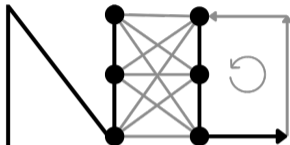


Hands on NeuLat: A Toolbox for **N**eural Samplers in **L**attice Field Theory



N E U L A T

Kim A. Nicoli, Christopher J. Anders et al.

December 06, 2024 - Taipei
Lattice Field Theory and Machine Learning Workshop

code: <https://github.com/neulat/neulat>

preprint: [LATTICE2023 PoS 286](#)

Sampling from Boltzmann Distributions

$$p(\phi) = \frac{\exp\{-S[\phi]\}}{Z}$$

Sampling from Boltzmann Distributions... with Generative Models

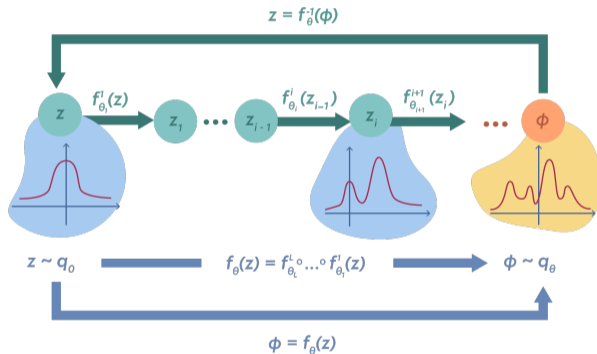
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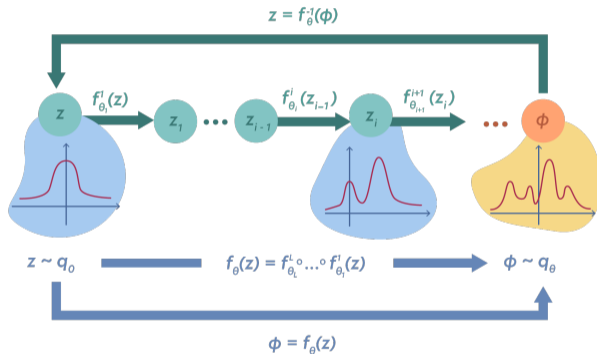
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Bare with me for now, and wait for Tej's Mathis' and Fernando's talks tomorrow!

Sampling with Normalizing Flows



Sampling with Normalizing Flows



$$q_{\theta}(\phi) = q_0(f_{\theta}^{-1}(\phi)) \left| \det \left(\frac{\partial f_{\theta}}{\partial z} \right) \right|^{-1}$$

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Benefits of Research Software Packages

- faster development of new ideas

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Existing examples:

- **SchNetPack** - Deep Neural Networks for Atomistic Systems
- **BGFlow** - Boltzmann Generators (BG) and other sampling methods

Why NeuLat?

There are already great tools available!

- Introduction to Normalizing Flows for LFT [[Albergo et al., 2101.08176 \(2021\)](#)]

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 - **nflows** [[github.com/VincentStimper/normalizing-flows](#)] (V. Stimper et al.)

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 - **GomalizingFlow.jl** [[github.com/AtelierArith/GomalizingFlow.jl](#)] (A. Tomiya)
 - **NeuMC** [[github.com/nmcmc/nmcmc-code](#)] (P. Bialas)

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But: We want to create a **highly customizable reference implementation**.

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- **Density Estimator:** Learn approximations of targeted Boltzmann distributions

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- **Modularity and Customizability:** Swiftly incorporate new actions/theories/models/techniques

Action

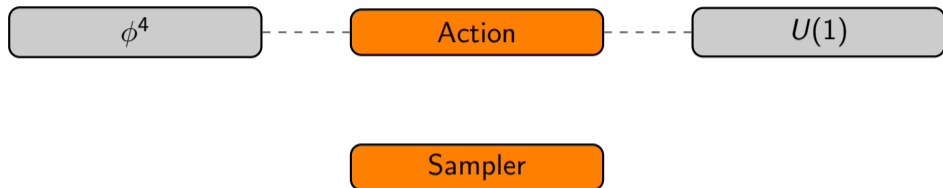
Actions $S[U]$ define target Boltzmann distributions $p(U) \propto e^{-S[U]}$

