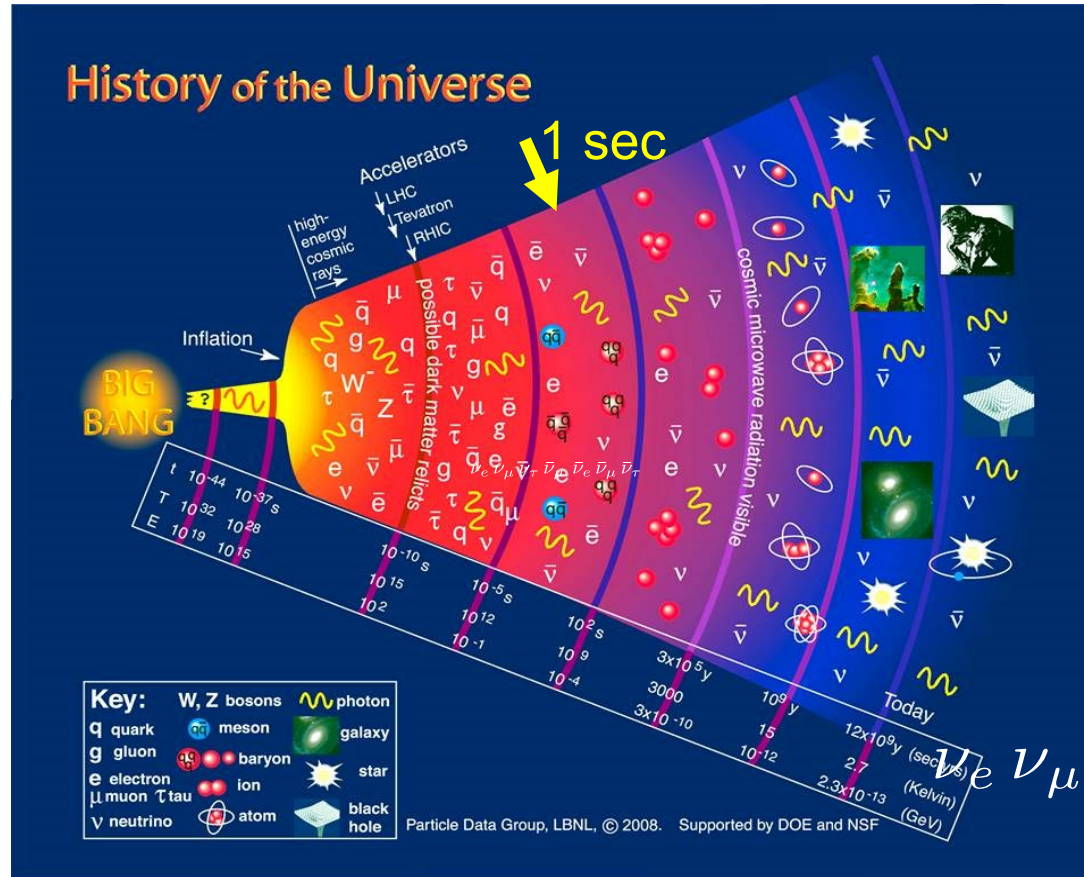
CHiP Annual Meeting
Nov. 20-21, 2024

Based on papers in collaboration
with Gordon Baym

Phys. Rev. Letts. 126, 191803 (2021);
Phys. Rev. D 103, 123019 (2021);
Phys. Rev. D 106, 063018 (2022);
arXiv: 2405.15011 (accepted by PNAS);
arXiv: 2403.02602



Relic neutrinos from the Big Bang forming the cosmic neutrino background (CvB)



Decoupling occurs at $t \sim 1$ sec, $T \sim 1$ MeV

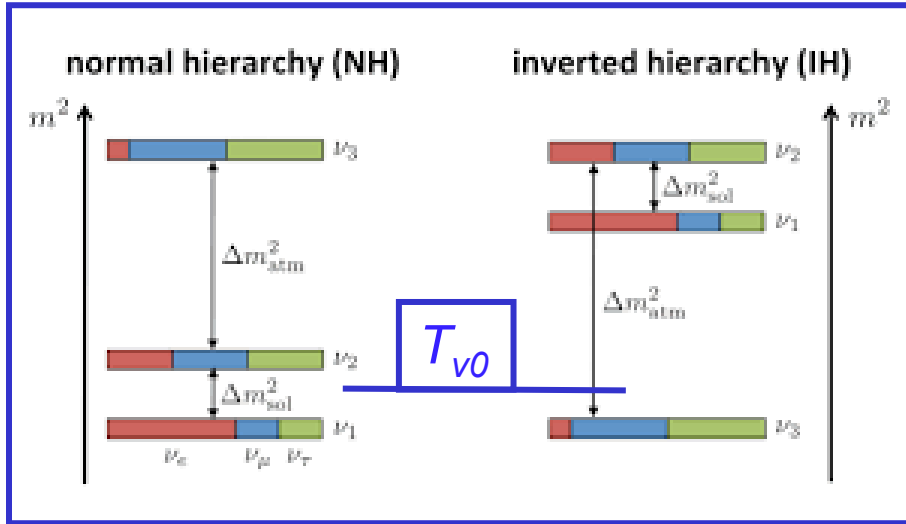
CvB has never been observed !

Cosmic neutrino background (CvB) versus cosmic microwave background (CMB)

| | CMB | CvB | Relation |
|---------------|--------------------------|-------------------------------------|---|
| Temperature | 2.73K | 1.9 K (1.7×10^{-4} eV) | $T_\nu/T_\gamma = (4/11)^{1/3}$ =0.714 |
| Decoupling at | 3.8×10^5 years | ~ 1 sec | |
| Density | $\sim 411 / \text{cm}^3$ | $\sim 336 / \text{cm}^3$ | $n_\nu = (9/11) n_\gamma$ |

- CvB took a snapshot of the Universe at a much earlier epoch than CMB
- At least two of the three neutrinos are non-relativistic
- $\sim 20,000,000$ of CvB inside you at this moment
- Density of CvB is ~ 100 times of solar neutrinos
- Produced as flavor eigenstates, now in mass eigenstates

At least 2 relic neutrino mass states are non-relativistic
 (Current temperature: $T_{\nu 0} = 1.945 \text{ K} = 1.676 \times 10^{-4} \text{ eV}$)



$$\Delta m_{21}^2 = 7.50 \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{31,N}^2 = 2.52 \times 10^{-3} \text{ eV}^2$$

$$\Delta m_{31,I}^2 = -2.51 \times 10^{-3} \text{ eV}^2$$

$$T_{\nu 0} = 1.945 \text{ K} = 1.676 \times 10^{-4} \text{ eV}$$

At least two neutrino masses are larger than 100 K
 with $m_i \gg T_{\nu 0} = 1.945 \text{ K} = 1.676 \times 10^{-4} \text{ eV}$

Normal Hierarchy: If $m_1 = 0$, $\beta_1 = 1$, $\beta_2 \sim 1/50$, $\beta_3 \sim 1/300$

Inverted Hierarchy: If $m_3 = 0$, $\beta_3 = 1$, $\beta_1 \sim \beta_2 \sim 1/300$

How to search for cosmic neutrino background (CvB) ?

Capture of CvB on radioactive nuclei

(S. Weinberg, 1962)

Tritium beta decay:



3-body β -decay with Q -value of

$$Q_a = M(\text{}^3\text{H}) - M(\text{}^3\text{He}) - M(e^-) - M(\bar{\nu}_e)$$

Inverse tritium beta decay (ITBD):

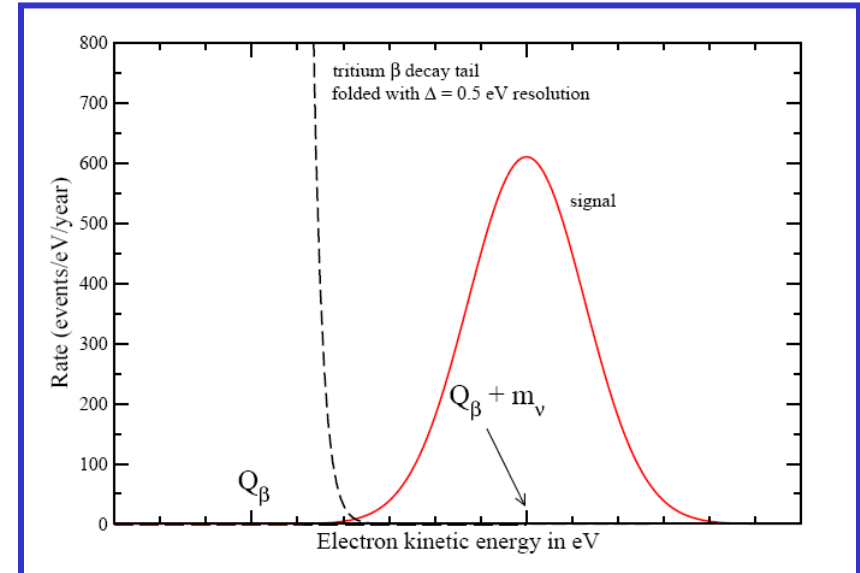


2-body reaction with the Q -value of

$$Q_b = M(\text{}^3\text{H}) - M(\text{}^3\text{He}) - M(e^-) + M(\bar{\nu}_e)$$

Therefore, $Q_b = Q_a + 2M(\bar{\nu}_e)$

Positive Q value implies low-energy relic neutrinos can be captured !



