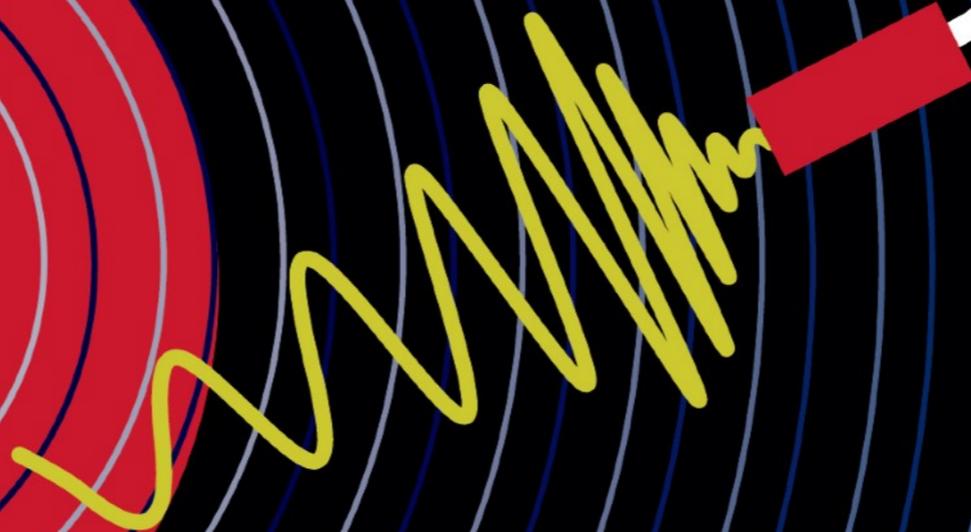
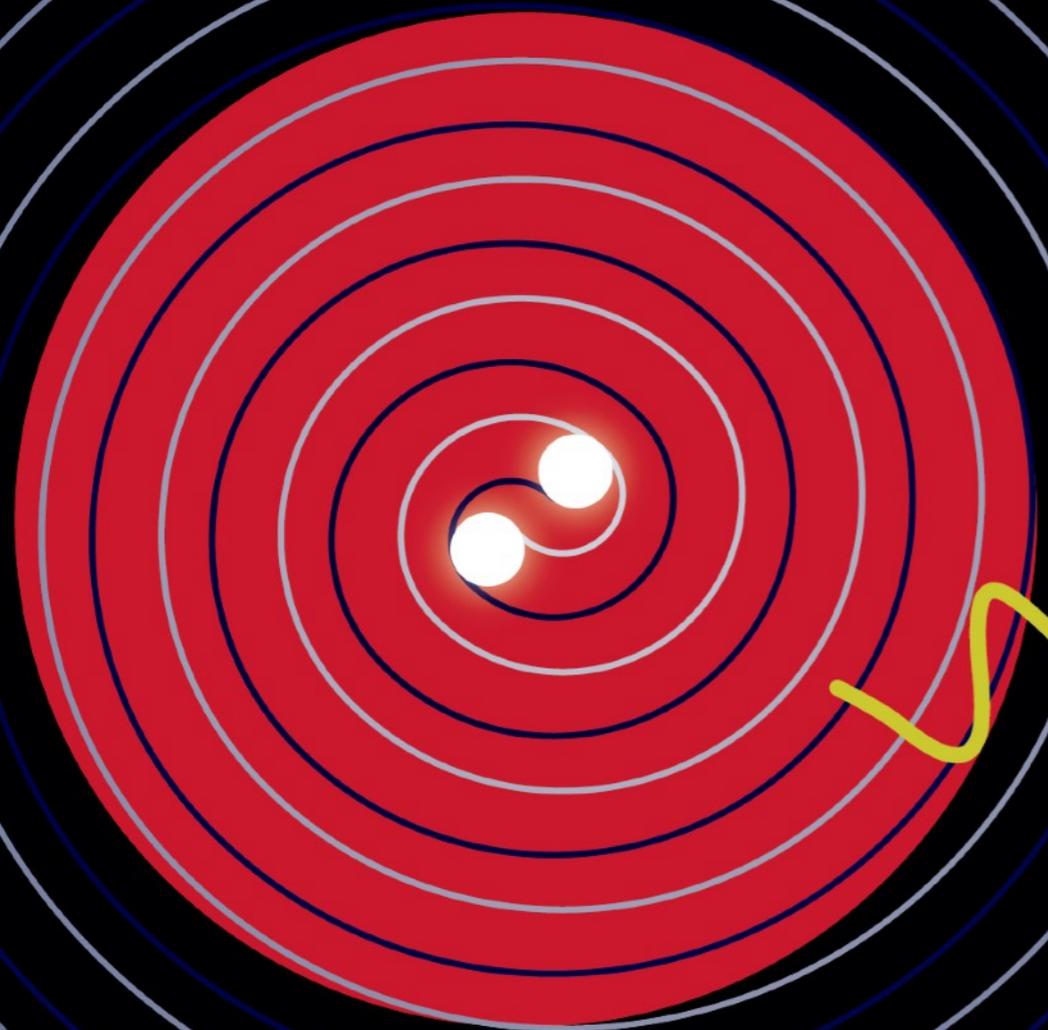


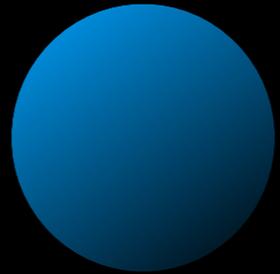
Gravitational-wave standard siren cosmology



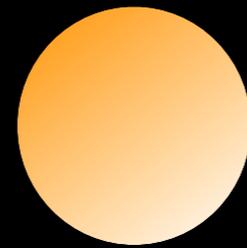
Hsin-Yu Chen

(NASA Einstein Fellow, MIT)

7th KAGRA International Workshop, December 2020

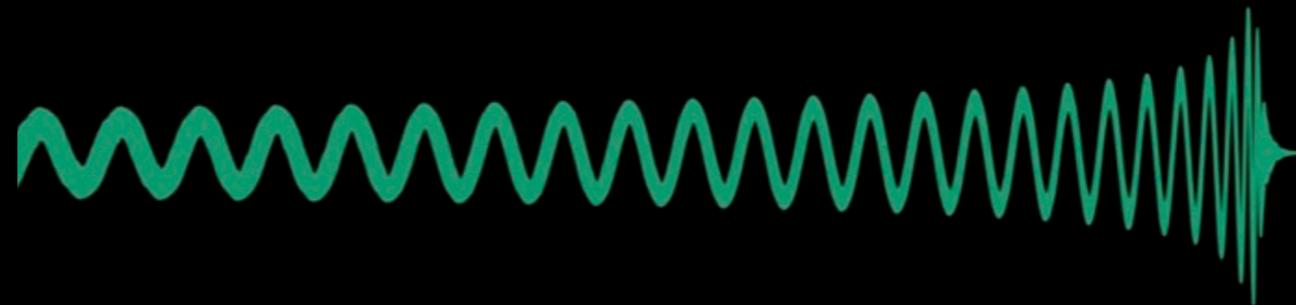


This is a black hole.



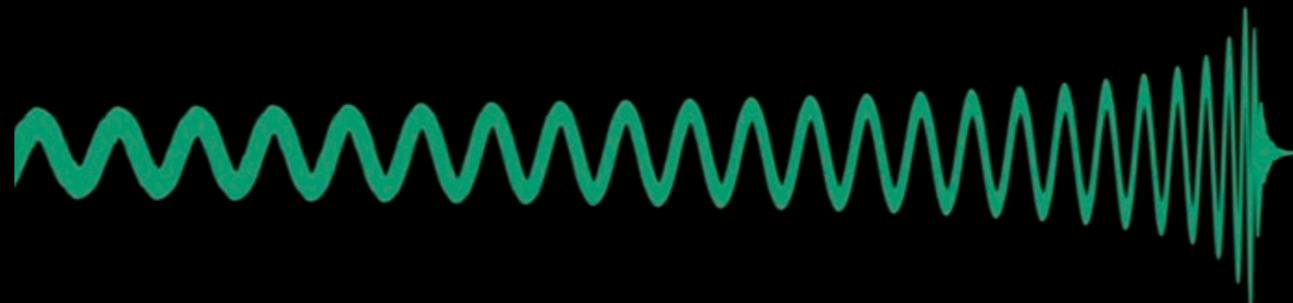
This is a neutron star.

Direct measurement of the luminosity distance



Luminosity Distance $\propto 1/\text{Amplitude}$

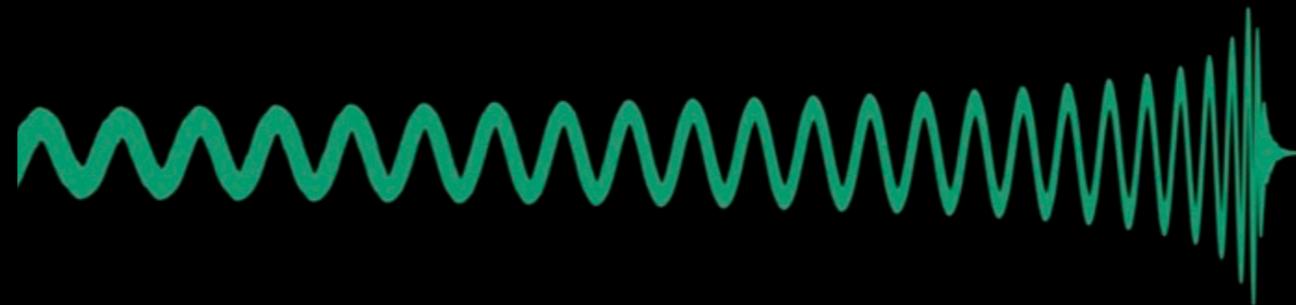
Direct measurement of the luminosity distance



Luminosity Distance $\propto 1/\text{Amplitude}$

-Mass, sky location, and binary orientation also affect the amplitude, however these parameters can either be determined independently or marginalized out.

Direct measurement of the luminosity distance



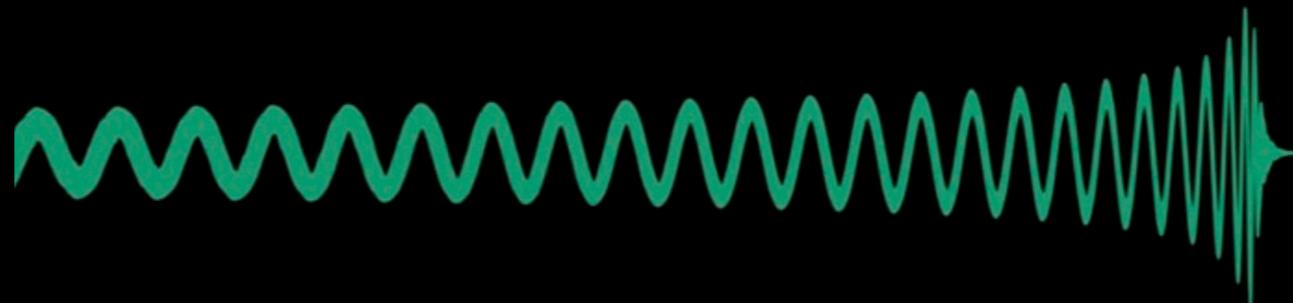
Luminosity Distance $\propto 1/\text{Amplitude}$

-Constrain the cosmological parameters with the redshift and luminosity distance:

$$D_L = c(1+z) \int_0^z \frac{dz'}{H(z')}$$

$$H(z) = H_0 \sqrt{\Omega_M(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda(1+z)^{3(1+w_0+w_a)} e^{-3w_a z/(1+z)}}$$

Direct measurement of the luminosity distance



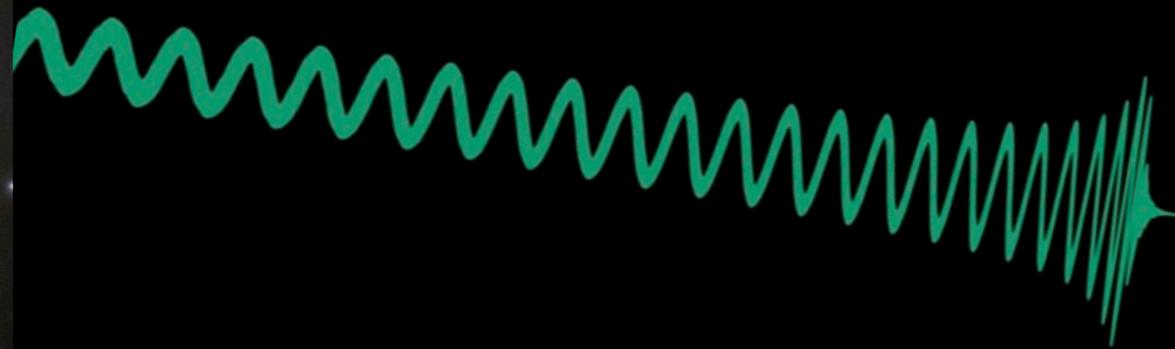
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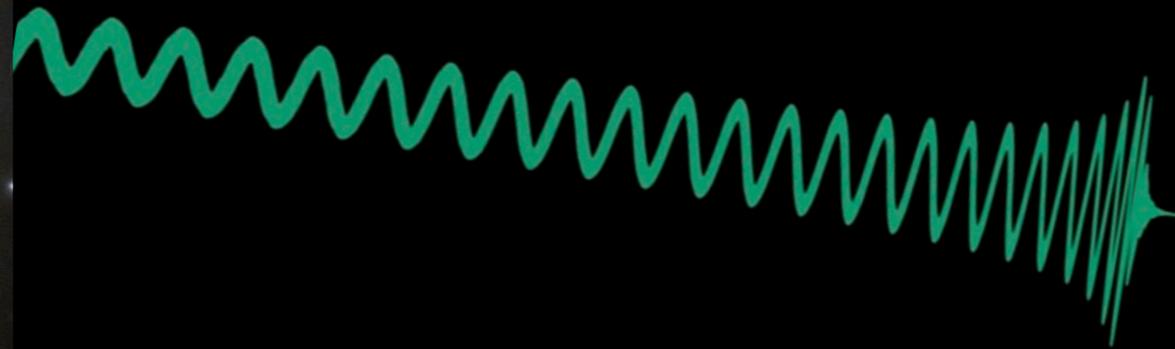
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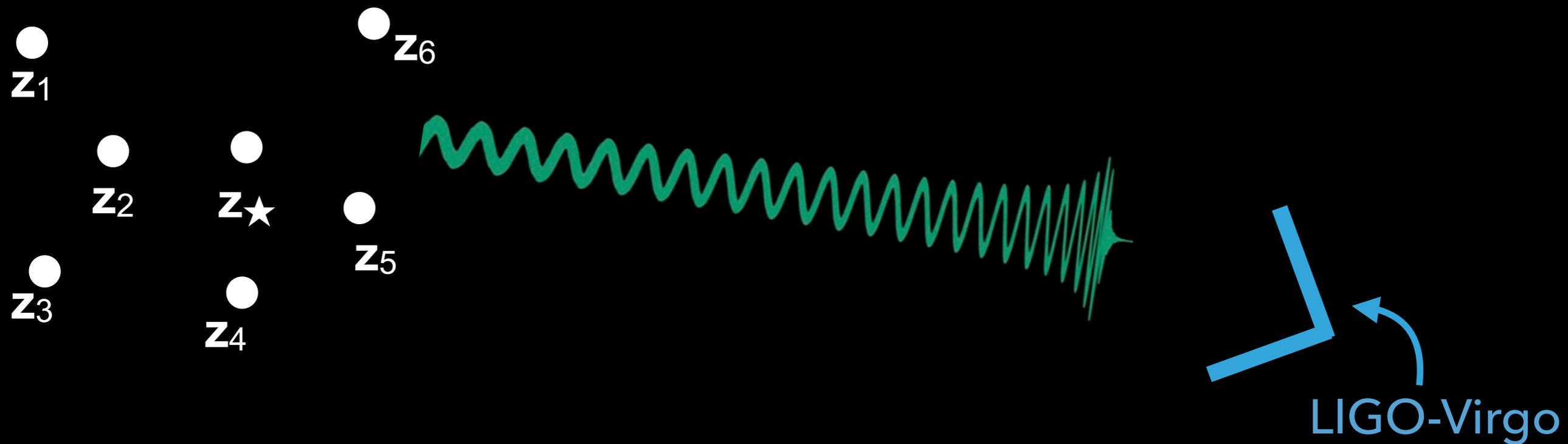
Determine the redshift of gravitational-wave source with the host galaxy