NeuLat Overview



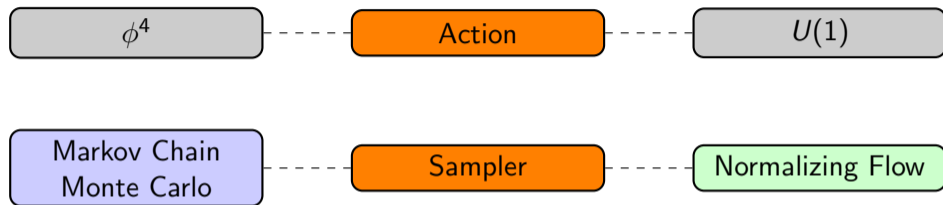
Actions are, e.g., ϕ^4 and $U(1)$

NeuLat Overview



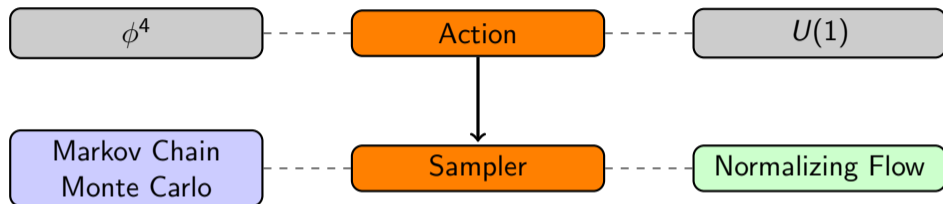
Samplers are **anything** that can be sampled from

NeuLat Overview



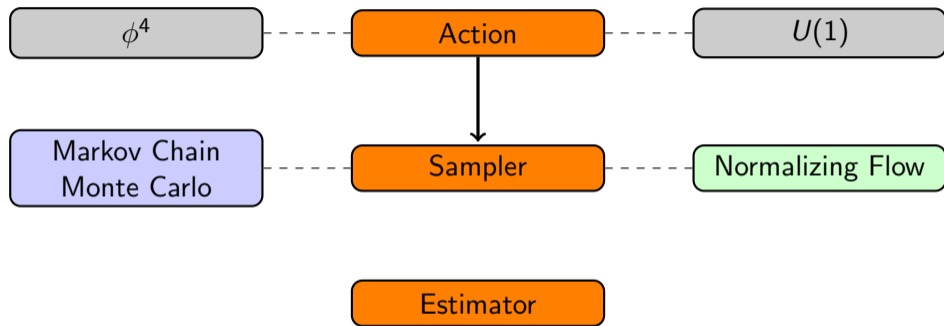
Samplers are, e.g., MCMCs, Flows, $\mathcal{N}(0, 1)$

