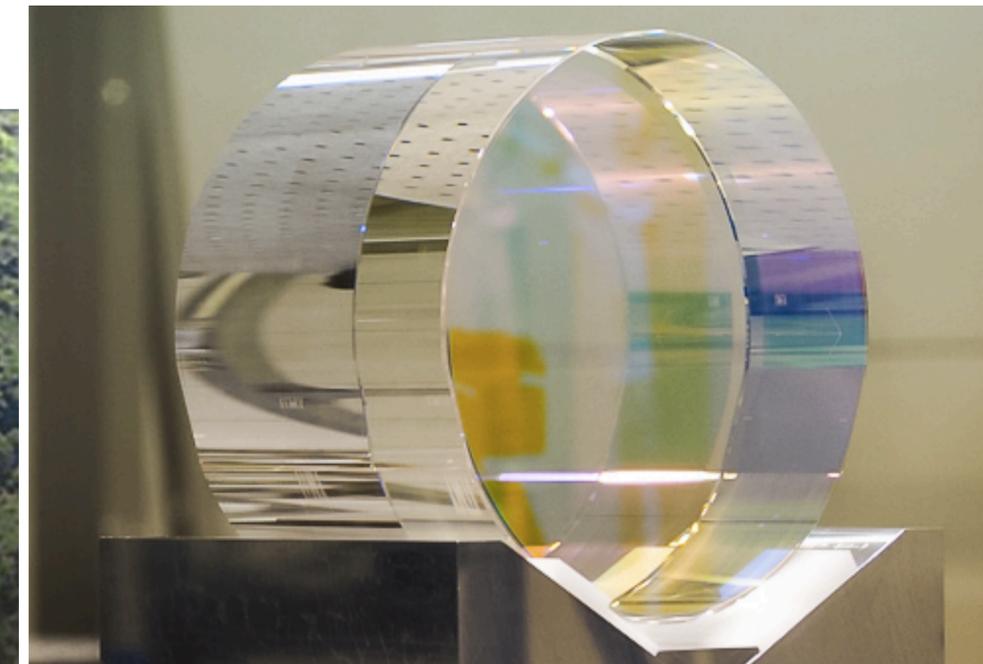


# Measurement of the mechanical loss of reflective coatings for Cryogenic Gravitational wave telescope

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Univ.Toyama, ICRR<sup>A</sup>

# Cryogenic Gravitational wave telescope KAGRA

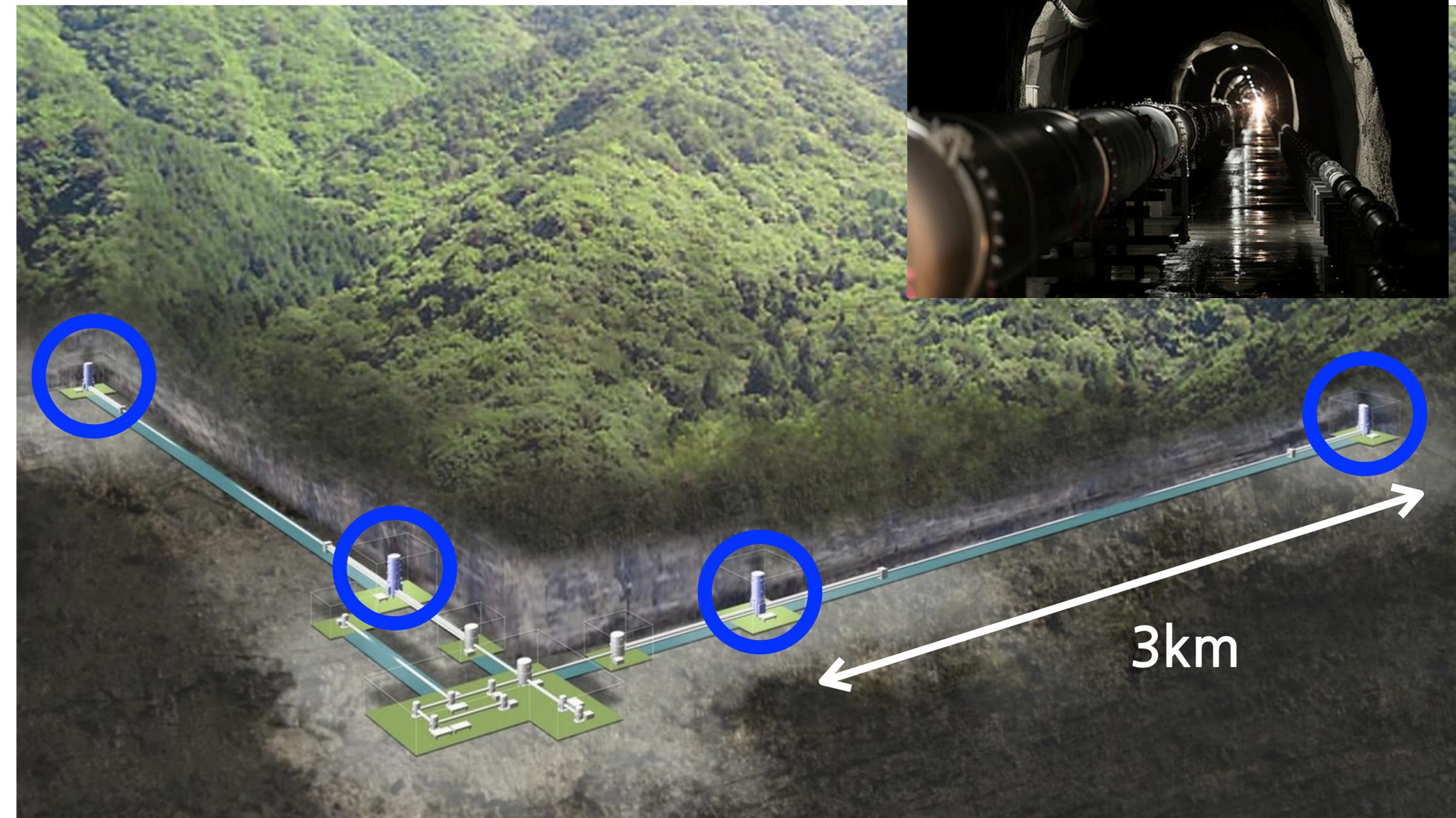
Michelson interferometer with 3 km Fabry-Perot cavity arms in Japan