Look for a mono-energetic peak beyond the endpoint of tritium beta decay

PTOLEMY experiment for this search (recent result from Katrin)

Helicity dependence of the ITBD



- ITBD for neutrino in mass eigenstate i and helicity h :

$$\sigma_i^h = \frac{G_F^2}{2\pi v_i} |V_{ud}|^2 |U_{ei}|^2 F(Z, E_e) \frac{m({}^3He)}{m({}^3H)} E_e p_e A_i^h (\bar{f}^2 + 3\bar{g}^2)$$

- The helicity-dependent factor, A_i^h , is given as

$$A_i^\pm = 1 \mp \beta_i; \quad \text{where } \beta_i = v_i / c$$

- For relativistic neutrinos, $\beta_i \rightarrow 1$, we have

$$A_i^+ \rightarrow 0 \quad \text{and} \quad A_i^- \rightarrow 2$$

- For non-relativistic neutrinos, $\beta_i \rightarrow 0$, we have

$$A_i^+ \rightarrow 1 \quad \text{and} \quad A_i^- \rightarrow 1$$

- ITBD rate depends on the helicity, h , of neutrinos

What are the helicities of relic neutrinos?

Helicity versus chirality for massive neutrino (where does the $1 \pm \beta$ factor come from?)

For a Dirac spinor of momentum p along the z -axis with negative helicity ($h = -1$) we have

$$u^-(p) = \begin{pmatrix} 0 \\ \sqrt{E+m} \\ 0 \\ -\sqrt{E-m} \end{pmatrix}; \quad P_R = \frac{1+\gamma^5}{2} = \frac{1}{2} \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{pmatrix}; \quad P_L = \frac{1-\gamma^5}{2} = \frac{1}{2} \begin{pmatrix} 1 & 0 & -1 & 0 \\ 0 & 1 & 0 & -1 \\ -1 & 0 & 1 & 0 \\ 0 & -1 & 0 & 1 \end{pmatrix}$$

$$u^-(p) = u_L^-(p) + u_R^-(p) = P_L u^-(p) + P_R u^-(p)$$

$$u_L^-(p) = \frac{1}{2} \begin{pmatrix} 0 \\ \sqrt{E+m} + \sqrt{E-m} \\ 0 \\ -\sqrt{E+m} - \sqrt{E-m} \end{pmatrix}; \quad u_R^-(p) = \frac{1}{2} \begin{pmatrix} 0 \\ \sqrt{E+m} - \sqrt{E-m} \\ 0 \\ \sqrt{E+m} - \sqrt{E-m} \end{pmatrix}$$

$$R = \frac{\sqrt{E+m} - \sqrt{E-m}}{\sqrt{E+m} + \sqrt{E-m}} = \frac{\sqrt{1-\beta}}{\sqrt{1+\beta}};$$

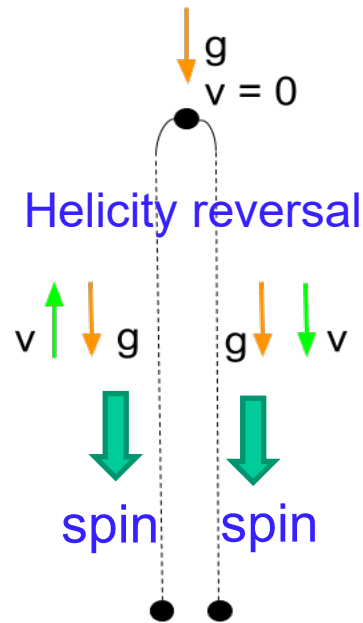
R is the relative amplitude for a negative helicity neutrino to be right-handed

Evolution of relic neutrino helicity

(from $t \sim 1$ sec to $t \sim 13.8$ billion years)

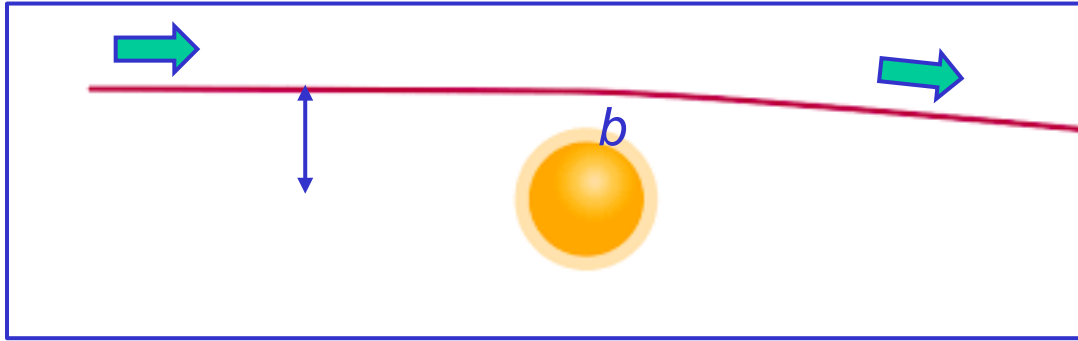
- Relic neutrinos decoupled at a temperature of ~ 1 MeV, and were highly relativistic. Neutrinos were produced essentially in $h = -1$ state, and antineutrinos in $h = +1$ state.
- Rotation of neutrino spin due to transverse matter source is less than the rotation of neutrino momentum (gravitational lensing of neutrino), changing neutrino helicity.
- Dirac neutrino with non-zero magnetic moment will precess in galactic or cosmic magnetic fields, changing neutrino helicity.

How would gravity modify the neutrino helicity?



If a neutrino with negative helicity is emitted upward from the Earth, it could fall back to the Earth having a positive helicity, affecting its weak interaction rate!

How would gravity modify the neutrino helicity?

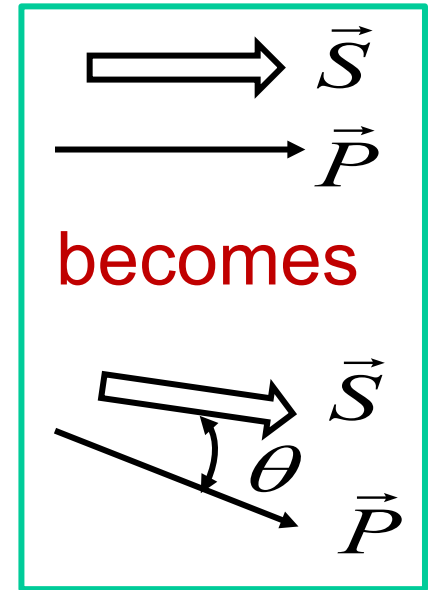


Momentum bending: $\Delta\theta_P = \frac{2MG}{bv^2}(1+v^2)$

Spin bending: $\Delta\theta_S = \frac{2MG}{b} \frac{2\gamma+1}{\gamma+1}; \quad (\gamma = 1/\sqrt{1-v^2})$

$$\theta \equiv \Delta\theta_S - \Delta\theta_P = -\frac{2MG}{b\gamma v^2}$$

(spin bending lags momentum bending)



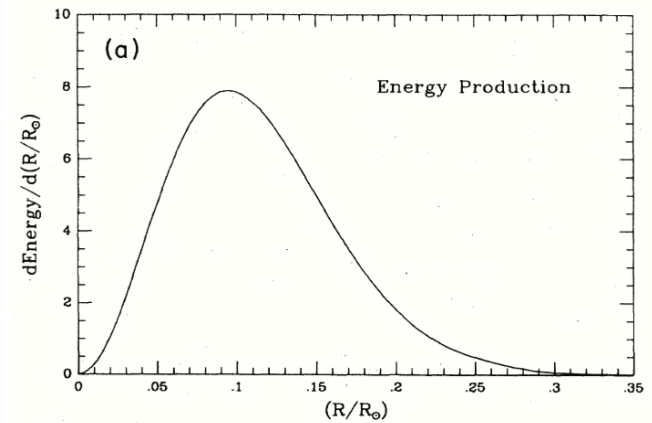
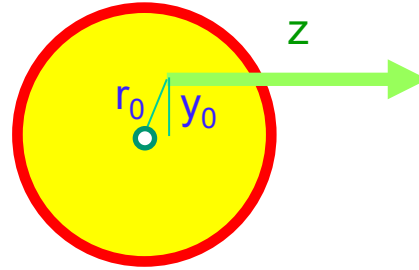
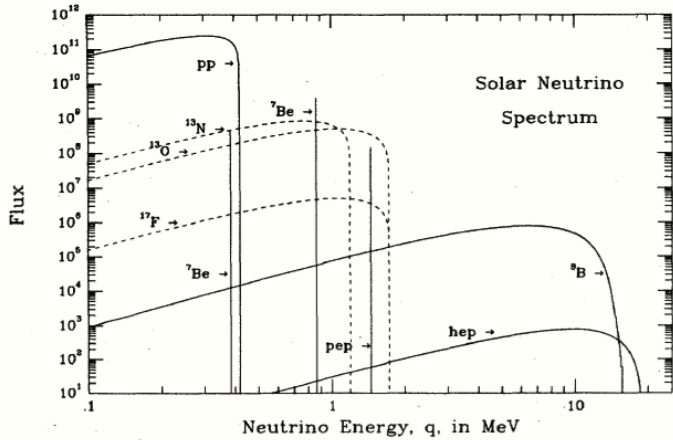
$\theta \rightarrow 0$ as $v \rightarrow 1$
 θ is large as $v \rightarrow 0$