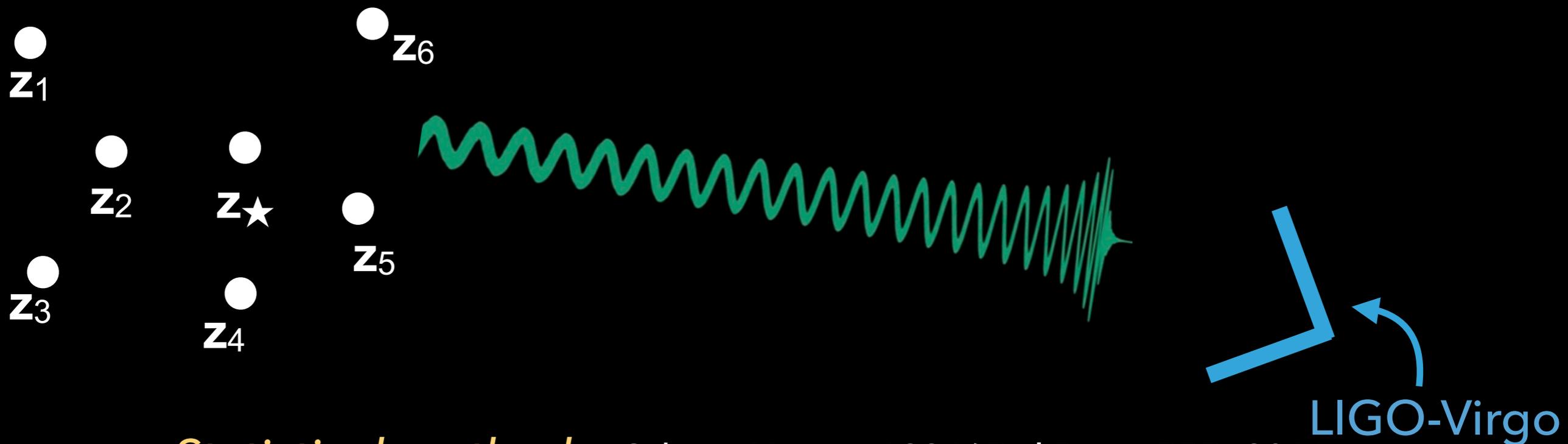
Determine the redshift of gravitational-wave source with the host galaxy



Determine the redshift of gravitational-wave source with the host galaxy



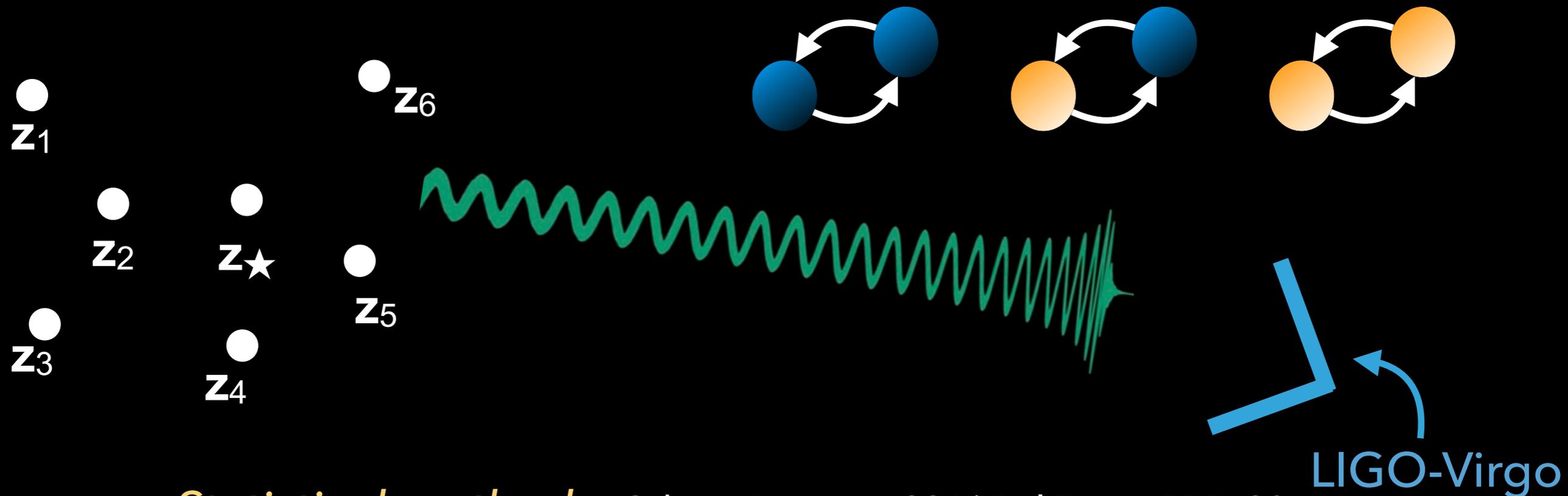
Determine the redshift of gravitational-wave source with the host galaxy



Statistical method: Schutz, Nature, 1986/ Del Pozzo, PRD, 2011

Combine the redshifts of all possible host galaxies.

Determine the redshift of gravitational-wave source with the host galaxy



Statistical method: Schutz, Nature, 1986/ Del Pozzo, PRD, 2011

Combine the redshifts of all possible host galaxies.

$$\text{-GW170814: } H_0 = 75.2^{+39.5}_{-32.4} \text{ km/s/Mpc}$$

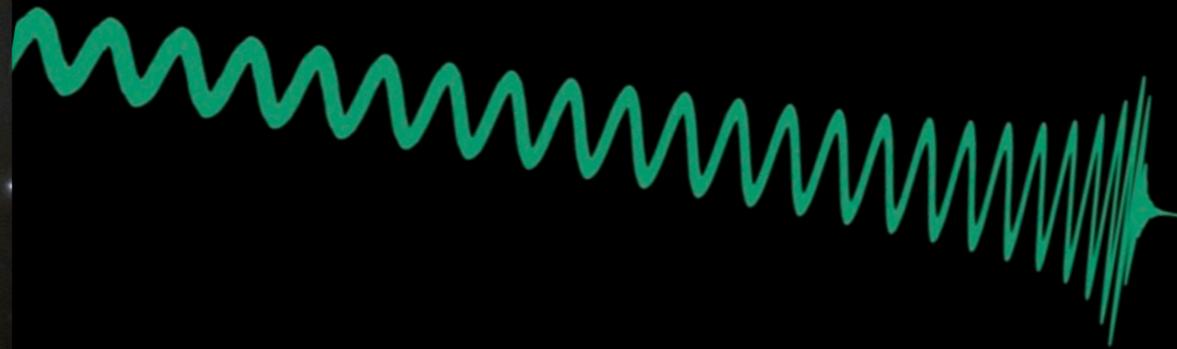
(Dark Energy Survey Year 3 data)

DES & LVC, 2019

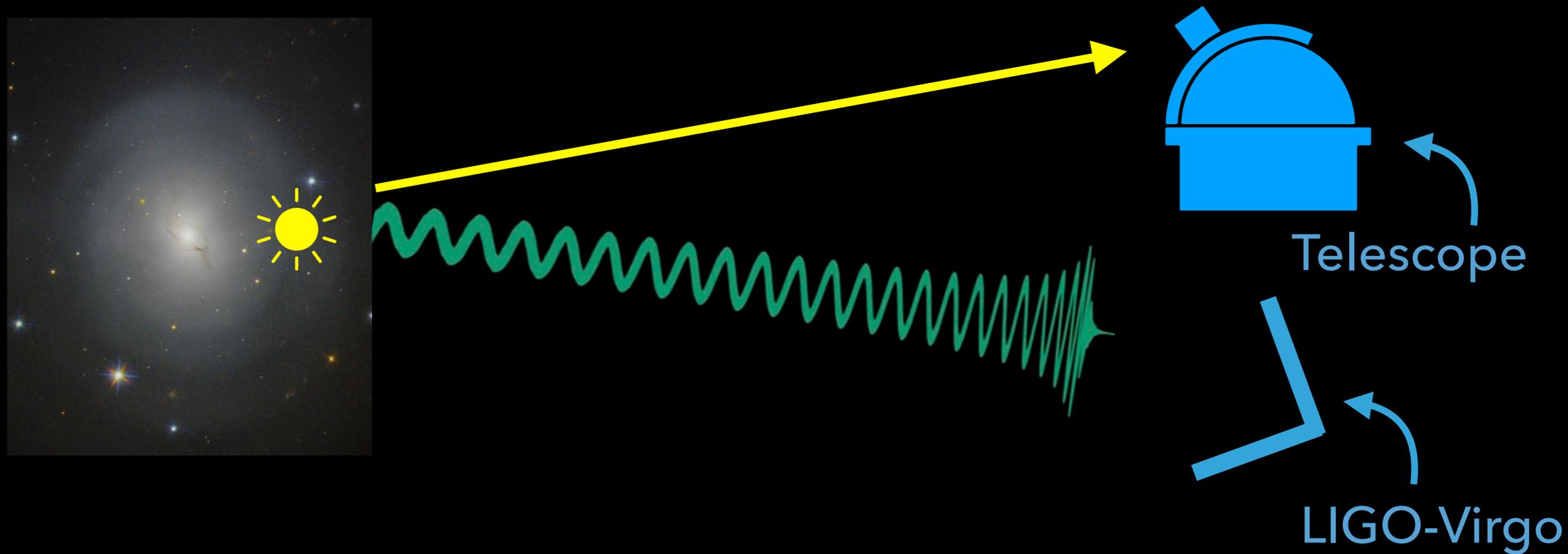
$$\text{-GW170817: } H_0 = 76^{+48}_{-23} \text{ km/s/Mpc}$$

Fishbach, ~Chen et al., ApJL, 2019

Determine the redshift of gravitational-wave source with the host galaxy



Determine the redshift of gravitational-wave source with the host galaxy

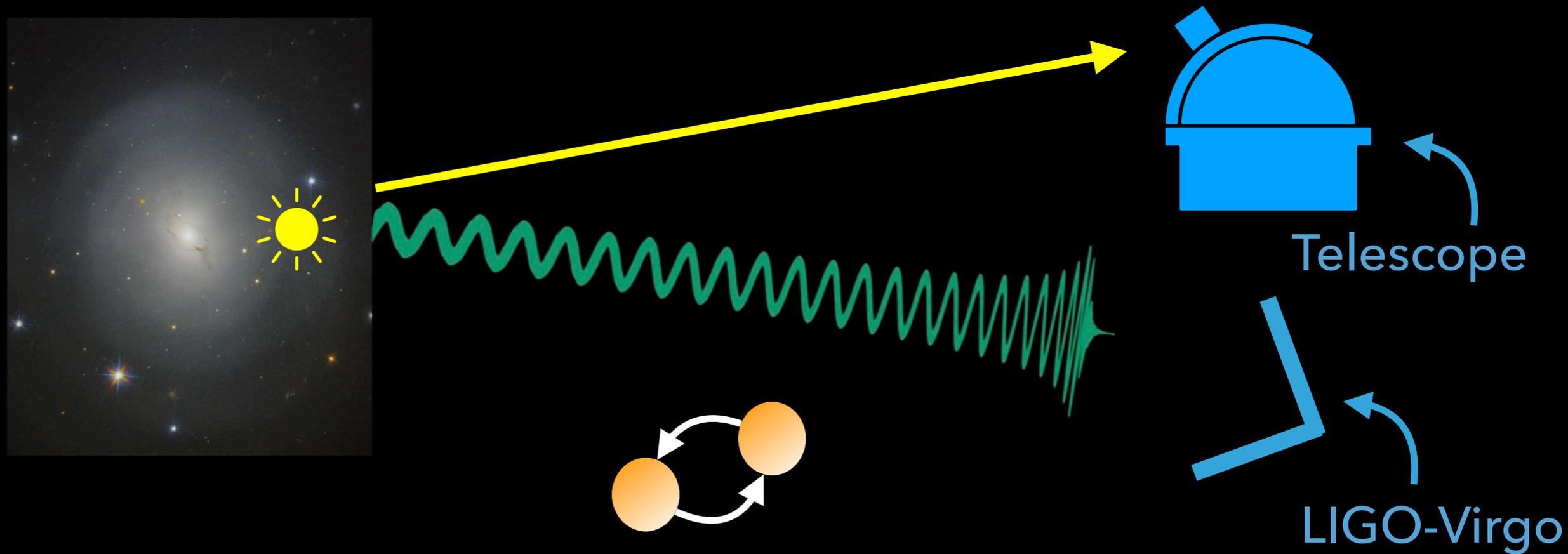


Counterpart method:

Find the host galaxy of the electromagnetic counterpart.

Schutz, Nature, 1986 / Holz & Hughes, ApJ, 2005

Determine the redshift of gravitational-wave source with the host galaxy



Counterpart method:

Find the host galaxy of the electromagnetic counterpart.

Schutz, Nature, 1986 / Holz & Hughes, ApJ, 2005

The first standard siren measurement with an electromagnetic counterpart

GW170817
DECam observation
(0.5–1.5 days post merger)



GW170817
DECam observation
(>14 days post merger)



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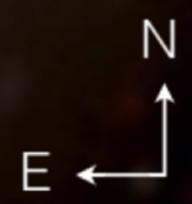


From LIGO-Virgo:

$$D_L = 43^{+2.9}_{-6.9} \text{ Mpc}$$



GW170817
DECam observation
(>14 days post merger)

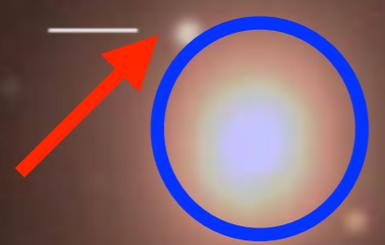


The first standard siren measurement with an electromagnetic counterpart

GW170817
DECAM observation
(0.5–1.5 days post merger)

From electromagnetic:

$$v = 3017 \pm 166 \text{ km/s}$$

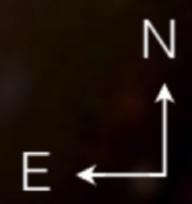


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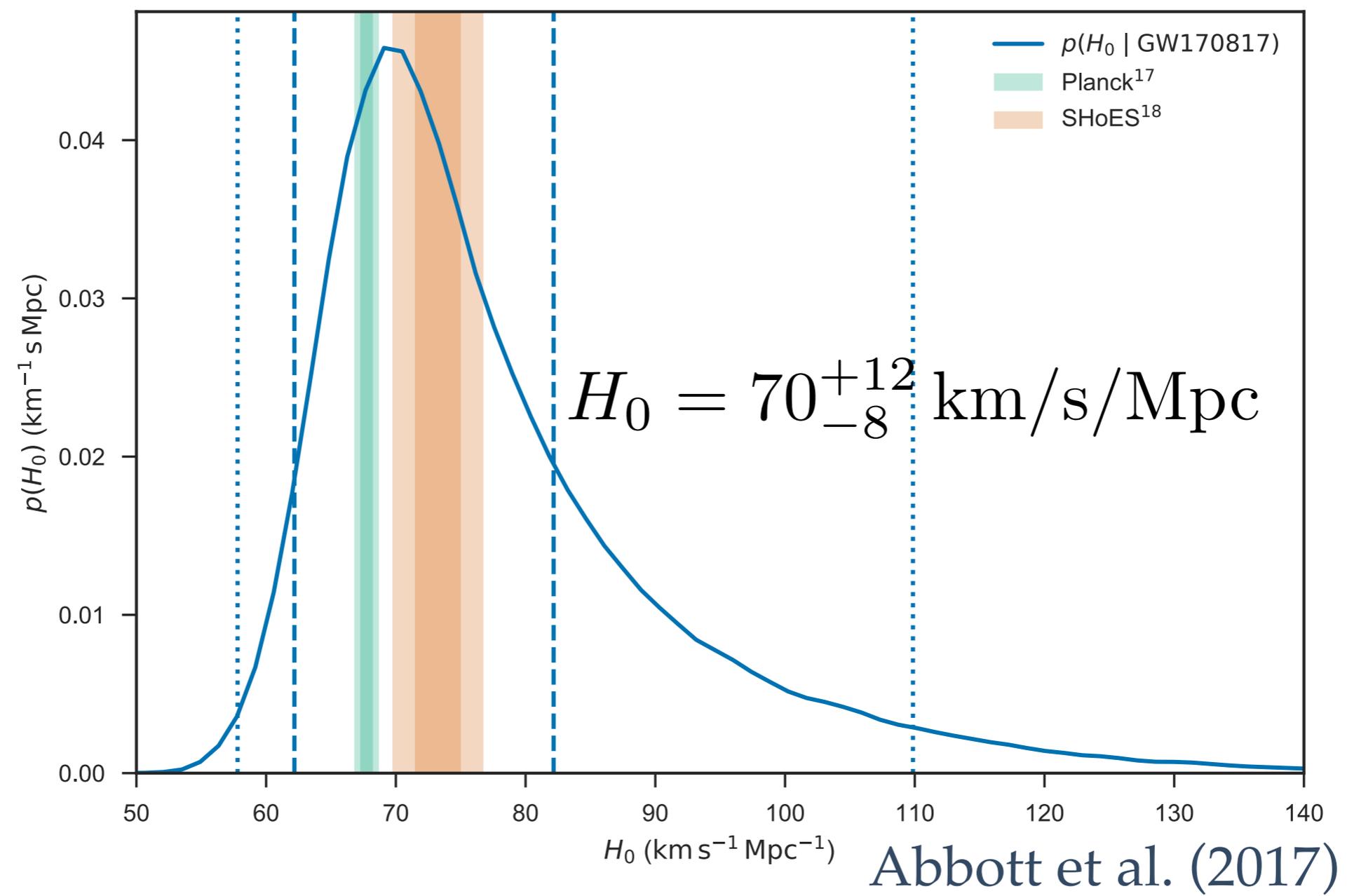


