An Overview of the GPD Program at COMPASS

TIDC Annual Meeting 2024

November 22, 2024

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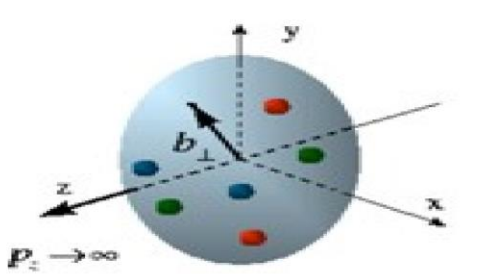
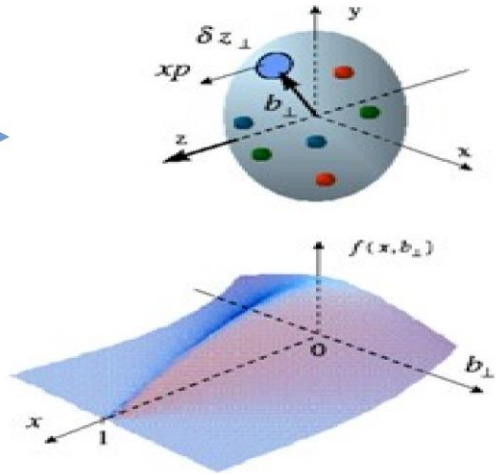
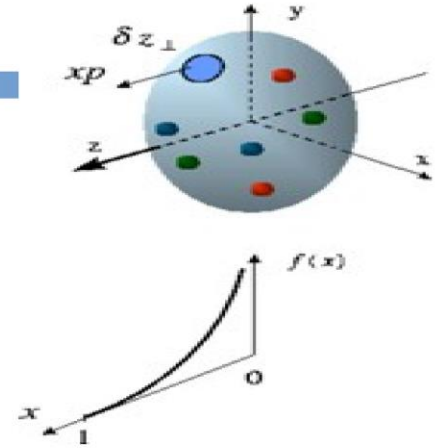
Beyond 1-D Picture of Nucleon



- **F**orm **F**actors **(FFs)**
  - ✔ Spatial distribution
  - ✗ Momentum distribution



- **G**eneralized **P**arton **D**istributions **(GPDs)**
  - ✔ Spatial distribution
  - ✔ Longitudinal momentum distribution

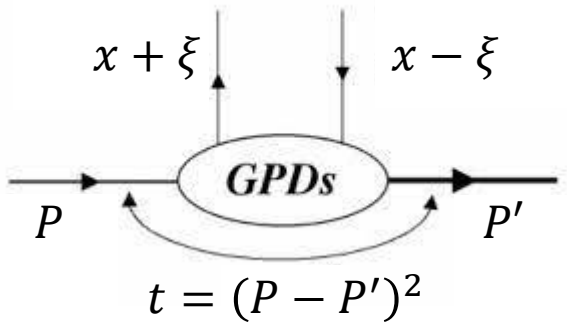


- **P**arton **D**istribution **F**unctions **(PDFs)**
  - ✔ Longitudinal momentum distribution
  - ✗ Spatial distribution

GPDs

- **Correlates the transverse position to the longitudinal momentum of the partons and thus provides a 3-D information of the nucleon.**

Generalized Parton Distributions (GPDs)

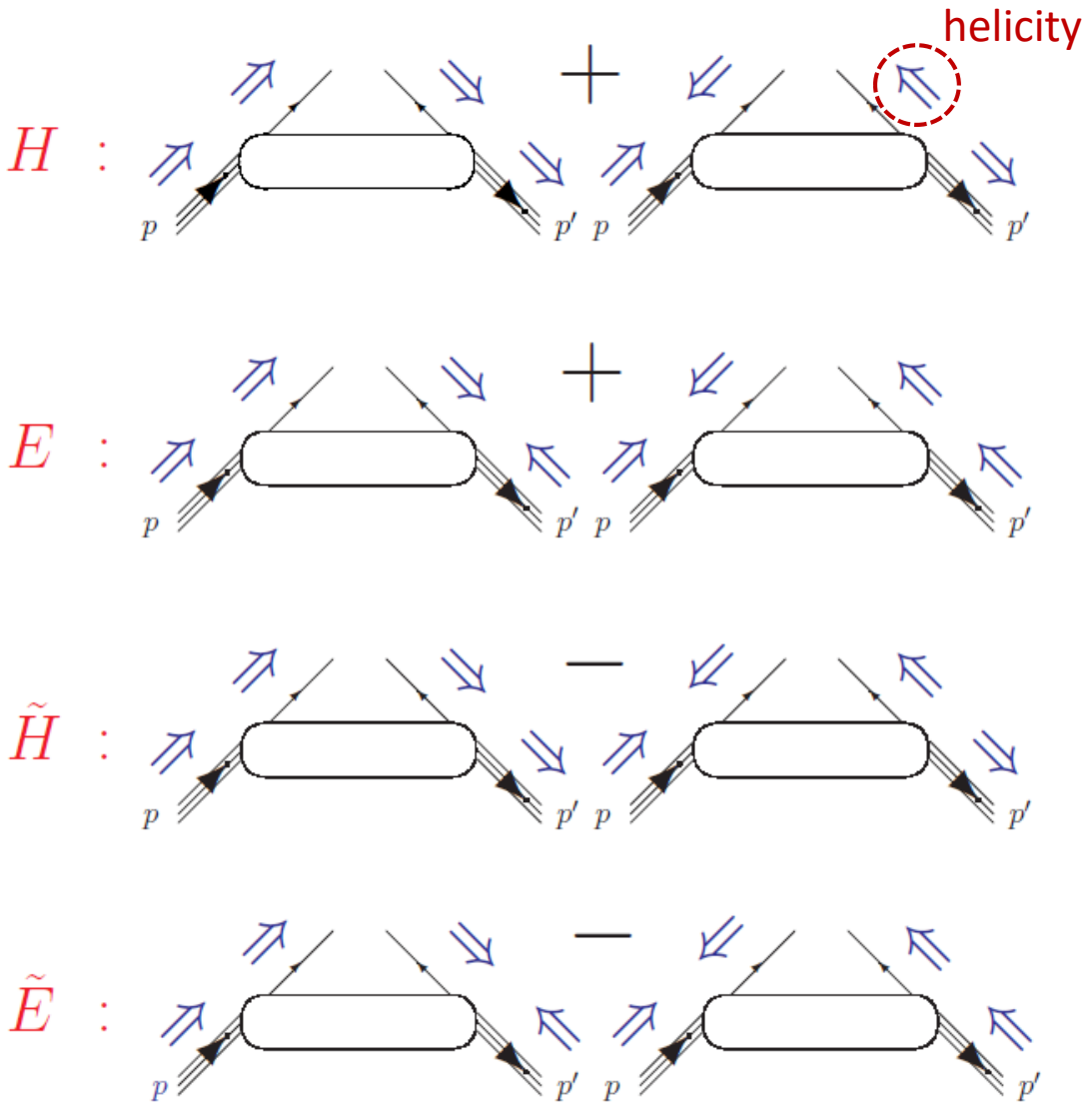


- At fixed Q^2, the GPDs depend on the following variables:
  - x: average longitudinal momentum fraction
  - ξ: longitudinal momentum difference
  - t: four momentum transfer (correlated to $b_\perp$ via Fourier transform)

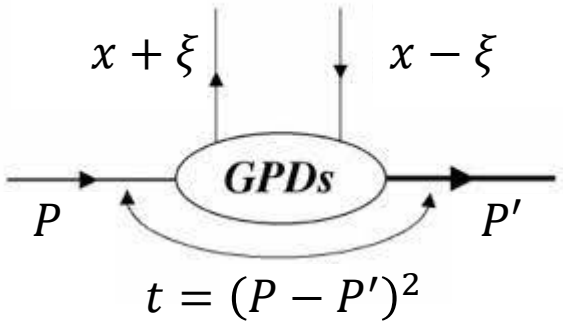
- A total of 8 GPDs for a specific parton

4 Chiral-even (parton helicity unchanged): $H, E, \tilde{H}, \tilde{E}$

4 Chiral-odd (parton helicity changed): $H_T, E_T, \tilde{H}_T, \tilde{E}_T$



Generalized Parton Distributions (GPDs)



Unpolarized

$H_f(x,0,0) = q_f(x)$

$\tilde{H}_f(x,0,0) = \Delta q_f(x)$

Polarized

$\xi = t = 0$ ← PDFs

First Moment → Form Factors

$\int H_f(x,\xi,t)dx = F_1^f(t)$ *Dirac FF*

$\int E_f(x,\xi,t)dx = F_2^f(t)$ *Pauli FF*

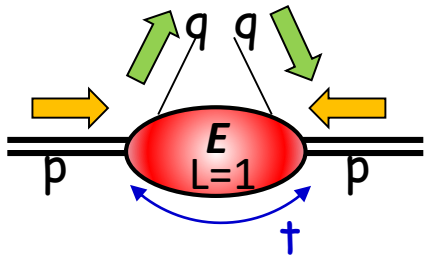
➢ **GPDs embody both PDFs and FFs**

Provides information on the interesting properties of the nucleon.

➢ **Mapping the transverse plane distribution of parton**

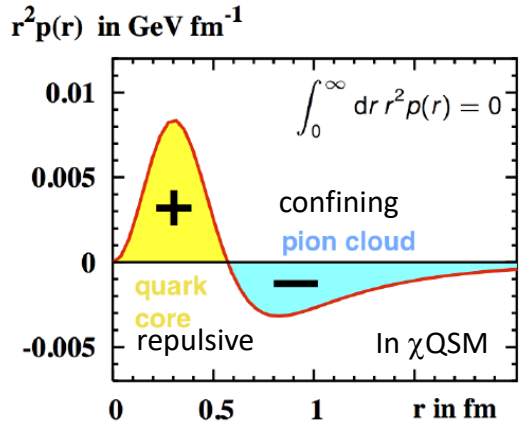
➢ **Pressure distribution inside nucleon**

➢ **Angular momentum of parton**



$$J_q = \frac{1}{2}\int_{-1}^{1} dx\, x[H^q(x,\xi,0) + E^q(x,\xi,0)]$$

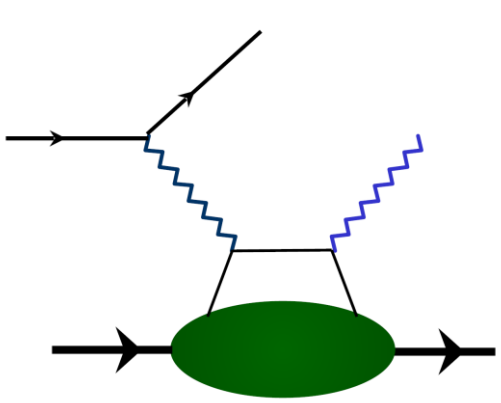
Ji's Sum Rule



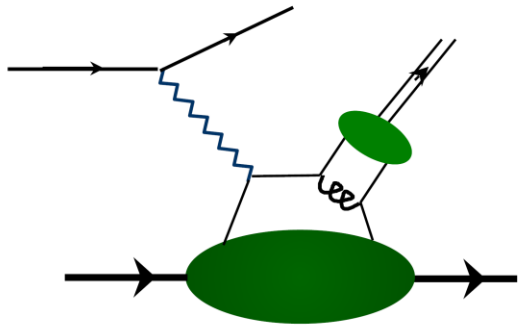
M. Polyakov, P. Schweitzer, Int.J.Mod.Phys. A33 (2018)

Exclusive Process

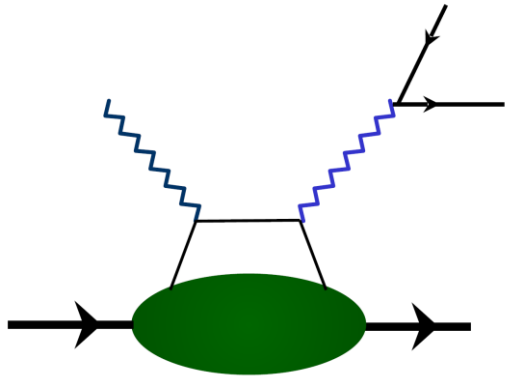
- Use exclusive processes, where all final state particles are “detected”, to access the muliti-variable dependence of GPDs, and constrain the GPD parameterization with measurements in various phase space.
- Processes:
  - Deeply Virtual Compton Scattering (DVCS)
  - Deeply Virtual Meson Production (DVMP)
  - Time-like Compton Scattering (TCS)
  - Double DVCS (DDVCS)
  - …



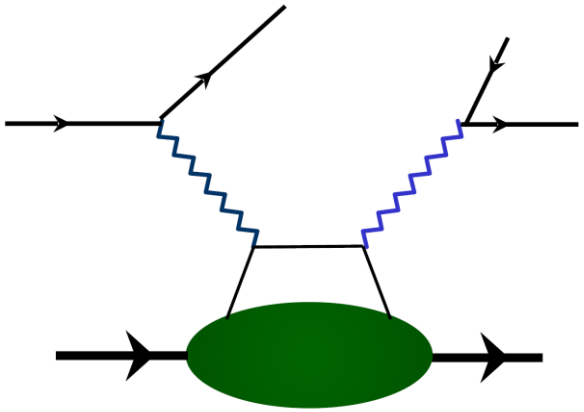
DVCS



DVMP



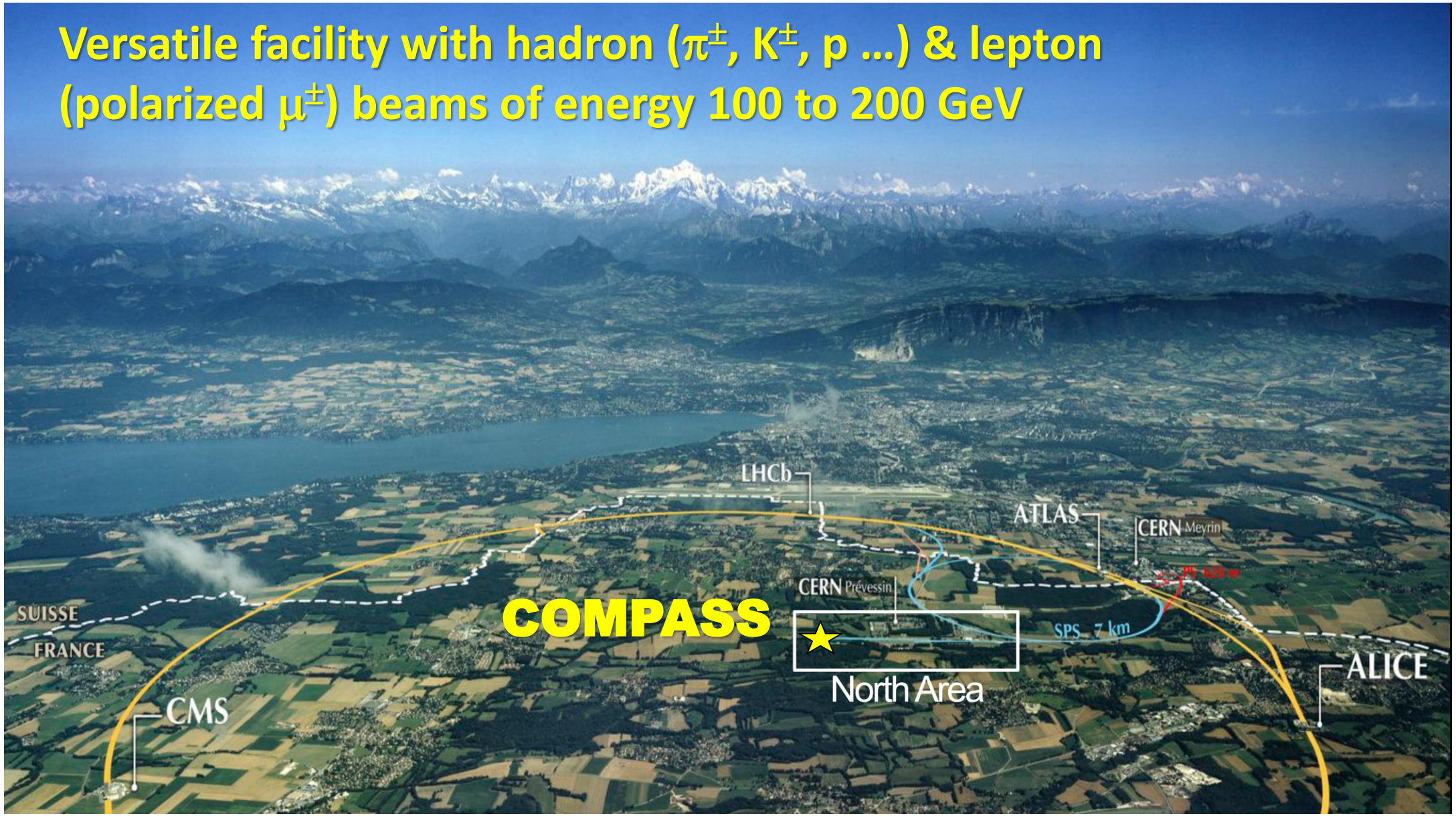
TCS



DDVCS

COMPASS Experiment

Versatile facility with hadron ($\pi^{\pm}$, $K^{\pm}$, p …) & lepton (polarized $\mu^{\pm}$) beams of energy 100 to 200 GeV

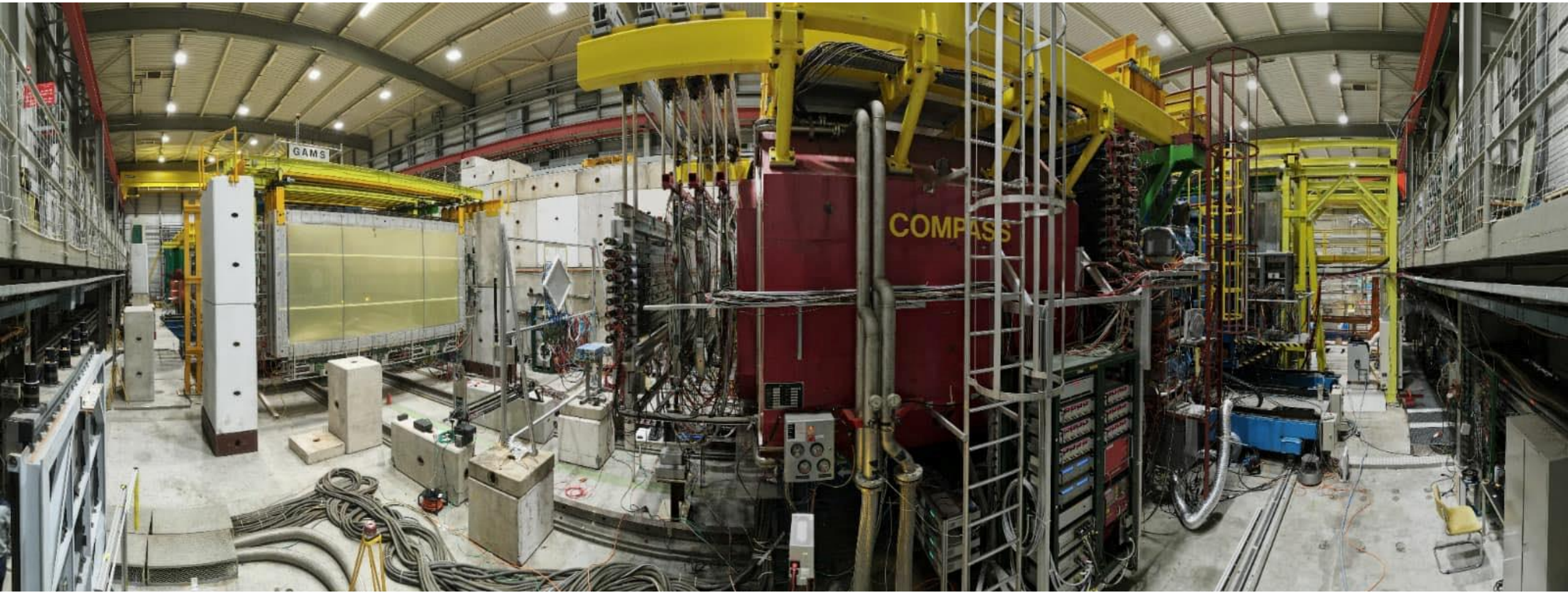


COmmon Muon and Proton Apparatus for Structure and Spectroscopy

COMPASS Experiment

~250 physicists from 24 Institutes of 13 Countries

COMPASS Experimental Setup



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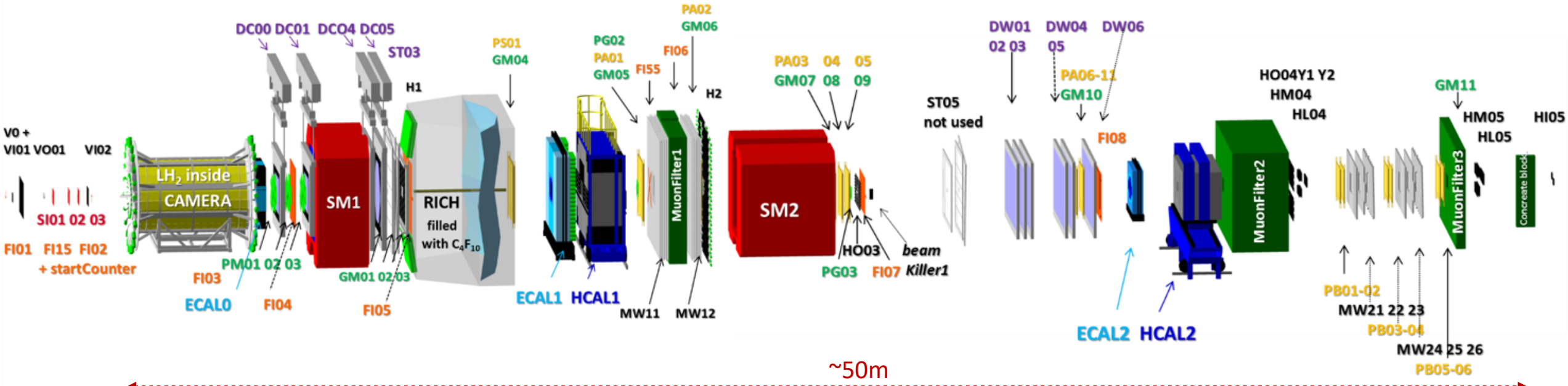


- Priamary beam – 400 GeV p from SPS
  - Impinging on Be production target
- 190 GeV secondary hadron beams
  - h^- beam: $97\%\ \pi^-, 2\%\ K^-, 1\%\ p$
  - h^+ beam: $75\%\ \pi^+, 24\%\ p, 1\%\ K^+$
- 160 GeV tertiary muon beams
  - $\mu^\pm$ longitudinally polarized

Large-acceptance forward spectrometer

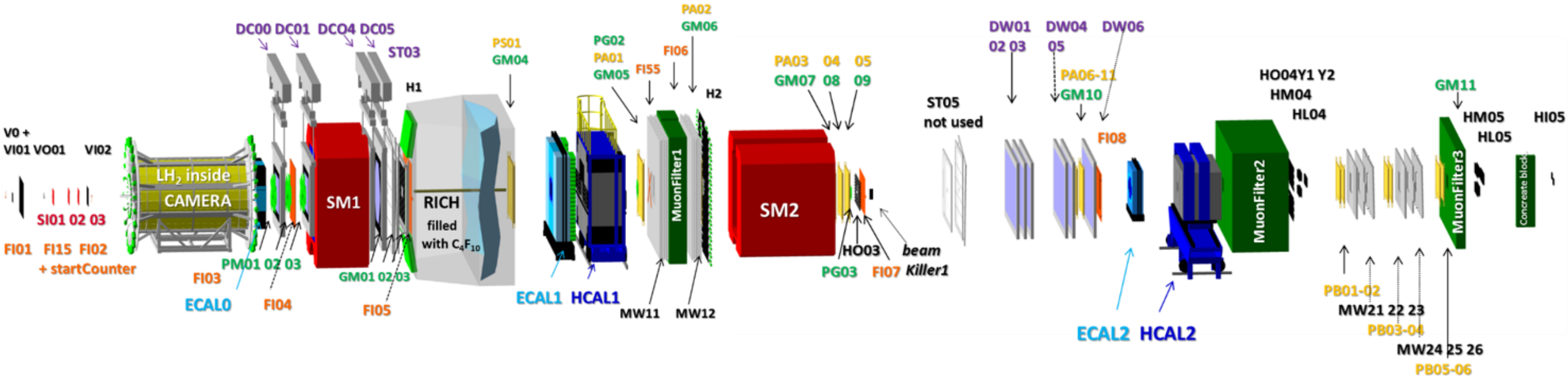
- Precise tracking (350 planes)
  SciFi, Silicon, MicroMegas, GEM, MWPC, DC, straw
- PID – CEDARs, RICH, calorimeters, Muon Walls