An angle θ between the spin and momentum directions means

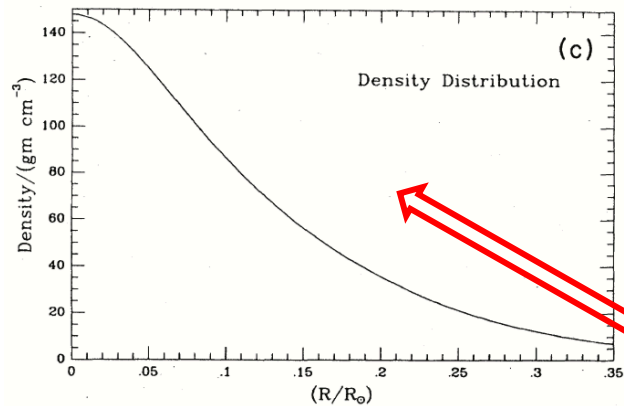
$$|h = +1\rangle \rightarrow \cos(\theta/2)|h = +1\rangle + \sin(\theta/2)|h = -1\rangle$$

Probability for $h = -1$ is $\sin^2(\theta/2)$

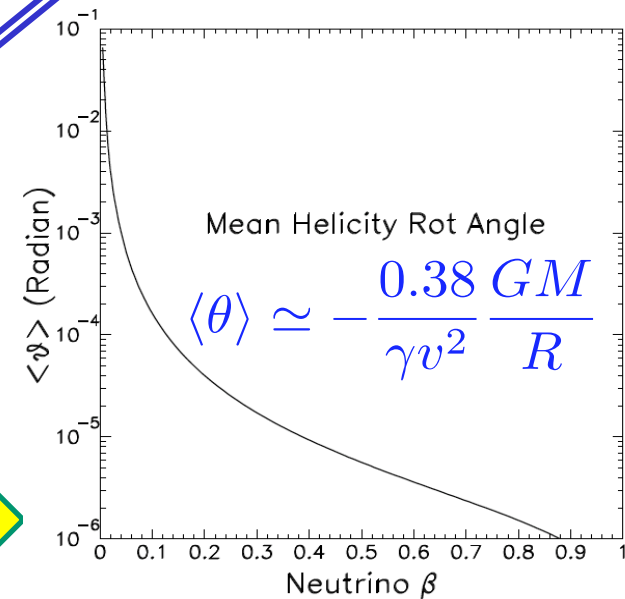
Helicity modification of solar neutrinos by Sun's gravity



$$\theta(y_0, r_0) = -\frac{1}{\gamma v^2} \int_{z_0}^{\infty} dz \frac{GM(r)y_0}{r^3}$$



Averaged over spatial distribution of solar neutrino emission and mass distribution in Sun



Significant helicity modification of heavy particles with spin, e.g., dark photons, from Sun

Neutrino propagation in an expanding universe

Metric of expanding universe with weak gravitational inhomogeneities

$$ds^2 = a(u)^2 \left[-(1 + 2\Phi) du^2 + (\delta_{ij} (1 - 2\Phi) + h_{ij}) dx_i dx_j \right]$$

a = scale factor (a grows from $\sim 10^{-10}$ at $T = 1$ MeV to $a = 1$ now)

u = conformal time; $dt = a du$

x_i = comoving spatial coordinates, h_{ij} = gravitational waves

Φ = weak potential driven by density fluctuations

$$\nabla_x^2 \Phi = 4\pi G (\delta\rho(x) + 3\delta P(x)) a(u)^2$$

Radiation dominated era ($P = \rho / 3$), down to redshift $\sim 10^4$

Matter dominated era ($P(x) \rightarrow 0$) from redshift $\sim 10^4$ to now

Gravitational spin rotation relative to momentum

For massive relic neutrinos, after including matter and dark energy

in $\bar{\rho}(a) = \rho_M / a^3 + \rho_V$:

$$\langle (\Delta\theta_p)^2 \rangle = \frac{9}{8\pi} PH_0^3 \int_0^1 \frac{da}{a^2} (\Omega_M a + \Omega_V a^4)^{3/2} v \left(\frac{1}{v} + v \right)^2$$

$$\langle (\Delta\theta_s)^2 \rangle = \frac{9}{8\pi} PH_0^3 \int_0^1 \frac{da}{a^2} (\Omega_M a + \Omega_V a^4)^{3/2} v^3 \left(\frac{2\gamma + 1}{\gamma + 1} \right)^2$$

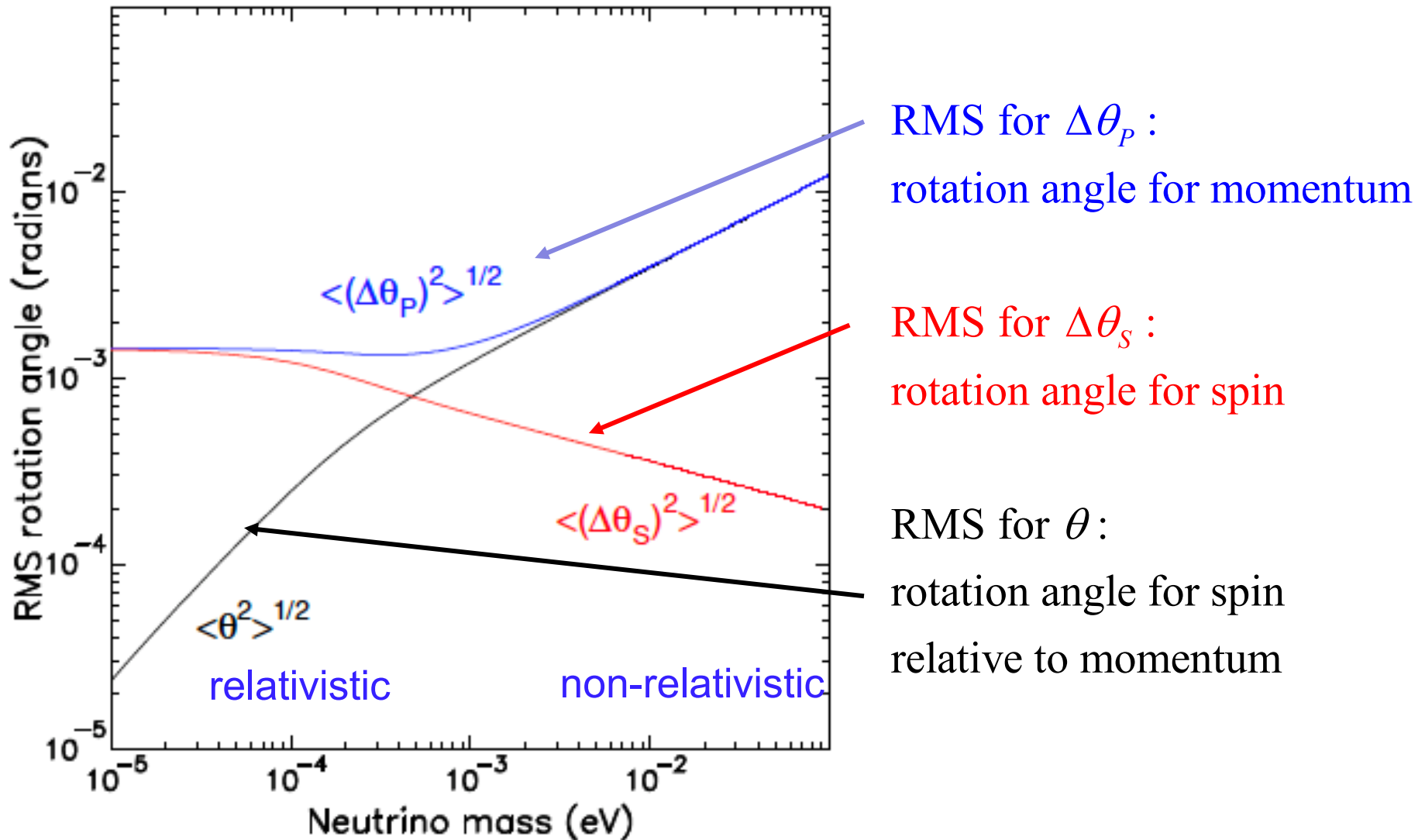
$$\langle \theta^2 \rangle \equiv \langle (\Delta\theta_p)^2 \rangle - \langle (\Delta\theta_s)^2 \rangle = \frac{9}{8\pi} PH_0^3 \int_0^1 \frac{da}{a^2} (\Omega_M a + \Omega_V a^4)^{3/2} \left(\frac{1}{v} - v \right)$$