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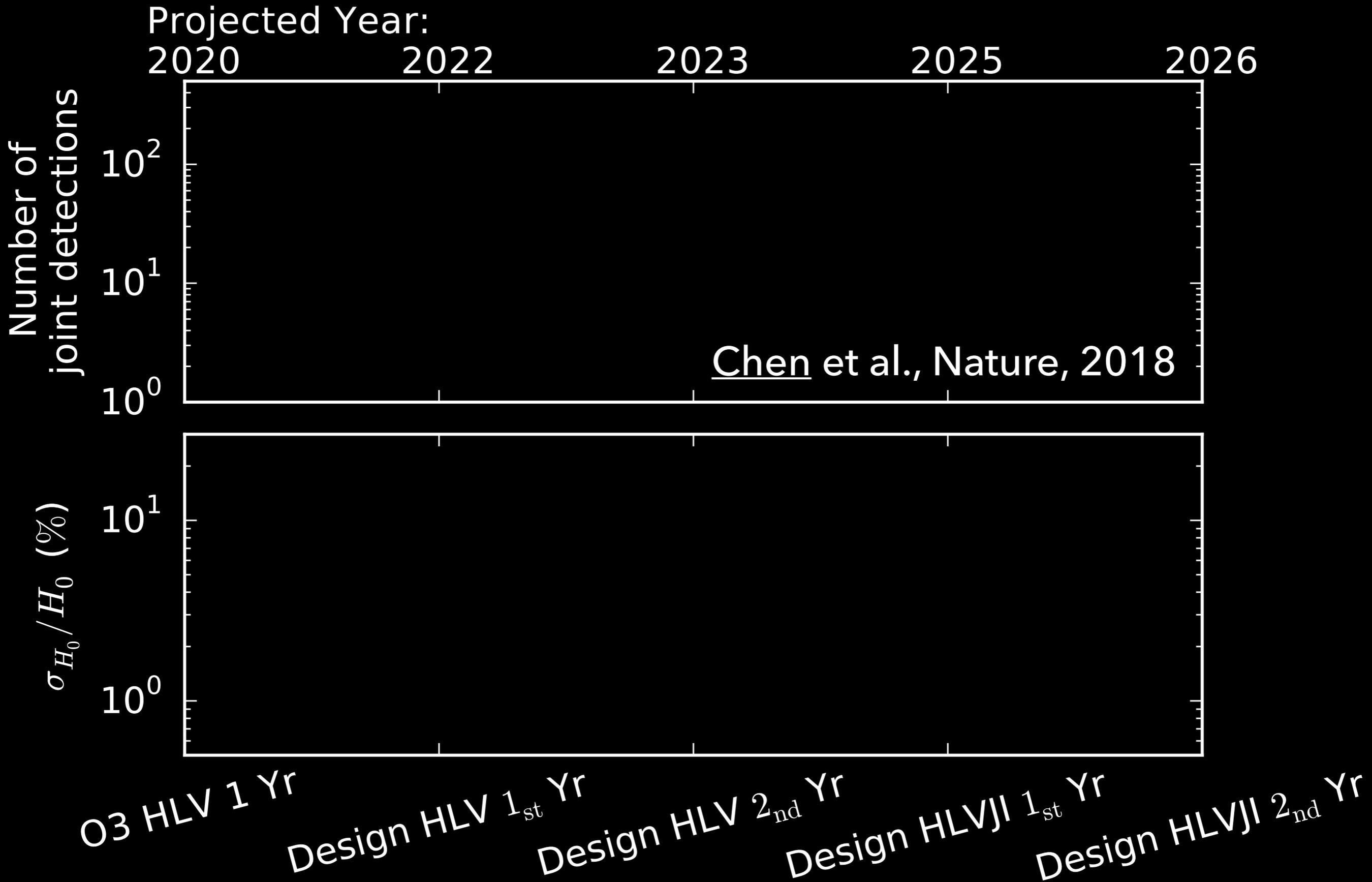
GW170817
DECam color
(0.5–1.5 μm)

From

$D_L =$

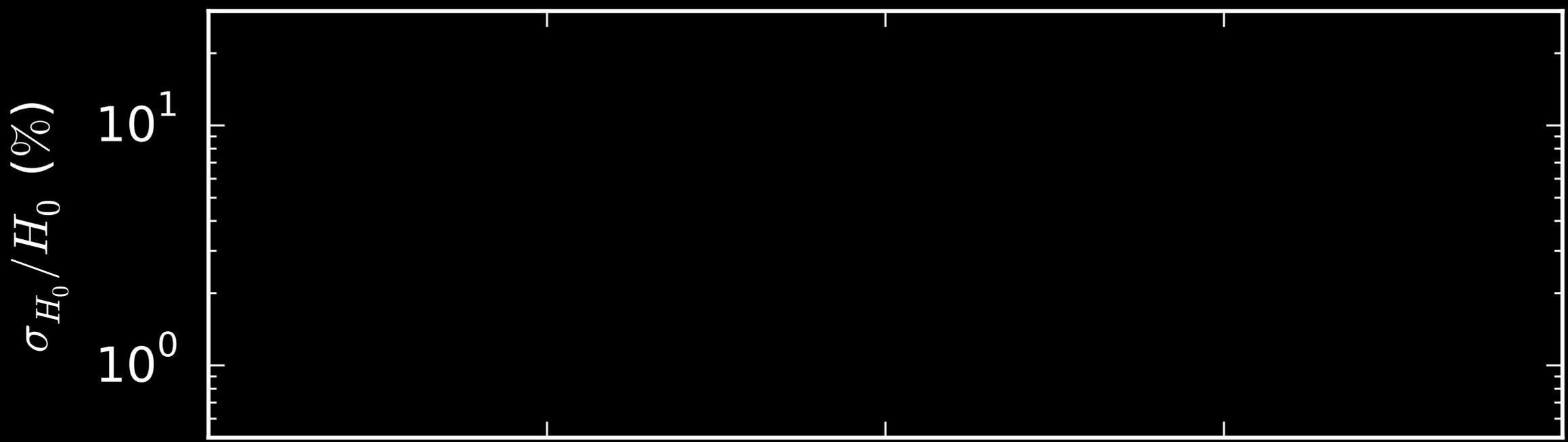
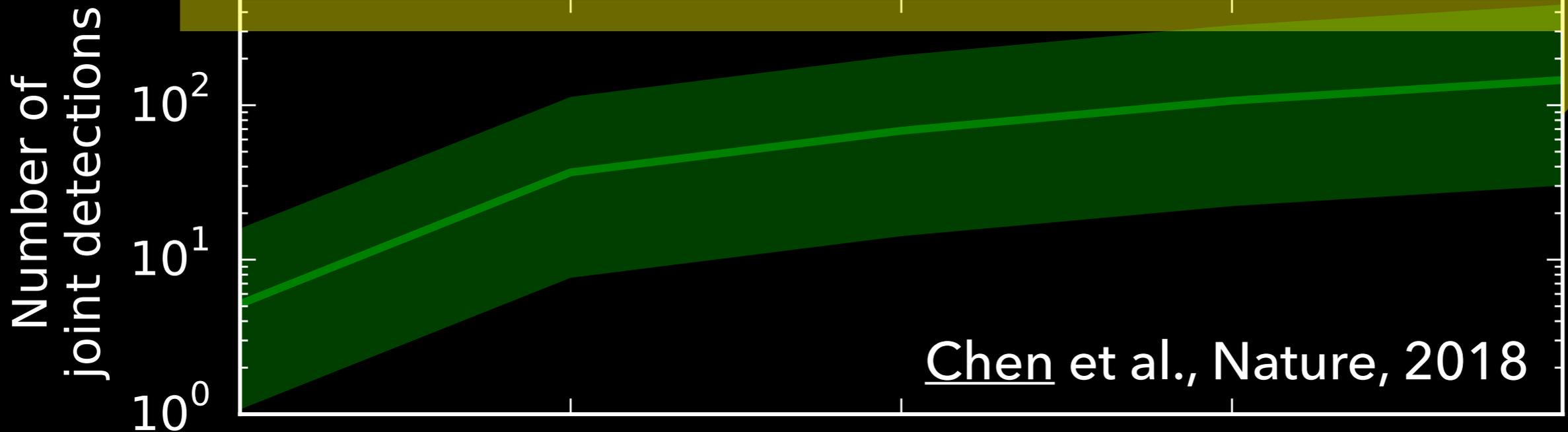


Percent-level Hubble constant measurement within a few years⁷



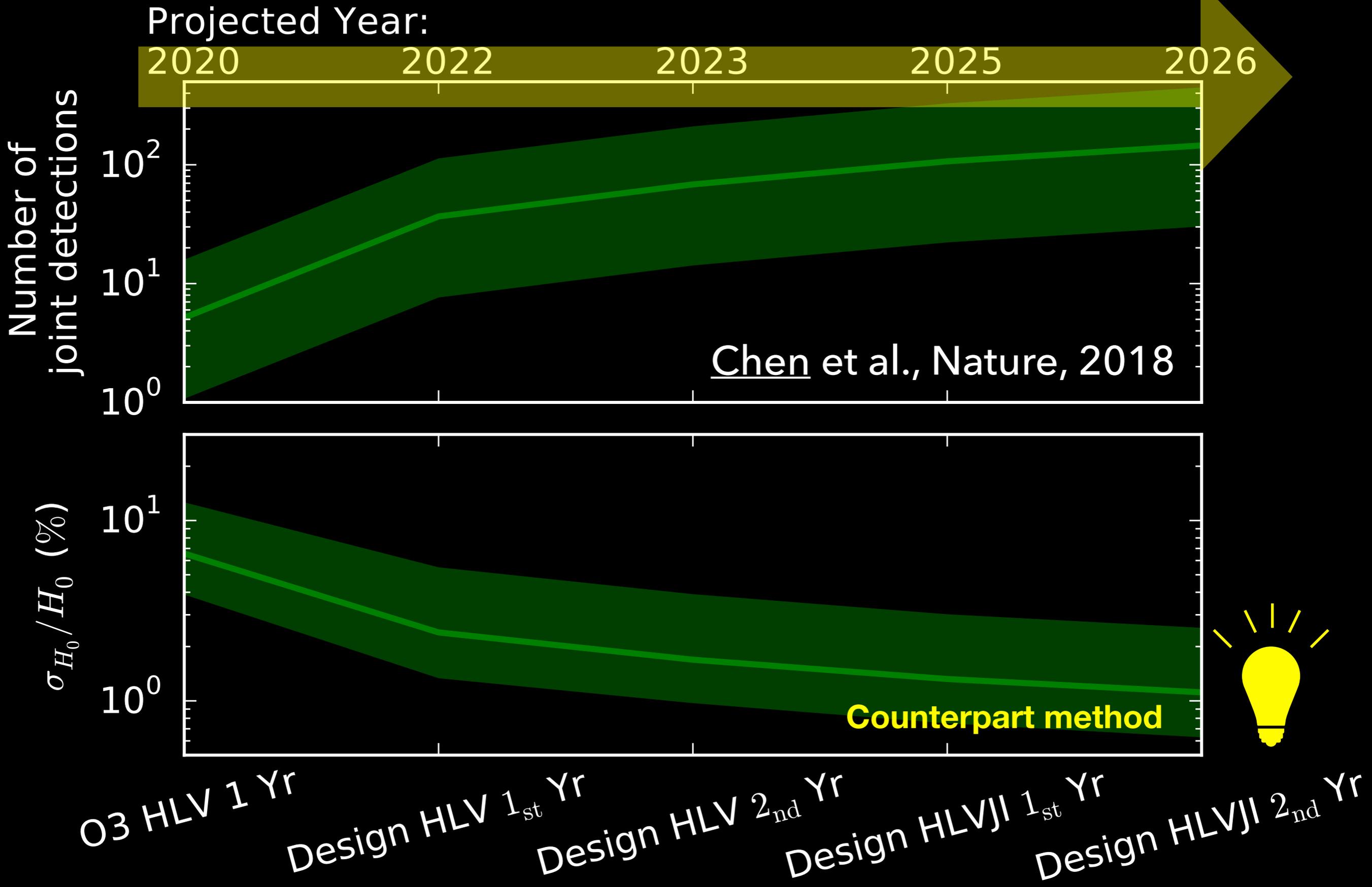
Percent-level Hubble constant measurement within a few years⁷

Projected Year:

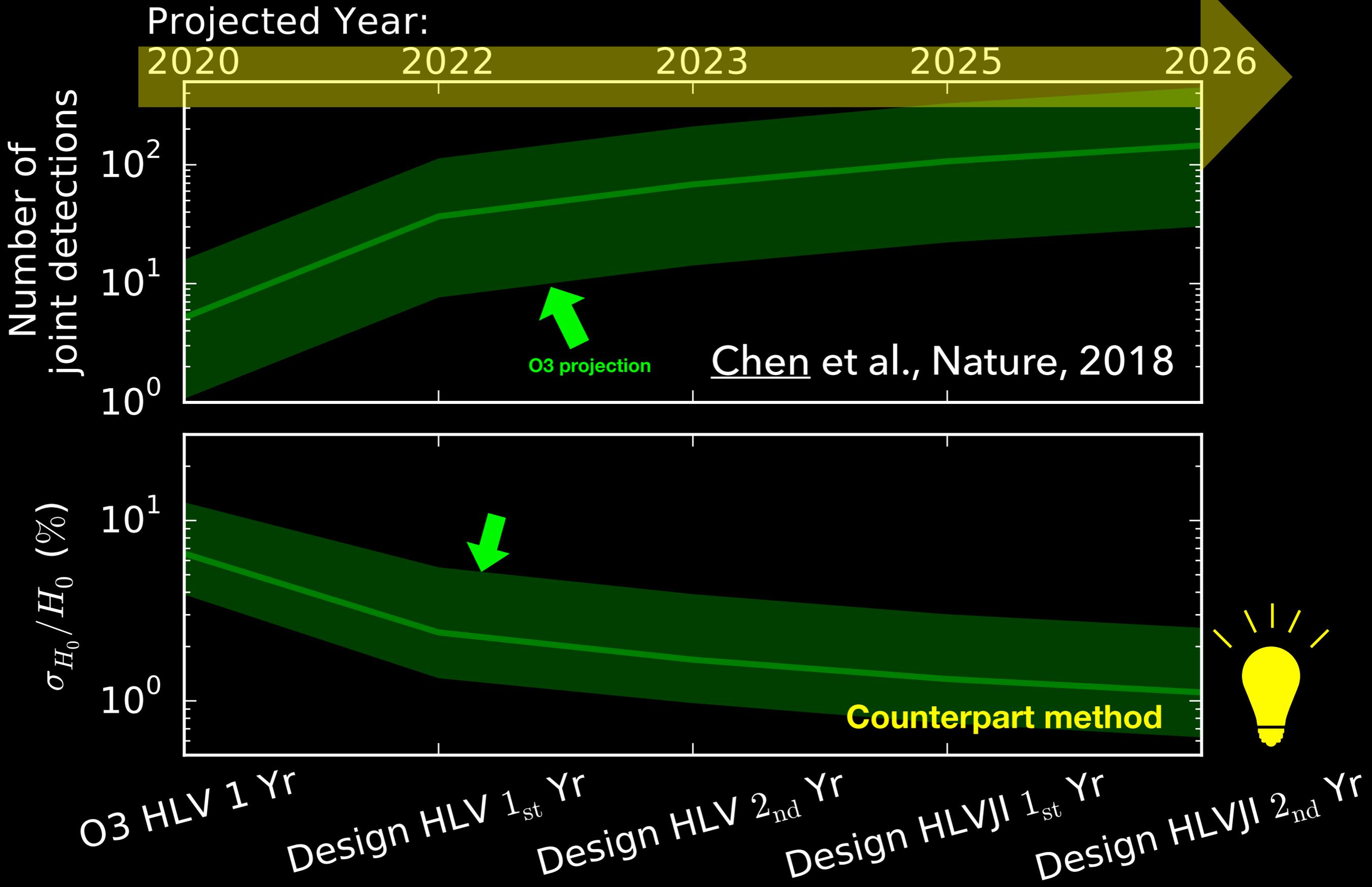


O3 HLV 1 Yr Design HLV 1_{st} Yr Design HLV 2_{nd} Yr Design HLVJI 1_{st} Yr Design HLVJI 2_{nd} Yr

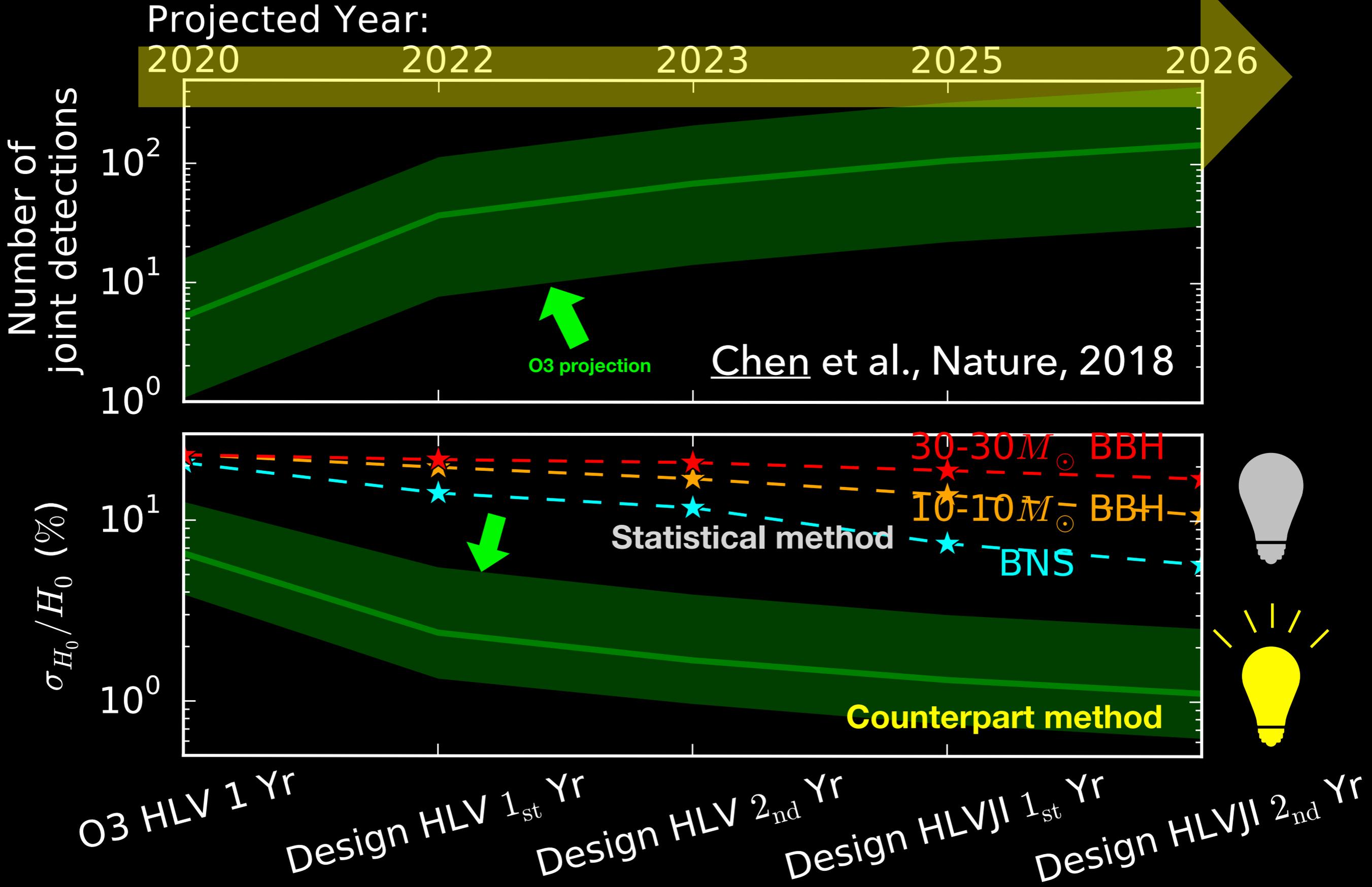
Percent-level Hubble constant measurement within a few years⁸