Various targets:

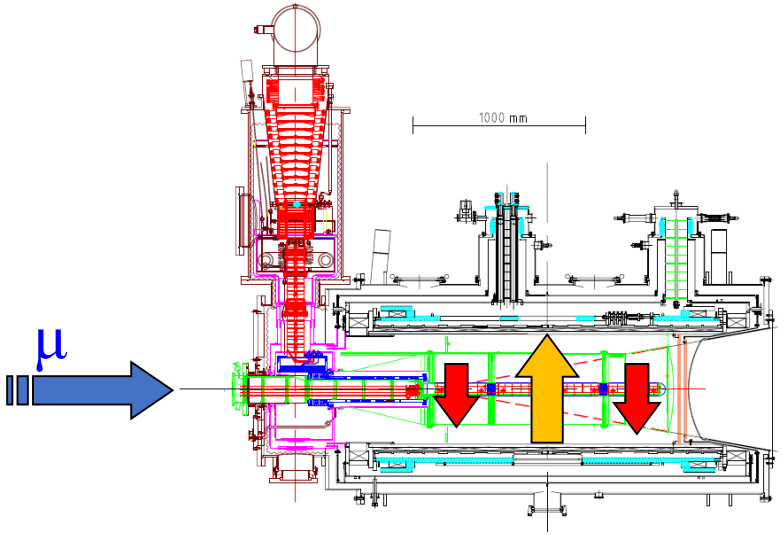
- Polarized soild-state NH_3 or ^6LiD
- Liquid H_2
- Solid-state nuclear targets

❖ NIM A 577 (2007) & NIM A 779 (2015) 69

COMPASS Experimental Setup

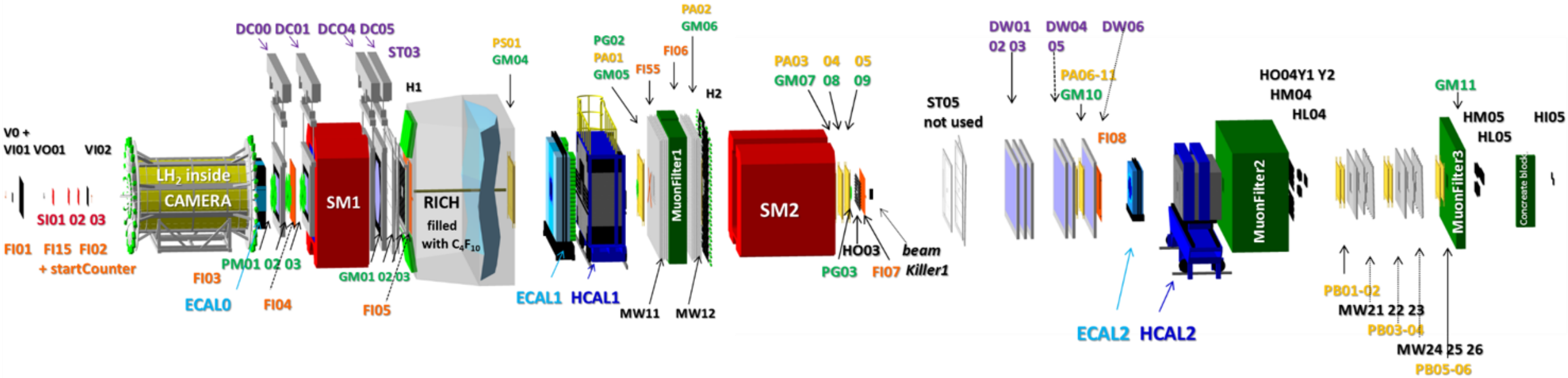


- Priamary beam – 400 GeV p from SPS
  - Impinging on Be production target
- 190 GeV secondary hadron beams
  - h^- beam: 97% π^-, 2% K^-, 1% p
  - h^+ beam: 75% π^+, 24% p, 1% K^+
- 160 GeV tertiary muon beams
  - $\mu^\pm$ longitudinally polarized



- In early GPD studies, transversely polarized target was used.
- Polarization reversal by magnetic field rotation
- 2.5m unpolarized LH_2 target used in GPD dedicated runs

COMPASS Setup for Exclusive Processes



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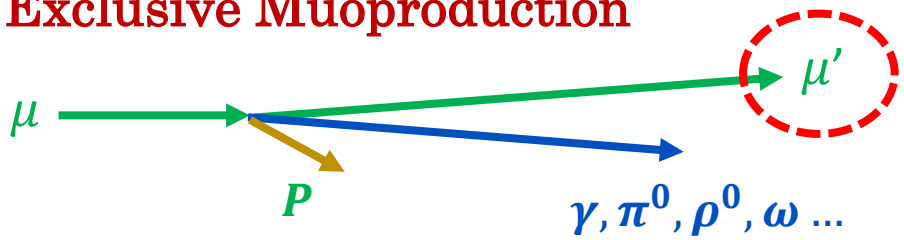
Exclusive Muoproduction



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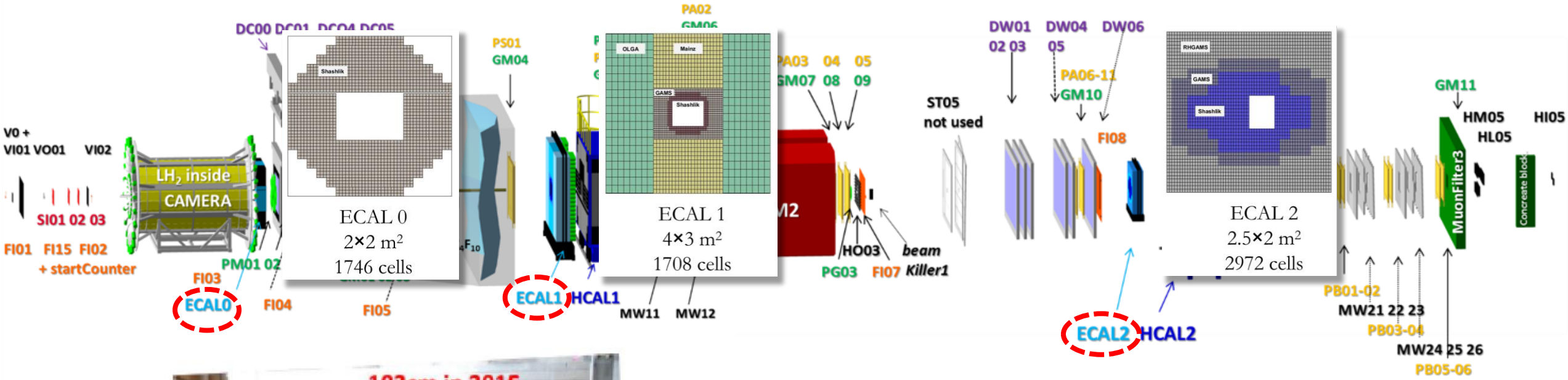

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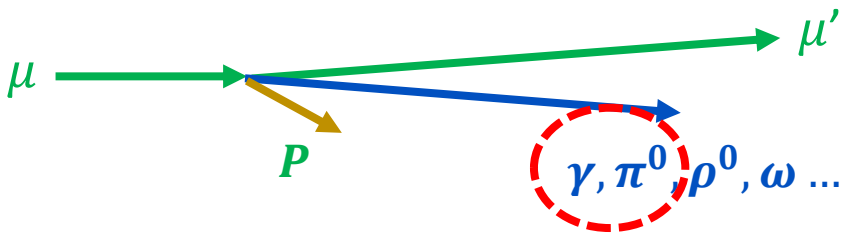

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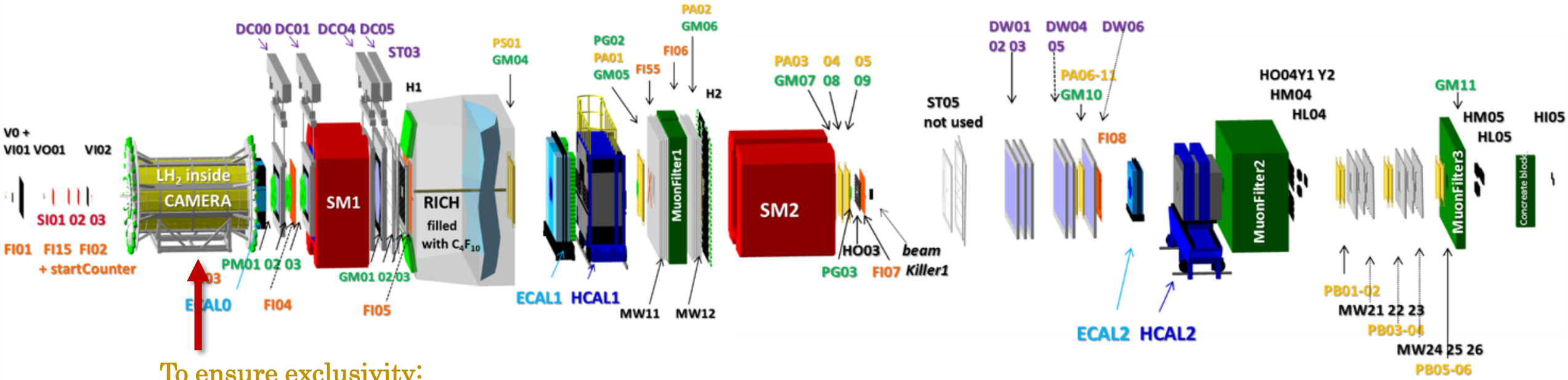
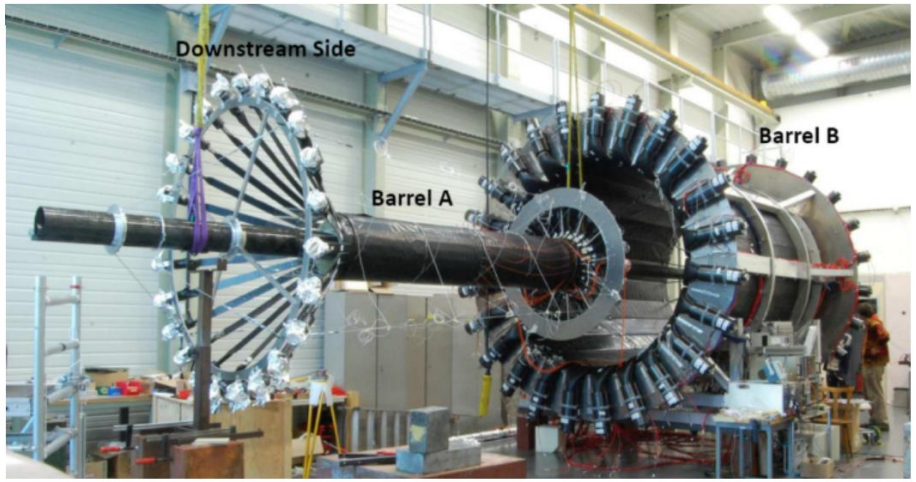
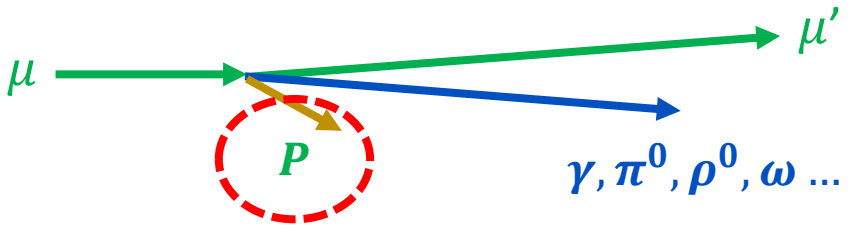


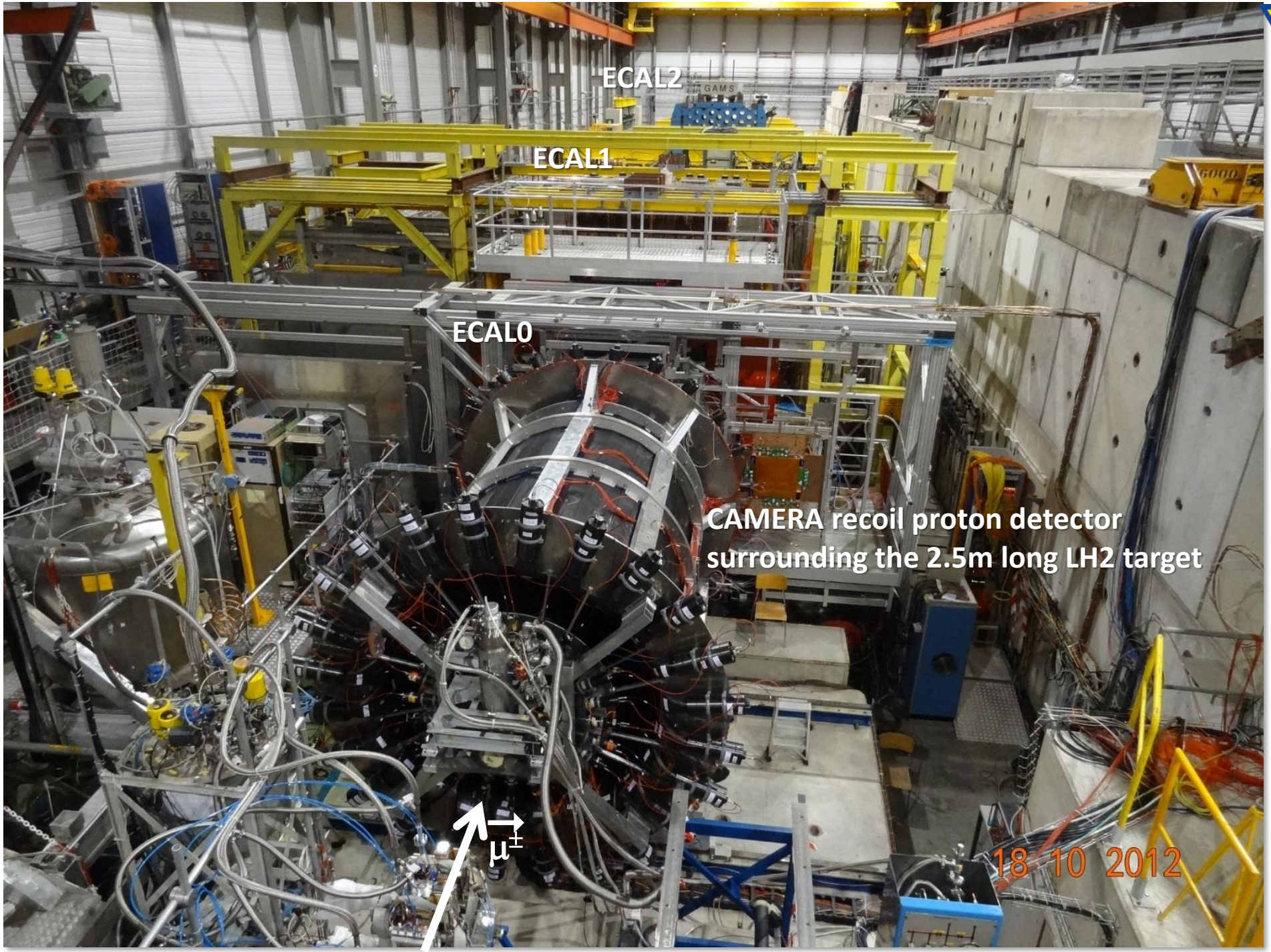
To ensure exclusivity:



CAMERA recoil proton detector

Exclusive Muoproduction




ECAL2
ECAL1
ECAL0
CAMERA recoil proton detector
surrounding the 2.5m long LH2 target
$\mu^{\pm}$
18 10 2012

COMPASS Experiment

2002-2022 COMPASS data taking

2002-2004	DIS & SIDIS, μ^+-**d**, 160 GeV, **L** & **T polarized target**
2005	*CERN accelerator shutdown, increase of COMPASS acceptance*
2006	DIS & SIDIS, μ^+-**d**, 160 GeV, **L polarized target**
2007	DIS & SIDIS, μ^+ -**p**, 160 GeV, **L** & **T polarized target**
2008-2009	Hadron spectroscopy & Primakoff reaction, **π/K/p** beam
2010	SIDIS, μ^+ -**p**, 160 GeV, **T polarized target**
2011	DIS & SIDIS, μ^+ -**p**, 200 GeV, **L polarized target**
2012	Primakoff reaction, **π/K/p** beam
2012 pilot run	DVCS/HEMP/SIDIS, μ^+ **&** μ^- -**p**, 160 GeV, **unpolarized target**
2013	*CERN accelerator shutdown, LS1*
2014-2015	Drell-Yan, **π-** -**p**, **T polarized target**
2016-2017	DVCS/HEMP/SIDIS, μ^+ **&** μ^- -**p**, 160 GeV, **unpolarized target**
2018	Drell-Yan, **π-** -**p**, **T polarized target**
2019-2020	*CERN accelerator shutdown, LS2*
2021-2022	SIDIS, μ^+-**d**, 160 GeV, **T polarized target**

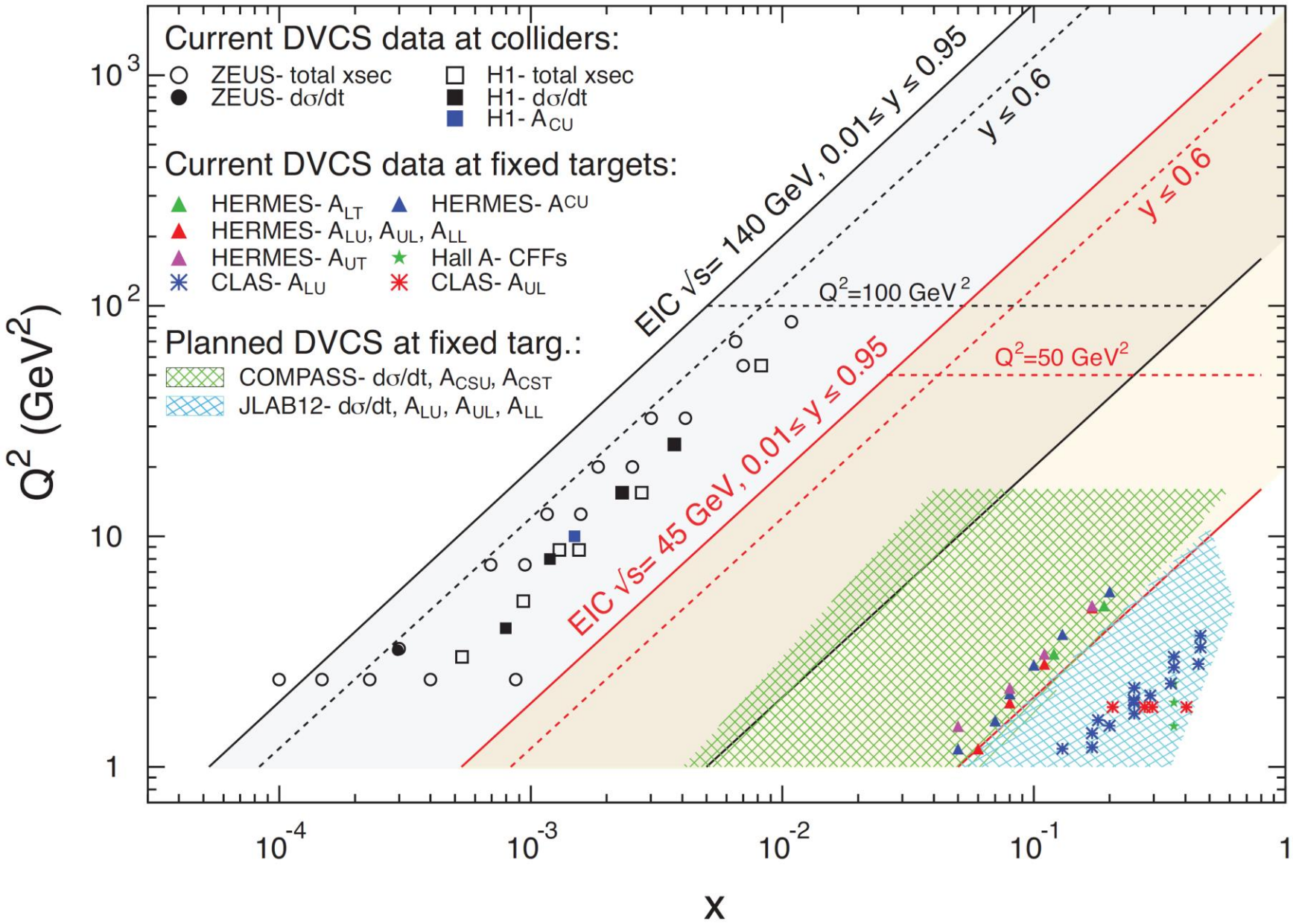
Study hadron structure with complmentary tools:

- **COMPASS holds the record for the longest-running CERN experiment**

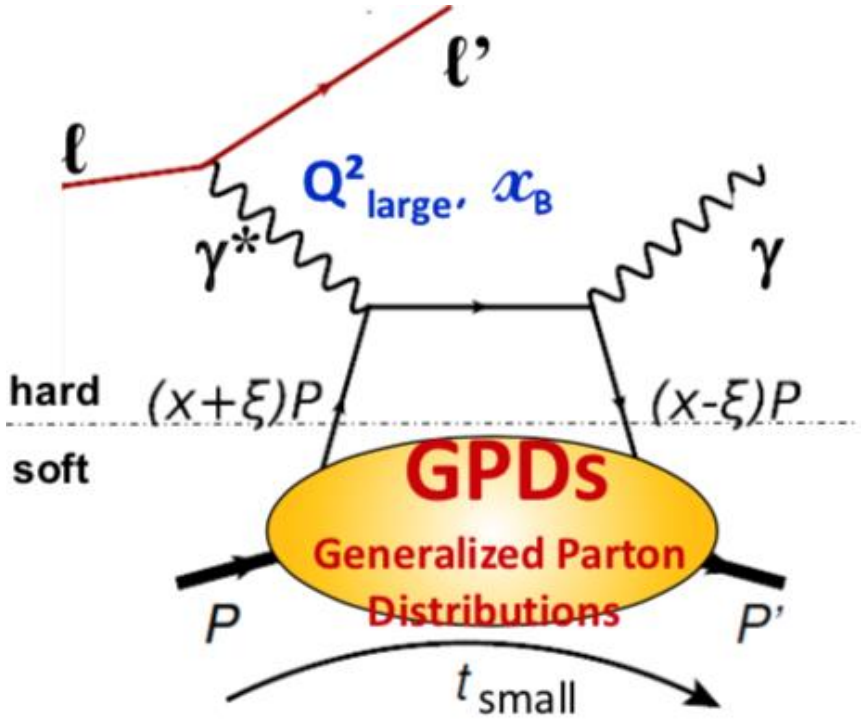
- 2012 pilot run with 4-week data taking
- 2016-17 dedicated run. 2 x 6 months.

Deeply Virtual Compton Scattering @ COMPASS

Lanscape – Global Programs of DVCS



DVCS



DVCS: $l + p \rightarrow l' + p' + \gamma$

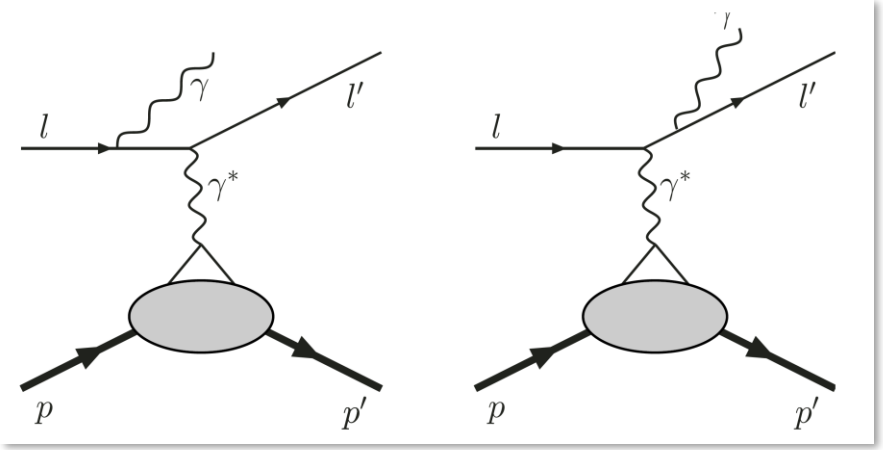
- As the golden channel to access GPDs, DVCS has been the workhorse for GPD Extraction.
- Its interference with the well-understood Bethe-Heitler process gives access to more info.