(where Ω_M = matter fraction, Ω_V = dark energy fraction)

Main effect is from matter dominated era (redshift $\sim 10^4$ to now)

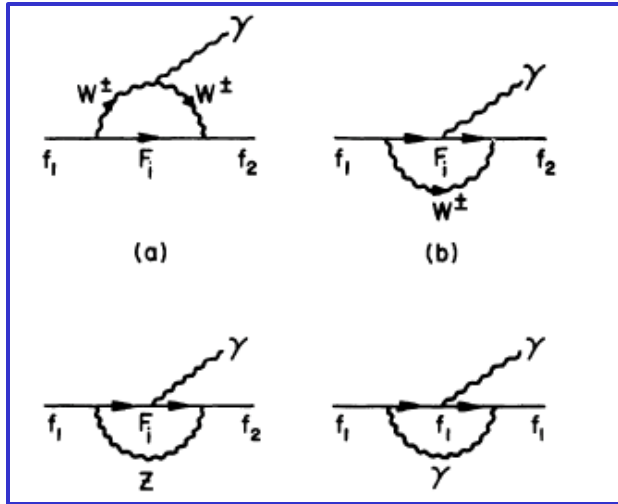
(For detailed derivation, see Baym and Peng, PRD 103 (2021))

Spin rotation relative to momentum rotation due to gravity for relic neutrino mass state (depending on neutrino's mass)



Rotation of neutrino spins in magnetic fields via neutrino magnetic moment

Standard model processes lead to a non-zero neutrino magnetic moment



$$\mu_\nu^{SM} \simeq \frac{3eG_F}{8\sqrt{2}\pi^2} m_\nu \simeq 3 \times 10^{-21} m_{-2} \mu_B$$

Fujikawa-Schrock, *PRL* 1980

μ_B = Bohr magneton = $e / 2m_e$

$$m_{-2} = m_\nu / 10^{-2} \text{ eV}$$

The magnetic moment could be much larger (BSM physics)

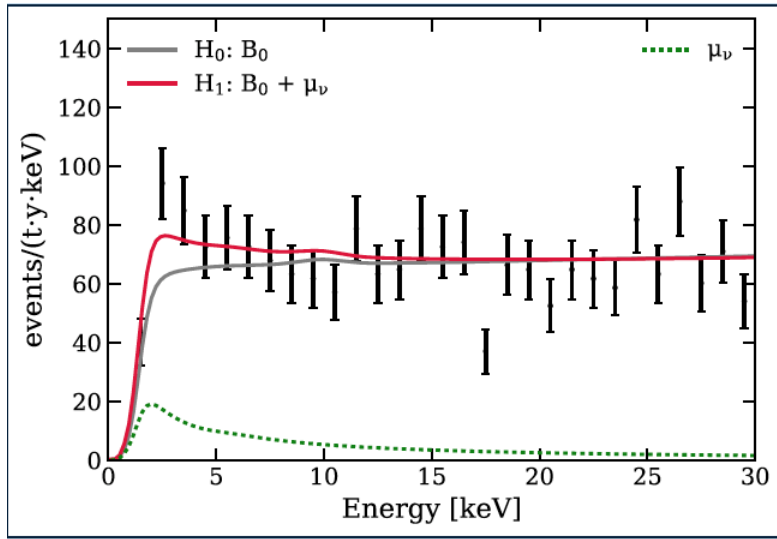
Upper bounds: $\mu_\nu < 2.9 \times 10^{-11} \mu_B$ GEMMA (2010)

$\mu_\nu < 7.4 \times 10^{-11} \mu_B$ TEXONO (2007)

$\mu_\nu < 2.8 \times 10^{-11} \mu_B$ Borexino (2017)

Naturalness upper bound: $\mu_\nu \leq 10^{-16} m_{-2} \mu_B$ Bell et al. *PRL* 2005

XENON1T low energy electron event excess



Excess of low energy electron events
1-7 keV over expected background???

Aprile et al. PR D 102, 072004 (2020)

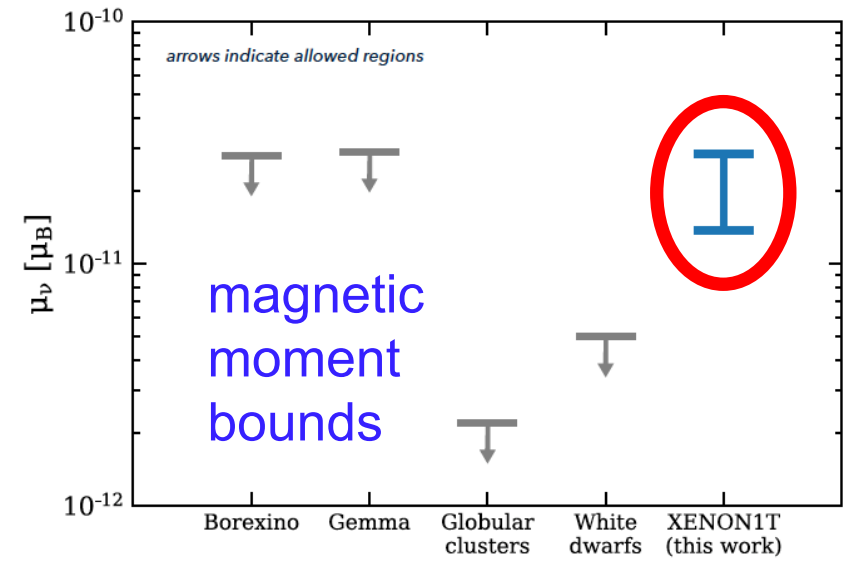
Possible explanations:

- Large neutrino magnetic moment (3.2σ)
- Solar axions (3.5σ)
- Tritium (in Xe) beta decays

Excess consistent with neutrino magnetic moment:

$$\mu_{\nu,1T} \sim 1.4 - 2.9 \times 10^{-11} \mu_B$$

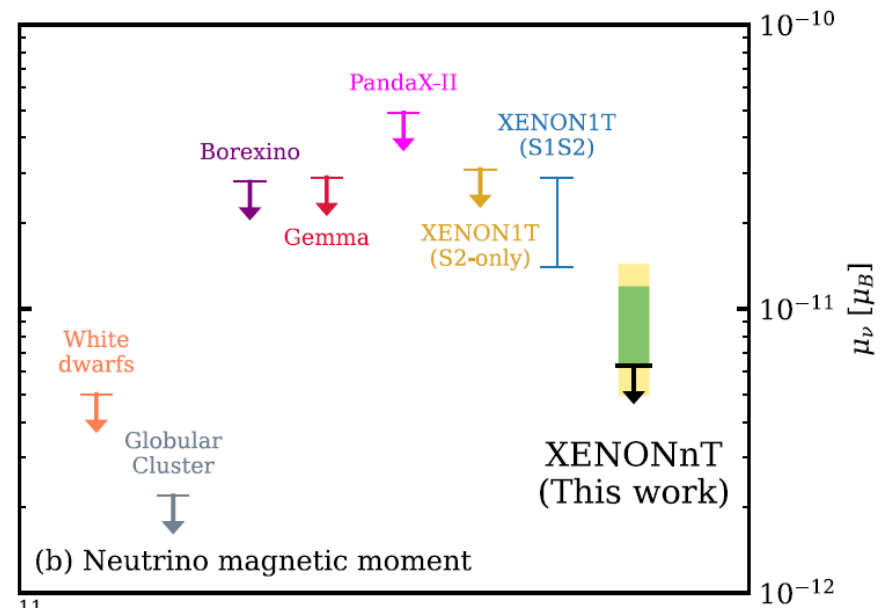
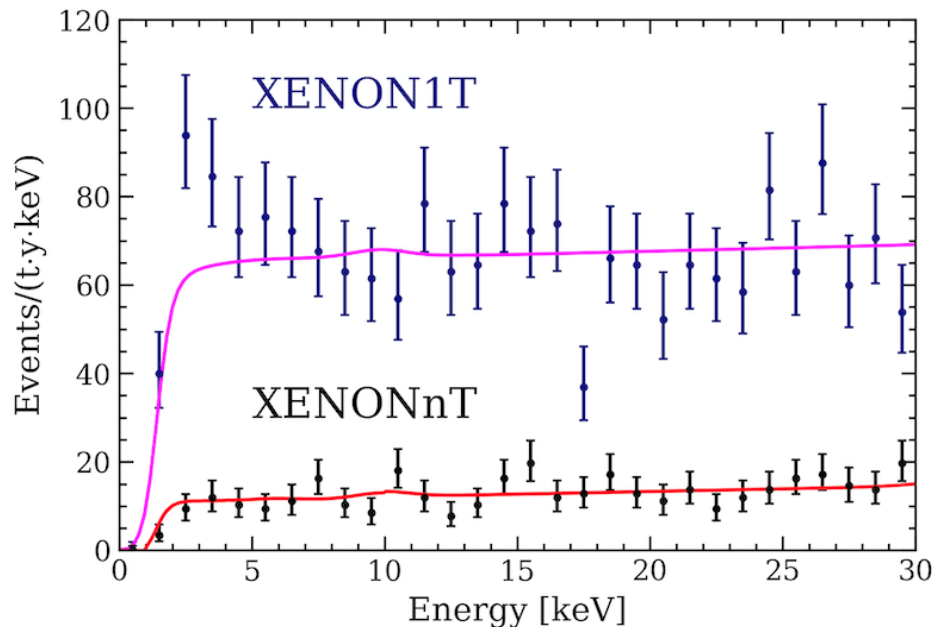
Beyond Standard Model physics??