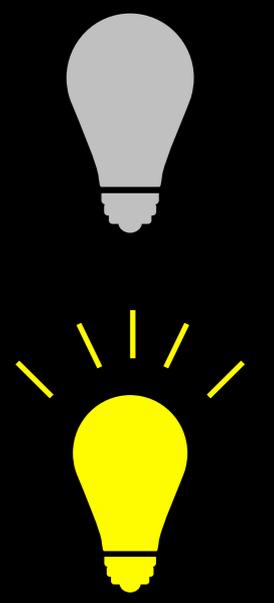
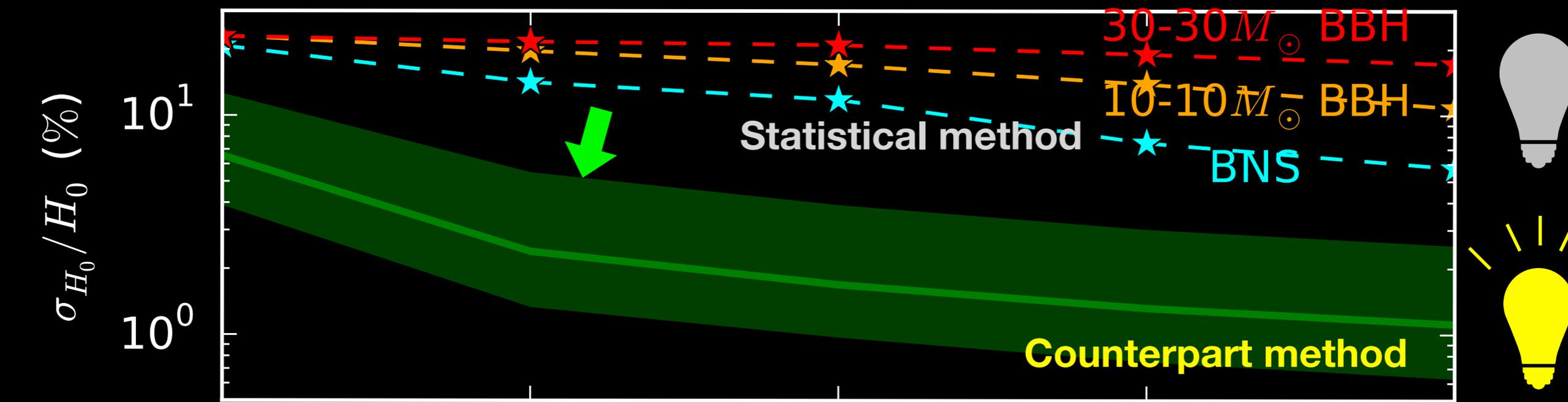
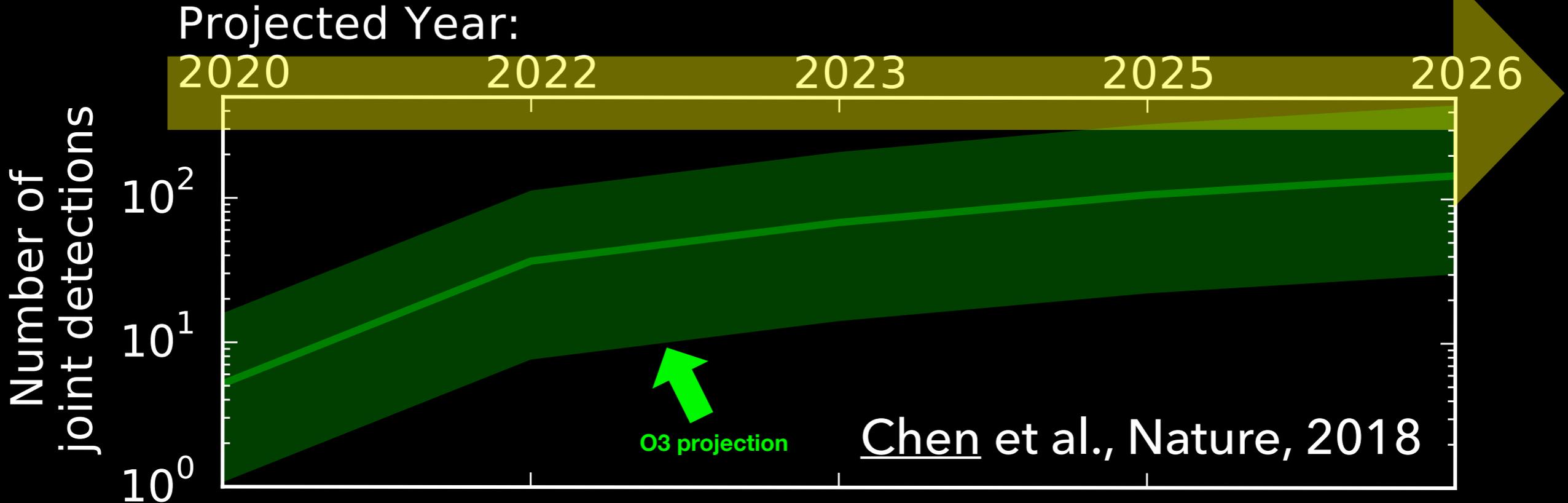
Percent-level Hubble constant measurement within a few years⁸



Percent-level Hubble constant measurement within a few years⁸



Percent-level Hubble constant measurement within a few years⁸

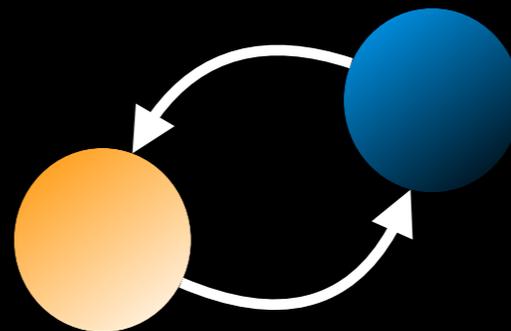
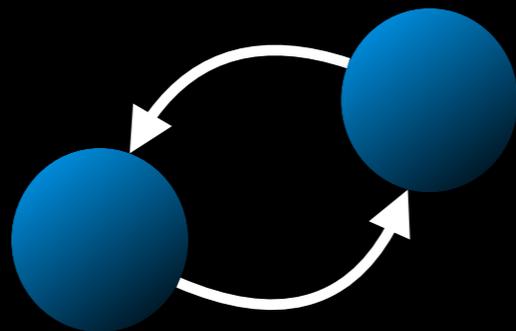


O3 HLV 1st

The search for electromagnetic counterparts is crucial for gravitational-wave cosmology.

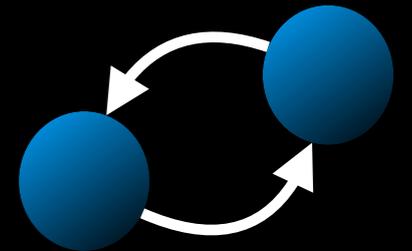
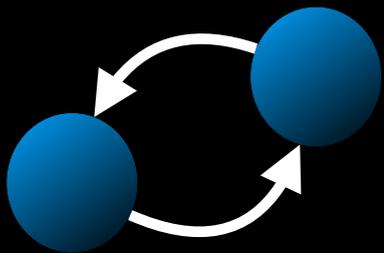
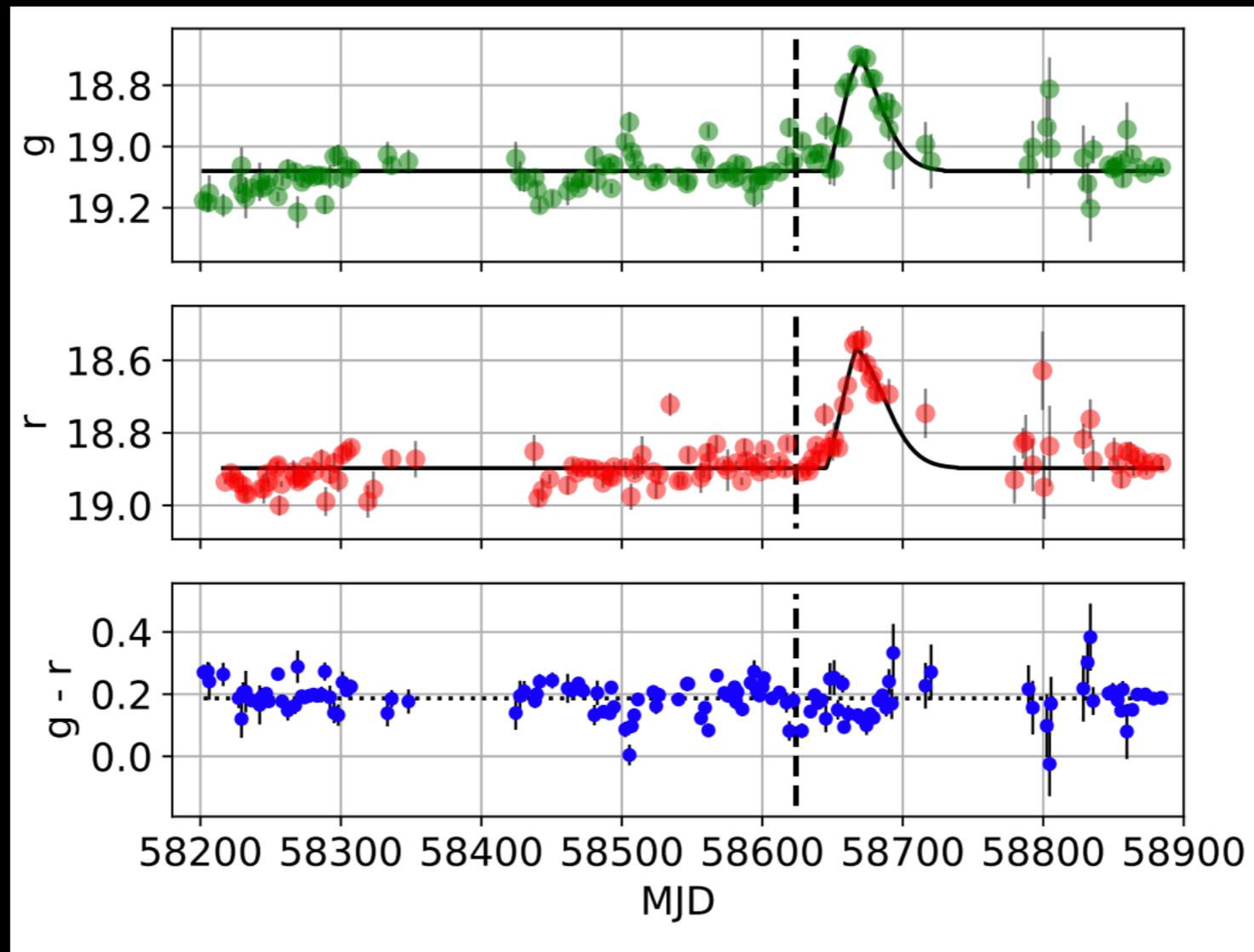
Ign HLVJI 2nd Yr

Could binary black hole or neutron star-black hole mergers have electromagnetic counterparts?



Binary black hole merger GW190521 and its potential electromagnetic counterpart

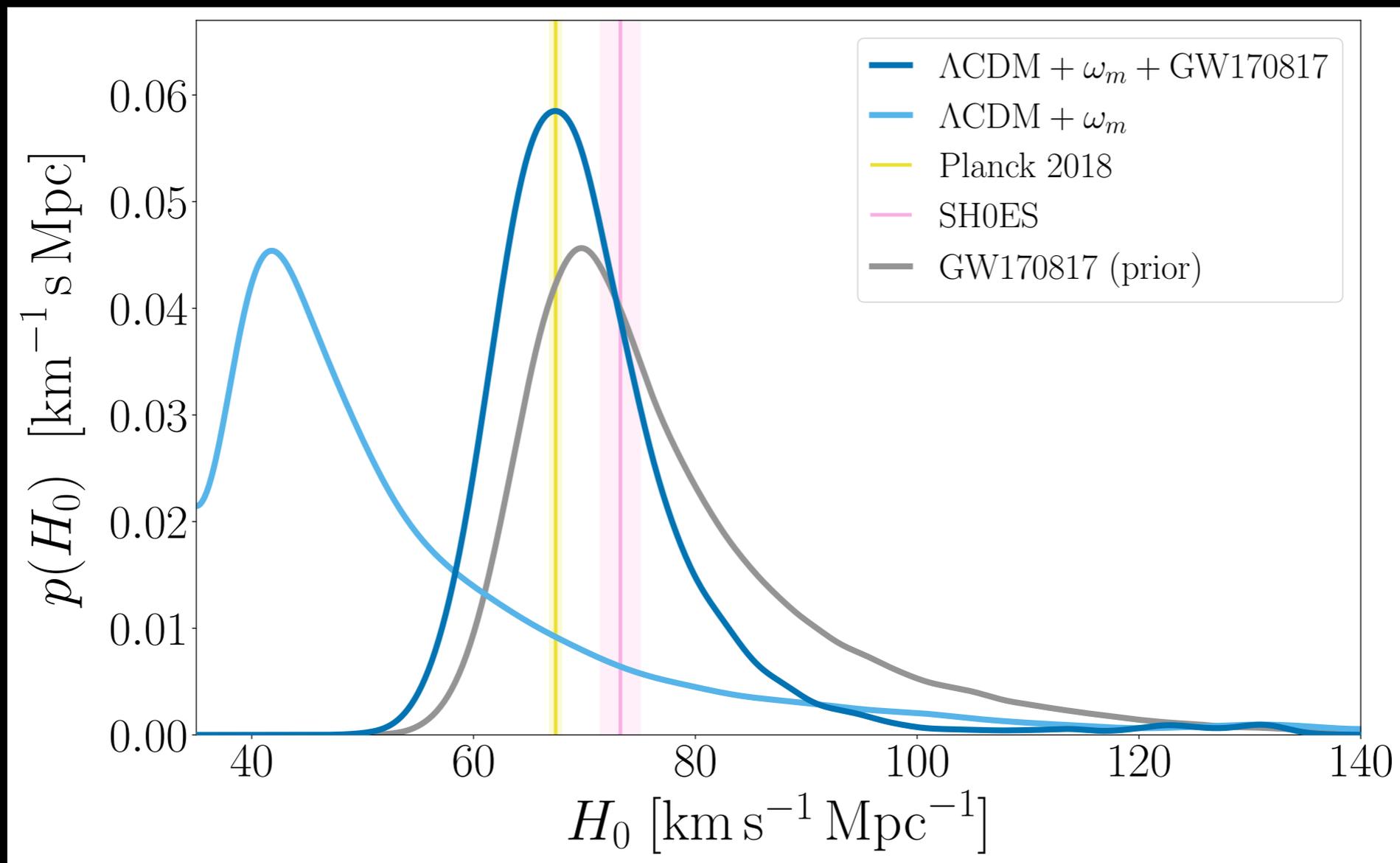
-Kicked black hole merger in the accretion disk of an Active Galactic Nuclei



Graham et al., PRL, 2020

Binary black hole merger GW190521 and its potential electromagnetic counterpart

-The uncertainty of H_0 improved from 15% to 10%.