- The variables measured in the experiment:

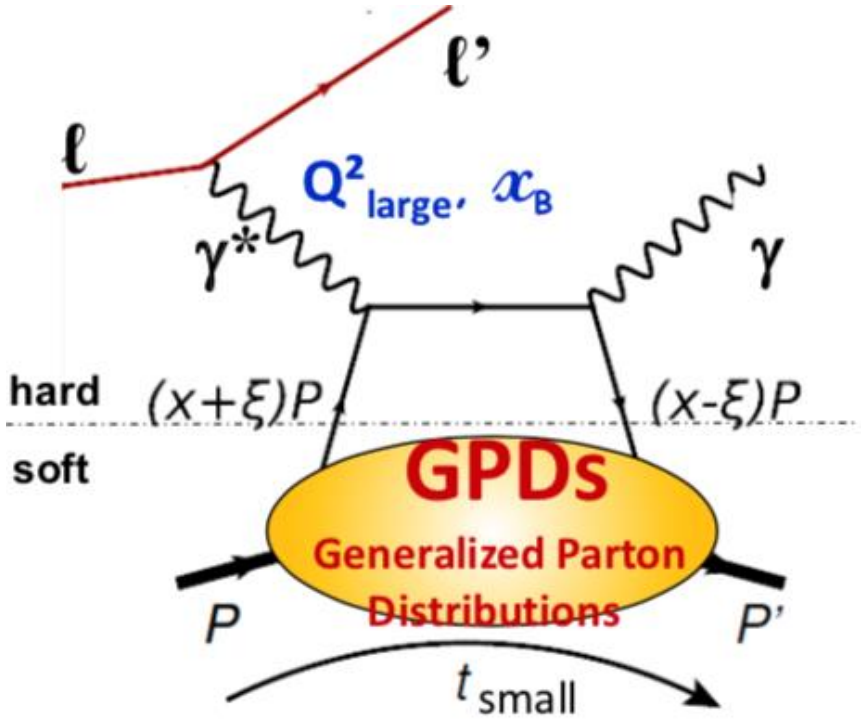
  E_ℓ, Q^2, $x_{Bj} \sim 2\xi/(1+\xi)$,

  t (or $\theta_{\gamma^*\gamma}$) and ϕ ($\ell\ell'$ plane/$\gamma\gamma^*$ plane)

BH Process



DVCS



DVCS: $l + p \rightarrow l' + p' + \gamma$

- With LH_2 target and small x_B coverage

→ focuses on **H** at COMPASS

CFF ⇢ $\mathcal{H}(\xi,t)$; GPD ⇢ $\mathbf{H}(x,\xi,t)$

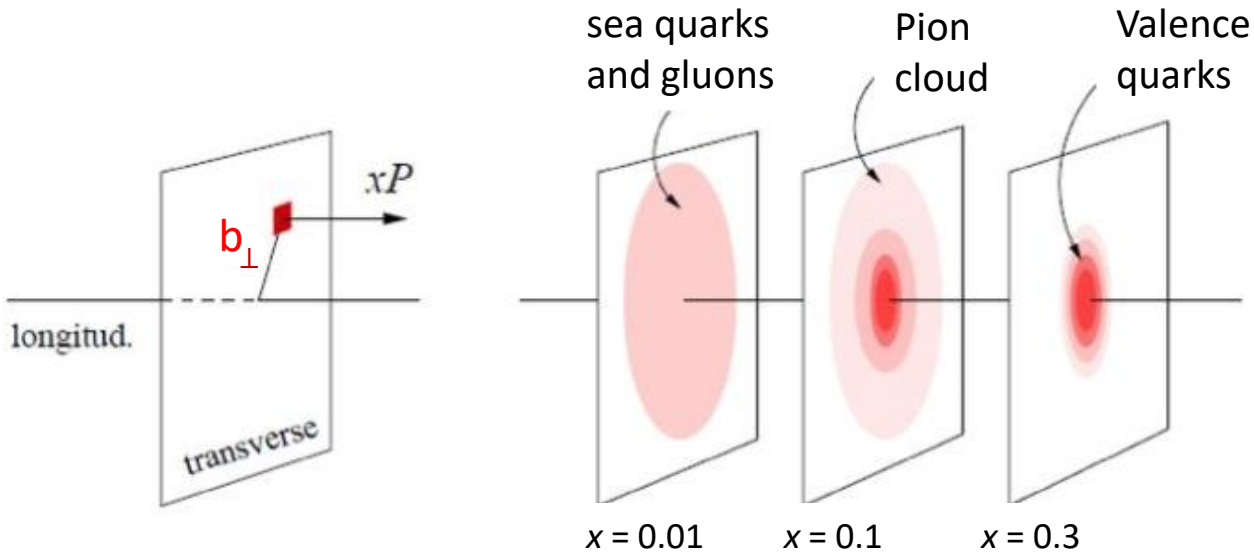
$$\mathcal{H}(\xi,t) = \int_{-1}^{+1} dx \frac{\mathbf{H}(x,\xi,t)}{x-\xi+i\varepsilon} + \ldots = \mathcal{P}\int_{-1}^{+1} dx \frac{\mathbf{H}(x,\xi,t)}{x-\xi} - i\pi\, \mathbf{H}(x=\pm\xi,\xi,t) + \ldots$$

REAL part — Imaginary part

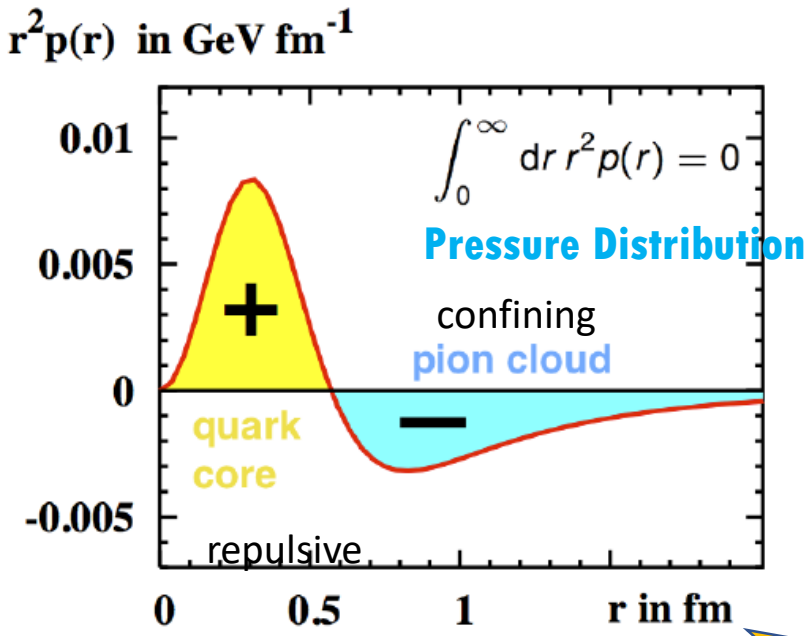
$$\mathcal{R}e\,\mathcal{H}(\xi,t) = \mathcal{P}\int dx \frac{Im\,\mathcal{H}(x,t)}{x-\xi} + \Delta(t)$$

Transverse Imaging and Pressure Distribution

Mapping in the transverse plane



M. Polyakov, P. Schweitzer, Int.J.Mod.Phys. A33 (2018)



FT of H(x, ξ=0,t)

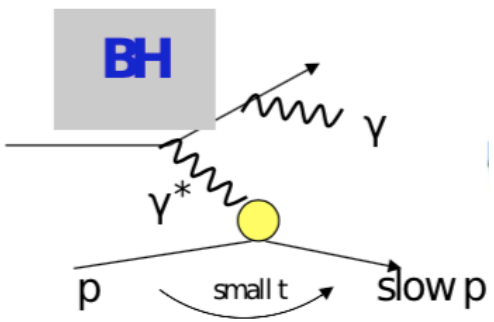
CFF → $\mathcal{H}(\xi,t)$ = GPD → $\int_{-1}^{+1} dx \frac{\mathbf{H}(x,\xi,t)}{x-\xi+i\varepsilon} + \ldots$

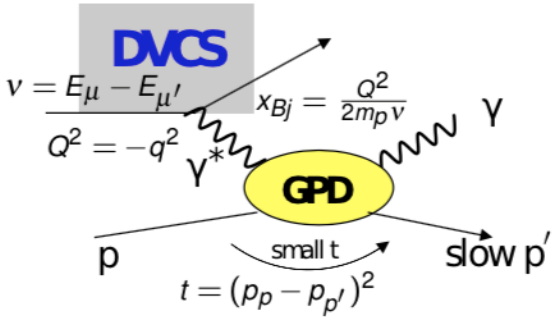
REAL part $= \mathcal{P}\int_{-1}^{+1} dx \frac{\mathbf{H}(x,\xi,t)}{x-\xi}$ **Imaginary part** $- i\pi\, \mathbf{H}(x=\pm\xi,\xi,t) + \ldots$

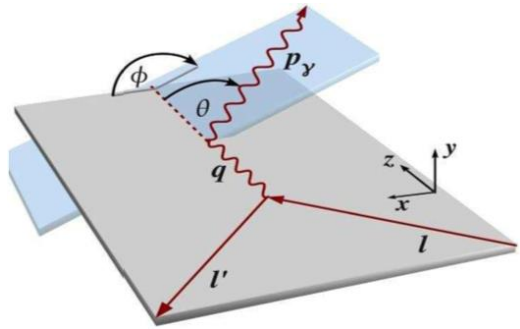
$$\mathcal{Re}\,\mathcal{H}(\xi,t) = \mathcal{P}\int dx \frac{Im\,\mathcal{H}(x,t)}{x-\xi} + \Delta(t)$$

D-term $d_1(t)$

Azimuthal Dependence of BH & DVCS







$$\frac{d^4\sigma(\ell p \to \ell p\gamma)}{dx_B dQ^2 d|t| d\phi} = \underbrace{d\sigma^{BH}}_{\text{Well known}} + \left(d\sigma^{DVCS}_{unpol} + P_\ell\, d\sigma^{DVCS}_{pol}\right) + \left(e_\ell \mathrm{Re}\, I + e_\ell P_\ell\, \mathrm{Im}\, I\right)$$

Beam Charge-spin difference & sum

$$\mathcal{D}_{CS,U}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) - d\sigma(\mu^{-\rightarrow})$$

$$\mathcal{S}_{CS,U}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) + d\sigma(\mu^{-\rightarrow})$$

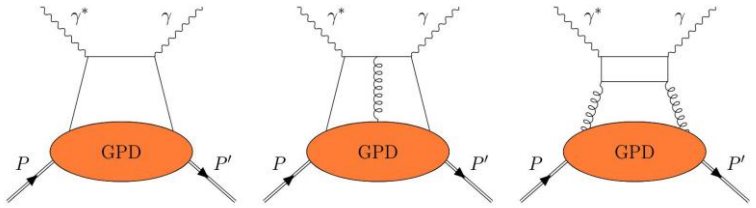
$$d\sigma^{BH} \propto c_0^{BH} + c_1^{BH}\cos\phi + c_2^{BH}\cos 2\phi$$

$$d\sigma^{DVCS}_{unpol} \propto c_0^{DVCS} + c_1^{DVCS}\cos\phi + c_2^{DVCS}\cos 2\phi$$

$$d\sigma^{DVCS}_{pol} \propto s_1^{DVCS}\sin\phi$$

$$\mathrm{Re}\, I \propto c_0^{I} + c_1^{I}\cos\phi + c_2^{I}\cos 2\phi + c_3^{I}\cos 3\phi$$

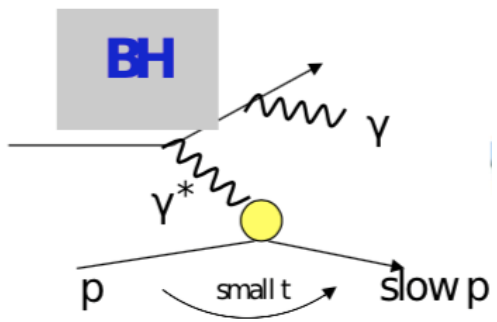
$$\mathrm{Im}\, I \propto s_1^{I}\sin\phi + s_2^{I}\sin 2\phi$$

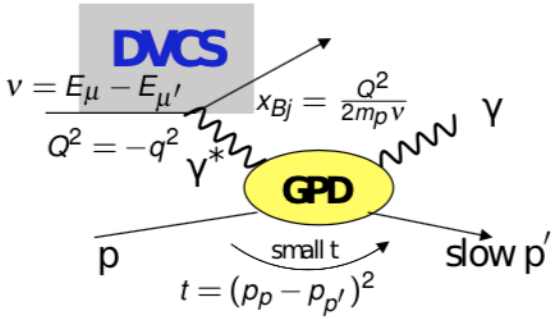


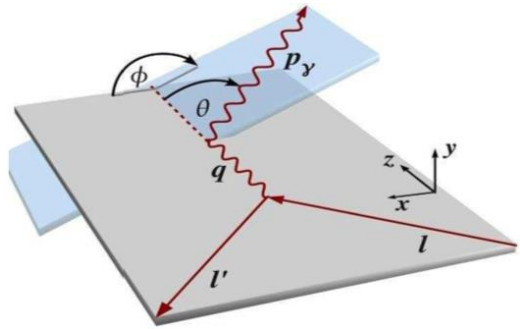
LO, Twist-2 | LO, Twist-3 | NLO, Twist-2 double helicity flip

Twist-2 >> Twist-3, Twist-2 - double helicity flip for gluons (NLO)

Azimuthal Dependence of BH & DVCS







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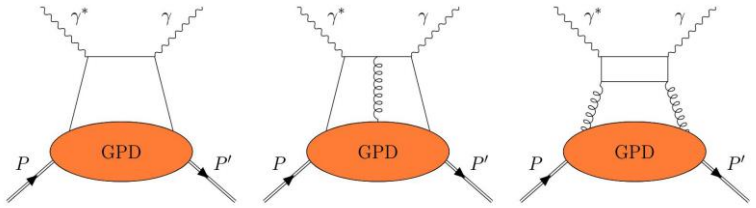
$$d\sigma^{DVCS}_{unpol} \propto c_0^{DVCS} + c_1^{DVCS}\cos\phi + c_2^{DVCS}\cos 2\phi$$

$$d\sigma^{DVCS}_{pol} \propto s_1^{DVCS}\sin\phi$$

$$\mathrm{Re}\, I \propto c_0^I + c_1^I\cos\phi + c_2^I\cos 2\phi + c_3^I\cos 3\phi$$

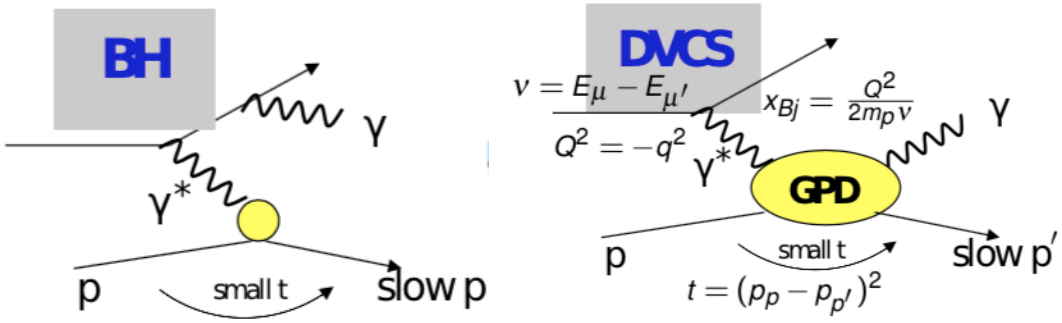
$$\mathrm{Im}\, I \propto s_1^I\sin\phi + s_2^I\sin 2\phi$$

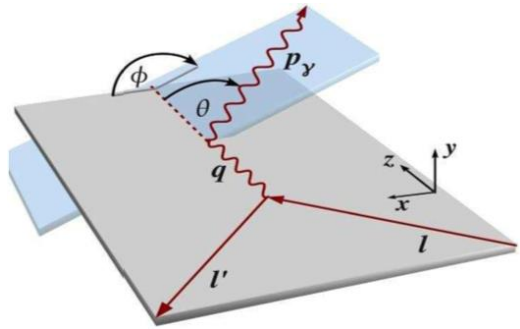
$\mathcal{D}_{CS,U}(\phi)$



Twist-2 >> Twist-3, Twist-2 - double helicity flip for gluons (NLO)

Azimuthal Dependence of BH & DVCS





$$\frac{d^4\sigma(\ell p \to \ell p\gamma)}{dx_B dQ^2 d|t| d\phi} = \underbrace{d\sigma^{BH}}_{\text{Well known}} + \left(d\sigma^{DVCS}_{unpol} + P_\ell\, d\sigma^{DVCS}_{pol}\right) + \left(e_\ell \mathrm{Re}\, I + e_\ell P_\ell\, \mathrm{Im}\, I\right)$$

Beam Charge-spin difference & sum

$$\mathcal{D}_{CS,\,U}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) - d\sigma(\mu^{-\rightarrow})$$

$$S_{CS,\,U}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) + d\sigma(\mu^{-\rightarrow})$$

$$d\sigma^{BH} \propto c_0^{BH} + c_1^{BH}\cos\phi + c_2^{BH}\cos 2\phi$$

$$d\sigma^{DVCS}_{unpol} \propto c_0^{DVCS} + c_1^{DVCS}\cos\phi + c_2^{DVCS}\cos 2\phi$$

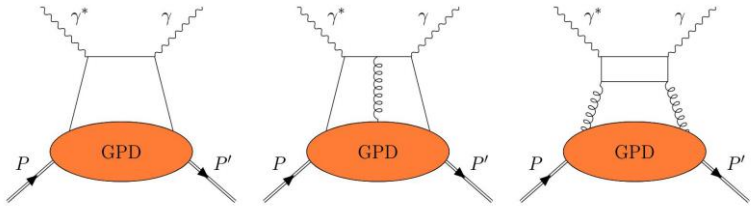
$S_{CS,\,U}(\phi)$

$$d\sigma^{DVCS}_{pol} \propto s_1^{DVCS}\sin\phi$$

$$\mathrm{Re}\, I \propto c_0^I + c_1^I\cos\phi + c_2^I\cos 2\phi + c_3^I\cos 3\phi$$

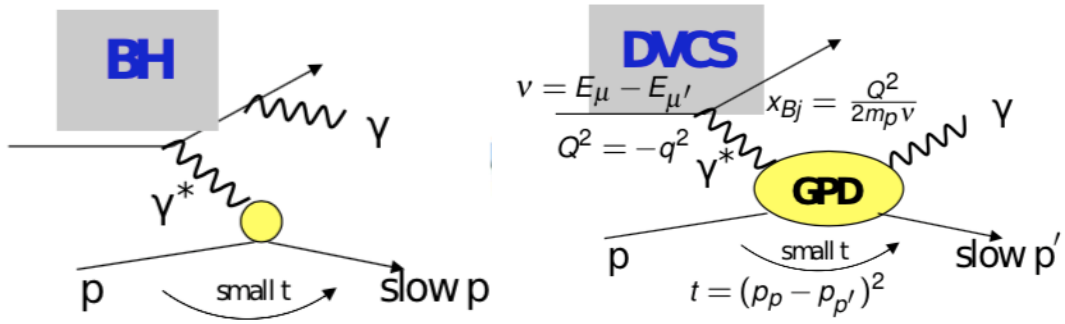
$$\mathrm{Im}\, I \propto s_1^I\sin\phi + s_2^I\sin 2\phi$$

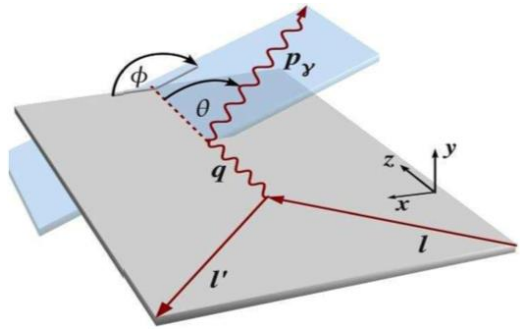
$S_{CS,\,U}(\phi)$



Twist-2 >> Twist-3, Twist-2 - double helicity flip for gluons (NLO)

Azimuthal Dependence of BH & DVCS





$$\frac{d^4\sigma(\ell p \to \ell p\gamma)}{dx_B dQ^2 d|t| d\phi} = \underbrace{d\sigma^{BH}}_{\text{Well known}} + \left(d\sigma^{DVCS}_{unpol} + P_\ell\, d\sigma^{DVCS}_{pol}\right) + \left(e_\ell \mathrm{Re}\, I + e_\ell P_\ell\, \mathrm{Im}\, I\right)$$

Beam Charge-spin difference & sum

$\mathcal{D}_{CS,U}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) - d\sigma(\mu^{-\rightarrow})$ ➡ $C_1^I \propto Re\ \mathcal{F}$ — More challenging

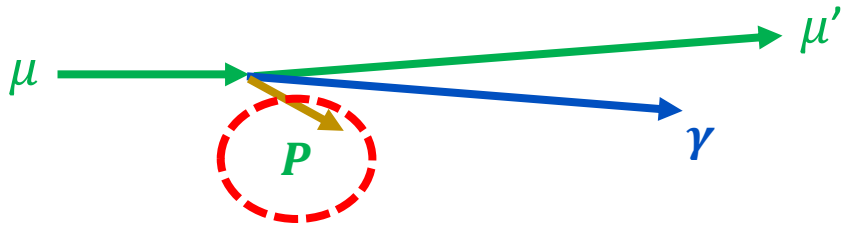
$\mathcal{S}_{CS,U}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) + d\sigma(\mu^{-\rightarrow})$ ➡ $C_0^{DVCS} \propto (Im\mathcal{H})^2$ and $S_1^I \propto Im\ \mathcal{F}$ — Easier to measure

$$\mathcal{F} = F_1\mathcal{H} + \xi(F_1+F_2)\mathcal{H} + t/4m^2 F_2\,\mathcal{E} \xrightarrow[\text{Small } x_B \text{ at COMPASS}]{\text{Proton Target}} F_1\mathcal{H}$$

Compton Form factor linked to GPD **H**

Twist-2 >> Twist-3, Twist-2 - double helicity flip for gluons (NLO)