Excess now tracked to tritium contamination

E. Aprile et al, PRL: 129, 161805 (2022)

XENONnT = 6 tons of Xe



No indication of BSM neutrino magnetic moment

Neutrino's spin precesses in B field, but momentum does not
(neutrinos are electrically neutral)

Magnetic fields change neutrino helicity: $h = \hat{S} \cdot \hat{p}$

Define spin in rest frame of neutrino.

Rest frame precession :

$$\frac{d\vec{S}}{d\tau} = 2\mu_\nu \vec{S} \times \vec{B}_R \quad B_R = \text{magnetic field in rest frame}$$

In terms of "lab" frame magnetic field: $B_{\parallel R} = B_{\parallel}$, $B_{\perp R} = \gamma B_{\perp}$

Bargmann-Michel-Telegdi (BMT) equation of motion:

$$\frac{d\vec{S}_{\perp}}{dt} = 2\mu_\nu \left(\vec{S}_{\parallel} \times \vec{B}_{\perp} + \frac{1}{\gamma} \vec{S}_{\perp} \times \vec{B}_{\parallel} \right)$$

Apply to both galactic and cosmic magnetic fields

Magnetic field lines in M51-Whirlpool Galaxy



SOFIA (on a 747) IR



Stratospheric Observatory for Infrared Astronomy



Neutrino spin rotation by galactic magnetic field

For uniform galactic magnetic field: $\theta_g \sim 2\mu_\nu B_g \frac{l_g}{v}$

l_g = mean crossing distance of the galaxy

Since galactic fields are uniform only over coherence length $\Lambda_g \sim kpc$, spin direction undergoes a random walk in magnetic field

$$\langle \theta^2 \rangle_g \simeq \left(2\mu_\nu B_g \frac{\Lambda_g}{v} \right)^2 \frac{l_g}{\Lambda_g}$$

Milky Way with characteristic parameters:

$$\langle \theta^2 \rangle_{MW} \sim 4 \times 10^{29} m_{-2}^2 \left(\frac{\Lambda_g}{1kpc} \right) \left(\frac{B_g}{10\mu G} \right)^2 \left(\frac{\mu_\nu}{\mu_B} \right)^2$$

$$\mu_\nu \sim 1.5 \times 10^{-15} \mu_B \sim 10^{-4} \mu_{1T} \Rightarrow \sqrt{\langle \theta^2 \rangle} \sim 1 \quad \text{helicity randomizes}$$

Cosmic magnetic field rotation of neutrino spin

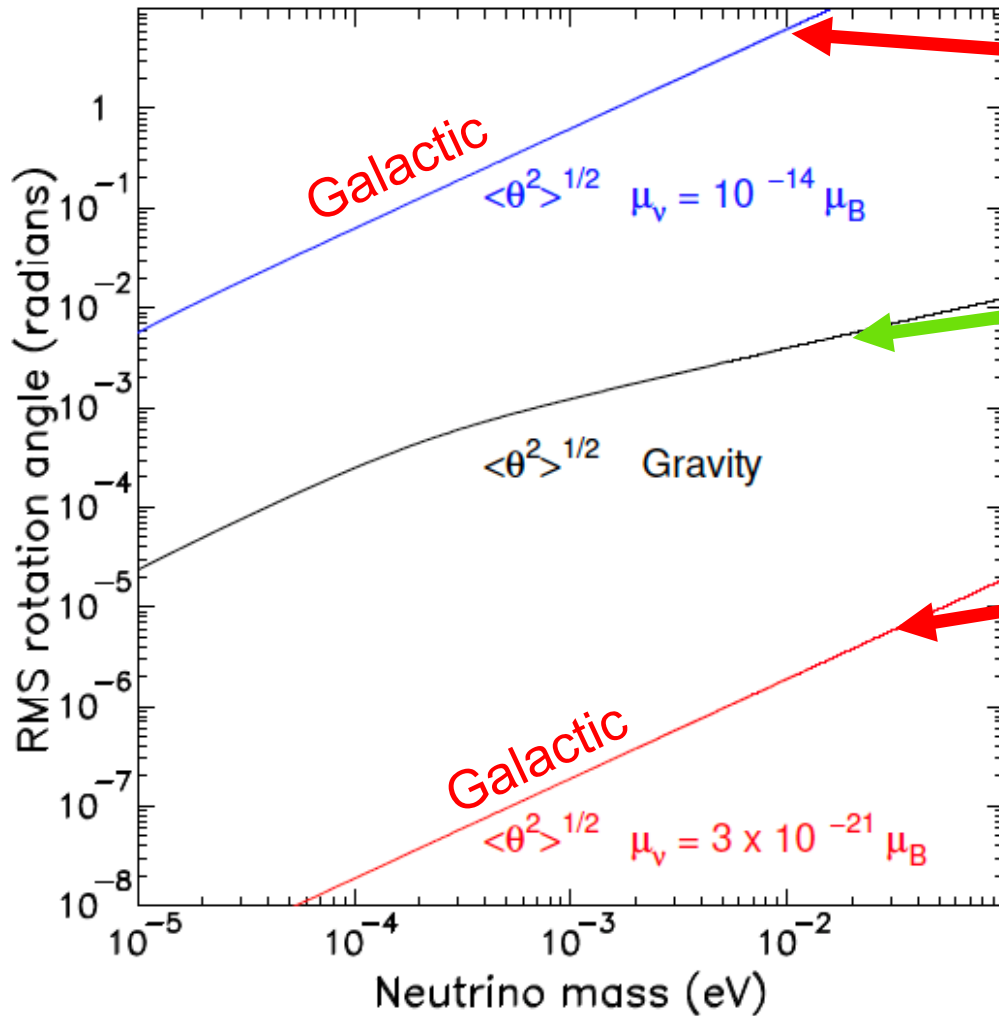
$$\langle \theta^2 \rangle_{\text{Galaxy}} \sim 4 \times 10^{29} m_{-2}^2 \left(\frac{\Lambda_g}{1 \text{ kpc}} \right) \left(\frac{B_g}{10 \mu\text{G}} \right)^2 \left(\frac{\mu_\nu}{\mu_B} \right)^2$$

$$\langle \theta^2 \rangle_{\text{Cosmic}} \sim 2 \times 10^{27} \left(\frac{\Lambda_0}{1 \text{ Mpc}} \right) \left(\frac{B_0}{10^{-12} \text{ G}} \right)^2 \left(\frac{\mu_\nu}{\mu_B} \right)^2$$

Λ_0 = coherence length of cosmic magnetic field

To within uncertainties in magnetic fields, coherence lengths, and neutrino masses, spin rotation in cosmic magnetic fields \sim galactic fields

Spin rotation from gravitational vs. magnetic fields



Rotation in Milky Way with magnetic moment ~ 100 times smaller than current upper limit