Cryogenic (about 20 K)

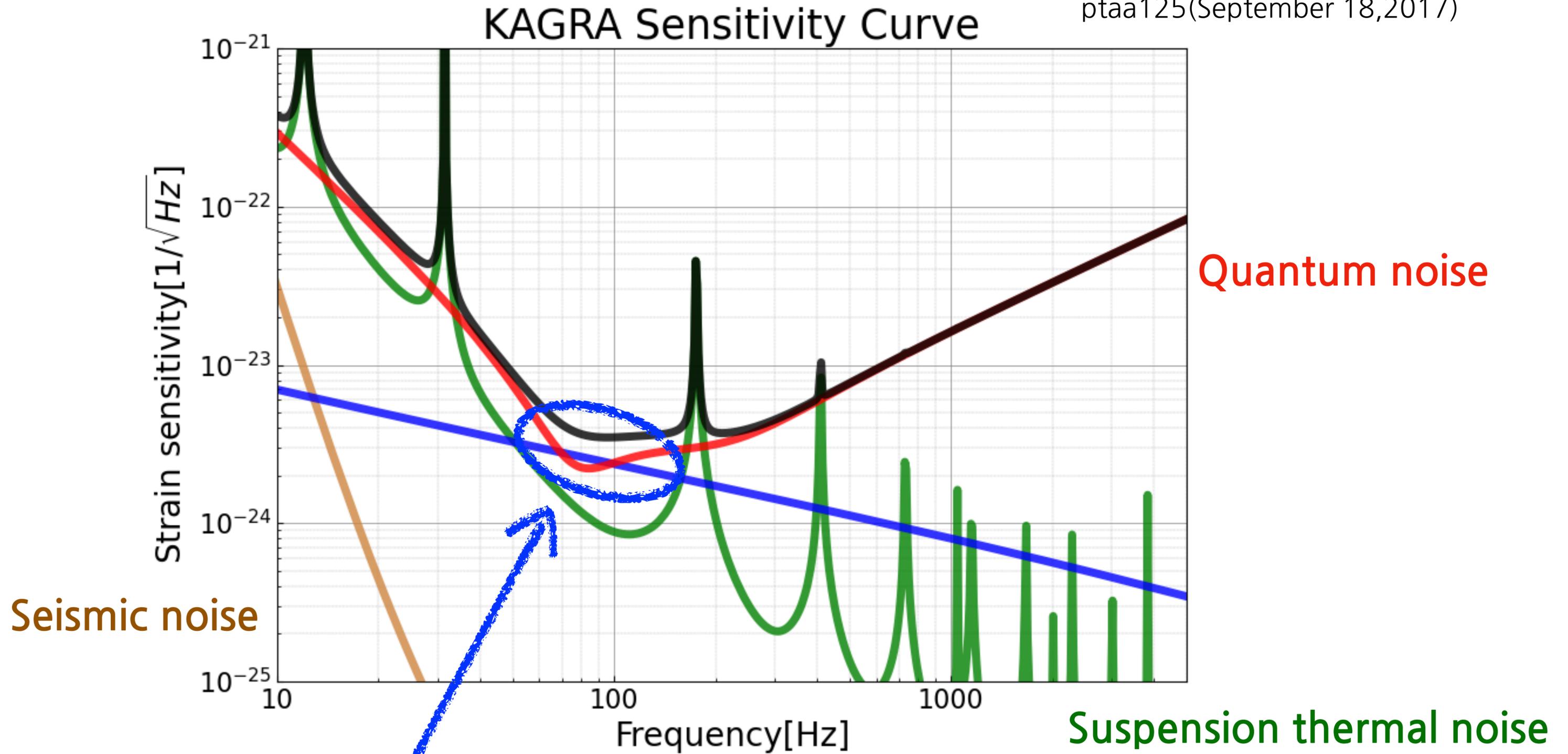
**Sapphire**

Excellent property  
at low temperature



# KAGRA target sensitivity

Progress of Theoretical and Experimental Physics,  
ptaa125(September 18,2017)