COMPASS 2016 Preliminary Results



$\Delta\varphi = \varphi^{cam.} - \varphi^{spec.}$

Proton azimuthal angle

$\Delta p_T = |p_T^{cam.}| - |p_T^{spec.}|$

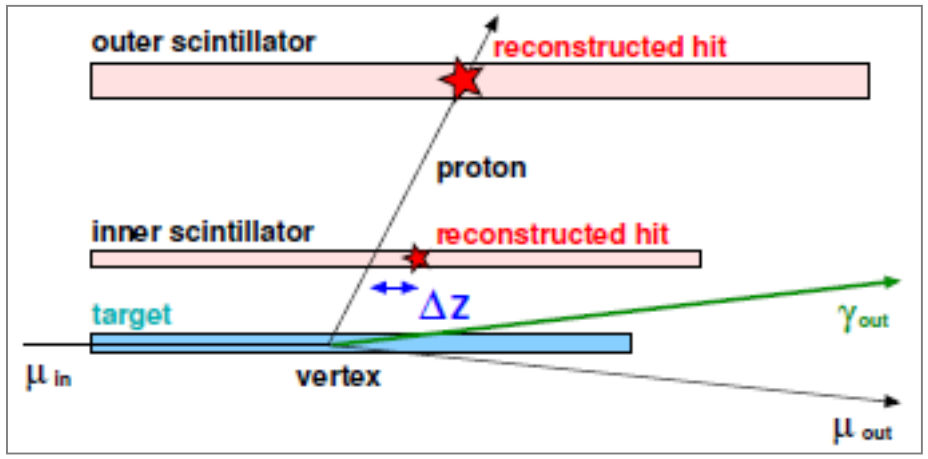
Proton momentum

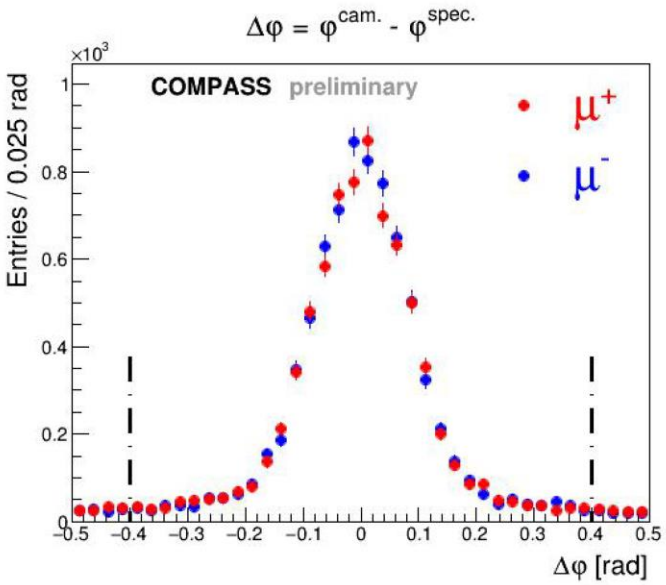
$\Delta z_A = z_A^{cam.} - z_A^{spec.}$

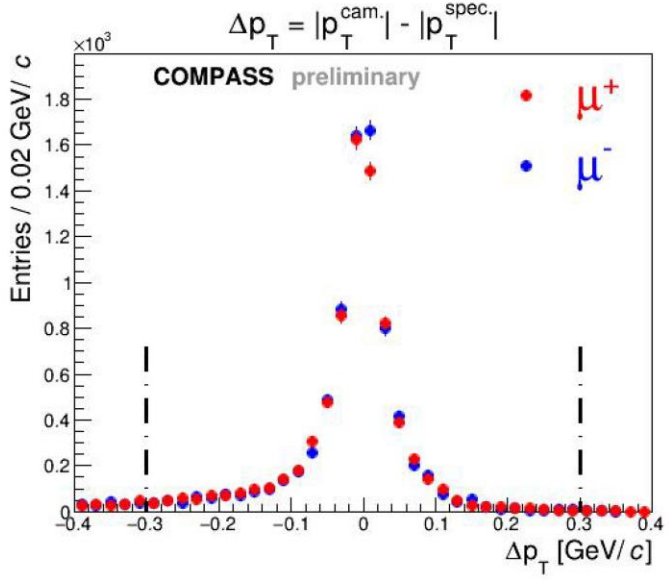
Proton track position

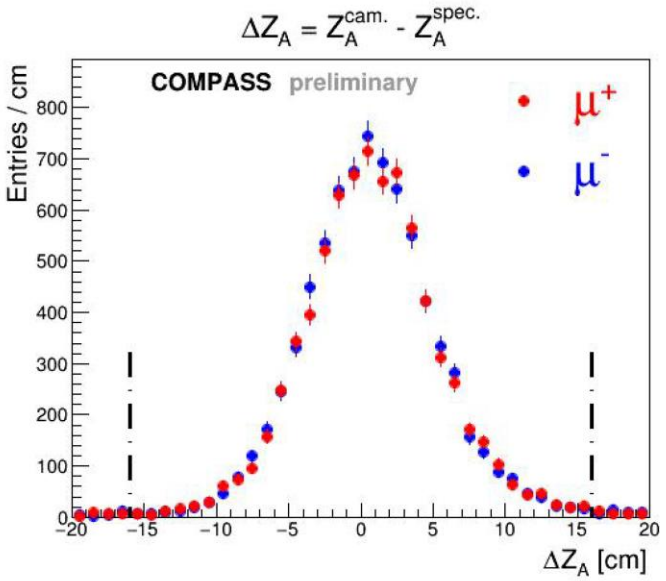
$M^2_{undet} = (k + p - k' - q' - p')^2$

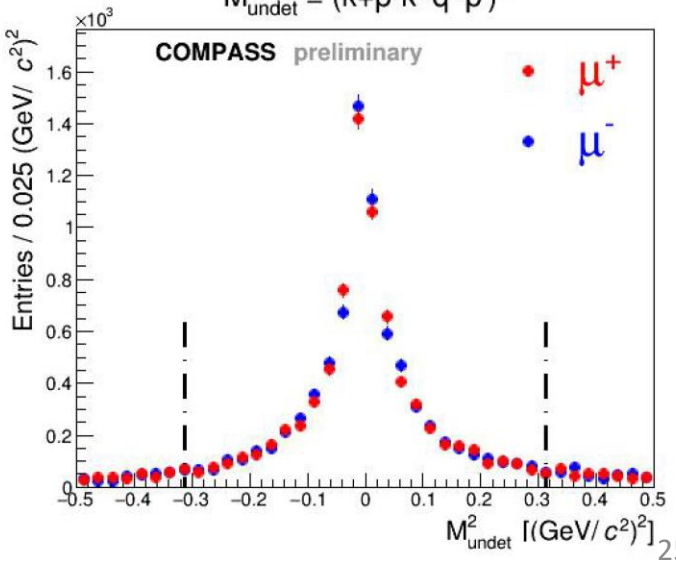
Energy momentum balance



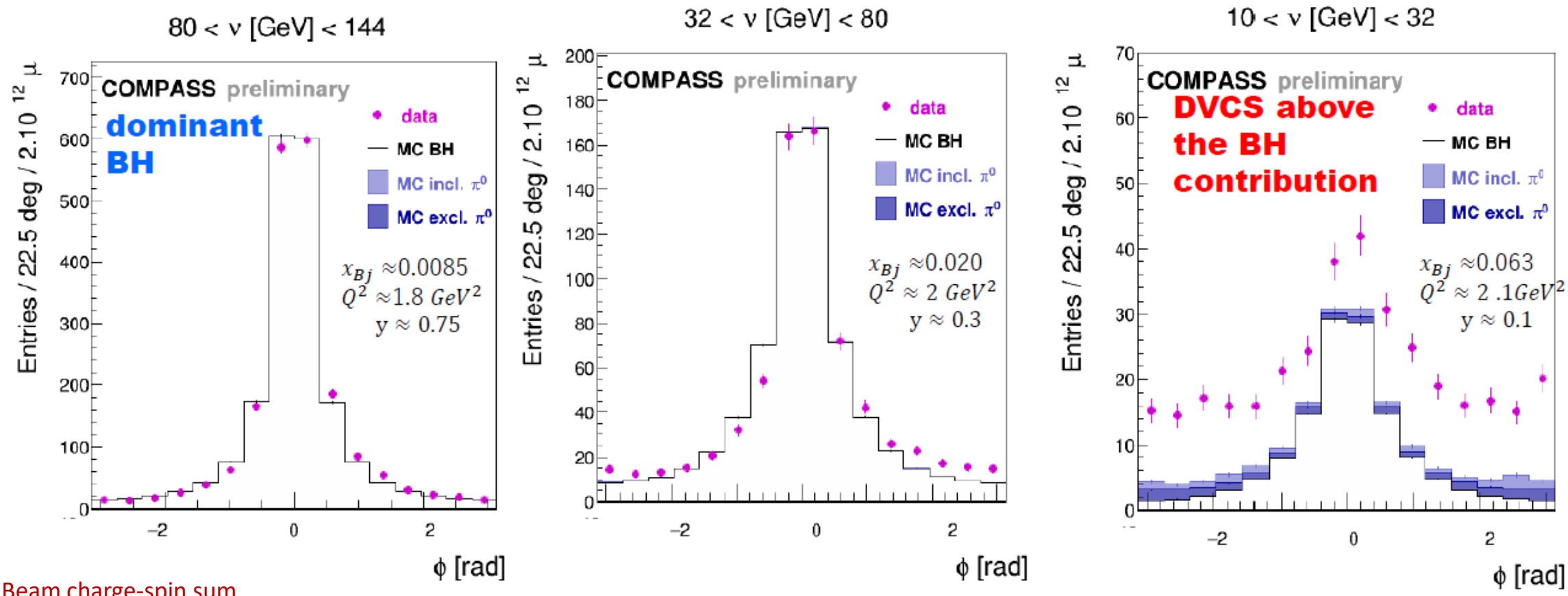








COMPASS 2016 Preliminary Results



- Beam charge-spin sum

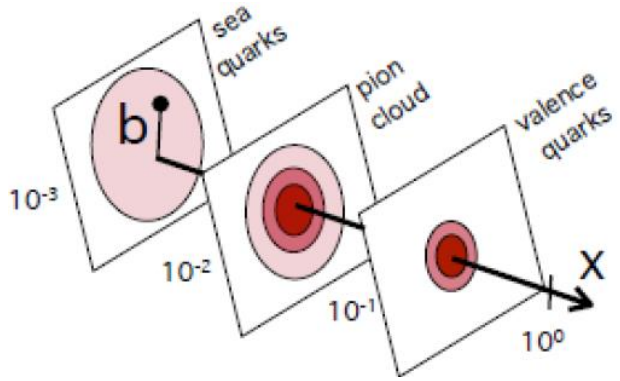
$$S_{CS,U}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) + d\sigma(\mu^{-\rightarrow}) = 2[\, d\sigma^{BH} + d\sigma^{DVCS}_{unpol} + \mathrm{Im}\, I\,]$$

$$= 2[\, d\sigma^{BH} + c_0^{DVCS} + c_1^{DVCS}\cos\phi + c_2^{DVCS}\cos 2\phi + s_1^{I}\sin\phi + s_2^{I}\sin 2\phi\,]$$

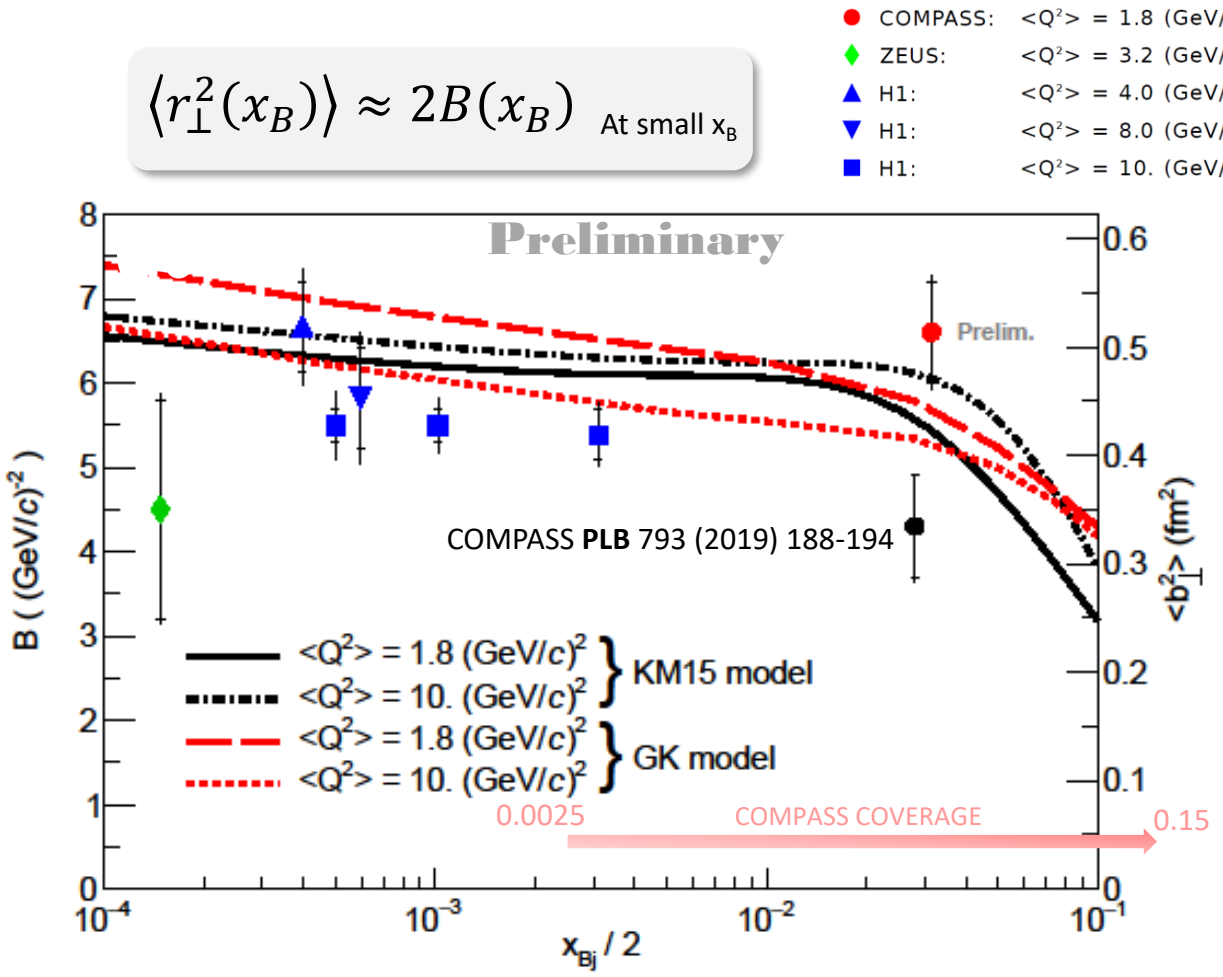
$$c_0^{DVCS} \propto 4(\mathcal{H}\mathcal{H}^* + \tilde{\mathcal{H}}\tilde{\mathcal{H}}^*) + \frac{t}{M^2}\mathcal{E}\mathcal{E}^* \rightarrow 4\,(Im\,\mathcal{H})^2$$

small x_{Bj} — model dependent

Tranverse extension of partons – 2016 data



$\langle r_\perp^2(x_B)\rangle \approx 2B(x_B)$ At small x_B



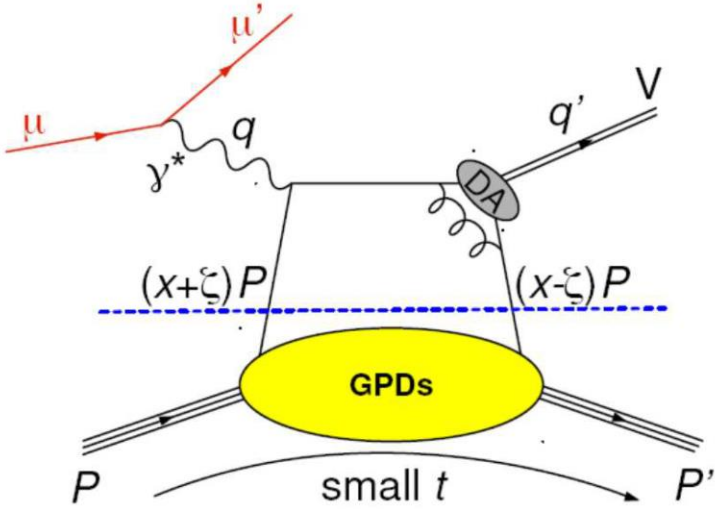
- Improvements in the 2016 analysis, relative to 2012
  - μ^+ and μ^- beams at same intensity
  - More advanced analysis with 2016 data, ongoing
  - Improved π^0 contamination estimation
  - Better MC description in ν

- The transverse-size evolution as a function of x_{Bj} → Expect at least 3 x_{Bj} bins from 2016-17 data

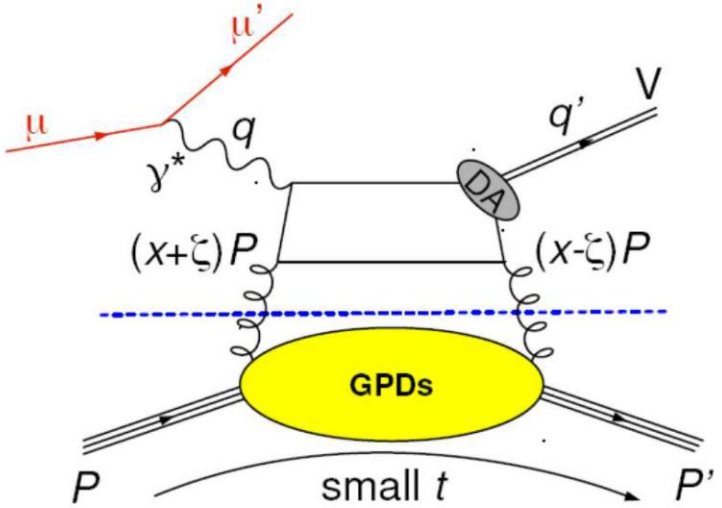
Deeply Virtual Meson Production @ COMPASS

GPDs in Deeply Virtual Meson Production

quark contribution



gluon contribution



4 chiral-even GPDs: helicity of parton unchanged

$H^q(x, \xi, t)$	$E^q(x, \xi, t)$	→ **Vector Meson**
$\tilde{H}^q(x, \xi, t)$	$\tilde{E}^q(x, \xi, t)$	→ **Pseudo-Scalar Meson**

+ 4 chiral-odd (transversity) GPDs: helicity of parton changed

(not possible in DVCS)

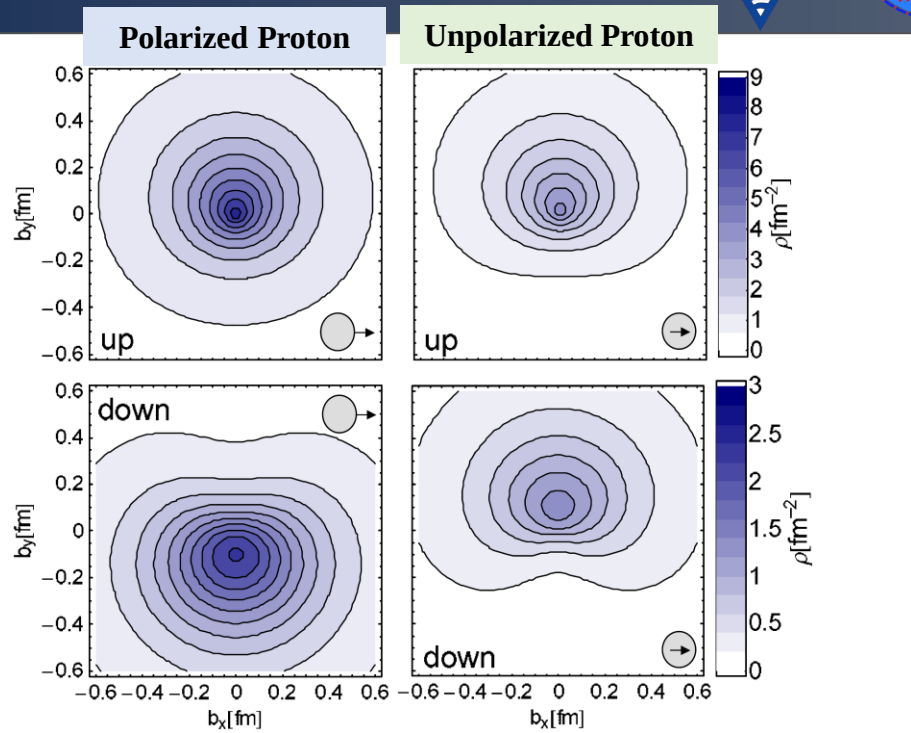
$H_T^q(x, \xi, t)$	$E_T^q(x, \xi, t)$
$\tilde{H}_T^q(x, \xi, t)$	$\tilde{E}_T^q(x, \xi, t)$

$$\overline{E}_T^q = 2\tilde{H}_T^q + E_T^q$$

- Ability to probe the chiral-odd GPDs.
- Universality of GPDs, quark flavor filter
- In addition to nuclear structure, provide insights into reaction mechanism.
- Additional non-perturbative term from meson wave function.

Chiral-odd GPDs

Nucleon polarization	Quark polarization: U	L	T
U	H		$\bar{E}_T$
L		$\tilde{H}$	$\tilde{E}_T$
T	E	$\tilde{E}$	$H_T,\ \tilde{H}_T$



Described by E

Described by $\bar{E}_T = 2\tilde{H}_T + E_T$

Lattice Calculation: Gockeler *PRL* 222001 (2007)

- $\bar{E}_T$ is related to the distortion of the polarized quark distribution in the transverse plane for an unpolarized nucleon
- Chiral-odd GPDs H_T
  - Generalization of transversity distribution $h_1(x)$
    → related to the transverse spin structure
  - Tensor charge

GPDs parametrization:

H_T

tensor charge: T.Ledwig, A.Silva, H.C. Kim

$$\int dx H_T(x,\xi,t)$$

transversity PDF: M.Anselmino

$$H_T(x,\xi=0,t=0) = h_1$$

Exclusive π^0 Production on Unpolarized Proton

$\mu\, p \rightarrow \mu\, \pi^0\, p$

$$\frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi}\left[\left(\frac{d\sigma_T}{dt} + \epsilon\frac{d\sigma_L}{dt}\right) + \epsilon\cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)}\cos\phi_\pi \frac{d\sigma_{LT}}{dt}\right]$$

ϵ : degree of longitudinal polarization

$$\frac{d\sigma_L}{dt} = \frac{4\pi\alpha}{k'}\frac{1}{Q^6}\left\{(1-\xi^2)\left|\langle\tilde{H}\rangle\right|^2 - 2\xi^2 \mathrm{Re}\left[\langle\tilde{H}\rangle^*\langle\tilde{E}\rangle\right] - \frac{t'}{4m^2}\xi^2\left|\langle\tilde{E}\rangle\right|^2\right\}$$

Leading twist expected be dominant

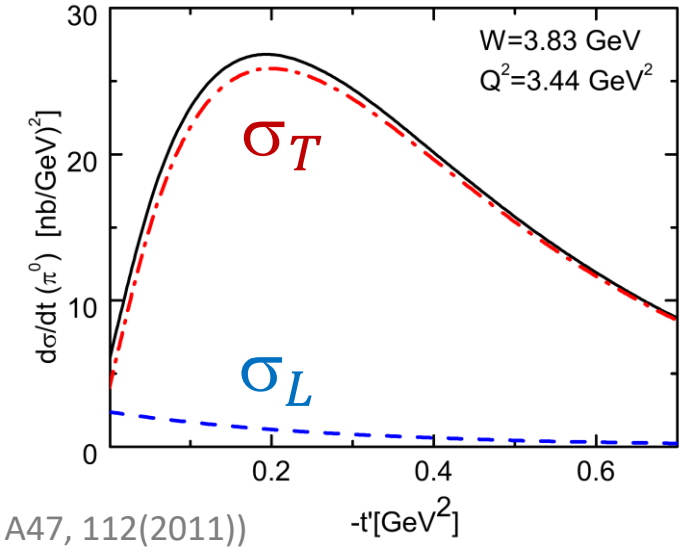
But measured as ≈ only a few % of $\frac{d\sigma_T}{dt}$

The other contributions arise from coupling between chiral-odd (quark helicity flip) GPDs to the twist-3 pion amplitude

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k'}\frac{\mu_\pi^2}{Q^8}\left[(1-\xi^2)\left|\langle H_T\rangle\right|^2 - \frac{t'}{8m^2}\left|\langle\bar{E}_T\rangle\right|^2\right]$$

$$\frac{\sigma_{LT}}{dt} = \frac{4\pi\alpha}{\sqrt{2}k'}\frac{\mu_\pi}{Q^7}\xi\sqrt{1-\xi^2}\frac{\sqrt{-t'}}{2m}\,\mathrm{Re}\left[\langle H_T\rangle^*\langle\tilde{E}\rangle\right]$$