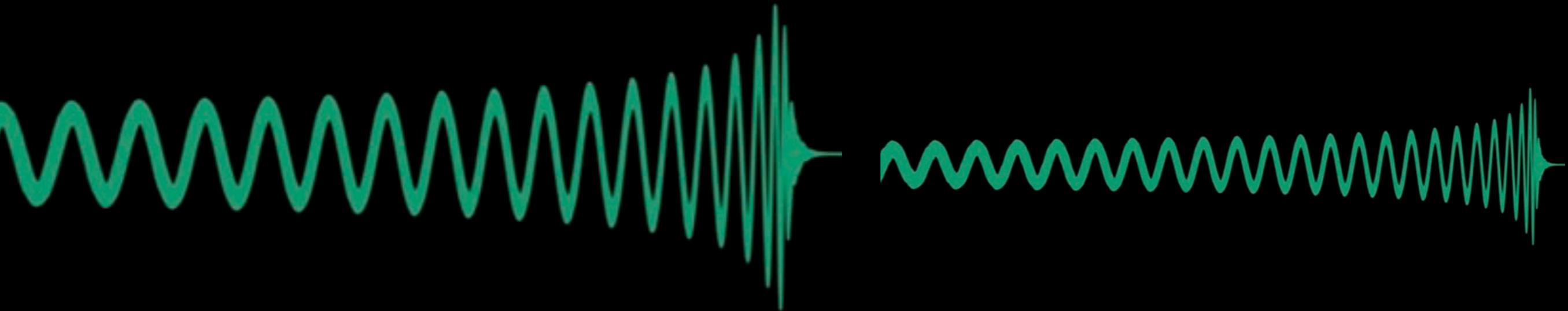
Chen et al., arXiv: 2009.14057

Improve the precision of standard sirens

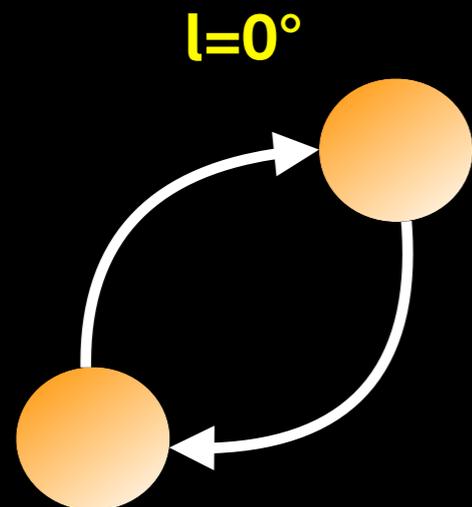
Improve the precision of standard sirens

-Break the distance-inclination degeneracy.

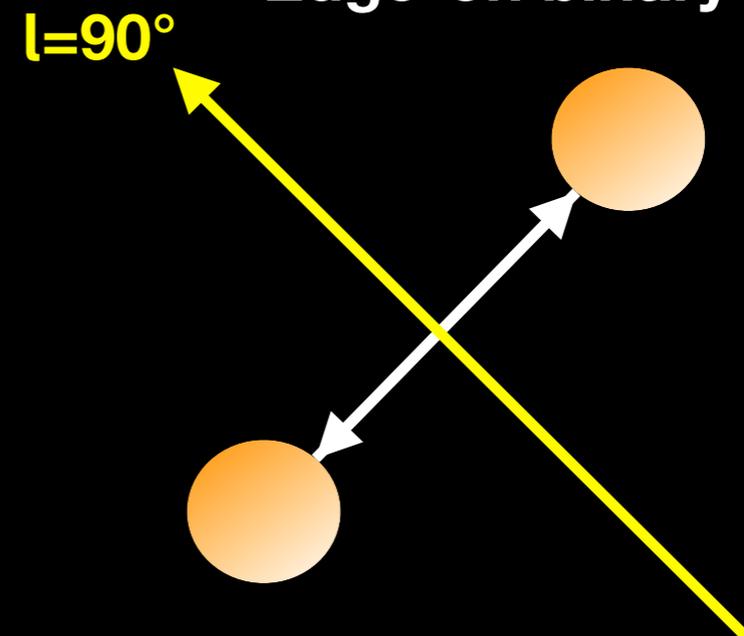
Distance-inclination degeneracy



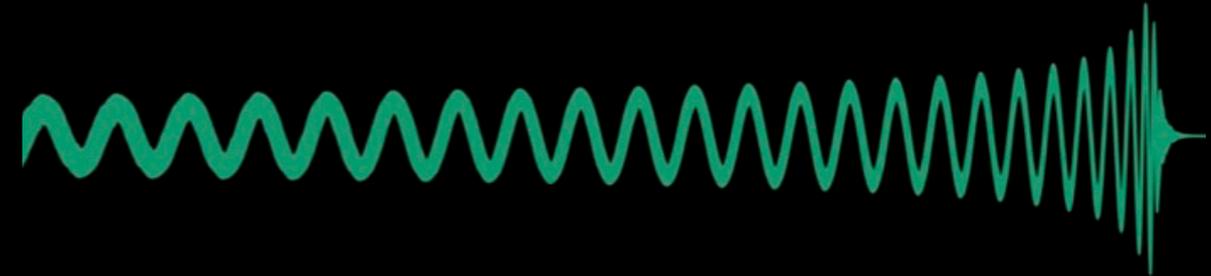
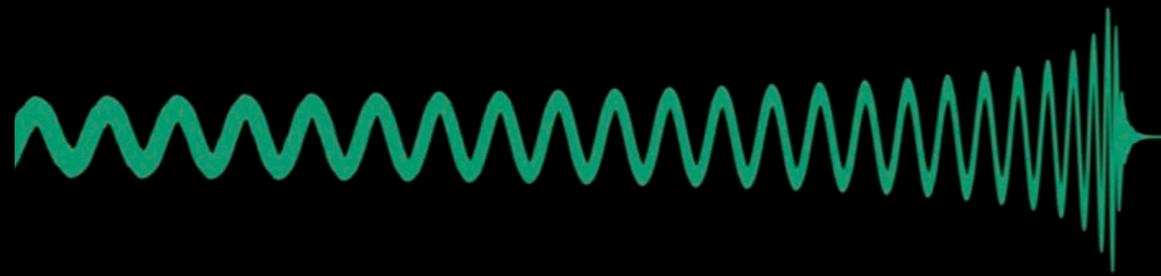
Face-on binary



Edge-on binary



Distance-inclination degeneracy

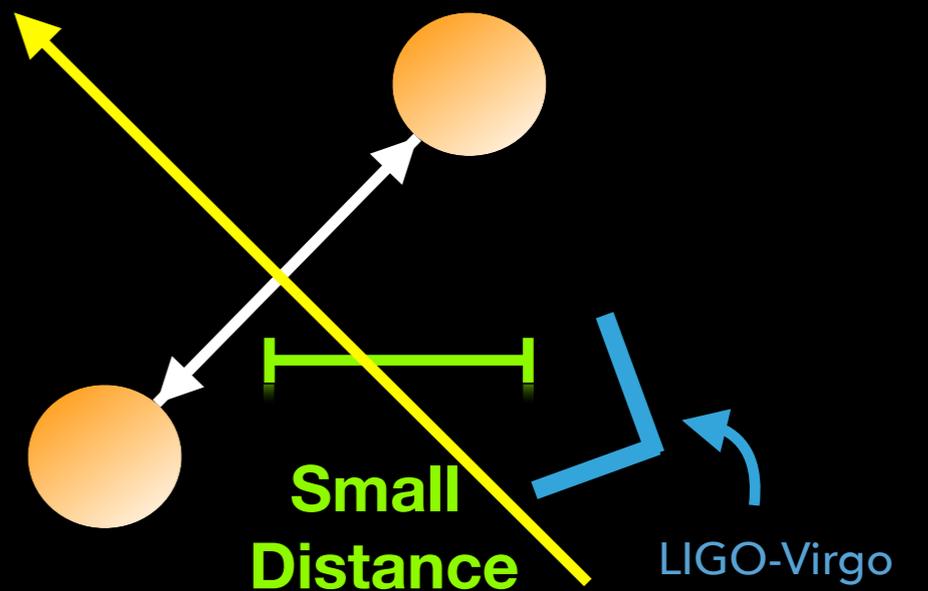


Face-on binary

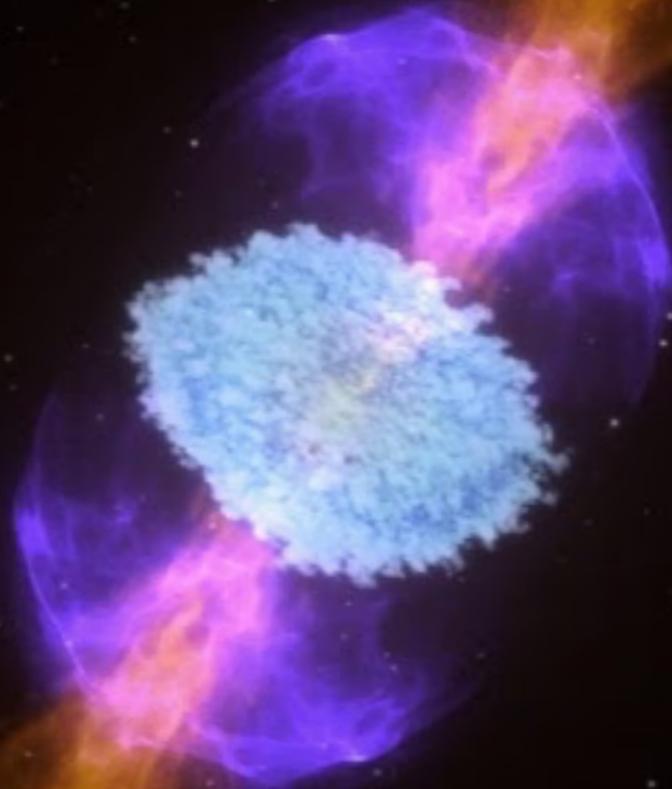
Edge-on binary

$i=0^\circ$

$i=90^\circ$



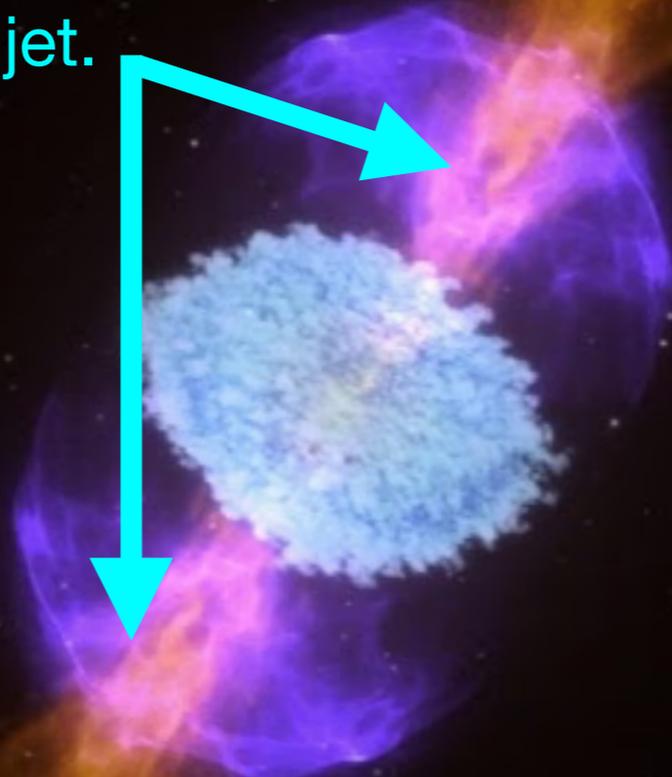
The electromagnetic counterpart emissions are not isotropic



The electromagnetic counterpart emissions are not isotropic

Short gamma-ray burst

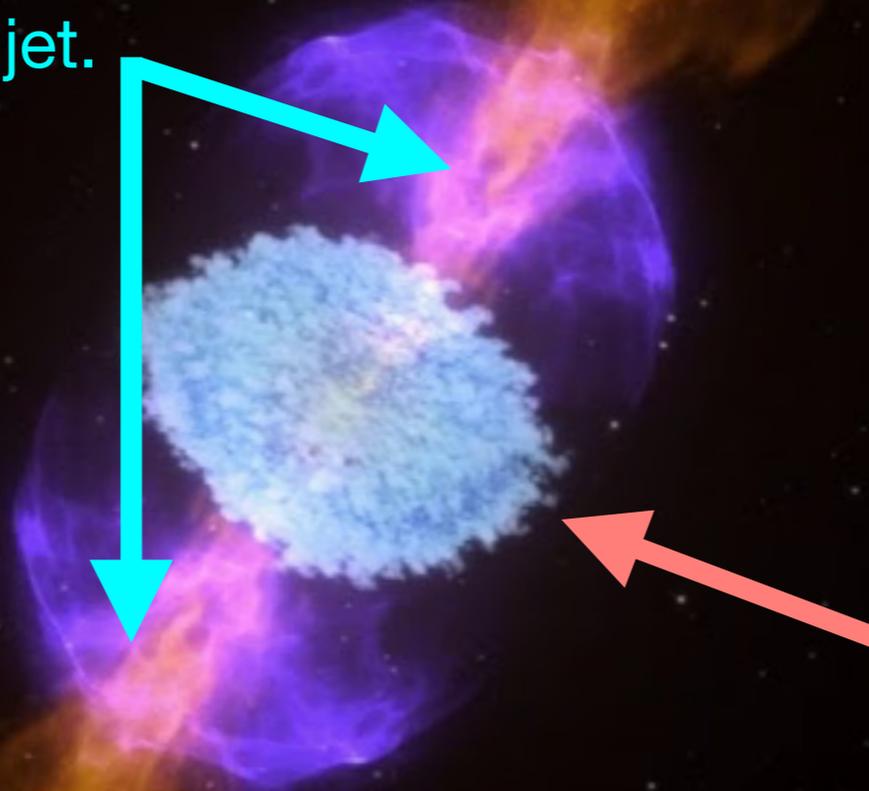
Various observations suggested they have beamed relativistic jet.



The electromagnetic counterpart emissions are not isotropic

Short gamma-ray burst

Various observations suggested they have beamed relativistic jet.



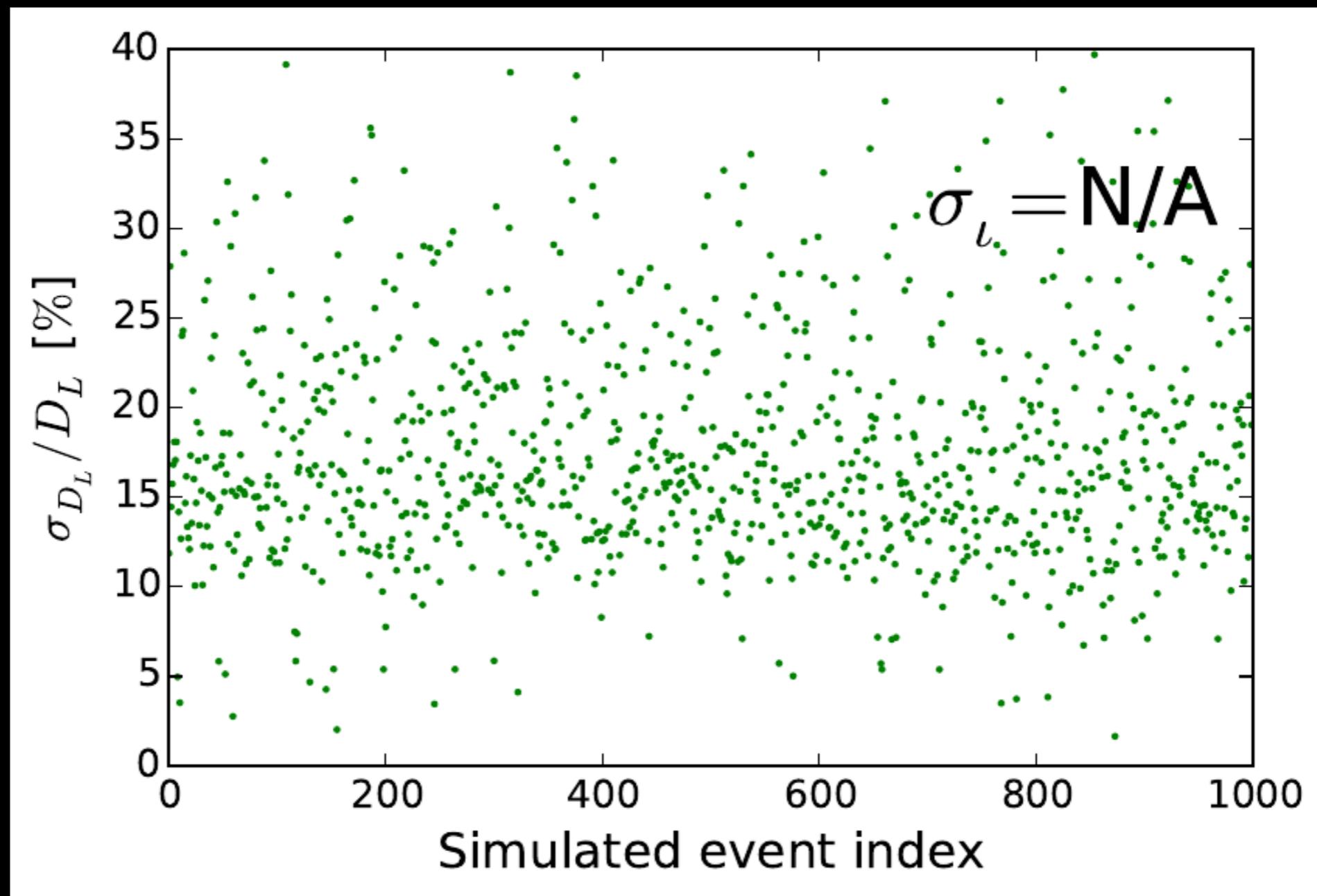
Kilonova

More isotropic than short gamma-ray burst but the exact emission geometry remains unclear.