Gravitational rotation *GB+JCP PRD*

Rotation in Milky Way with standard model magnetic moment

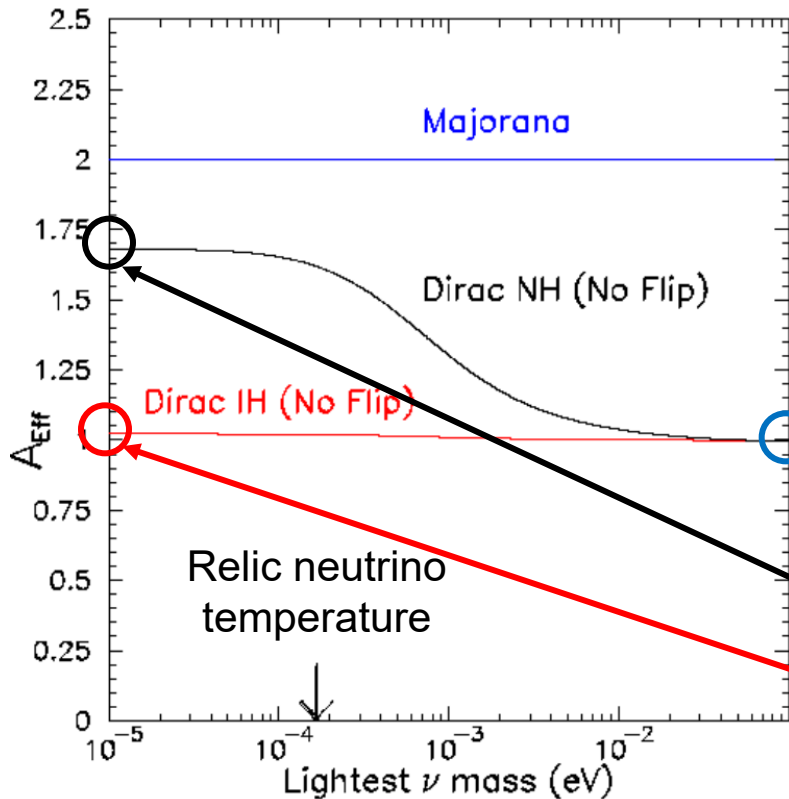
ITBD rate for Dirac neutrinos without helicity flip

- For Majorana type, both neutrinos and antineutrinos contribute

$$A_{eff,M} = (1 + \sum_i |U_{ei}|^2 \langle \beta_i \cos \theta_i \rangle_T) + (1 - \sum_i |U_{ei}|^2 \langle \beta_i \cos \theta_i \rangle_T) = 2$$

- For Dirac type, only neutrinos (not antineutrinos) contribute

$$A_{eff,D} = \sum_{i,h=\pm} |U_{ei}|^2 \langle A_i^h \rangle_T = 1 + \sum_i |U_{ei}|^2 \langle \beta_i \cos \theta_i \rangle_T$$



- For Dirac neutrinos without helicity flip ($\cos \theta_i = 1$)

$$A_{eff,D} = 1 + \sum_i |U_{ei}|^2 \langle \beta_i \rangle_T$$

- If all neutrinos are non-relativistic, $\beta_i \rightarrow 0$, then

$$A_{eff,D} = 1$$

- If the lightest neutrino is relativistic, then

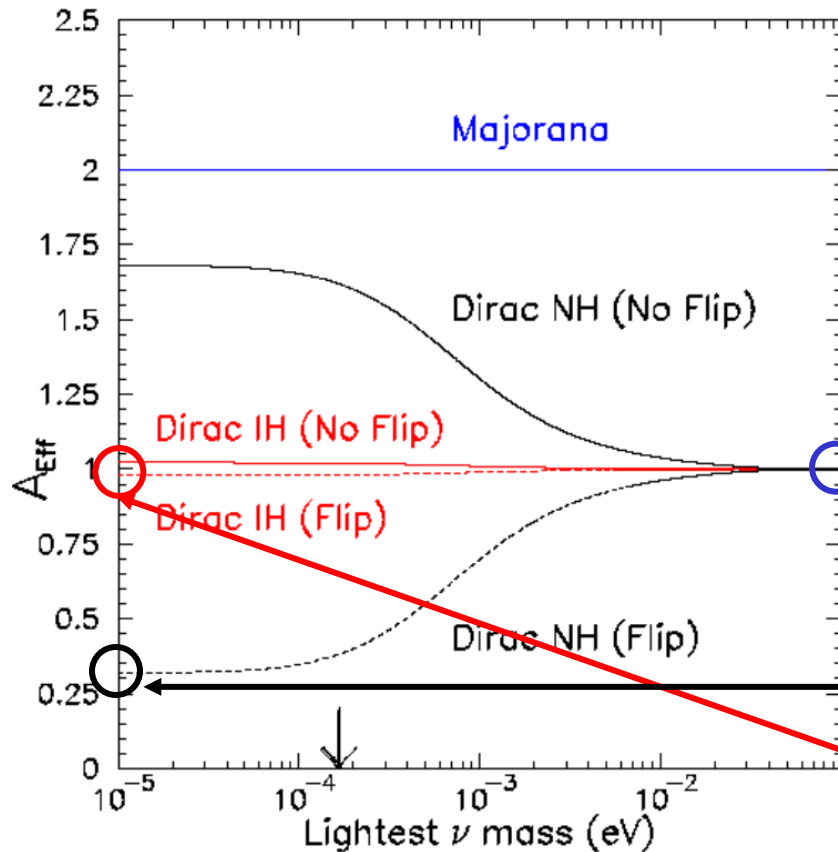
$$A_{eff,D} = 1 + |U_{e1}|^2 = 1.68 \quad \text{for normal mass hierarchy}$$

$$A_{eff,D} = 1 + |U_{e3}|^2 = 1.02 \quad \text{for inverted mass hierarchy}$$

ITBD rate for Dirac neutrinos with helicity flip

- For Dirac type, only neutrinos (not antineutrinos) contribute

$$A_{eff,D} = \sum_{i,h=\pm} |U_{ei}|^2 \langle A_i^h \rangle_T = 1 + \sum_i |U_{ei}|^2 \langle \beta_i \cos \theta_i \rangle_T$$



- Dirac neutrinos with helicity flip ($\cos \theta_i = -1$)

$$A_{eff,D} = 1 - \sum_i |U_{ei}|^2 \langle \beta_i \rangle_T$$

- If all neutrinos are non-relativistic, $\beta_i \rightarrow 0$,

$$A_{eff,D} = 1$$

- If the lightest neutrino is relativistic,

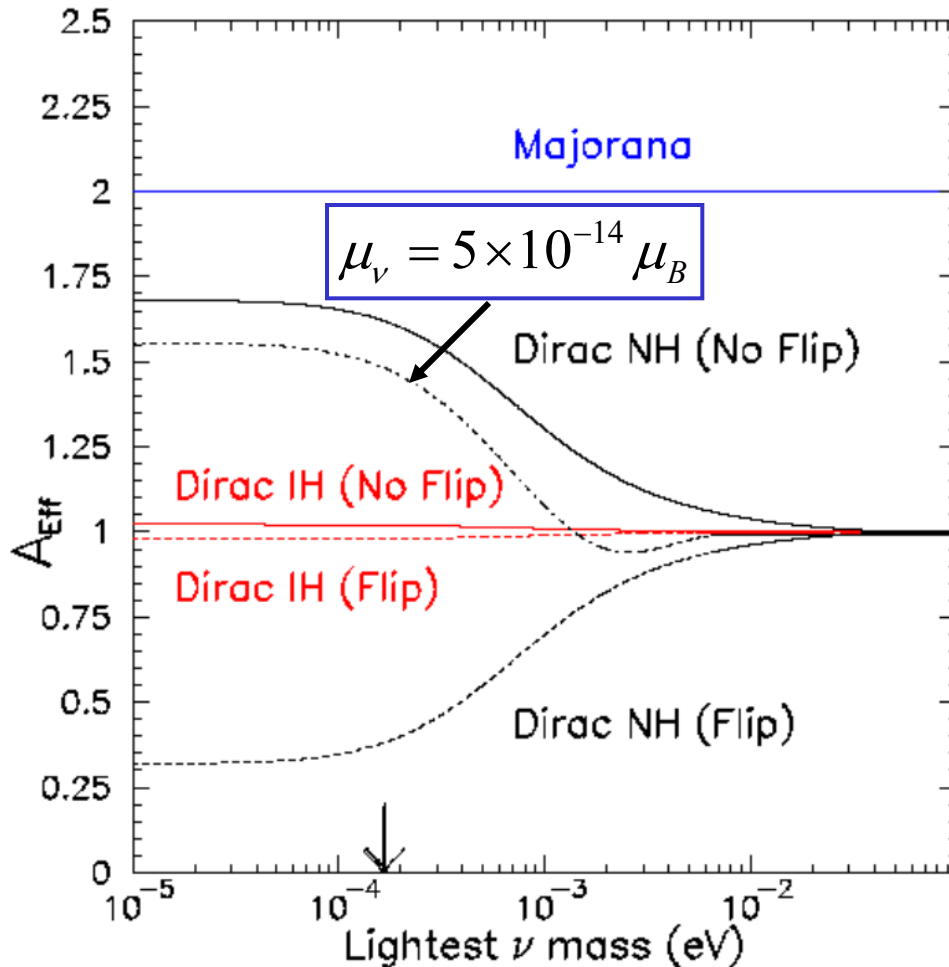
$$A_{eff,D} = 1 - |U_{e1}|^2 = 0.32 \quad \text{normal hierarchy}$$

$$A_{eff,D} = 1 - |U_{e3}|^2 = 0.98 \quad \text{inverted hierarchy}$$

ITBD rate for Dirac neutrinos with partial helicity flip

- For Dirac type, only neutrinos (not antineutrinos) contribute

$$A_{eff,D} = \sum_{i,h=\pm} |U_{ei}|^2 \langle A_i^h \rangle_T = 1 + \sum_i |U_{ei}|^2 \langle \beta_i \cos \theta_i \rangle_T$$



- For Dirac with NH, ITBD rate is modified even with a modest

$$\mu_\nu \text{ of } 5 \times 10^{-14} \mu_B$$

- For Dirac with IH $A_{eff,D} \approx 1$ insensitive to μ_ν

- For Majorana neutrinos

$$A_{eff,M} = 2, \text{ independent of } \mu_\nu$$

Baym and Peng, PRL 126, 191803 (2021)

The ITBD has never been observed yet !