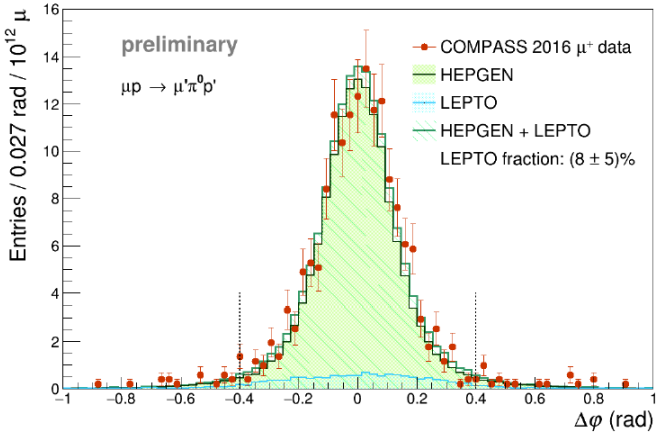
$$\frac{\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k'}\frac{\mu_\pi^2}{Q^8}\frac{t'}{16m^2}\left|\langle\bar{E}_T\rangle\right|^2$$

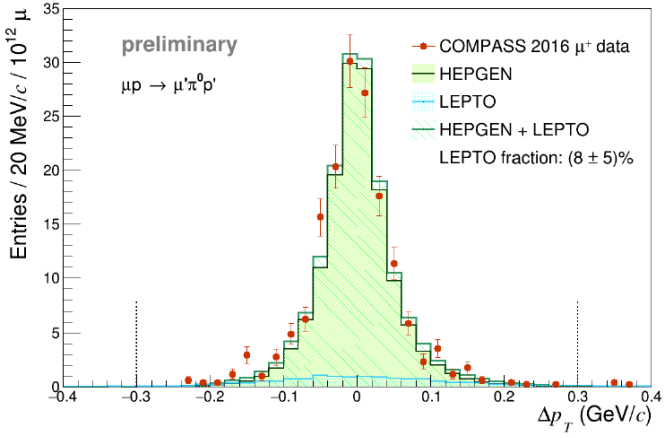


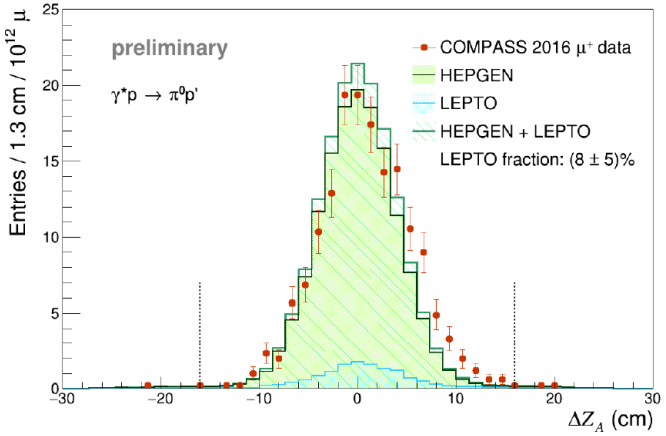
S. Goloskokov and P. Kroll (Eur.Phys.J A47, 112(2011))

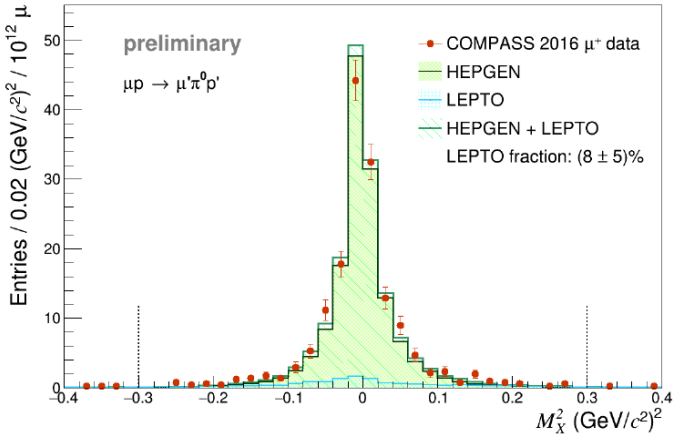
Exclusive π^0 Selection and Background Estimation

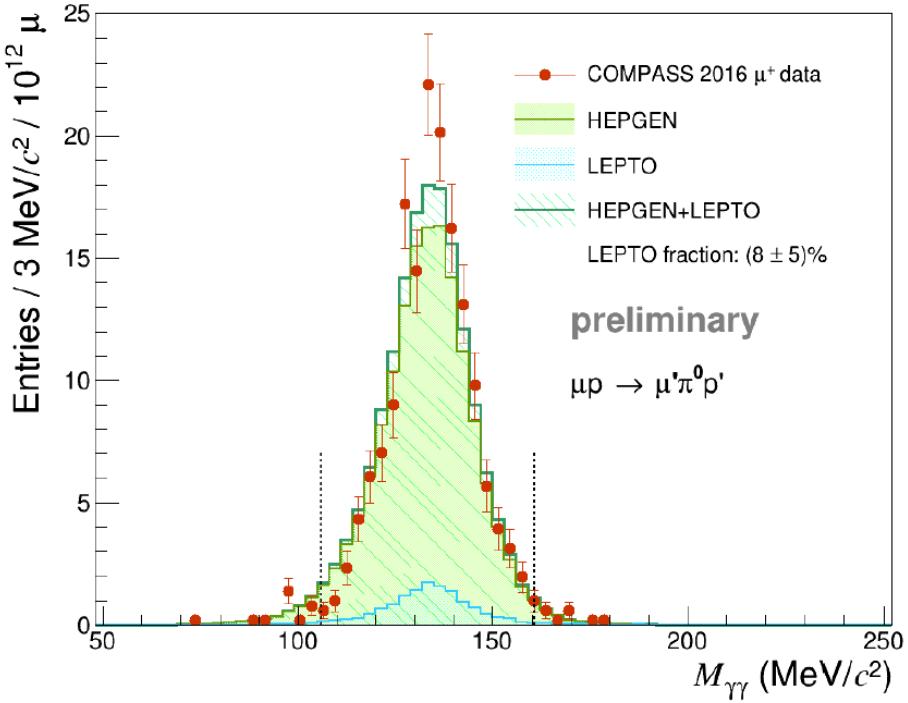
- Exclusivity ensured by cuts on *exclusivity variables, similar to DVCS.*
- Background fraction determined by fitting the exclusivity variables with Monte Carlo simulations.
  - *LEPTO* for non-exclusive background
  - *HEPGEN* of exclusive π^0 for signal







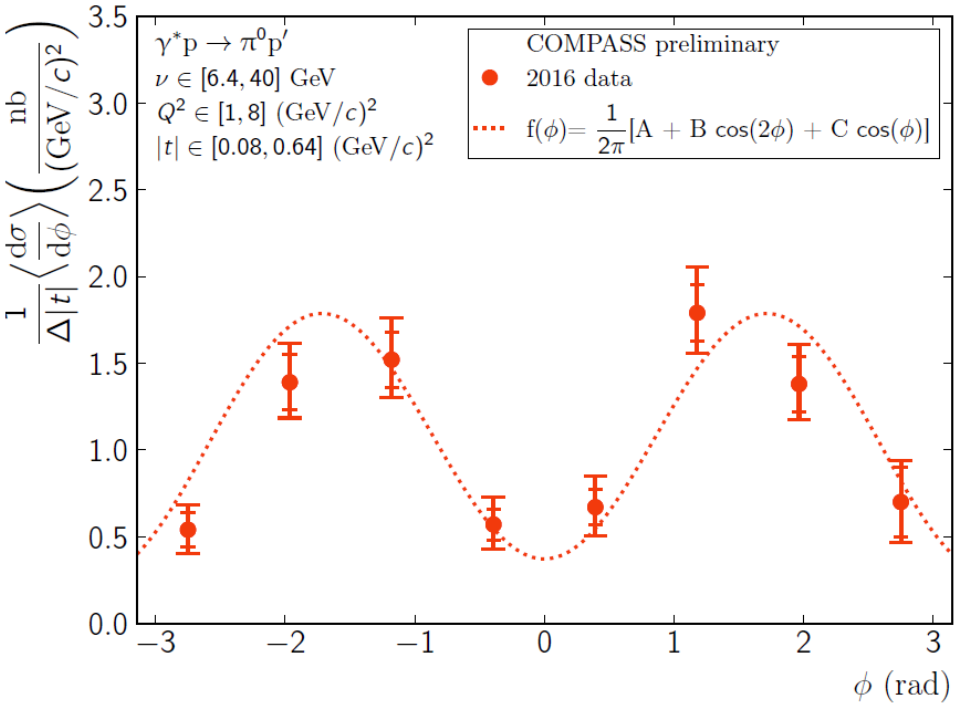


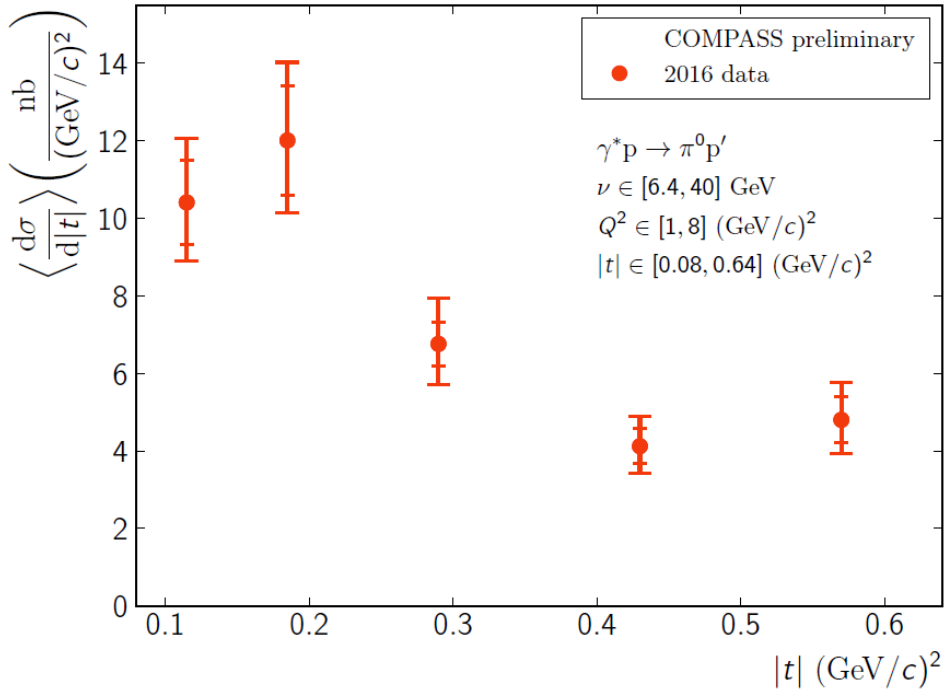


- In 2016 data, non-exclusive background fraction in data → 8 ± 5 %

New 2016 Exclusive π^0 Prod. on Unpolarized Proton

- Kinematic domain: $\nu \in [6.4, 40]$ GeV and $Q^2 \in [1,8]$ GeV$^2/c^2$, $\langle x_B \rangle = 0.134$





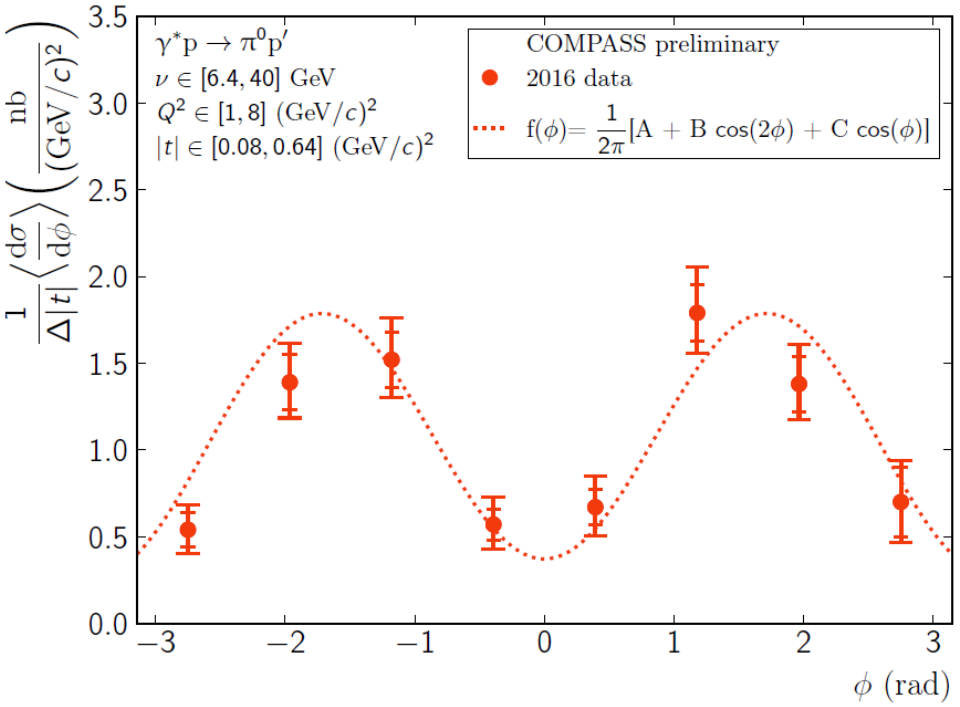
$\mu\, p \to \mu\, \pi^0\, p$

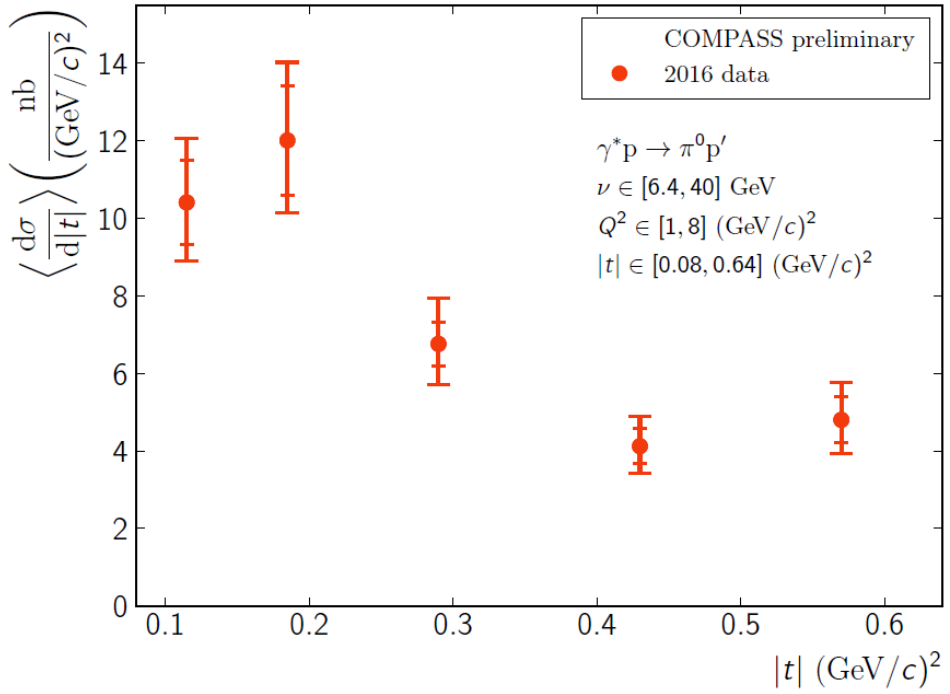
$$\frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi}\left[\left(\frac{d\sigma_T}{dt} + \epsilon\frac{d\sigma_L}{dt}\right) + \epsilon\cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)}\cos\phi_\pi \frac{d\sigma_{LT}}{dt}\right]$$

Chiral-odd GPDs

New 2016 Exclusive π^0 Prod. on Unpolarized Proton

- Kinematic domain: $\nu \in [6.4, 40]$ GeV and $Q^2 \in [1,8]$ GeV$^2/c^2$, $\langle x_B \rangle = 0.134$





$$\left\langle \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right\rangle = \left(6.6 \pm 0.3_{stat}{}^{+0.9}_{-0.8}\Big|_{sys}\right) \frac{nb}{(GeV/c)^2}$$

$$\left\langle \frac{d\sigma_{TT}}{dt} \right\rangle = \left(-4.6 \pm 0.5_{stat}{}^{+0.3}_{-0.3}\Big|_{sys}\right) \frac{nb}{(GeV/c)^2}$$

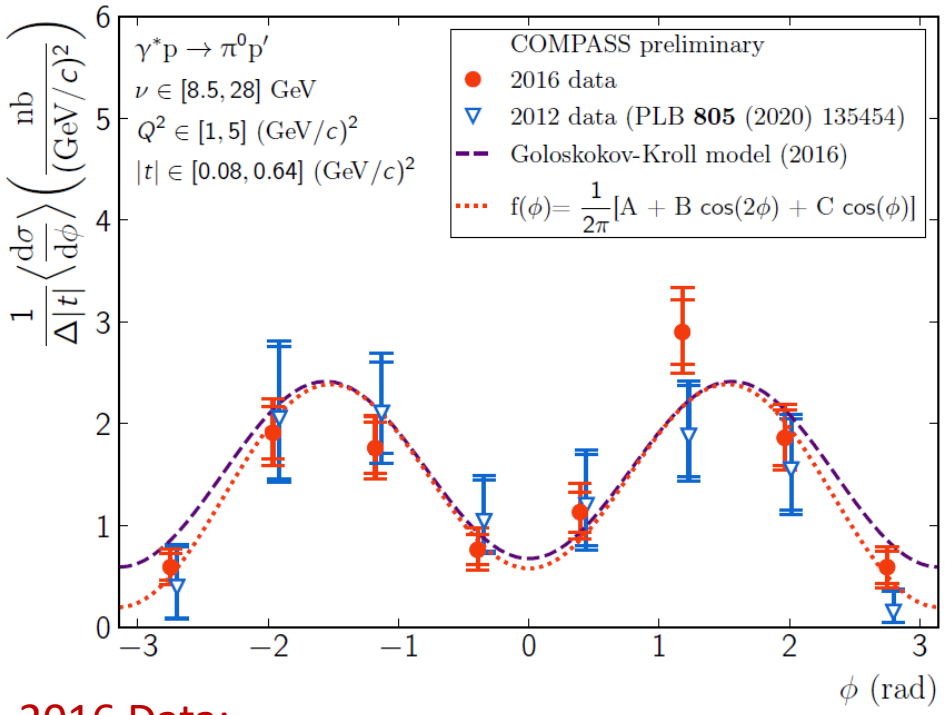
$$\left\langle \frac{d\sigma_{LT}}{dt} \right\rangle = \left(0.2 \pm 0.2_{stat}{}^{+0.2}_{-0.2}\Big|_{sys}\right) \frac{nb}{(GeV/c)^2}$$

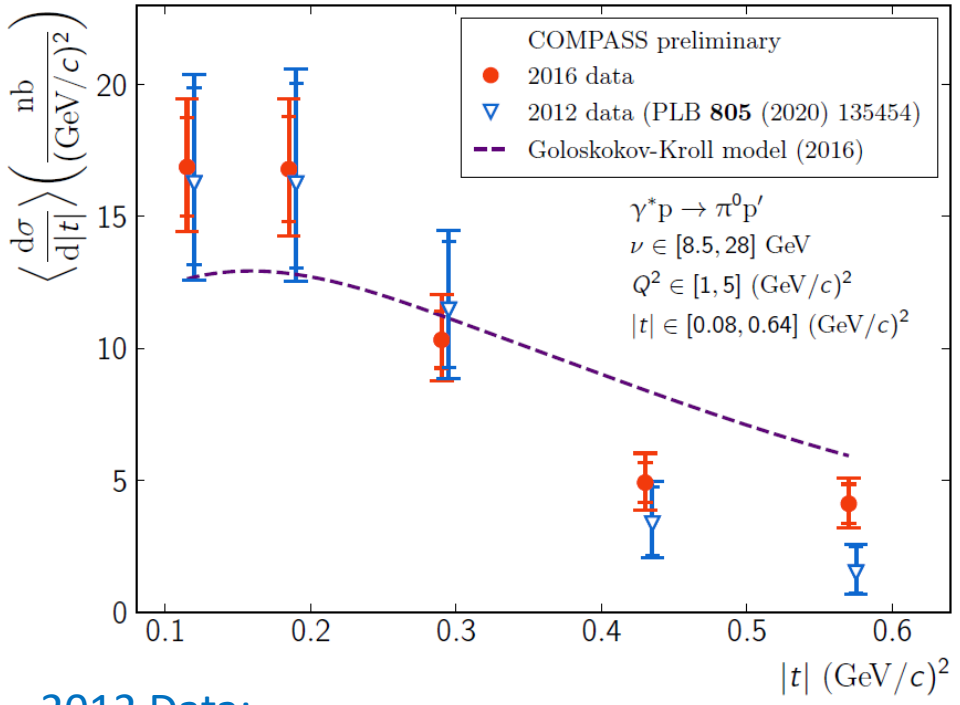
$\langle \epsilon \rangle = 0.997$

- Cross section extracted in a larger (ν, Q^2) domain, compared with the 2012 result. (COMPASS, **PLB** 805 (2020) 135454)
- Comparable $|\sigma_{TT}|$ and $\sigma_T + \epsilon\sigma_L$

2012-16 Exclusive π^0 Prod. Comparison

- Kinematic domain: $\nu \in [8.5, 28]$ GeV and $Q^2 \in [1,5]$ GeV$^2/c^2$, $\langle x_B \rangle = 0.10$





2016 Data:

$$\left\langle \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right\rangle = \left(8.7 \pm 0.5_{stat}{}^{+1.0}_{-1.0}\Big|_{sys} \right) \frac{nb}{(GeV/c)^2}$$

$$\left\langle \frac{d\sigma_{TT}}{dt} \right\rangle = \left(-6.3 \pm 0.8_{stat}{}^{+0.4}_{-0.5}\Big|_{sys} \right) \frac{nb}{(GeV/c)^2}$$

$$\left\langle \frac{d\sigma_{LT}}{dt} \right\rangle = \left(0.6 \pm 0.3_{stat}{}^{+0.3}_{-0.3}\Big|_{sys} \right) \frac{nb}{(GeV/c)^2}$$

$$\langle \epsilon \rangle = 0.996$$

2012 Data:

$$\left\langle \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right\rangle = \left(8.1 \pm 0.9_{stat}{}^{+1.1}_{-1.0}\Big|_{sys} \right) \frac{nb}{(GeV/c)^2}$$

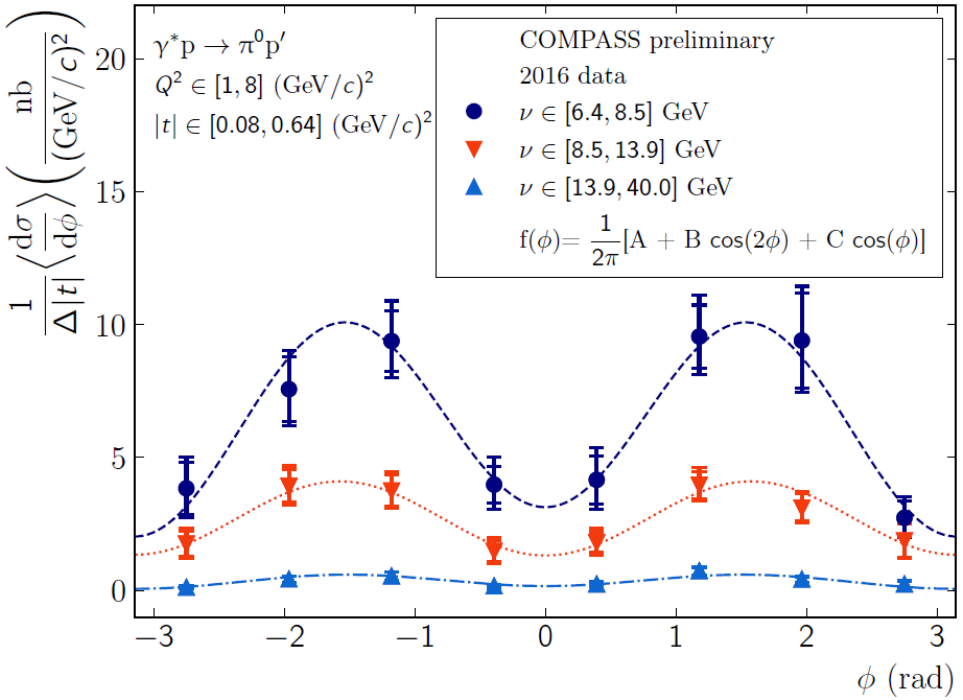
$$\left\langle \frac{d\sigma_{TT}}{dt} \right\rangle = \left(-6.0 \pm 1.3_{stat}{}^{+0.7}_{-0.7}\Big|_{sys} \right) \frac{nb}{(GeV/c)^2}$$