NeuLat Overview



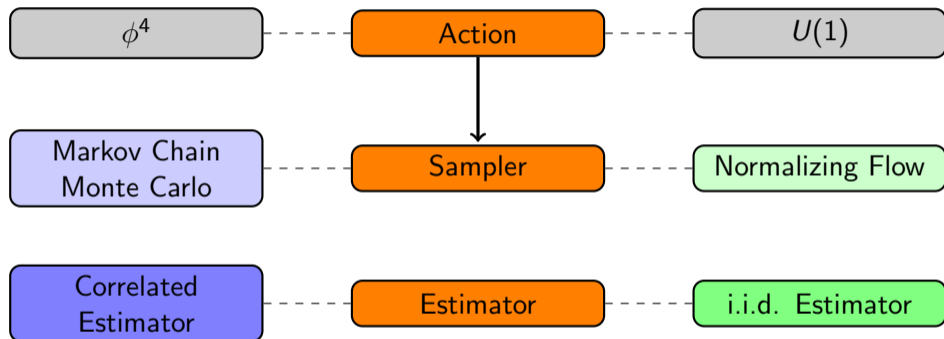
Samplers **require** Actions

NeuLat Overview



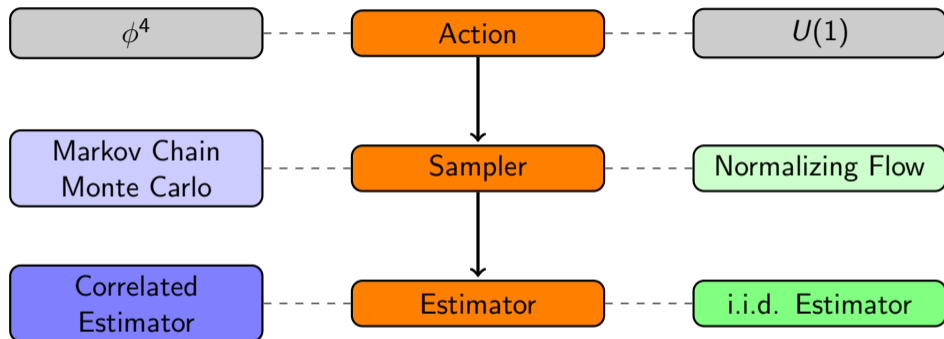
Estimators are used to estimate observables

NeuLat Overview



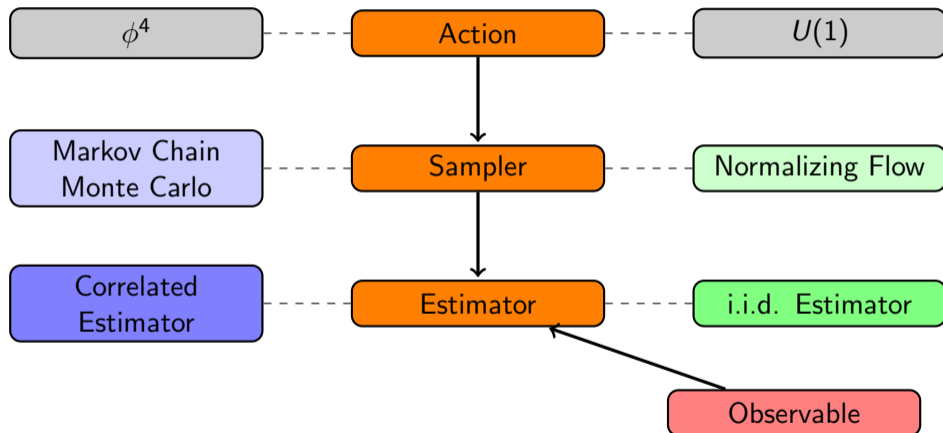
Estimators are, e.g., **i.i.d** or **correlated**, based on the samples

NeuLat Overview



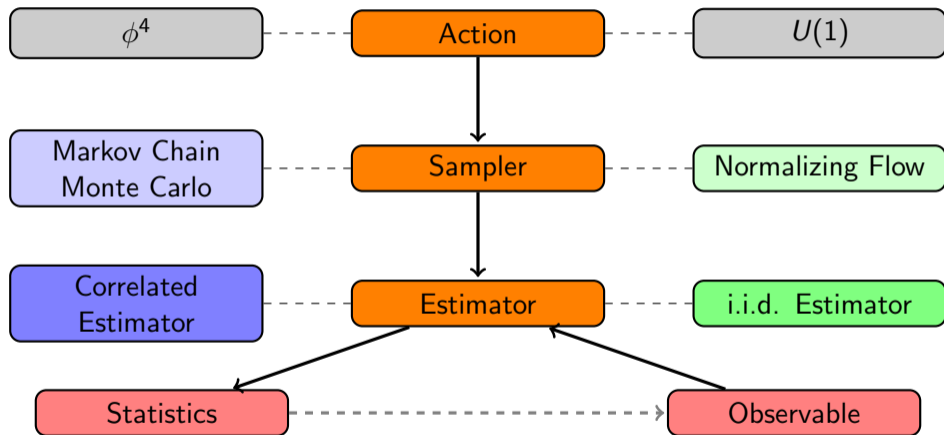
Estimators require **samples** from Samplers

NeuLat Overview



Observables, e.g., Magnetization, Topological Charge, etc., are used by the Estimator