To detect the ITBD, use known sources of electron neutrinos

Peng and Baym, PRD 106, 063018 (2022)

Solar Neutrinos and ^{51}Cr sources



| Experiment | Isotope | Strength | Production Process |
|------------|------------------|-----------|--|
| GALLEX [3] | ^{51}Cr | 1.69 MCi | Thermal neutron capture on ^{50}Cr |
| SAGE [2] | ^{51}Cr | 0.517 MCi | Epithermal neutron capture on ^{50}Cr |
| GALLEX [1] | ^{51}Cr | 1.87 MCi | Thermal neutron capture on ^{50}Cr |
| SAGE [4] | ^{37}Ar | 0.409 MCi | Fast neutron $^{40}\text{Ca}(n, \alpha)^{37}\text{Ar}$ |
| BEST [5] | ^{51}Cr | 3.4 MCi | Thermal neutron capture on ^{50}Cr |

Table 1: Mega-Curie-scale electron capture neutrino sources that have been produced.

Coloma et al. (Snowmass 2020)

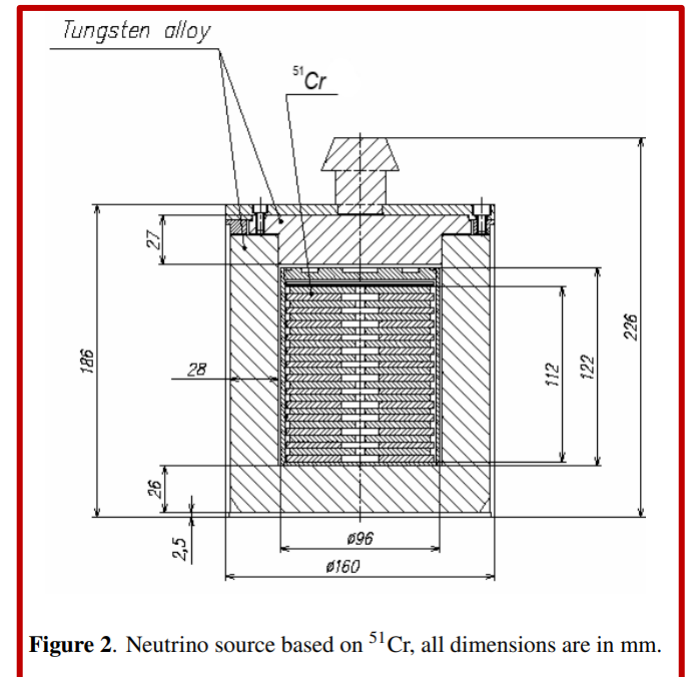
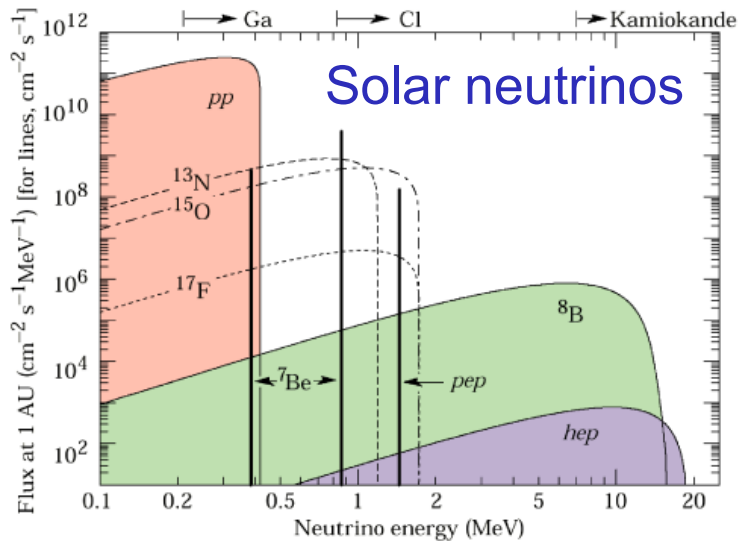


Figure 2. Neutrino source based on ^{51}Cr , all dimensions are in mm.

3.4 MCi ^{51}Cr source for the experiment
BEST

Expected ITBD rates from various sources

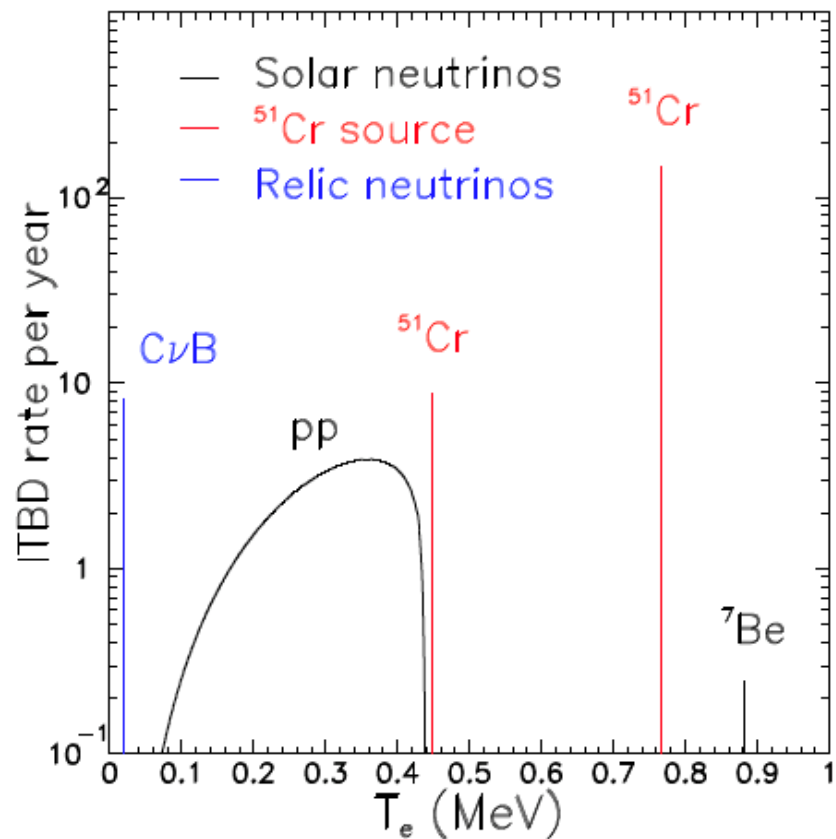
Assuming a 100 g tritium target

Peng and Baym, PRD 106, 063018 (2022)

3.0-MCi ^{51}Cr at 50 cm away
from 100 g tritium target

TABLE I. ITBD rate for various sources of electron neutrinos, together with the electron kinetic energies, T_e . The relic neutrinos are assumed to be Majorana in the rate calculation.

| Source | T_e (MeV) | Rate (1/year) |
|--|----------------|---------------|
| ^{51}Cr 0.427 + 0.432 MeV ν_e | 0.447 | 8.8 |
| ^{51}Cr 0.747 + 0.752 MeV ν_e | 0.767 | 147.0 |
| Solar pp ν_e | 0.0186 to 0.44 | 0.8 |
| Solar ^7Be ν_e | 0.881 | 0.23 |
| Relic $\nu_e/\bar{\nu}_e$ | 0.018 | 8.2 |



Conclusion

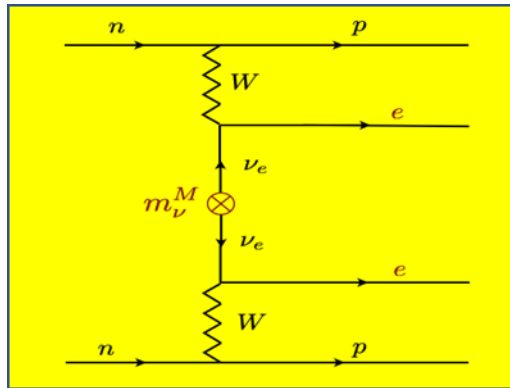
- Relic neutrino helicities could be modified by gravity and magnetic fields
- Detection rate of relic neutrinos via the ITBD reaction is sensitive to the Dirac/Majorana nature of neutrino, and to the lightest mass of neutrinos and the mass hierarchy
- For Dirac neutrino with normal hierarchy, the ITBD rate also depends on neutrino helicity, which is sensitive to neutrino magnetic moment
- Detection of relic neutrinos can reveal fundamental properties of neutrinos and the Early Universe