Break the distance-inclination degeneracy

Neutron star mergers with **viewing angles constrained by electromagnetic emission.**

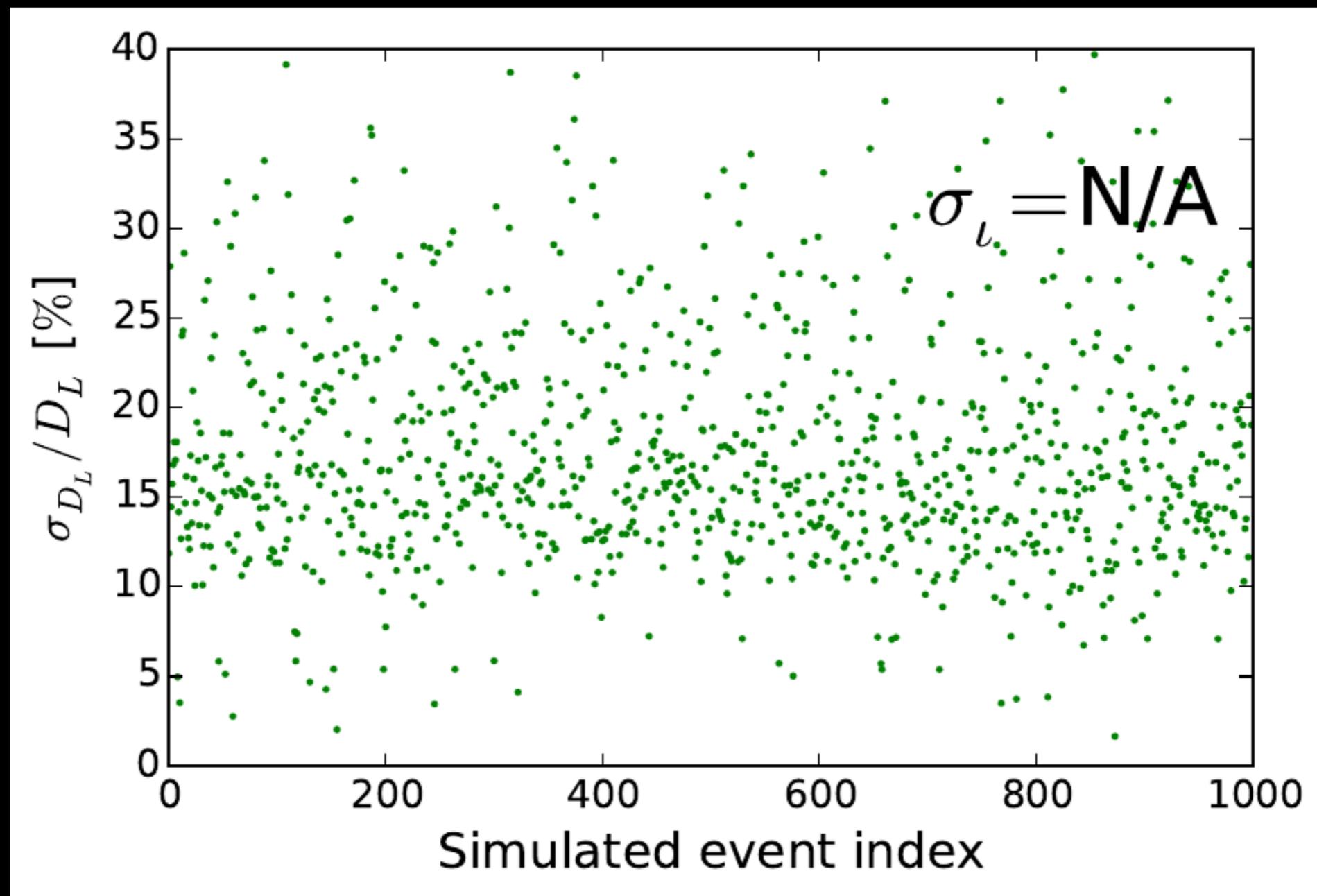
Chen, Vitale & Narayan, PRX, 2019



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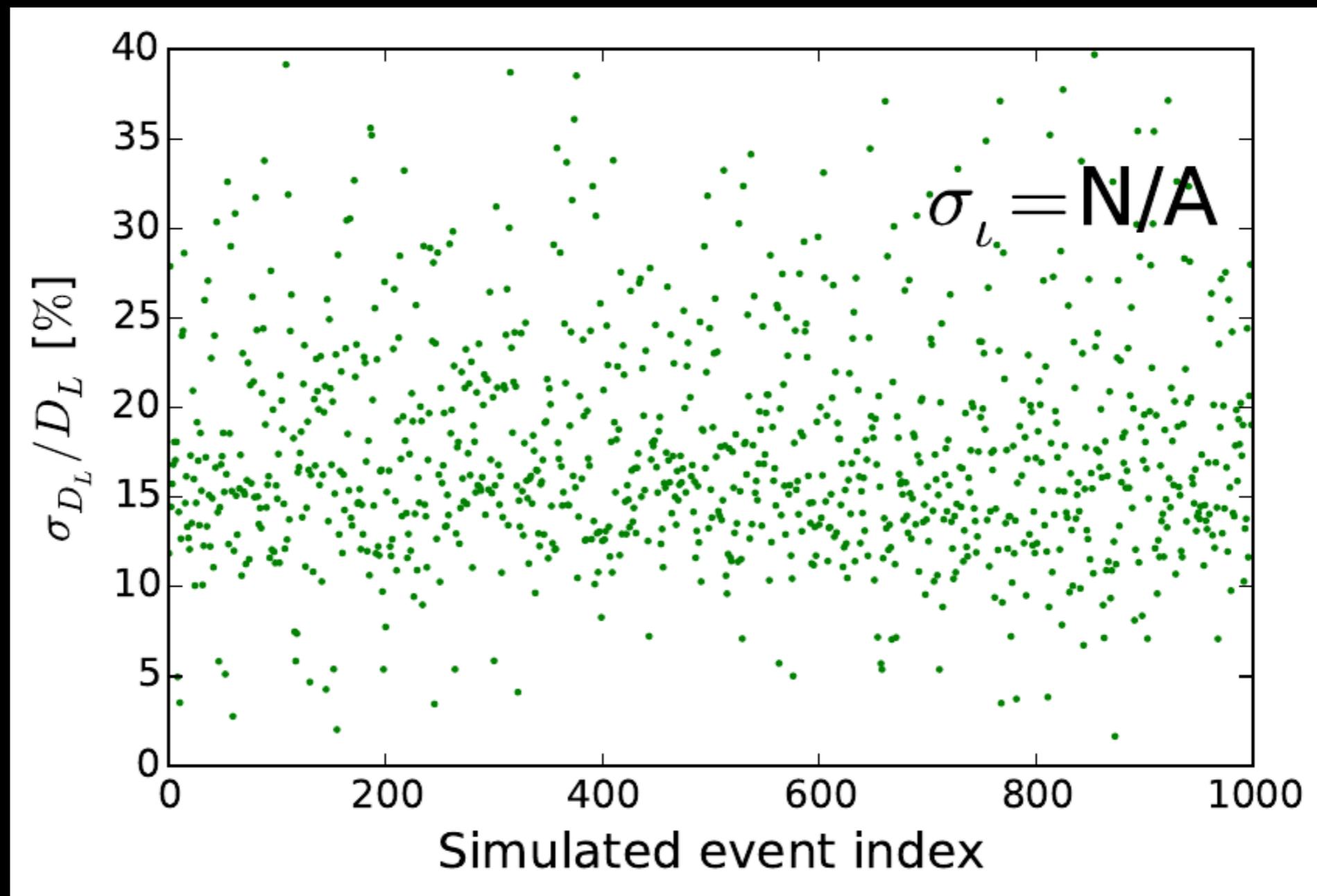
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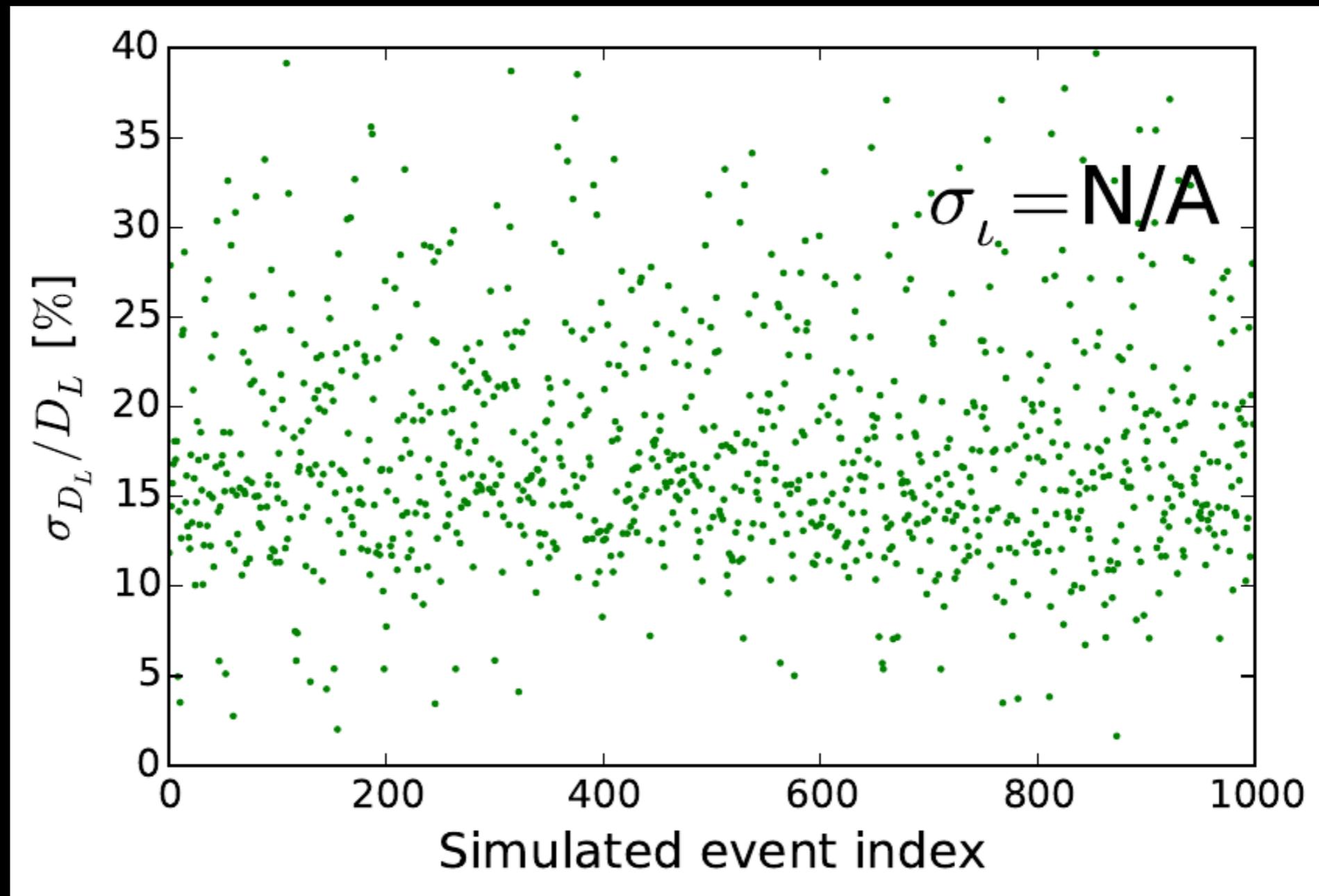


Can be viewed
as →
 H_0 uncertainty

Break the distance-inclination degeneracy

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Chen, Vitale & Narayan, PRX, 2019



Can be viewed
as →
 H_0 uncertainty

$$\sigma_{H_0} \propto \frac{1}{\sqrt{N}}$$

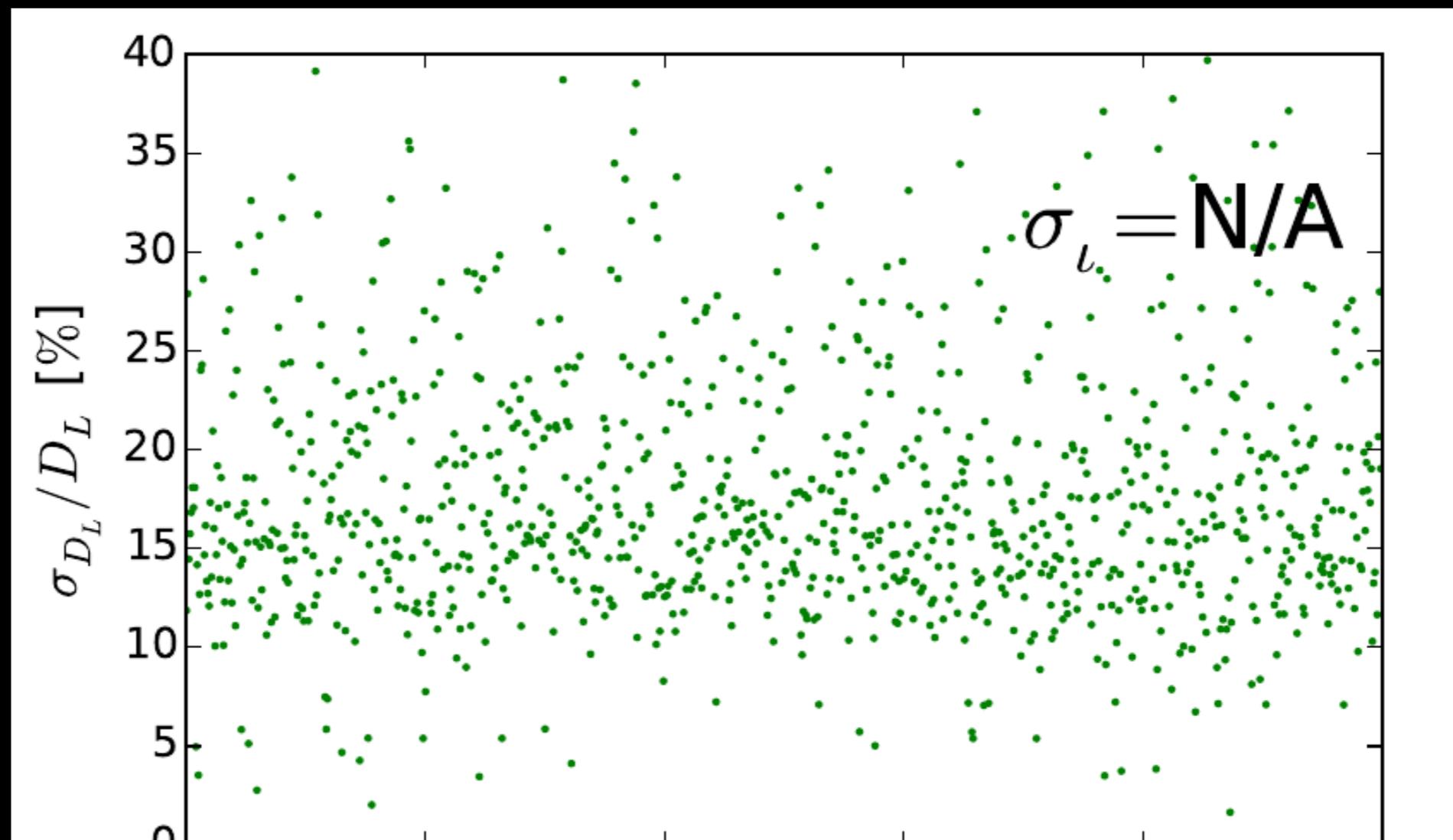
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as →
H₀ uncertainty

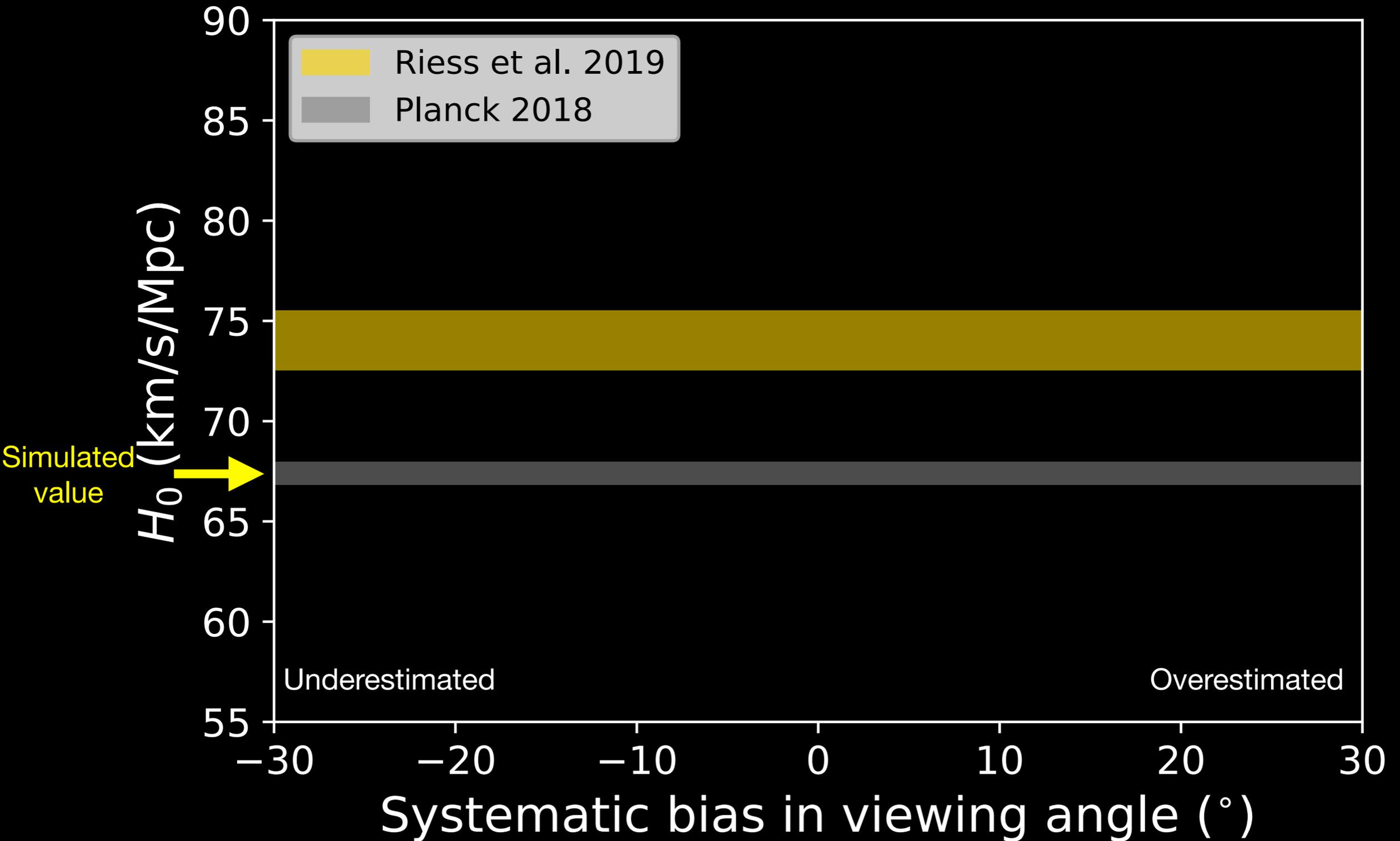
$$\sigma_{H_0} \propto \frac{1}{\sqrt{N}}$$