NeuLat Overview



The resulting Statistics are **estimations** for the Observables

Actions

Actions are classes (objects) and need to be instantiated.

```
1 import torch
2 from neulat.action.phi4 import Phi4Action
3
4 # ndim_features is the number of dimensions in the lattice
5 action = Phi4Action(kappa=0.3, lamb=0.022, ndim_features=2)
```

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```

Action objects can be called to compute action values for configurations.

```
1 config = torch.randn(8, 8)
2 unnormalized_prob = torch.exp(-action(config))
```

Defining Actions

Actions are **very simple** to implement, for instance the ϕ^4 action reads:

```
1  from neulat.action.base import Action
2
3  class Phi4Action(Action):
4      name = 'phi4_action'
5      def __init__(self, kappa, lambda, ndim_feature=2):
6          ...
7      def forward(self, config):
8          dims = tuple(range(-1, -self.ndim_feature, -1))
9          kinetic = (-2 * self.kappa) * config * sum(
10             torch.roll(config, 1, dim) for dim in dims)
11          mass = (1 - 2 * self.lambda) * config ** 2
12          inter = self.lambda * config ** 4
13          return (kinetic + mass + inter).sum(dim=dims)
```


Samplers

At the core of NeuLat are Samplers, which are anything from which we can **sample**.

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For instance, the normal distribution is also a Sampler in NeuLat:

```
1 from neulat.sampler.distribution import Normal
2
3 normal = Normal(loc=0., scale=1., feature_shape=(8, 8))
```

Sampling

Samplers can sample, and **may or may not** support probability values.

```
1 samples = normal.sample(sample_shape=8)
2 logprobs = normal.logprob(samples)
3
4 samples2, logprobs2 = normal.sample_with_logprob((2, 2))
```

Sampling

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```

In NeuLat, we assume configurations of shape (`*sample_shape`, `*feature_shape`).

- `sample_shape` is the number of samples, supporting arbitrary shapes
- `feature_shape` is the shape of the lattice (i.e., # of dimensions)

Hamiltonian Monte Carlo

A more involved Sampler is the HMC:

```
1  from neulat.sampler.mc.hmc import HMCMarkovChain
2
3  hmc = HMCMarkovChain(
4      action, # action
5      feature_shape=(8, 8), # lattice shape
6      burn_in=5000, # equilibration steps
7      skip_interval=1, # skipped samples in chain
8      overrelax_interval=50, # steps between sign flips
9      eps=0.05, # step size along a trajectory
10     traj_steps=20, # number of steps in the trajectory
11     bias=0.0, # bias in initialization
12 )
```

HMC Sampling 1/2

As for any Sampler, we can sample from HMC

```
1 configs = hmc.sample(sample_shape=13)
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```

However, HMC does not implement `logprob` and, by extension, `sample_with_logprob`, as no normalized probabilities are available.
(unnormalized logprobs possible)

```
1 # both cause exceptions:  
2 # logprobs = hmc.logprob(sample_shape=13)  
3 # configs2, logprobs2 = hmc.sample_with_logprob(13)
```

HMC Sampling 2/2

One can also iterate over HMC chains to sample

```
1 configs = []
2 for n, config in zip(range(25), hmc):
3     configs.append(config)
4     print(f'Sampled config number {n}.')
5
6 # this gives a list of configs, combine them:
7 configs = torch.cat(configs)
```


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!! But be careful, HMC chains are infinite iterators. !!

Normalizing Flows

Normalizing flows [Papamakarios et al., JMLR (2021)] require a base distribution, and a transform.

```
1 from neulat.sampler.flow import Flow, SequentialTransform
2
3 flow = Flow(
4     base_distribution=Normal(feature_shape=(8, 8)),
5     transform=SequentialTransform([]) # identity for demo
6 )
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Normalizing flows are **(i.i.d.) Samplers supporting logprobs.**

```
1 configs, logprobs = flow.sample_with_logprob(8)
```

Normalizing Flows: Base Distributions

The base distribution can be any sampler that supports logprobs.