Macroscopic neutrinoless double beta decay: long range quantum coherence

Gordon Baym and Jen-Chieh Peng

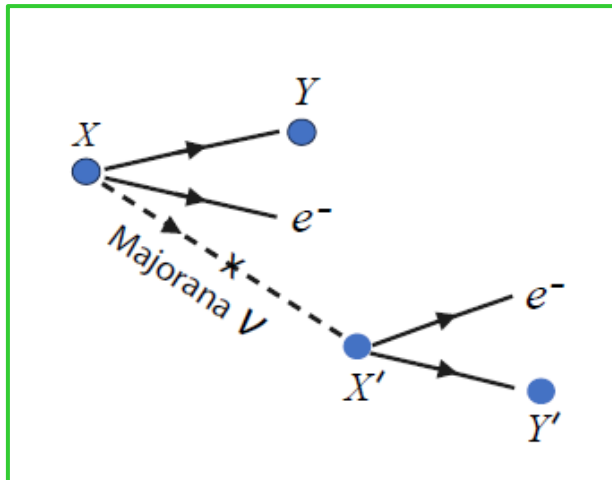
Illinois Center for Advanced Studies of the Universe

and Department of Physics, University of Illinois, 1110 W. Green Street, Urbana, IL 61801



0νDBD (neutrinoless
double-beta decay)

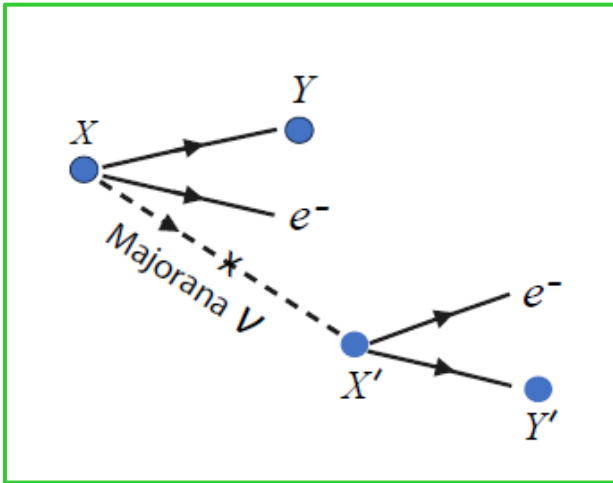
$$(A, Z) \rightarrow (A, Z + 2) + e^{-} + e^{-}.$$



MDBD (macroscopic
double-beta decay)

$$X + X' \rightarrow Y + Y' + e^{-} + e^{-},$$

Consider tritium beta decay followed by inverse tritium beta decay



MDBD (macroscopic double-beta decay)

Similarities and differences of 0νDBD and MDBD

0νDBD:

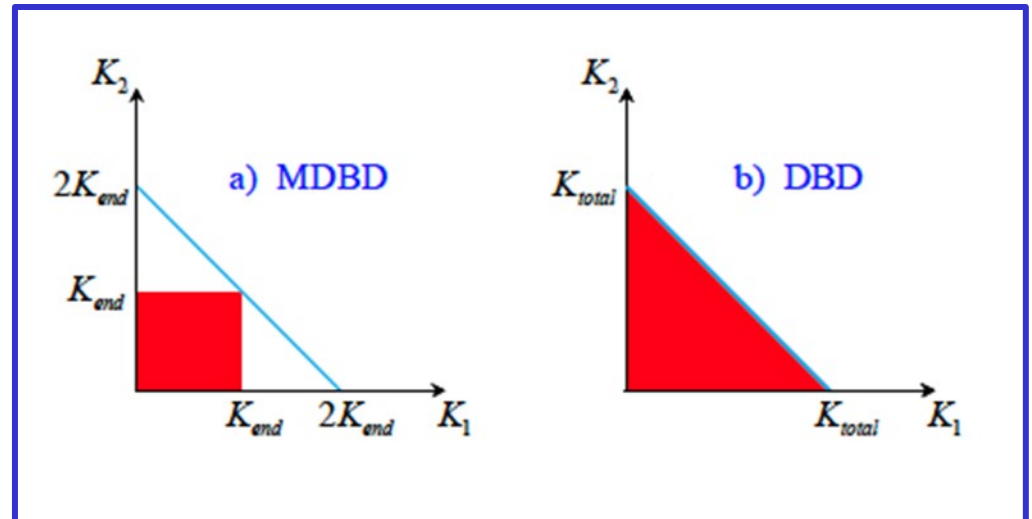
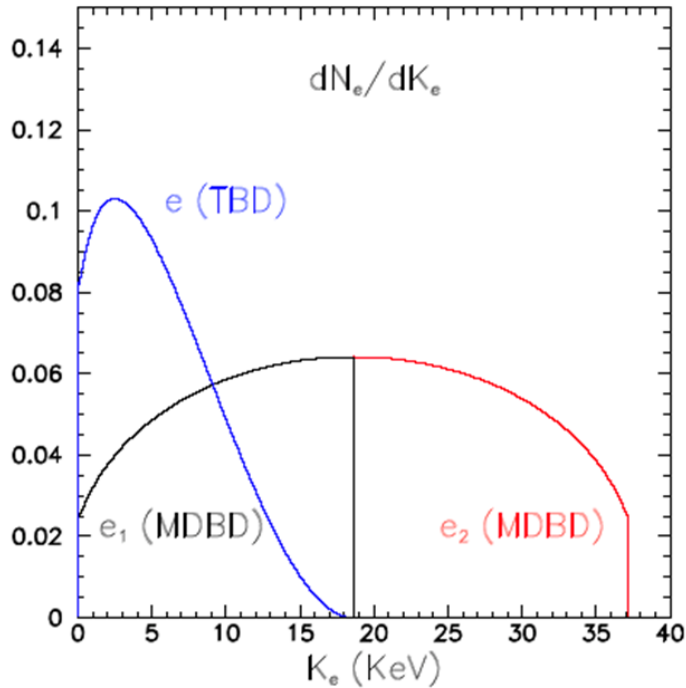
- Only limited number of nuclei are candidates.
- Large uncertainty in matrix elements for the process, since can have, in addition to Majorana neutrinos. beyond-standard=model exchanges:
RH weak currents, exchange of heavy neutrinos, or supersymmetric particles.
- Independent of source geometry.

MDBD:

- All beta unstable nuclei are candidates (leads to large radioactivity though).
- Matrix elements for beta decay and inverse beta decay are well known.
- Only Majorana neutrino can give rise to process, since exchanged neutrino propagates as a real particle and thus requires energy conservation.
- Depends on geometry of source. Rate $\sim N^{4/3}$.

Both processes involve quantum coherence between different neutrino mass eigenstates. In MDBD have coherence over macroscopic distances!

Consider tritium beta decay followed by inverse tritium beta decay



Comparison with ongoing 0νDBD experiments

⁷⁶Ge: Majorana, GERDA

¹³⁶Xe: KamLAND-Zen, XENONnT, EXO

¹³⁰Te: CUORE

⁸²Se: CUPID, NEMO

¹⁰⁰Mo: CUPID-Mo

No 0νDBD events have been positively identified!! Only upper bounds.

Yields for 100 g of source per year

| Nucleus | $T_{1/2}$ for $\bar{m} = 0.1$ eV | Yield per 100 g-yr |
|-----------------------------------|--|---|
| ³ H (MDBD) | – | 2.3×10^{-7} |
| <i>n</i> (MDBD) | – | 3.4×10^{-2} |
| ¹¹ C (MDBD) | – | 5.1×10^{-5} |
| ⁷⁶ Ge (0νDBD) [18, 19] | $3.7 \times 10^{25} < T_{1/2} < 2.0 \times 10^{26}$ yr | $2.7 \times 10^{-3} < Y < 1.5 \times 10^{-2}$ |
| ¹³⁶ Xe (0νDBD) [20–22] | $0.1 \times 10^{26} < T_{1/2} < 1.8 \times 10^{26}$ yr | $1.7 \times 10^{-3} < Y < 3.0 \times 10^{-2}$ |
| ¹³⁰ Te (0νDBD) [23] | $5.9 \times 10^{24} < T_{1/2} < 6.7 \times 10^{25}$ yr | $4.7 \times 10^{-3} < Y < 5.4 \times 10^{-2}$ |
| ⁸² Se (0νDBD) [24, 25] | $1.0 \times 10^{25} < T_{1/2} < 7.5 \times 10^{25}$ yr | $6.8 \times 10^{-3} < Y < 4.8 \times 10^{-2}$ |
| ¹⁰⁰ Mo (0νDBD) [26] | $4.7 \times 10^{24} < T_{1/2} < 1.4 \times 10^{25}$ yr | $2.9 \times 10^{-2} < Y < 8.8 \times 10^{-2}$ |

MDBD is not now a practical alternative to 0νDBD single nucleus experiments

谢谢

Thank You!