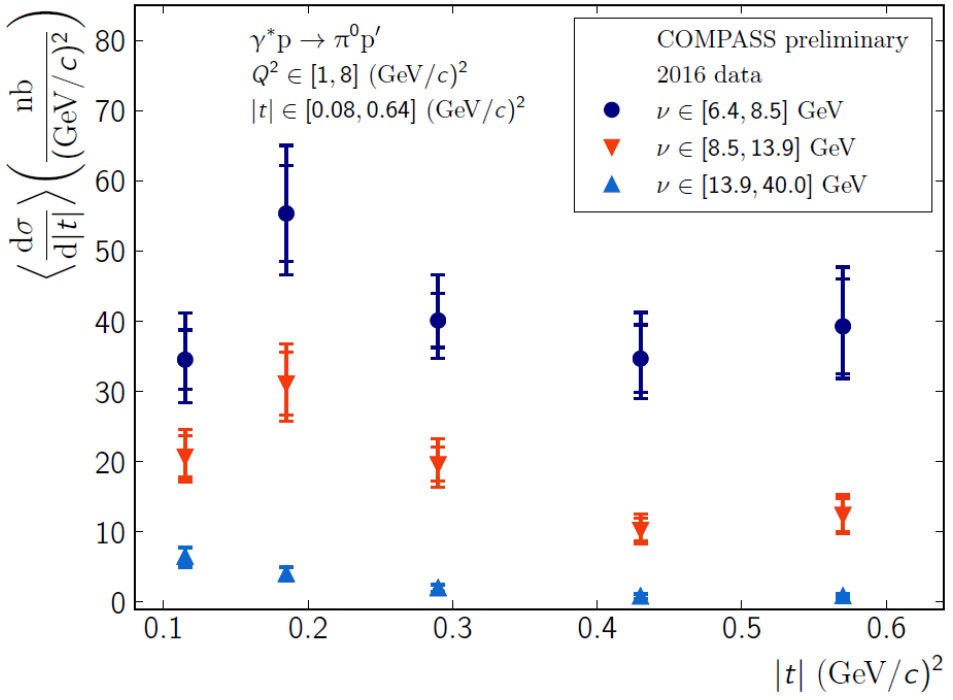
$$\left\langle \frac{d\sigma_{LT}}{dt} \right\rangle = \left(1.4 \pm 0.5_{stat}{}^{+0.3}_{-0.2}\Big|_{sys} \right) \frac{nb}{(GeV/c)^2}$$

$$\langle \epsilon \rangle = 0.996$$

New 2016 Exclusive π^0 Cross-section Evolution with ν

- Cross section decreases with increasing ν

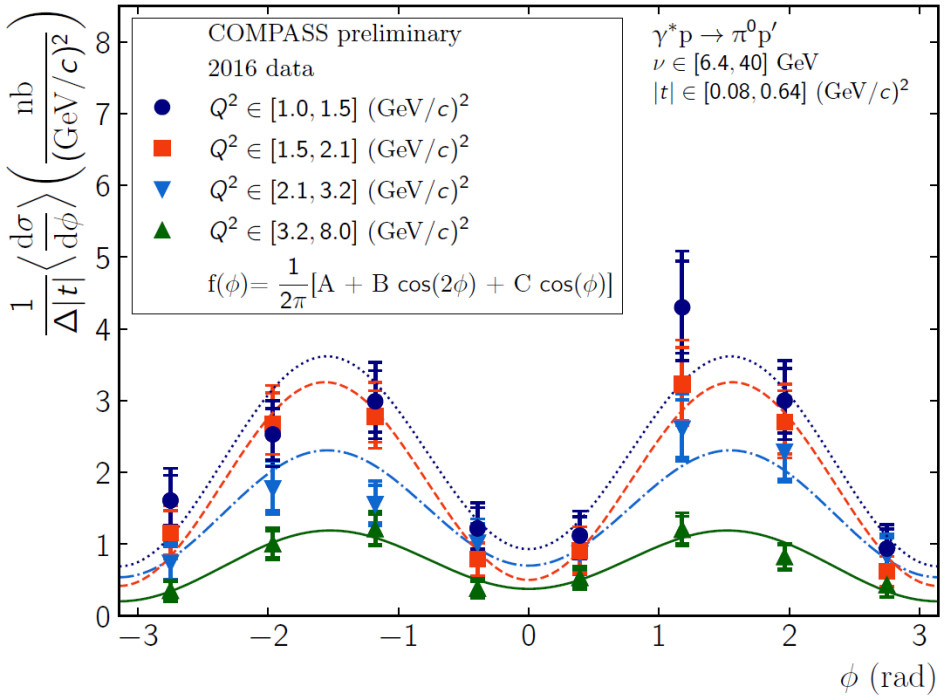


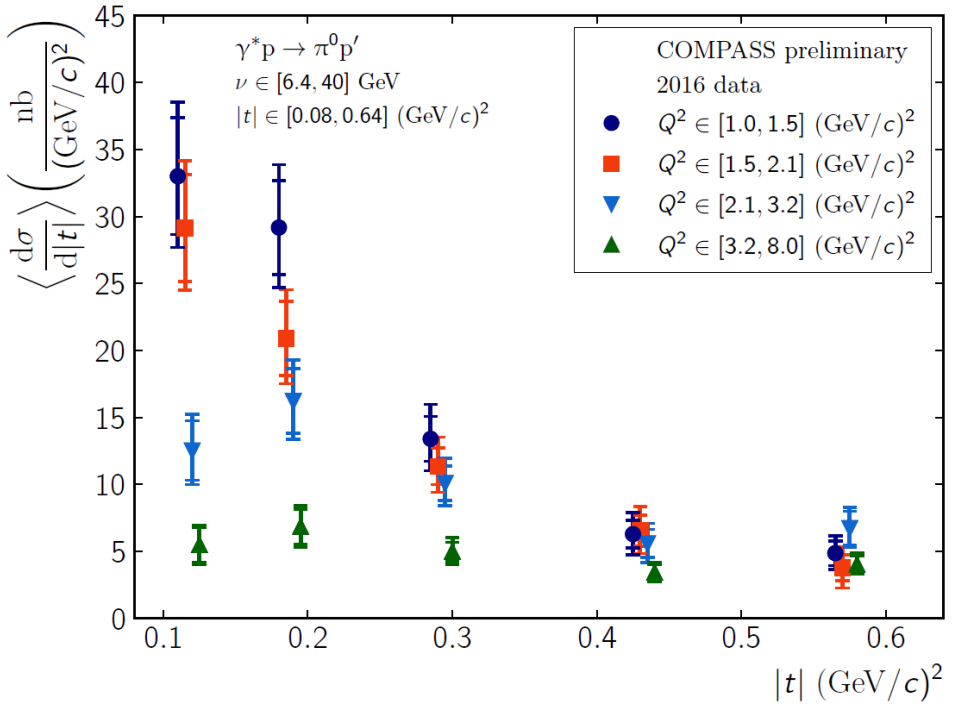


	$\langle\nu\rangle$ [GeV]	$\langle Q^2\rangle$ [GeV$^2/c^2$]	$\langle x_B\rangle$	$\langle\epsilon\rangle$
$\nu \in [6.4, 8.5]$	7.35	2.15	0.156	0.999
$\nu \in [8.5, 13.9]$	10.32	2.50	0.131	0.998
$\nu \in [13.9, 40.0]$	21.08	2.09	0.057	0.989

New 2016 Exclusive π^0 Cross-section Evolution with Q^2

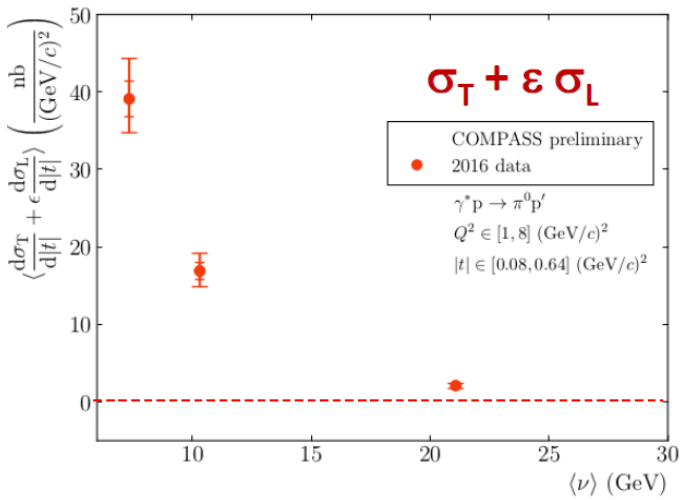
- Cross section decreases with increasing Q^2

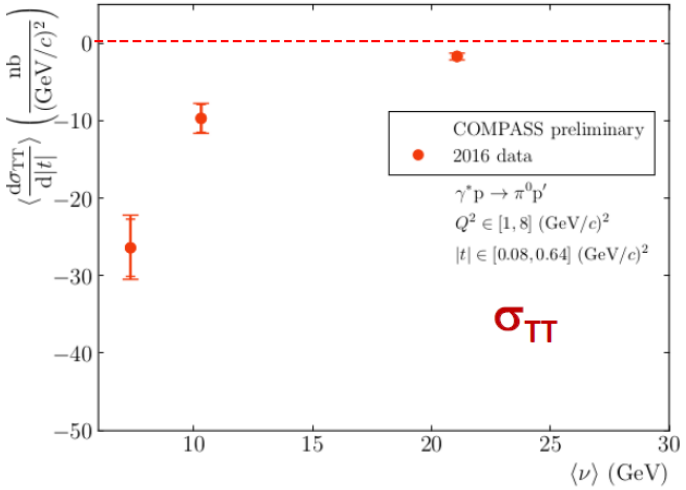


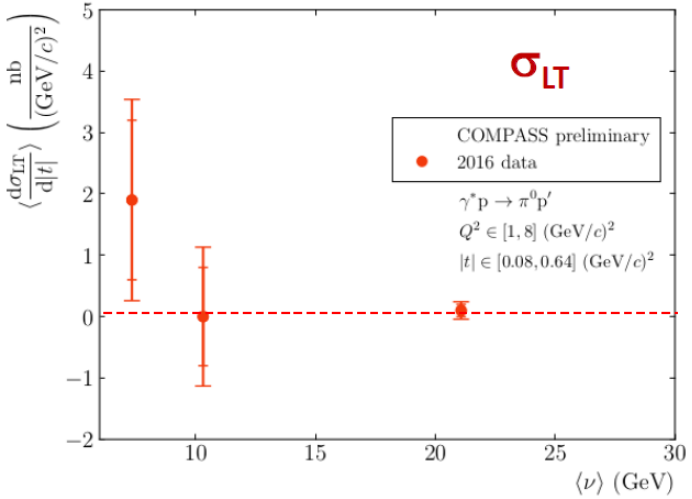


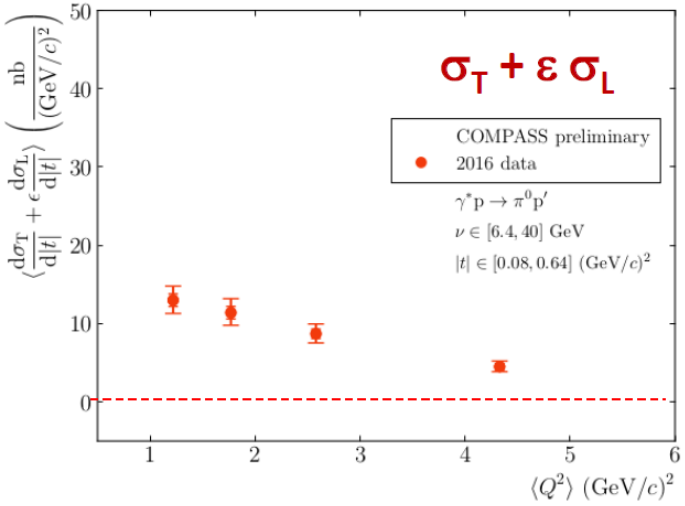
	$\langle Q^2 \rangle$ [GeV$^2/c^2$]	$\langle \nu \rangle$ [GeV]	$\langle x_B \rangle$	$\langle \epsilon \rangle$
$Q^2 \in [1.0, 1.5]$	1.22	10.54	0.072	0.997
$Q^2 \in [1.5, 2.1]$	1.77	9.81	0.109	0.997
$Q^2 \in [2.1, 3.2]$	2.58	9.82	0.157	0.997
$Q^2 \in [3.2, 8.0]$	4.33	10.39	0.247	0.997

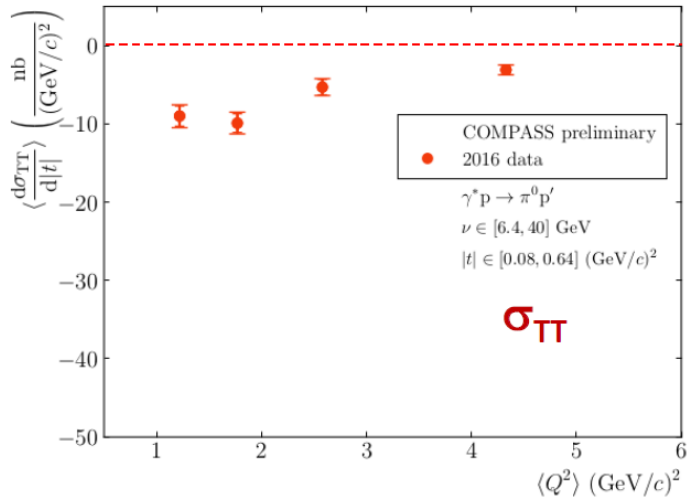
New 2016 Evolution of the Structure Functions

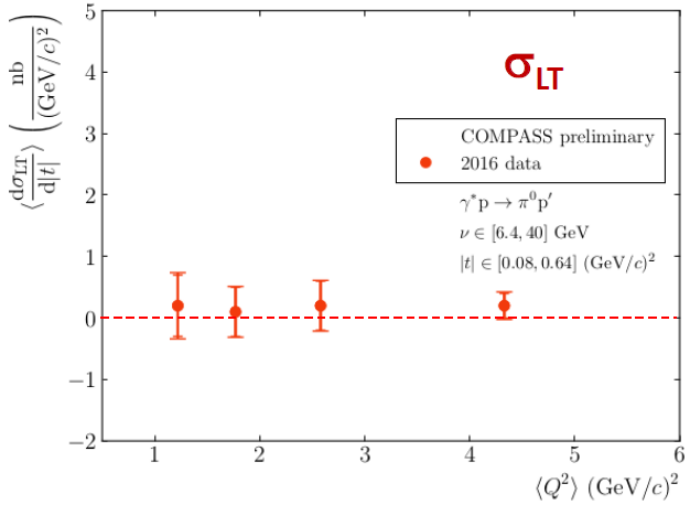










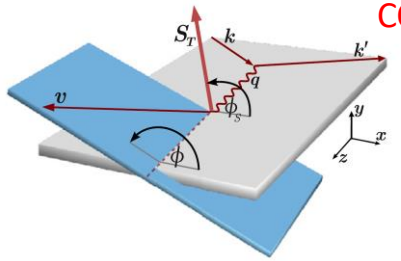


For both $\sigma_T + \epsilon\sigma_L$ and σ_{TT}
→ Relatively larger evolution in ν, smaller in Q^2

σ_{LT} consistent with 0

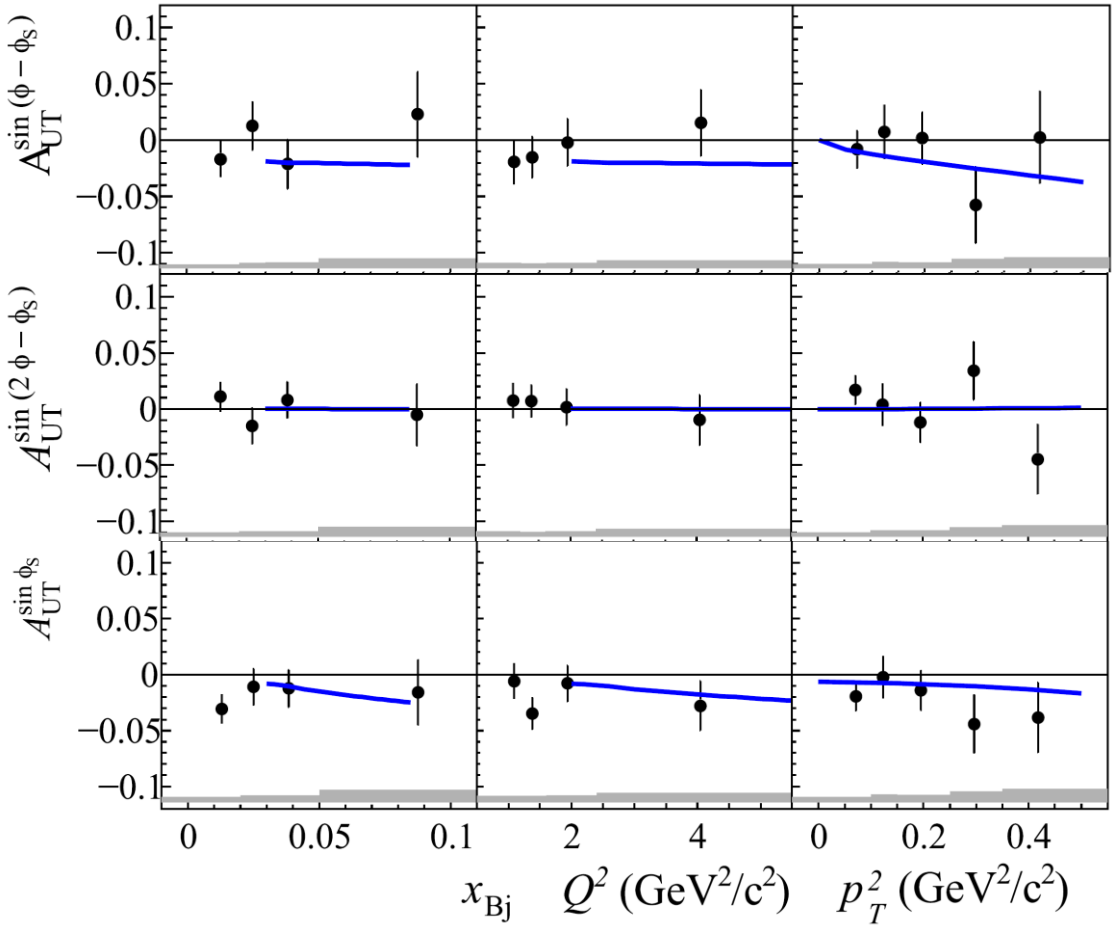
2007 & 2010 HEMP with Transversely Polarized Target

COMPASS, **NPB** 865 (2012) 1-20, **PLB** 731 (2014) 19



$$\rho^0 \to \pi^+\pi^-$$

$$E_{\rho^0} = \frac{1}{\sqrt{2}}\left(\frac{2}{3}E^u + \frac{1}{3}E^d + \frac{3}{4}E^g/x\right)$$

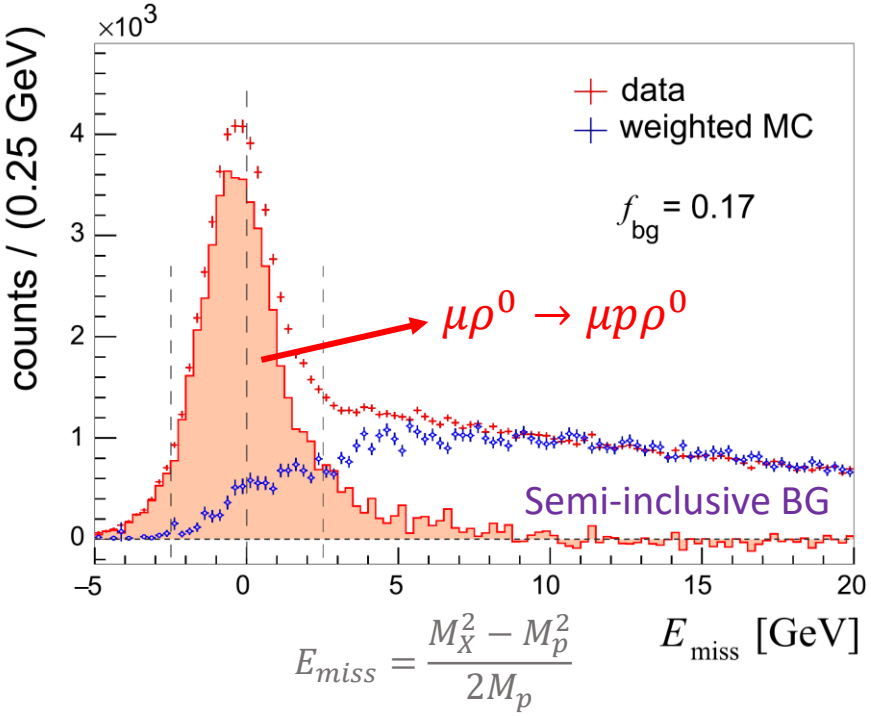


$\propto Im(E^*H)$

$\propto Im(E^*\bar{E}_T)$

$\propto Im(E^*\bar{E}_T - H^*H_T)$

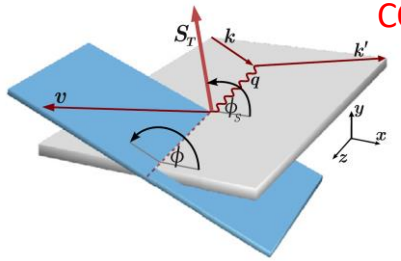
- Exclusivity ensured by "missing mass technique"



- Sensibility to E and H_T

GK Model EPJC 42, 50, 53, 59, 65, 74

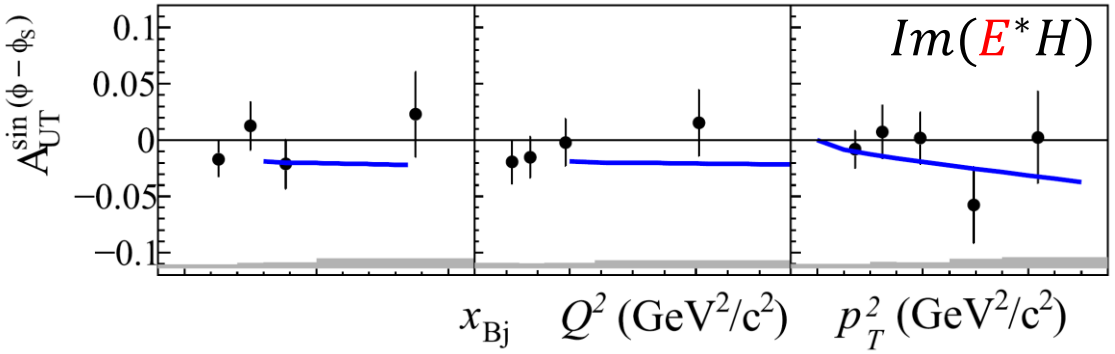
2007 & 2010 HEMP with Transversely Polarized Target



COMPASS, **NPB** 865 (2012) 1-20, **PLB** 731 (2014) 19

$$\rho^0 \rightarrow \pi^+\pi^-$$

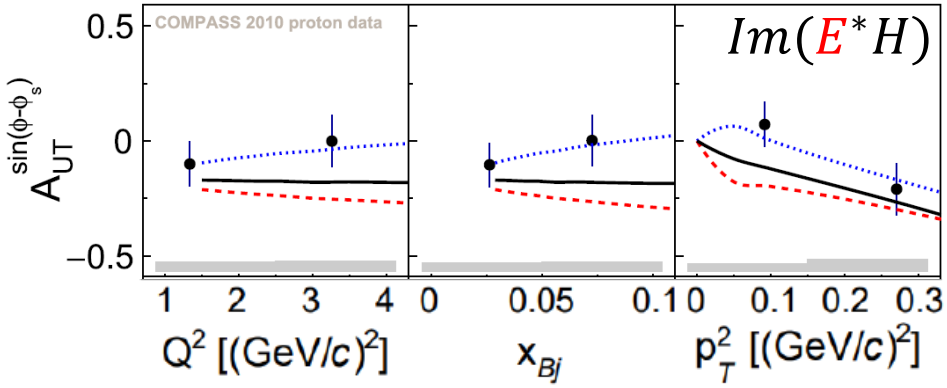
$$E_{\rho^0} = \frac{1}{\sqrt{2}}\left(\frac{2}{3}E^u + \frac{1}{3}E^d + \frac{3}{4}E^g/x\right)$$