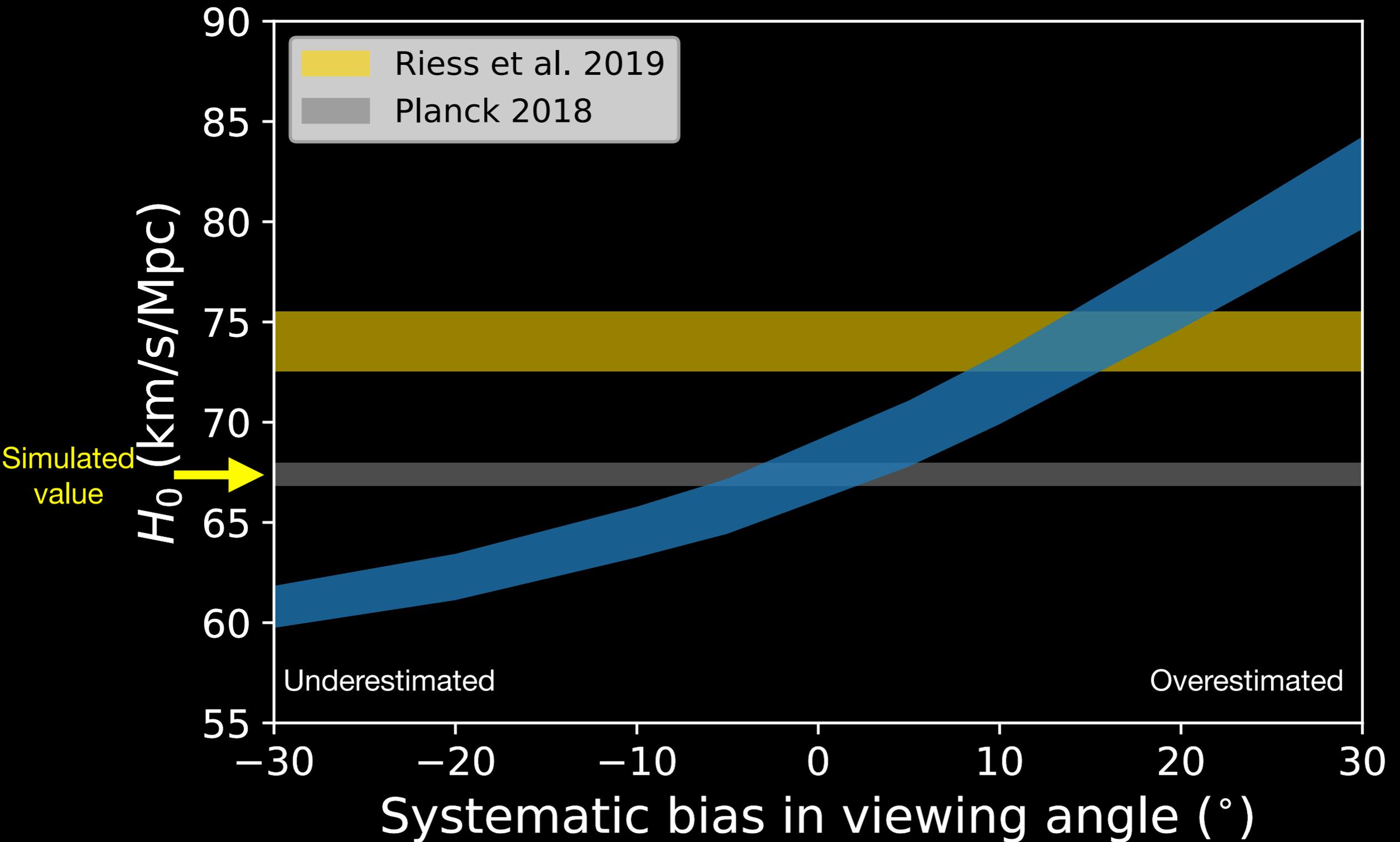
A factor of 5 to 10 fewer events are required to reach the same Hubble Constant precision if the viewing angle is constrained.

However, the estimation of viewing angle from electromagnetic observations has to be very accurate.

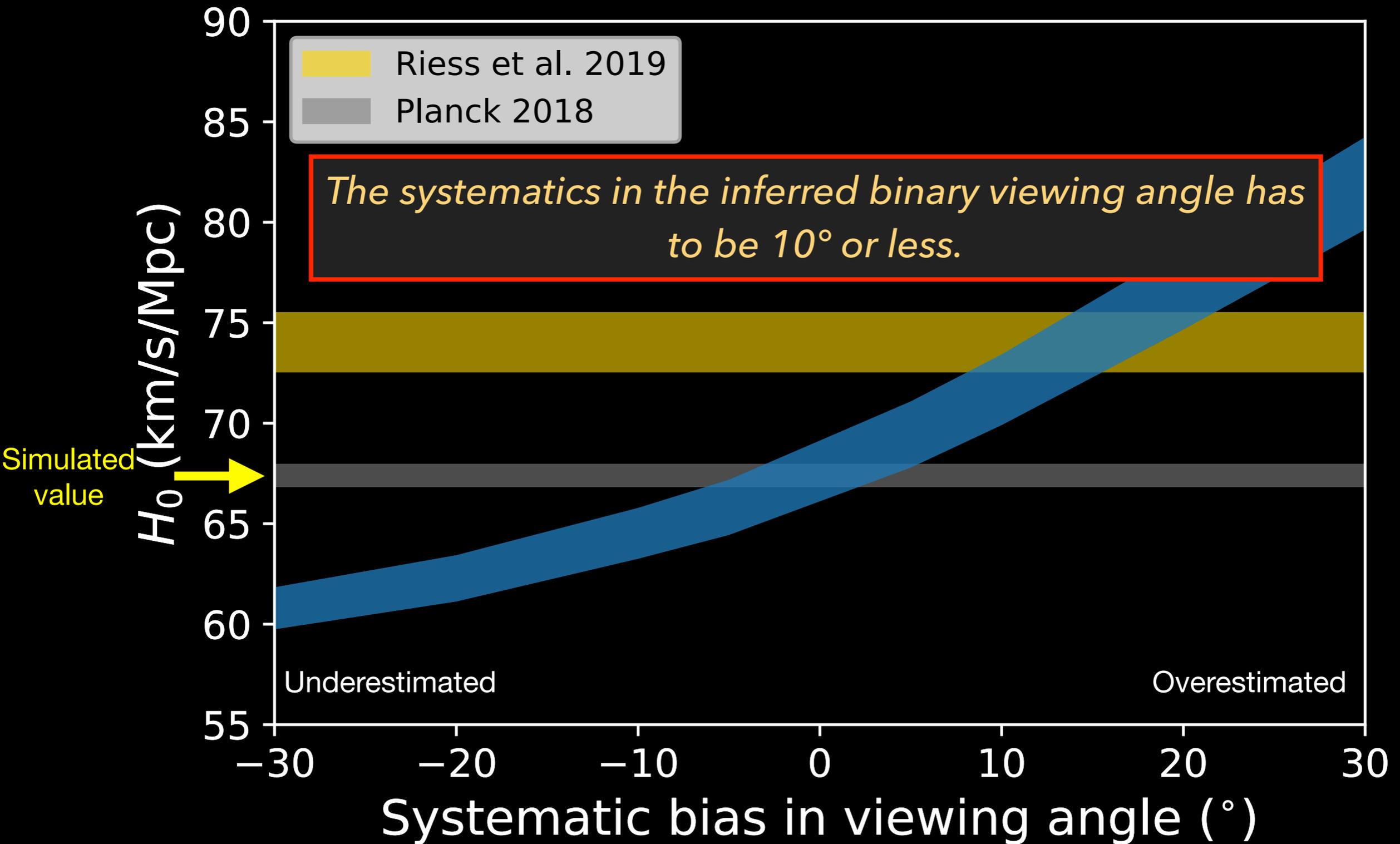
If the EM inferred viewing angle is biased



If the EM inferred viewing angle is biased



If the EM inferred viewing angle is biased



What if we don't use the viewing angle information from EM observations?

What if we don't use the viewing angle information from EM observations?

-The binaries available for standard siren measurement can still suffer from the undetermined selection over binary viewing angle.