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Commonly, simple distributions such as $\mathcal{N}(0, 1)$ are used.

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```

Flows themselves **support logprobs**, and can thus **be base distributions**.

```
1 flow2 = Flow(  
2     base_distribution=flow,  
3     transform=SequentialTransform([]) # identity for demo  
4 )
```

Normalizing Flows: Transforms 1/2

Transforms are (optionally) invertible PyTorch modules, and require (either or both) a `forward` and a `inverse`.

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E.g., implementation for transform $f(\mathbf{x}) = -\mathbf{x}$, $f^{-1}(\mathbf{x}) = -\mathbf{x}$

```
1  from sampler.flow.base import Transform, withlogdet
2
3  class FlipSign(Transform):
4      @withlogdet
5      def forward(self, input):
6          return -input, 0.
7      @withlogdet
8      def inverse(self, input):
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Decorator @withlogdet ensures the logdet is accumulated between transforms.

Normalizing Flows: Transforms 2/2

A useful transform is the `SequentialTransform`, which is used to apply transforms sequentially:

```
1 from sampler.flow.base import SequentialTransform
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3 flip_a_bunch = SequentialTransform([
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```

For common *Coupling* Flows, e.g., NICE, RealNVP, there is, however, a more convenient way.

Coupling Flows

Coupling flows like NICE consist of two parts, a `partitioner`, and a `net_factory`

```
1 from neulat.sampler.flow.coupling import NICE
2
3 coupling = NICE(
4     partitioner=partitioner,
5     net_factory=net_factory
6 )
```

- The `partitioner` *partitions* (or masks) the input into *active* and *passive* components.

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6 )
```

- The `partitioner` *partitions* (or masks) the input into *active* and *passive* components.
- The `net_factory` is a function that constructs the *conditioner*, e.g., a neural network that acts on the partitioned input.

Coupling Flows: Partitioners

A very simple partitioner is the `AltFlatPartitioner`, which stands for **alternating flattened partitioner**

```
1 partitioner = AltFlatPartitioner(feature_shape=(2, 2)),
2 input = torch.tensor([[1., 2.],[3., 4.]])
3 active, passive = partitioner(input)
4 active += 10
5 output = partitioner(active, passive)
```

- This will generate an output of $\begin{pmatrix} 11 & 2 \\ 13 & 4 \end{pmatrix}$

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- **N.B.** Inputs can be partitioned into more than two parts, e.g., active, passive, frozen.

Coupling Flows: Flipping Partitioners

Partitioners usually flip the active and passive elements.
Such a partitioner can be created by calling `.flip()`:

```
1 flipped = partitioner.flip()
2 input = torch.tensor([[1., 2.],[3., 4.]])
3 active, passive = flipped(input)
4 active += 1
5 output = flipped(active, passive)
```


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5 output = flipped(active, passive)
```

- This will generate an output of $\begin{pmatrix} 1 & 12 \\ 3 & 14 \end{pmatrix}$

Coupling Flows: Net Factory (Conditioner)

The `net_factory` defines the *conditioner* Θ that transforms the passive input:

$$\mathbf{x}_{\text{active}}^{l+1} = h(\mathbf{x}_{\text{active}}^l, \Theta(\mathbf{x}_{\text{passive}}^l)) \quad (1)$$

```
1 from functools import partial
2 from neulat.sampler.flow.coupling.affine import NICE, MLP
3
4 net_factory = partial(
5     MLP,
6     n_blocks=3,
7     latent_size=1024,
8     activation=torch.nn.Tanh,
9     bias=False,
10 )
```

Coupling Flows: Defining Couplings

The coupling Transform itself is mostly only concerned with implementing the coupling function h . E.g. in NICE: $h(\mathbf{x}_{\text{active}}, \mathbf{x}_{\text{passive}}) = \mathbf{x}_{\text{active}} + m_{\theta}(\mathbf{x}_{\text{passive}})$

```
1 class NICE(Coupling):
2     @withlogdet
3     @partitioned
4     def forward(self, active, passive):
5         return active + self.net(passive), 0.
6
7     @withlogdet
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9     def inverse(self, active, passive):
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Recall: @withlogdet makes sure the log abs jacobian det is propagated.

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```

New: @partitioned automates the partitioning in subsequent couplings!

Coupling Flows: Assembling the Flow

Putting all the previous parts together, we can create a Flow in the following way:

```
1 flow = Flow(  
2     base_distribution=Normal(0.0, 1.0, feature_shape=(8, 8)),  
3     transform=6 * NICE(  
4         partitioner=AltFlatPartitioner(feature_shape=(8, 8)),  
5         net_factory=partial(MLP, n_blocks=3, latent_size=1024,  
6             activation=torch.nn.Tanh, bias=False)  
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```

Note: the `transform=6 * NICE`. This creates a sequential transform of 6 Couplings, with alternating masking/partitioning!

Coupling Flows: Global Scaling

Global scaling is a Transform that scales all elements of the input tensor by the **same** scalar value.

This is necessary to enhance the convergence of the model:

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```

Note: Transform has an add method that allows simple concatenation of different types of transforms.

Coupling Flows: Training

Training of the flow with, e.g., ReverseKL, is straightforward:

```
1  from neulat.loss import ReverseKLLoss
2
3  optim = torch.optim.Adam(flow.transform.parameters(), lr=5e-4)
4  loss_fn = ReverseKLLoss()
5  for _ in range(1000):
6      configs, log_probs = flow.sample_with_logprob(10)
7      loss = loss_fn(action(configs), log_probs) # loss contains `mean` and `std`
8      optim.zero_grad()
9      loss.mean.backward() # we train only using the loss `mean`
10     torch.nn.utils.clip_grad_norm_(model.transform.parameters(), 1.0) # clipping
11     optim.step()
```

Estimating Observables: IidEstimator

Observables themselves are classes in NeuLat. In order to estimate them, we additionally need an Estimator, and configurations. For instance:

```
1 from neulat.observable.base import AbsMagnetization, Magnetization
2 from neulat.estimator.base import IidEstimator
3
4 observables = [AbsMagnetization(), Magnetization(), action]
5 iid_estimator = IidEstimator(observables)
6 configs = flow.sample(1000)
7 flow_statistics = iid_estimator.named_evaluate(configs)
```

The dict `flow_statistics` will contain one entry per observable:

```
{'absmag': Statistics(mean=0.6408, std=0.0473), 'mag': ...}
```

Estimating Observables: CorrelatedEstimator

Estimation of Observables from correlated samples (e.g., from HMC) requires the use of the appropriate estimator:

```
1 from neulat.estimator.base import CorrelatedEstimator
2
3 correlated_estimator = CorrelatedEstimator(observables)
4 configs = hmc.sample(1000)
5 hmc_statistics = correlated_estimator.named_evaluate(configs)
```

The dict `hmc_statistics` will instead contain correlated statistics objects:

```
{'absmag': CorrelatedStatistics(mean=32.82628, std=1.4674,
tau_int=0.5909, tau_int_err=0.3162), ...}
```

Estimating Observables: ImportanceSamplingEstimator

To obtain an unbiased estimator, [Nicoli et al., \(2020\)](#) proposed to use **Neural Importance Sampling (NIS)**.

This additionally requires the logprobs from the flow, as well as the specific action:

```
1 from neulat.estimator.base import ImportanceSamplingEstimator
2
3 flow_configs, flow_logprobs = flow.sample_with_logprob(1000)
4 iw_estimator = ImportanceSamplingEstimator(observables, action)
5 flow_iw_stats = iw_estimator.named_evaluate(flow_configs, flow_logprobs)
```

The dict `flow_iw_statistics` will contain the same `Statistics` object returned by the `IidEstimator`:

```
{'absmag': Statistics(mean=2.6021, std=0.4674), ...}
```

Planned Features

With the help of the community, we plan to extend NeuLat into many directions, including following features

- Non-Equilibrium MCMC [[Caselle et al., Phys. Rev. D \(2016\)](#)]

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- **YOUR FEATURE HERE!**

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And now it's time for a real demo...

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Thank you for your attention!