COMPASS, **NPB** 865 (2012) 1-20, **PLB** 731 (2014) 19

$$\omega \rightarrow \pi^+\pi^-\pi^0$$

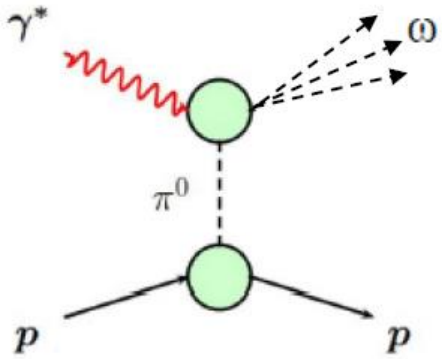
$$E_{\omega} = \frac{1}{\sqrt{2}}\left(\frac{2}{3}E^u - \frac{1}{3}E^d + \frac{1}{4}E^g/x\right)$$



No pion pole

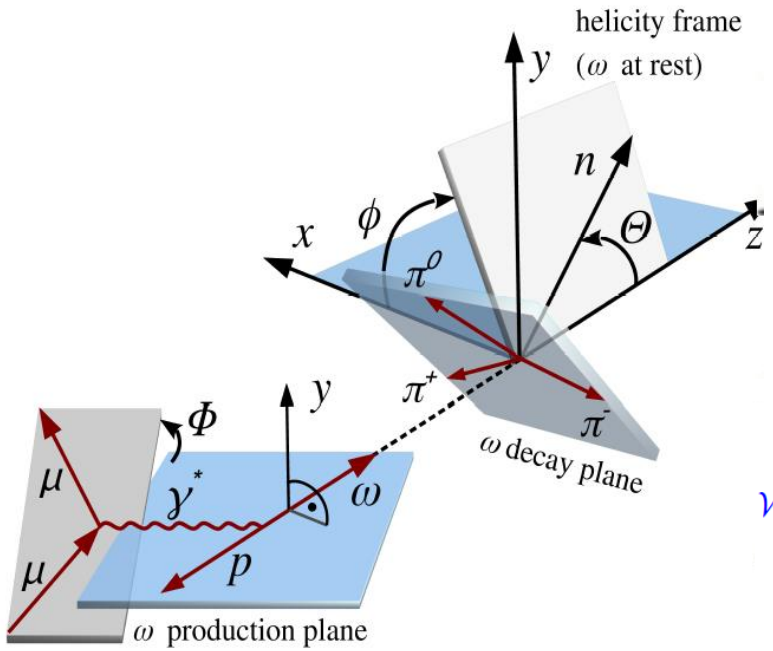
Negative $\pi\omega$ form factor

Positive $\pi\omega$ form factor



- E^u and E^d are of opposite sign → ω is more promising for GPD study
- Nevertheless, obscured by the inherent pion pole contribution

Exclusive ω Production on Unpolarized Proton



Experimental angular distributions

$$\mathcal{W}^{U+L}(\Phi,\phi,\cos\Theta) = \mathcal{W}^{U}(\Phi,\phi,\cos\Theta) + P_b\mathcal{W}^{L}(\Phi,\phi,\cos\Theta)$$

15 unpolarized SDMEs in $\mathcal{W}^U$ and 8 polarized in $\mathcal{W}^L$

$$\begin{aligned}
\mathcal{W}^{U}(\Phi,\phi,\cos\Theta) = \frac{3}{8\pi^2}\Big[&\frac{1}{2}(1-r^{04}_{00}) + \frac{1}{2}(3r^{04}_{00}-1)\cos^2\Theta - \sqrt{2}\mathrm{Re}\{r^{04}_{10}\}\sin 2\Theta\cos\phi - r^{04}_{1-1}\sin^2\Theta\cos 2\phi \\
&-\epsilon\cos 2\Phi\left(r^{1}_{11}\sin^2\Theta + r^{1}_{00}\cos^2\Theta - \sqrt{2}\mathrm{Re}\{r^{1}_{10}\}\sin 2\Theta\cos\phi - r^{1}_{1-1}\sin^2\Theta\cos 2\phi\right) \\
&-\epsilon\sin 2\Phi\left(\sqrt{2}\mathrm{Im}\{r^{2}_{10}\}\sin 2\Theta\sin\phi + \mathrm{Im}\{r^{2}_{1-1}\}\sin^2\Theta\sin 2\phi\right) \\
&+\sqrt{2\epsilon(1+\epsilon)}\cos\Phi\left(r^{5}_{11}\sin^2\Theta + r^{5}_{00}\cos^2\Theta - \sqrt{2}\mathrm{Re}\{r^{5}_{10}\}\sin 2\Theta\cos\phi - r^{5}_{1-1}\sin^2\Theta\cos 2\phi\right) \\
&+\sqrt{2\epsilon(1+\epsilon)}\sin\Phi\left(\sqrt{2}\mathrm{Im}\{r^{6}_{10}\}\sin 2\Theta\sin\phi + \mathrm{Im}\{r^{6}_{1-1}\}\sin^2\Theta\sin 2\phi\right)\Big],
\end{aligned}$$

$$\begin{aligned}
\mathcal{W}^{L}(\Phi,\phi,\cos\Theta) = \frac{3}{8\pi^2}\Big[&\sqrt{1-\epsilon^2}\left(\sqrt{2}\mathrm{Im}\{r^{3}_{10}\}\sin 2\Theta\sin\phi + \mathrm{Im}\{r^{3}_{1-1}\}\sin^2\Theta\sin 2\phi\right) \\
&+\sqrt{2\epsilon(1-\epsilon)}\cos\Phi\left(\sqrt{2}\mathrm{Im}\{r^{7}_{10}\}\sin 2\Theta\sin\phi + \mathrm{Im}\{r^{7}_{1-1}\}\sin^2\Theta\sin 2\phi\right) \\
&+\sqrt{2\epsilon(1-\epsilon)}\sin\Phi\left(r^{8}_{11}\sin^2\Theta + r^{8}_{00}\cos^2\Theta - \sqrt{2}\mathrm{Re}\{r^{8}_{10}\}\sin 2\Theta\cos\phi - r^{8}_{1-1}\sin^2\Theta\cos 2\phi\right)\Big]
\end{aligned}$$

- $\epsilon \to 1$, small $\mathcal{W}^L$

2012 Exclusive ω Prod. on Unpolarized Proton

SCHC ($\lambda_\gamma = \lambda_V$)
(S-Channel Helicity Conservation)

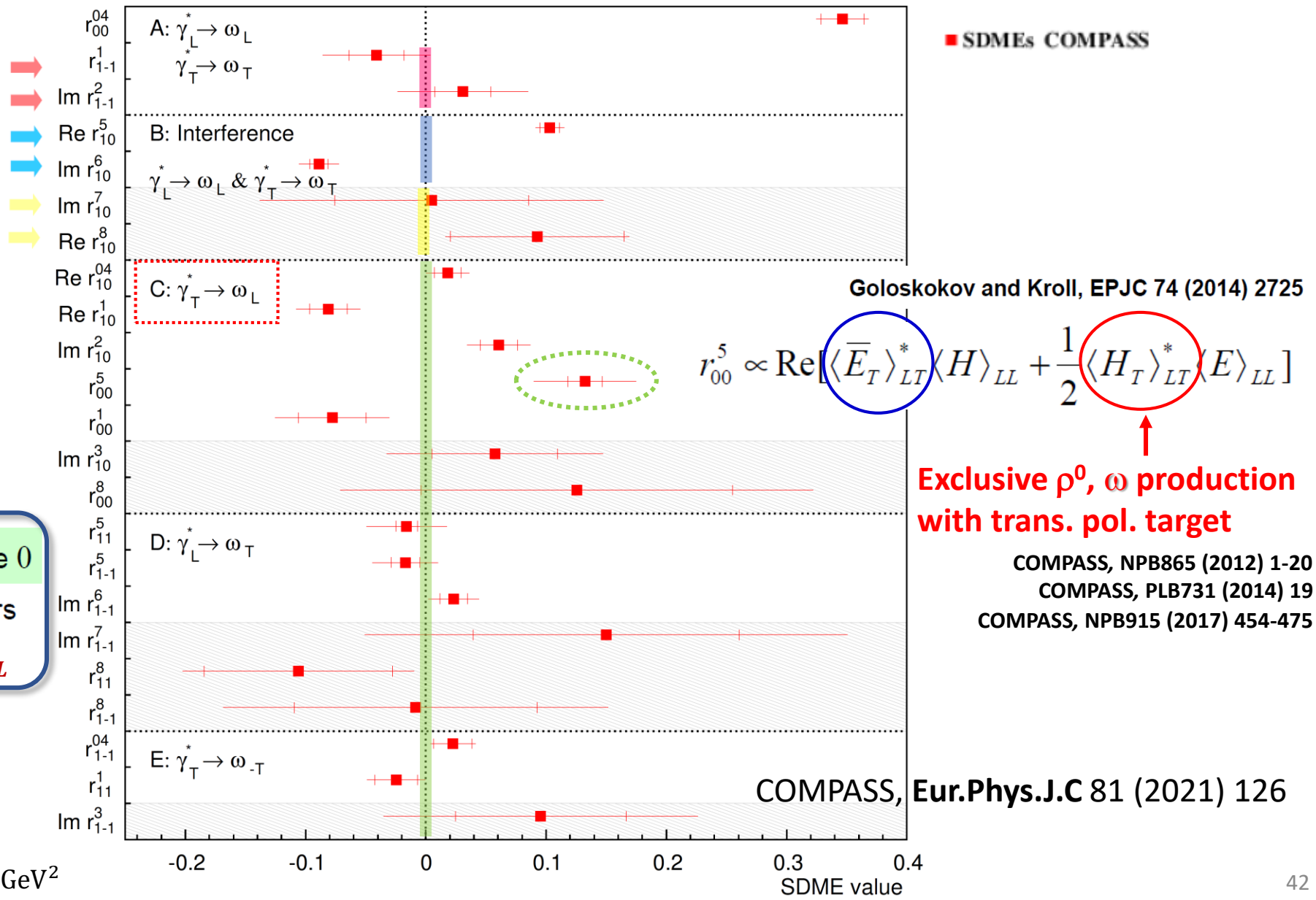
SCHC implies:

- $r^1_{1-1} + \mathrm{Im}\, r^2_{1-1} = 0$
  = - 0.010 ± 0.032 ± 0.047 OK
- $\mathrm{Re}\, r^5_{10} + \mathrm{Im}^6_{10} = 0$
  = 0.014 ± 0.011 ± 0.013 OK
- $\mathrm{Im}\, r^7_{10} - \mathrm{Re}\, r^8_{10} = 0$
  = - 0.088 ± 0.110 ± 0.196 OK

- all elements of classes C, D, E should be 0

for $\gamma^*_L \to \omega_T$ and $\gamma^*_T \to \omega_{-T}$ OK within errors

NOT OBSERVED for transitions $\gamma^*_T \to \omega_L$



■ SDMEs COMPASS

Goloskokov and Kroll, EPJC 74 (2014) 2725

$$r^5_{00} \propto \mathrm{Re}\left[\langle \bar{E}_T \rangle^*_{LT} \langle H \rangle_{LL} + \frac{1}{2} \langle H_T \rangle^*_{LT} \langle E \rangle_{LL}\right]$$

Exclusive ρ^0, ω production with trans. pol. target

COMPASS, NPB865 (2012) 1-20
COMPASS, PLB731 (2014) 19
COMPASS, NPB915 (2017) 454-475

COMPASS, **Eur.Phys.J.C** 81 (2021) 126

$\langle Q^2 \rangle = 2.1\ \mathrm{GeV}^2, \langle W \rangle = 7.6\ \mathrm{GeV}, \langle P_T^2 \rangle = 0.16\ \mathrm{GeV}^2$

2012 Exclusive ρ^0 Prod. on Unpolarized Proton

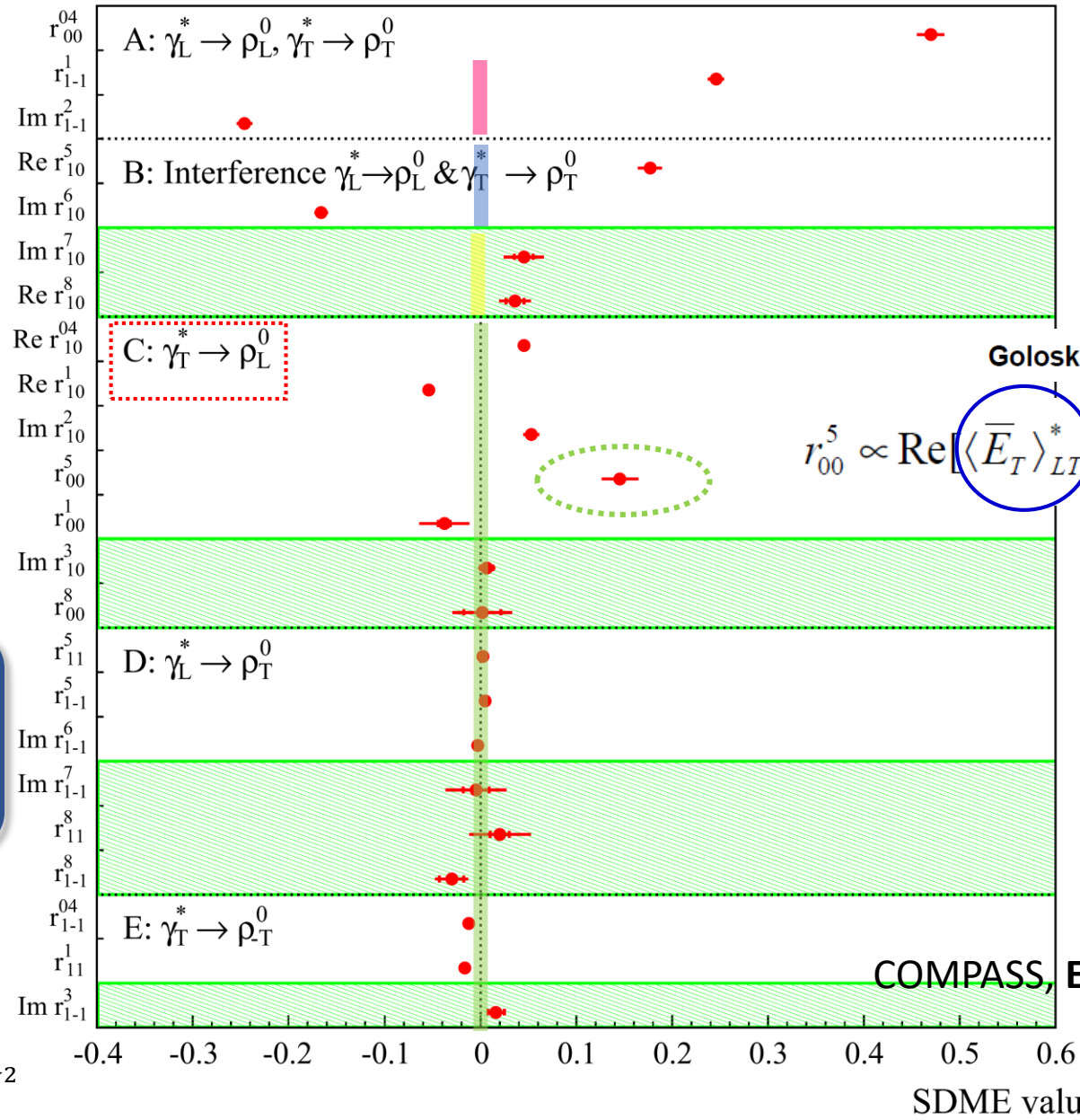
SCHC ($\lambda_\gamma = \lambda_V$)
(S-Channel Helicity Conservation)

SCHC implies:

- $r^1_{1-1} + \mathrm{Im}\, r^2_{1-1} = 0$
  = -0.000 ± 0.006 OK
- $\mathrm{Re}\, r^5_{10} + \mathrm{Im}^6_{10} = 0$
  = -0.011 ± 0.003 Violation
- $\mathrm{Im}\, r^7_{10} - \mathrm{Re}\, r^8_{10} = 0$
  = -0.009 ± 0.031 OK

- all elements of classes C, D, E should be 0
  for $\gamma^*_L \to \omega_T$ and $\gamma^*_T \to \omega_{-T}$ OK within errors

NOT OBSERVED for transitions $\gamma^*_T \to \rho^0_L$



■ SDMEs COMPASS

Goloskokov and Kroll, EPJC 74 (2014) 2725

$$r^5_{00} \propto \mathrm{Re}\left[\langle \bar{E}_T \rangle^*_{LT} \langle H \rangle_{LL} + \frac{1}{2} \langle H_T \rangle^*_{LT} \langle E \rangle_{LL}\right]$$

First term dominates
→ Probes $\bar{E}_T$

COMPASS, **Eur.Phys.J.C** 83 (2023) 924

$\langle Q^2 \rangle = 2.4\ \mathrm{GeV}^2, \langle W \rangle = 9.9\ \mathrm{GeV}, \langle P_T^2 \rangle = 0.18\ \mathrm{GeV}^2$

Summary

DVCS cross sections with polarized μ+ and μ-

- Beam charge-spin sum → Im$\mathcal{H}$(ξ,t) → Transverse extension of partons as a function of x_{Bj}
- Beam charge-spin difference → Re$\mathcal{H}$(ξ,t) → D-term, pressure distribution

HEMP of π^0, ρ, ω, ϕ, J/ψ

- Cross setion of π^0 → To be published
- SDME of ρ & ω → Transversity GPDs & Flavor Decomposition
- ϕ, J/ψ → underway

➢ **COMPASS has entered its analysis phase, expect more results soon!**

Backup Slides

➢ Main background of exclusive single photon events: π^0 decay

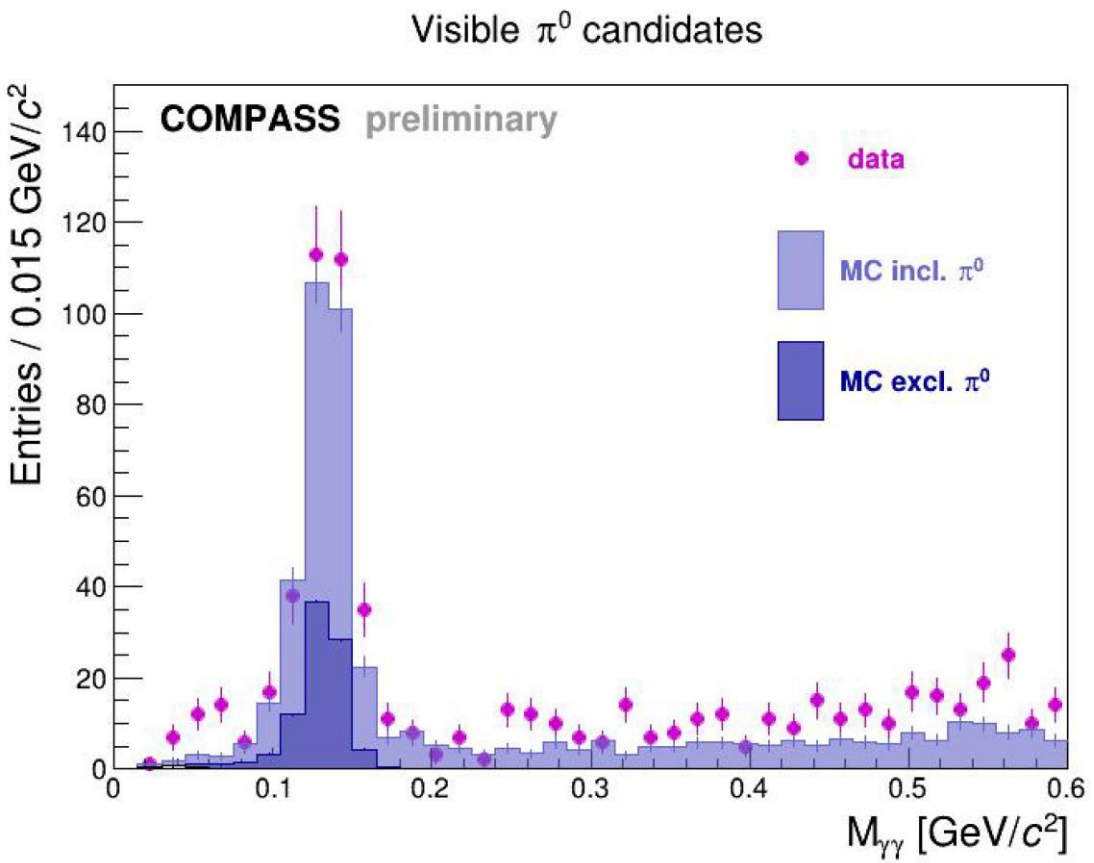
➢ **Visible** (both γ detected) – subtracted

A high-energy DVCS photon candidate is combined with all detected photons with energies lower than the DVCS threshold: (4,5) GeV in Ecal (0,1) respectively

➢ **Invisible** (one γ lost) – estimated by MC

- **Semi-inclusive LEPTO 6.1**
- **Exclusive HEPGEN π^0** (GK model)

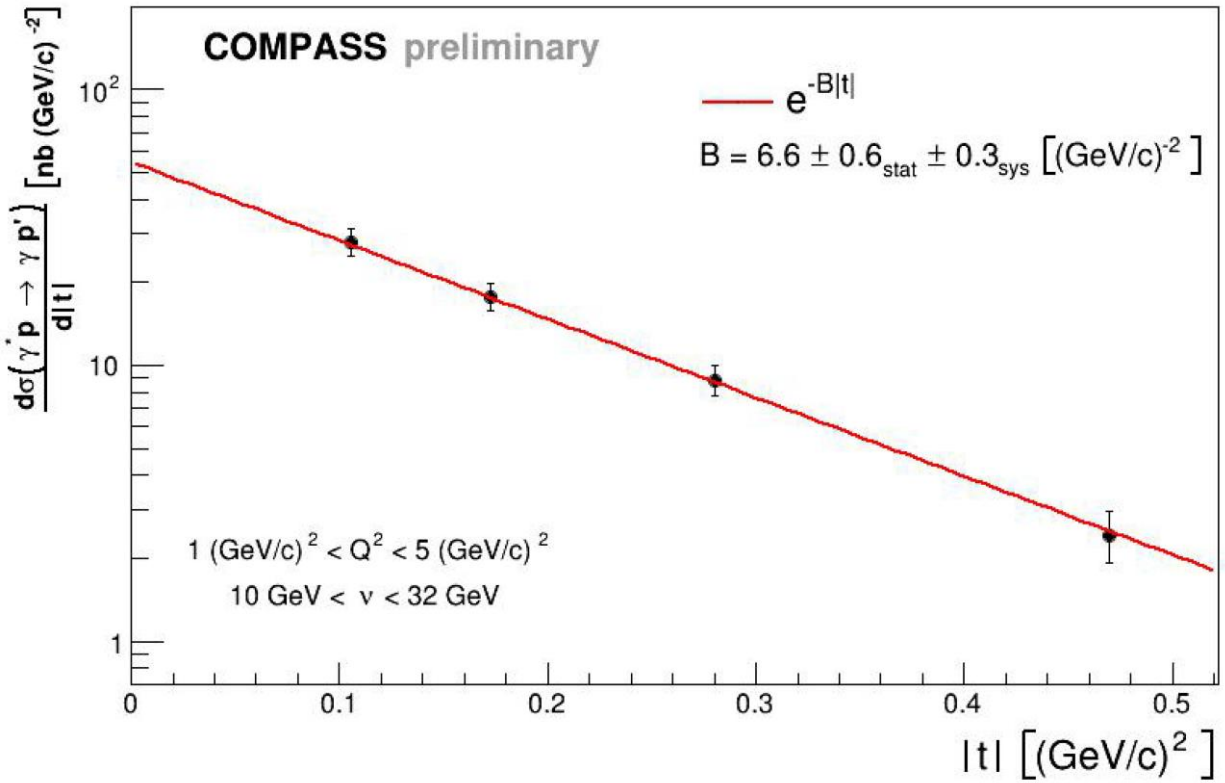
The sum of LEPTO and HEPGEN contributions is normalized to the π^0 peak in $M_{\gamma\gamma}$ of the real data