Selection effect from binary viewing angle

Easy to observe

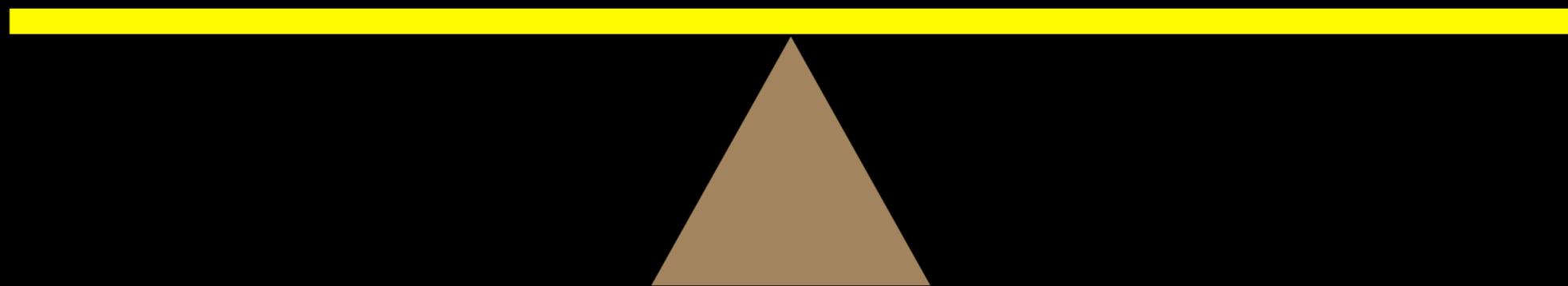


H_0 value
A

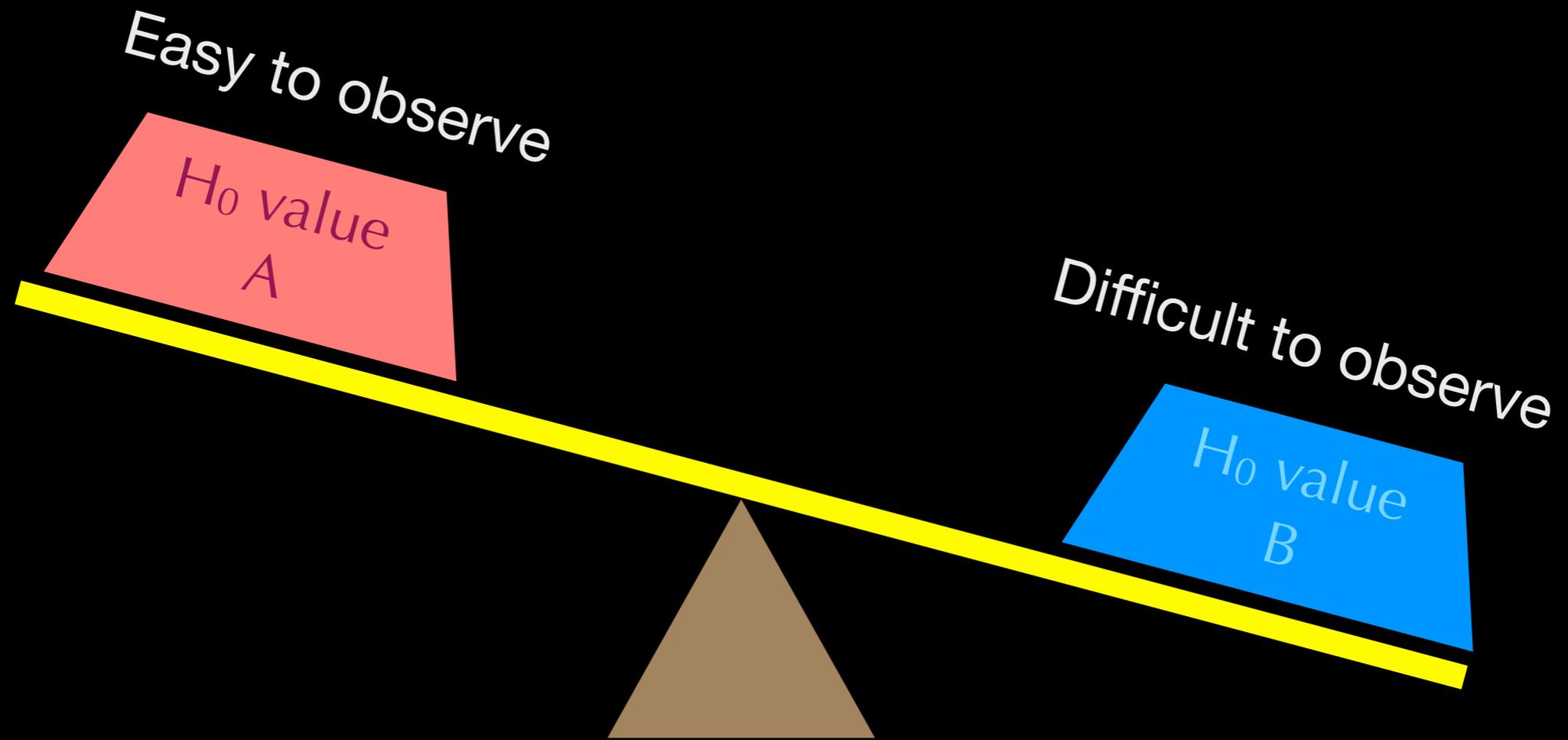
Difficult to observe



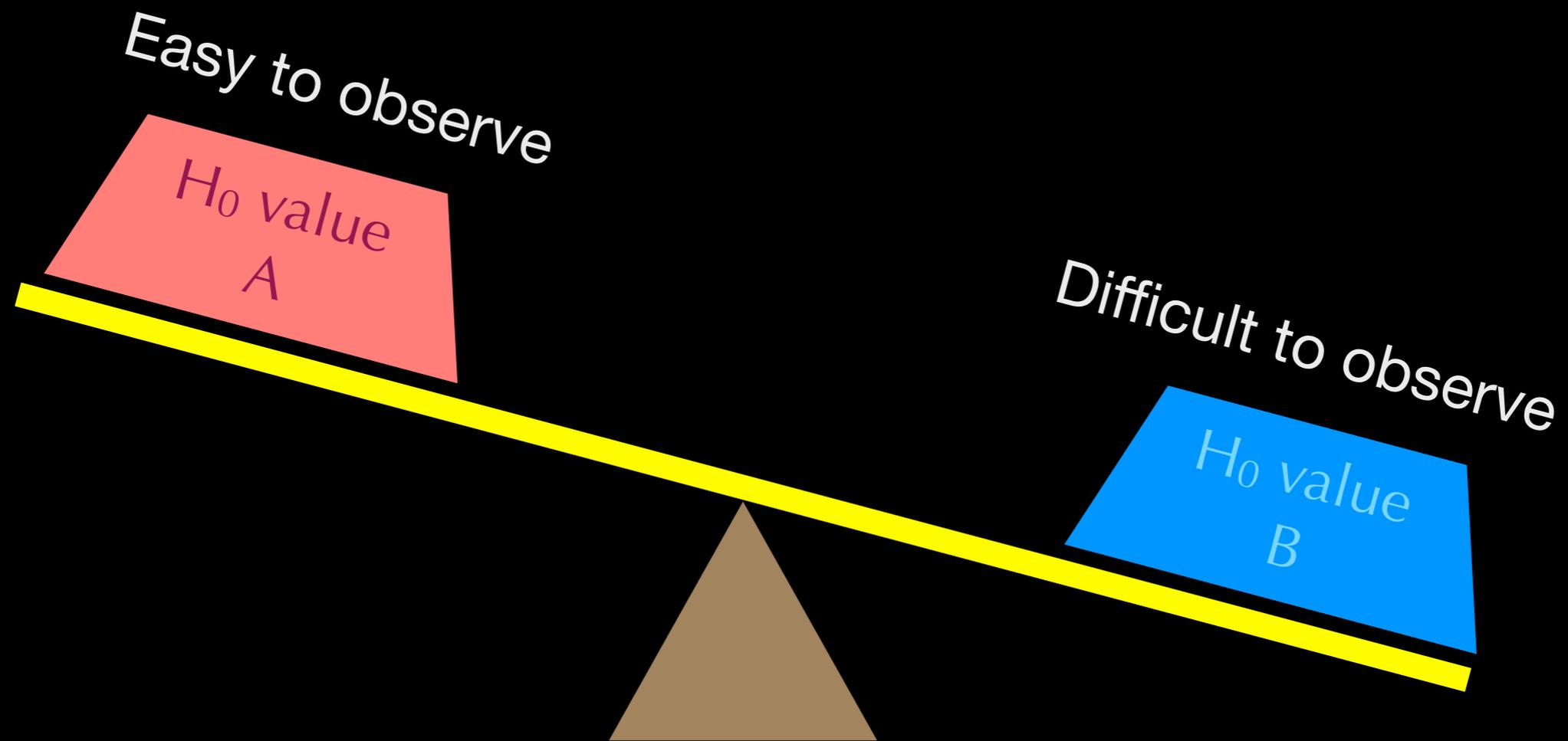
H_0 value
B



Selection effect from binary viewing angle

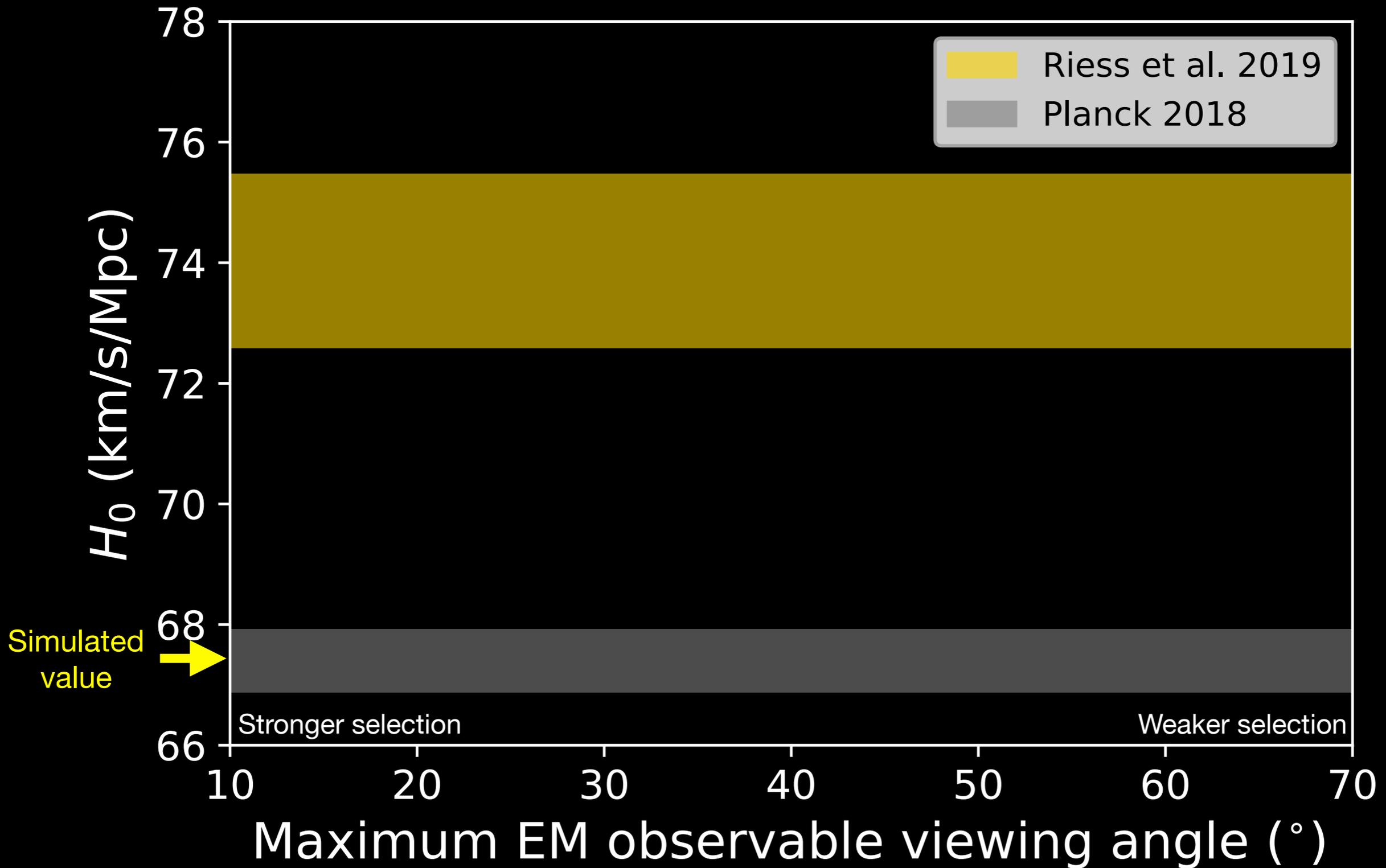


Selection effect from binary viewing angle

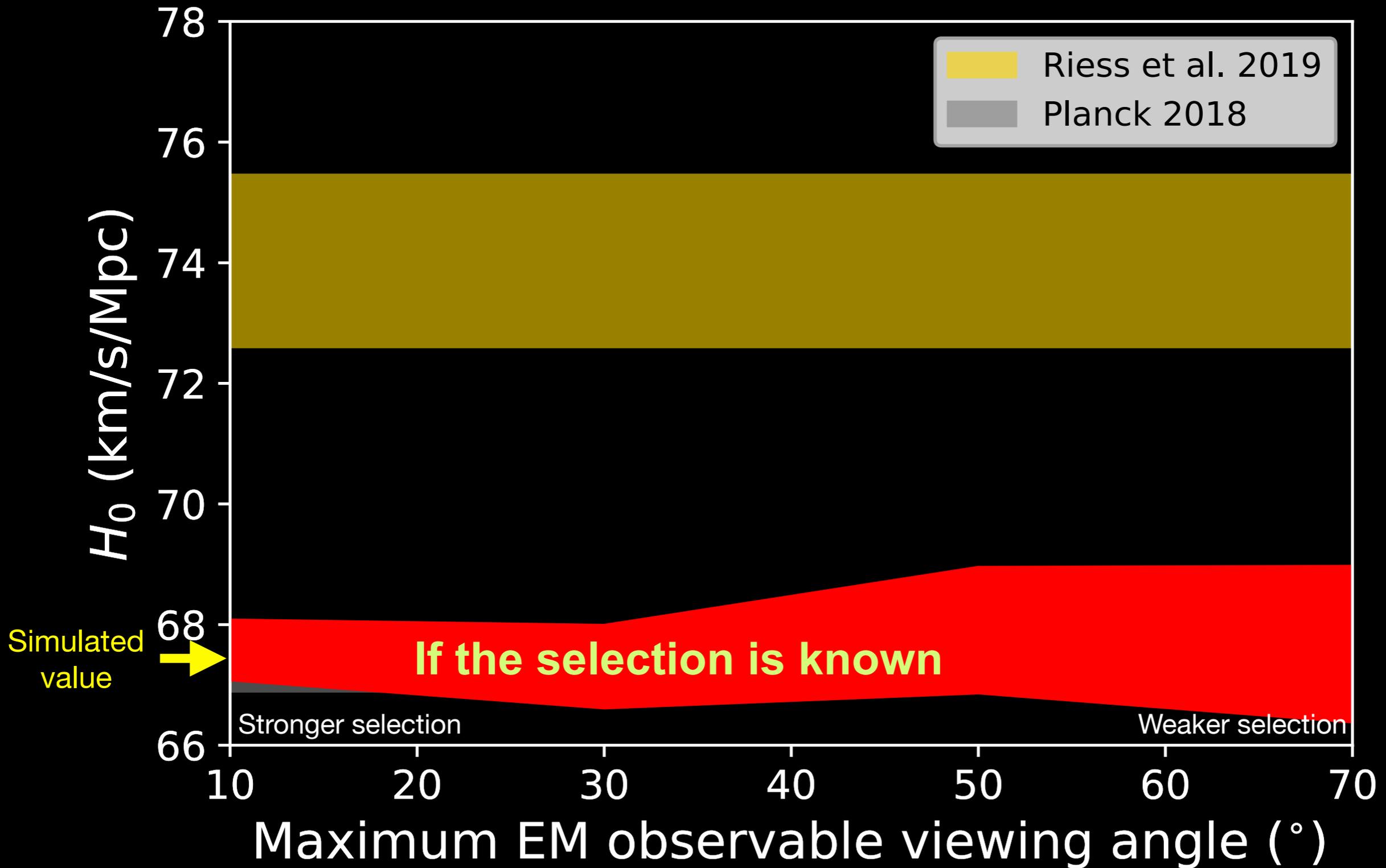


We don't know how to reweigh if the selection effect is unclear.

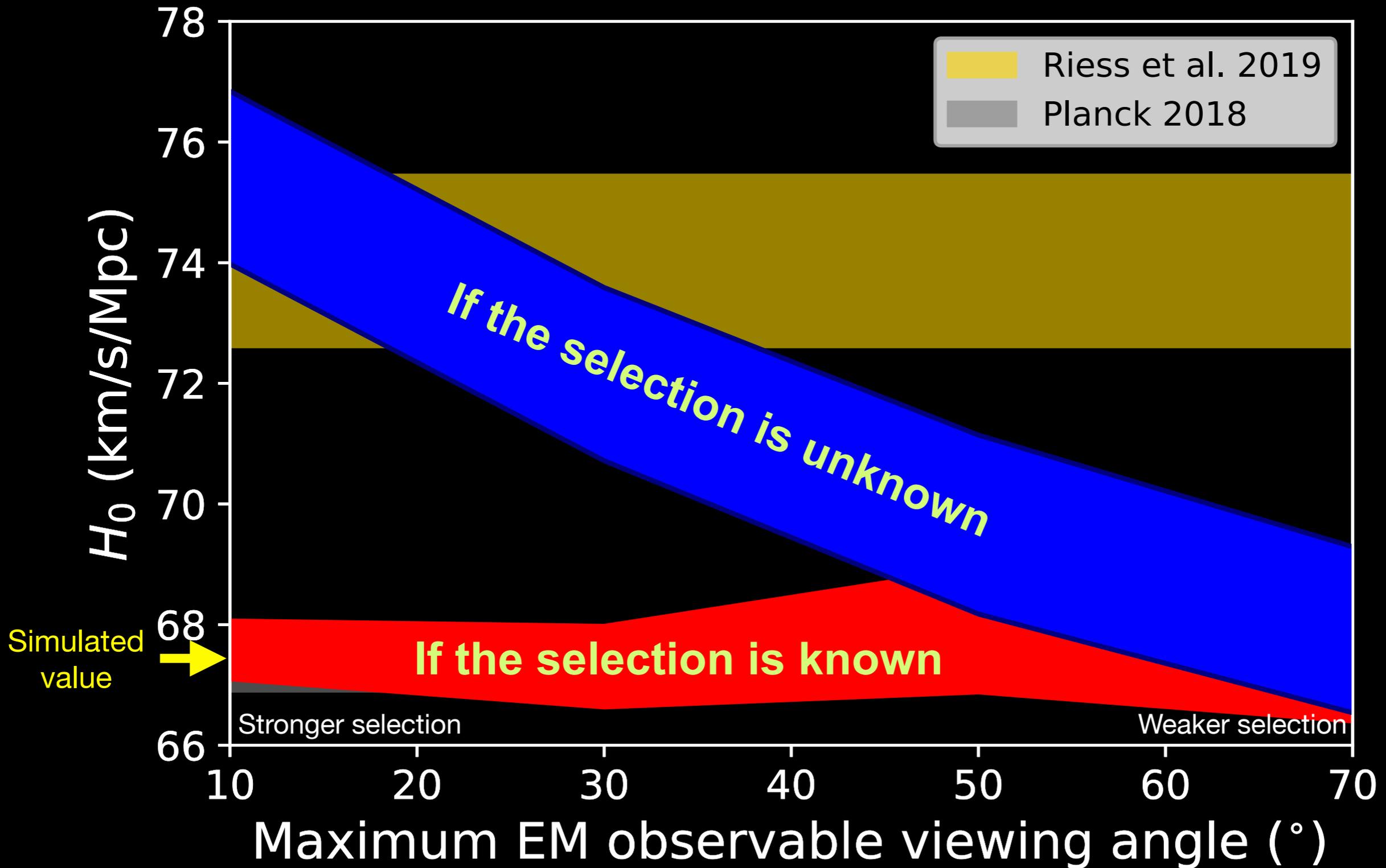
If the EM emissions are only observable up to a maximum viewing angle



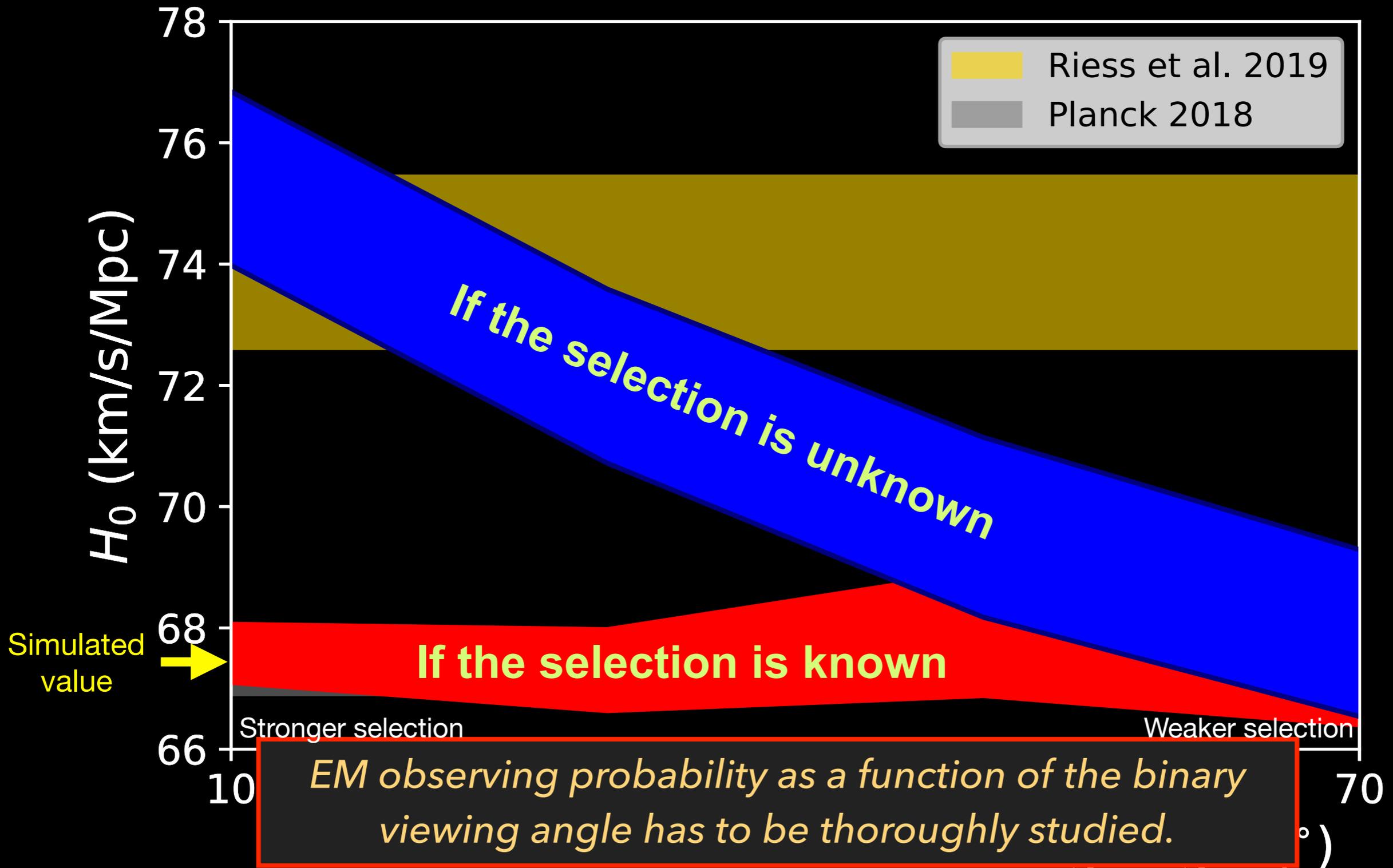
If the EM emissions are only observable up to a maximum viewing angle



If the EM emissions are only observable up to a maximum viewing angle



If the EM emissions are only observable up to a maximum viewing angle



Comparing to other systematic uncertainties of standard sirens

Host galaxy peculiar velocities

Howlett & Davis (2019), Mukherjee et al. (2019), Nicolaou et al. (2019)

Gravitational waveform systematics

Abbott et al., PRX, 2019

Instrumental calibration uncertainty

- *<2% for LIGO-Virgo third observing run.*

Sun et al. (2020)

- *Expected to be smaller in the future.*

Karki et al. (2016)

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Viewing angle selection effect can dominate the systematics of standard sirens.

Summary

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-Gravitational waves can serve as an independent probe to the Hubble constant.

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- Gravitational waves can serve as an independent probe to the Hubble constant.
- There are many different possibilities to reduce the statistical uncertainty of standard siren measurements.
- However, we have to first figure out how to reduce the systematics!

Thank you!