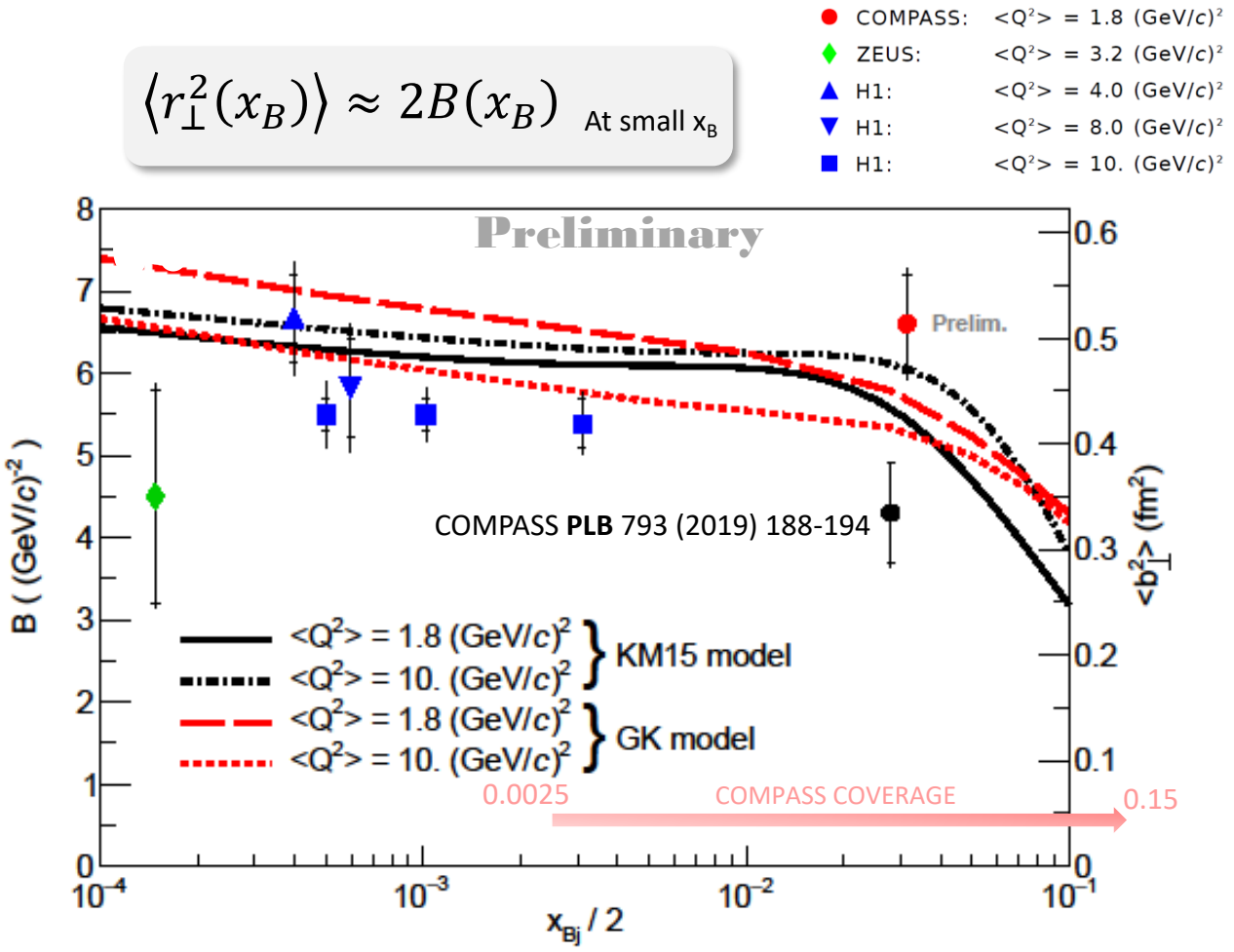


Tranverse extension of partons – 2016 data

$d\sigma^{DVCS}/d|t| \propto e^{-B|t|}$

$\langle r_\perp^2(x_B)\rangle \approx 2B(x_B)$ At small x_B





➢ The transverse-size evolution as a function of x_{Bj} → Expect at least 3 x_{Bj} bins from 2016-17 data

Beam Charge-spin Difference

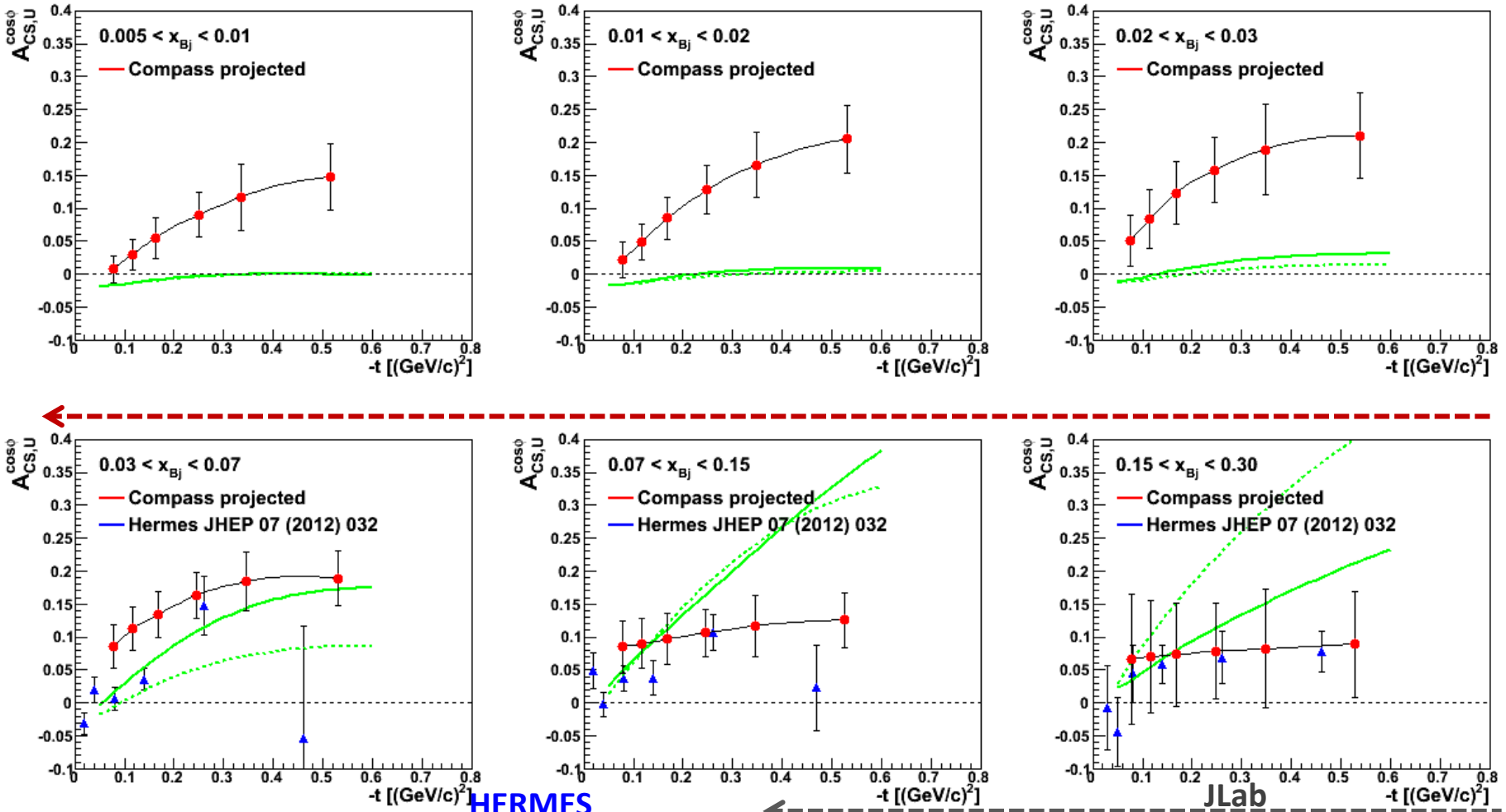
$$\mathcal{D}_{CS,U}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) - d\sigma(\mu^{-\rightarrow}) \rightarrow c_0^I + c_1^I \cos\phi$$

$$\text{BCSA} = \mathcal{D}_{CS,U}/S_{CS,U} = A_0 + A_{CS,U}^{\cos\phi}\cos\phi + A_2\cos 2\phi$$

$c_1^I \rightarrow \mathcal{R}e\, F_1\mathcal{H}$

VGG

KM10 – fit to data



- With $\mathcal{R}e\, F_1\mathcal{H}$ and $Im\, F_1\mathcal{H}$
  → Extraction of D-term

$\mathcal{R}e\,\mathcal{H}$ **> 0** at H1

< 0 at HERMES

Value of x_{Bj} for the node?

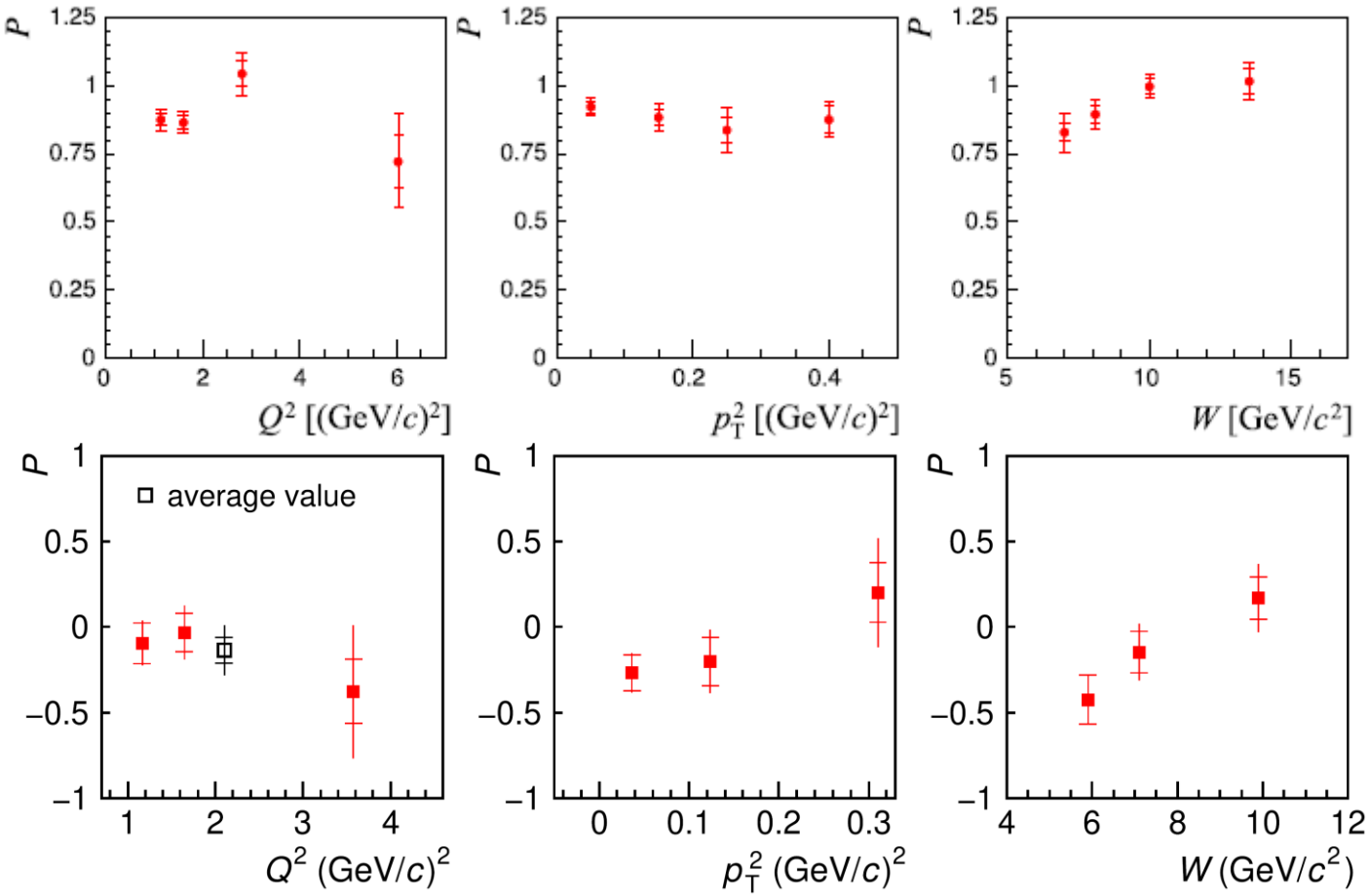
COMPASS 2 years of data Eμ= 160 GeV $1 < Q^2 < 8$ GeV²

2012 NPE-to-UPE Asymmetry

$$P = \frac{2r^1_{1-1}}{1 - r^{04}_{00} - 2r^{04}_{1-1}} \approx \frac{d\sigma^N_T(\gamma^*_T \to V_T) - d\sigma^U_T(\gamma^*_T \to V_T)}{d\sigma^N_T(\gamma^*_T \to V_T) + d\sigma^U_T(\gamma^*_T \to V_T)}$$

NPE-to-UPE asymmetry of cross sections for transitions $\gamma^*_T \to V_T$

- NPE: Natural Parity Exchange
- UPE: Unnatural Parity Exchange



ρ^0

COMPASS, **Eur.Phys.J.C** 83 (2023) 924

- **NPE Dominance**
- **NPE → GPDs E, H**

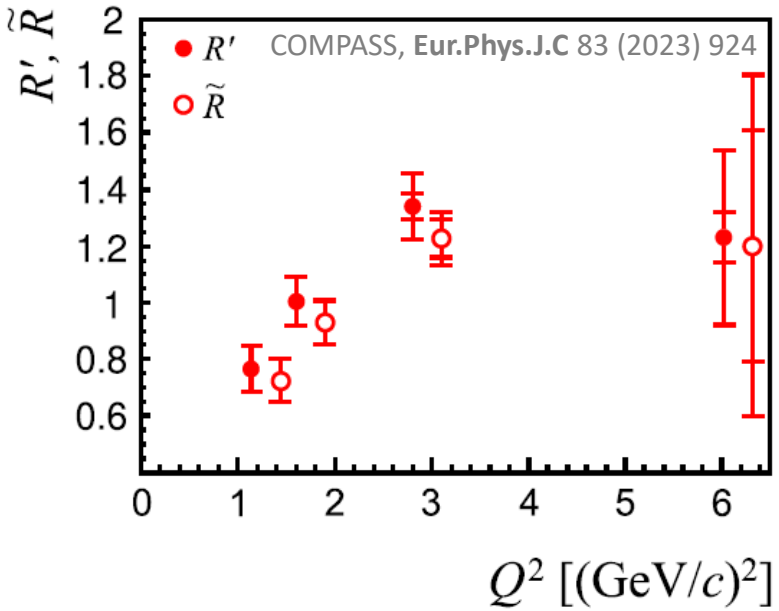
ω

COMPASS, **Eur.Phys.J.C** 81 (2021) 126

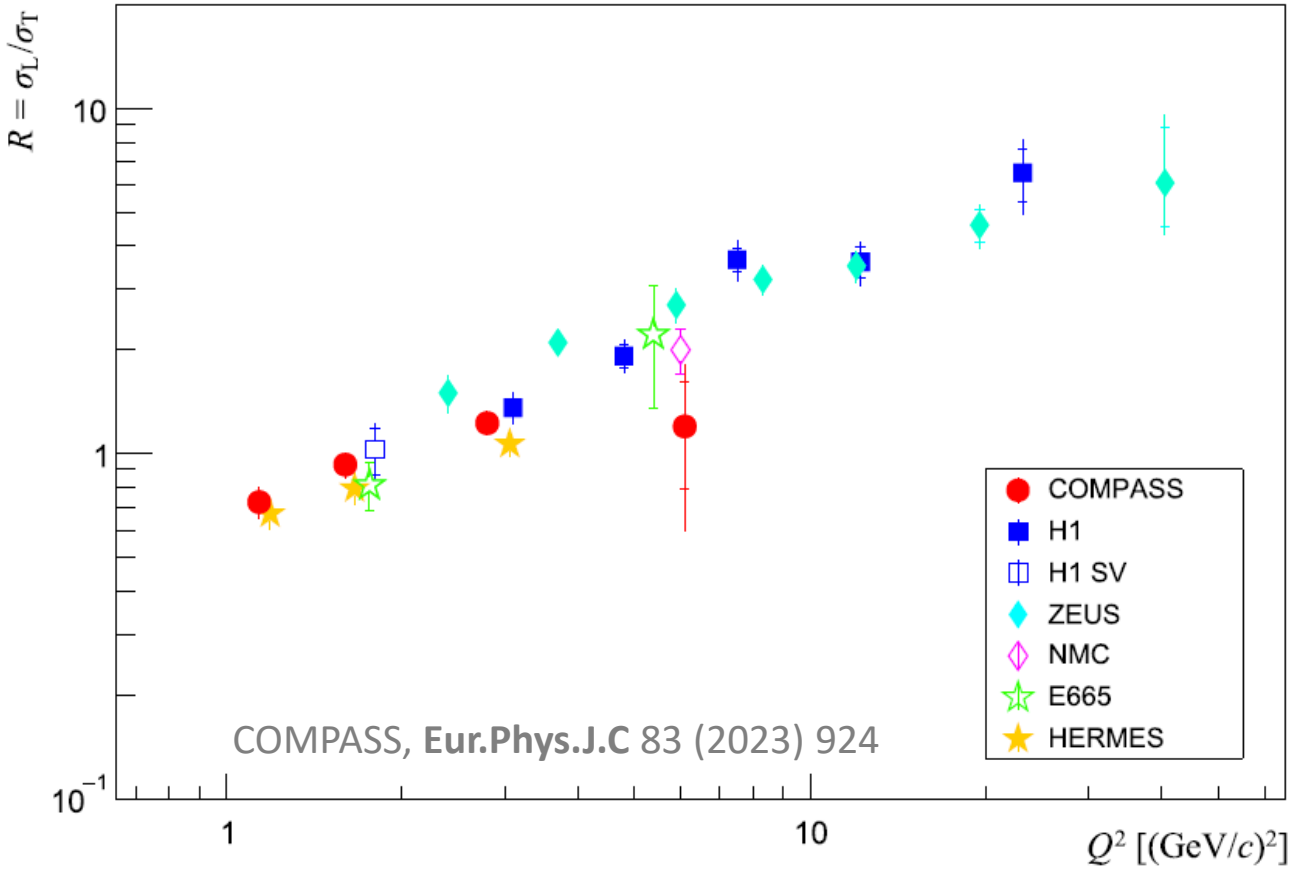
- **NPE ≈ UPE on average**
- **UPE Dominance at small W and p_T^2**
- **UPE → GPDs $\widetilde{E}, \widetilde{H}$**
  + Pion pole (dominant)

2012 $R = \sigma_L/\sigma_T$ for Exclusive ρ^0 Production

- Longitudinal-to-transverse γ^* cross section ratio: $R = \dfrac{\sigma_L(\gamma_L^* \to V)}{\sigma_T(\gamma_T^* \to V)}$
- Commonly used "effective" ratio ($R' = R$ only if SCHC): $R' = \dfrac{1}{\epsilon}\dfrac{r_{00}^{04}}{1 - r_{00}^{04}}$
- Use of $\tilde{R}$, which takes SCHC violation into consideration, is preferred.



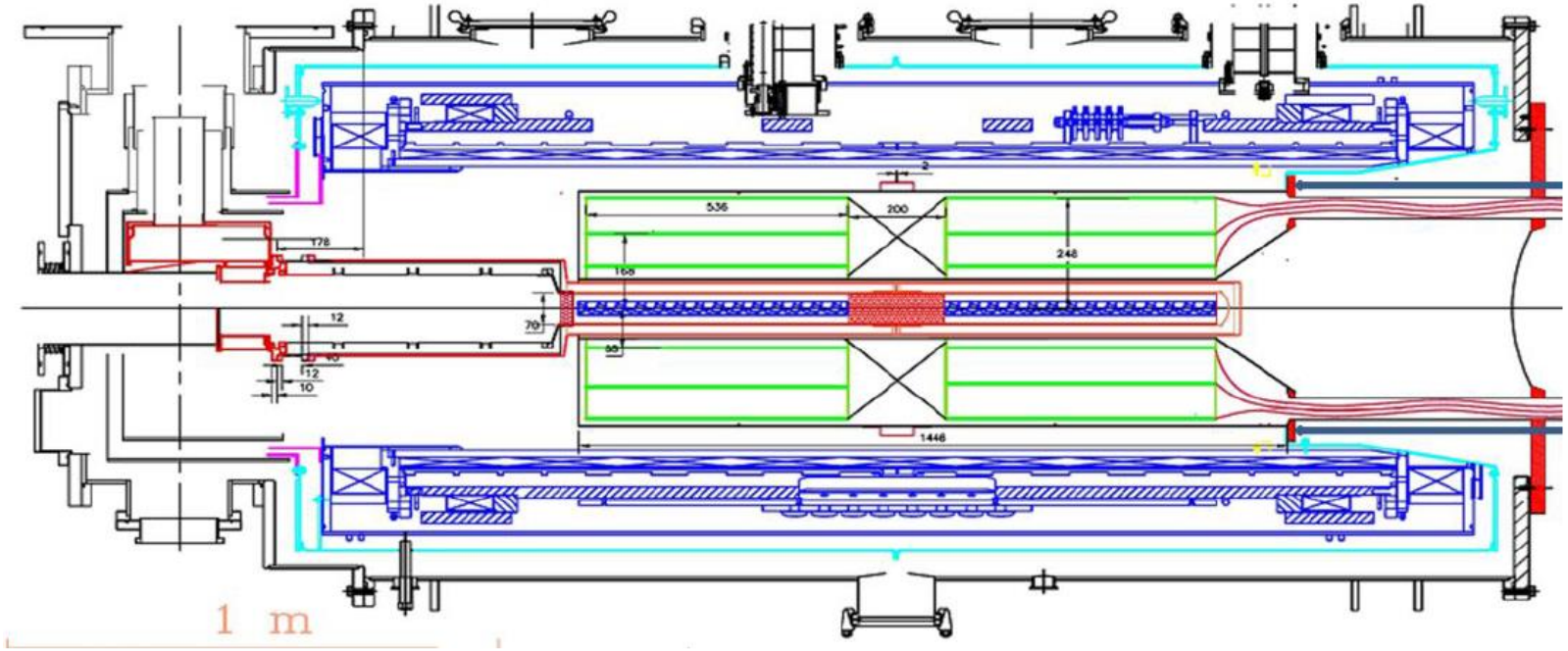
Results of all experiments with $Q^2 > 1$ (GeV/c)^2

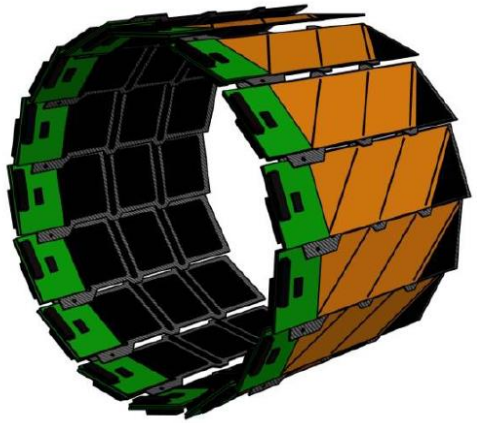


- Leading-order pQCD predction: Q^2/M_ρ^2 → deviation due to effect of QCD evolution and q_T

Possible RPD for COMPASS^{++}/AMBER

A recoil proton detector (RPD) is mandatory to ensure the exclusivity. A Silicon detector is included *between* the target surrounded by the modified MW cavity *and* the polarizing magnet





A technology developed at JINR for NICA for the BM@N experiment

No possibility for ToF ➔ PID of p/π with dE/dx

Momentum and trajectory measurments

$|t|_{min} \sim 0.1$ GeV