Seismic noise

Quantum noise

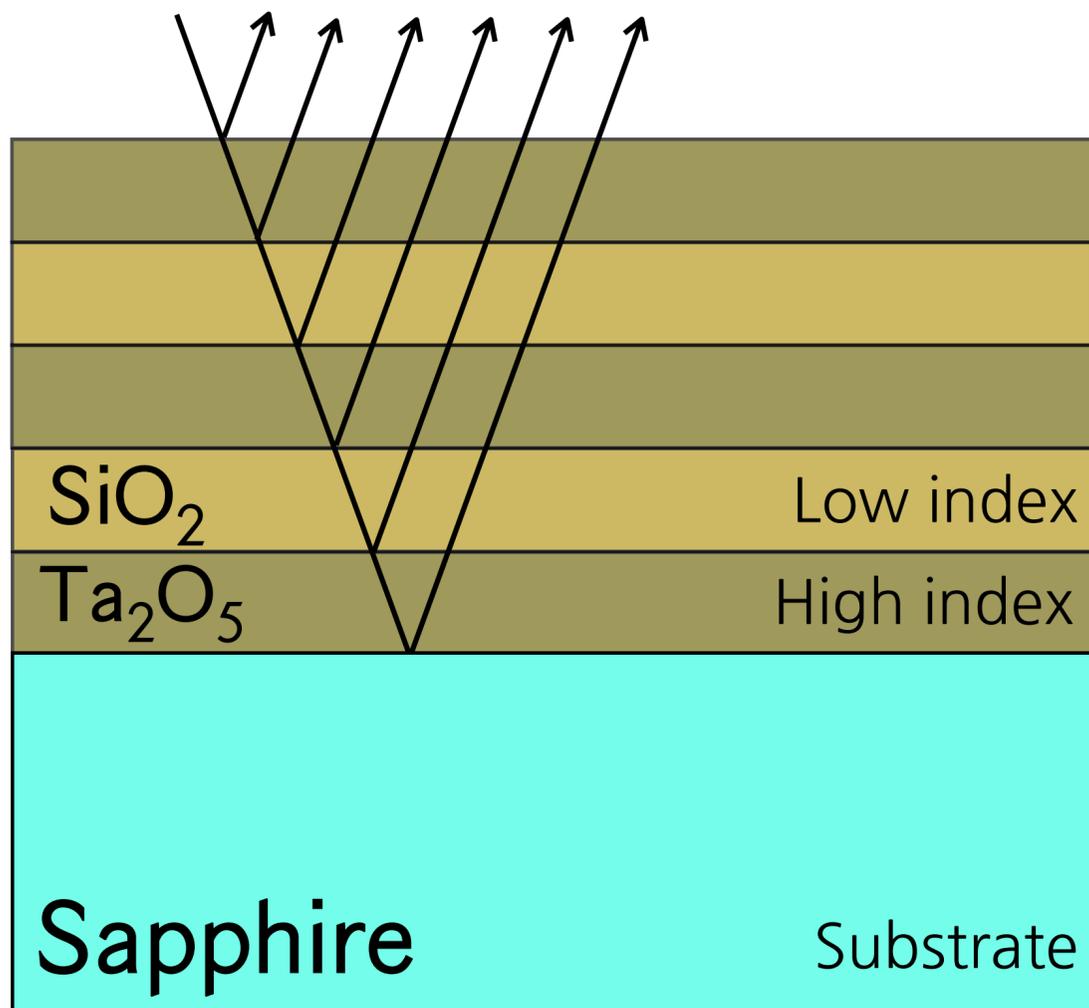
Suspension thermal noise

**Mirror thermal noise** mainly comes from the coating of the mirror

# Coating

## Coating

The mirror requires high reflectance to reduce the shot noise.  
The surface of the mirror is coated with the dielectric multilayer (Coating).



### The dielectric multilayer

- Alternating layers of low and high index materials.

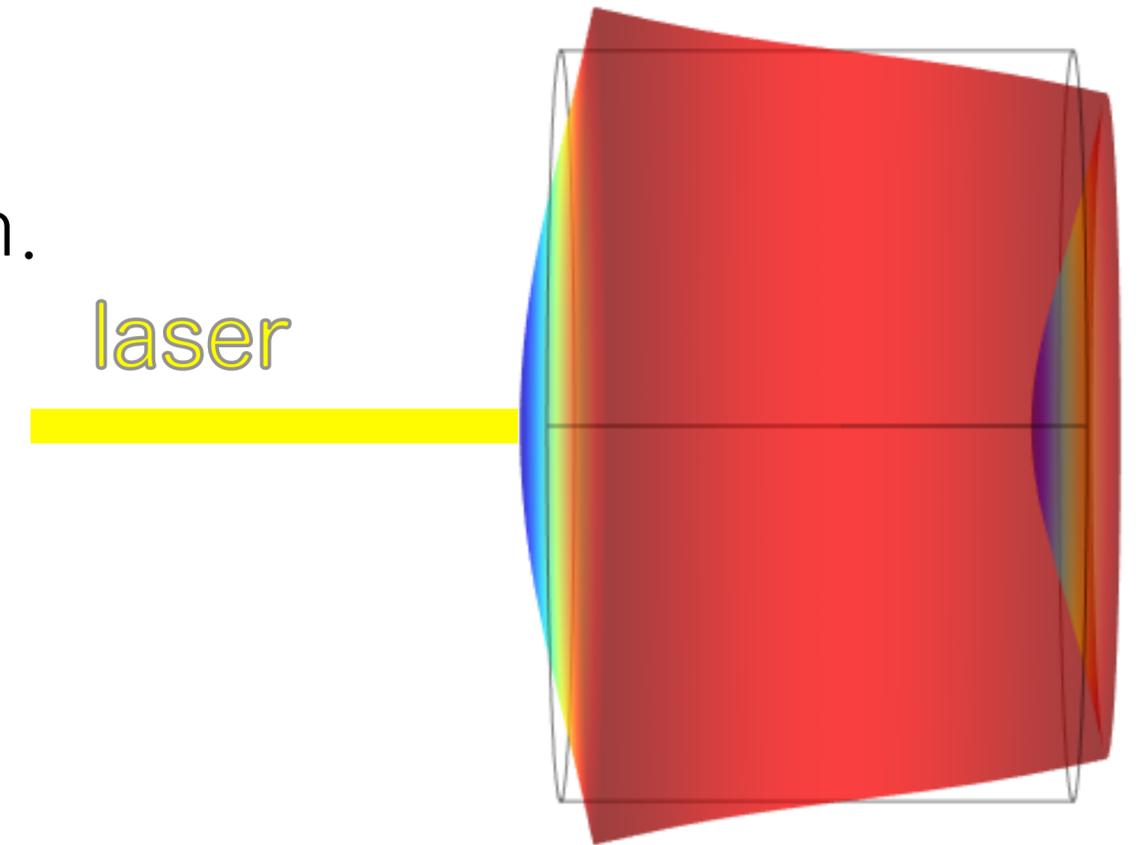
KAGRA of end test mass : 40 layers of  $\text{SiO}_2/\text{Ta}_2\text{O}_5$

- The optical thickness of each layer is  $\lambda/4$  ( $\lambda=1064$  nm).
- Since the interferences between reflected light on the layer boundaries are constructive, the reflectance of the coating is quite high.

# Mirror thermal noise

## Mechanism of mirror thermal noise

- Mirror receives the energy from Heat Bath at random.
- Mirror elastic vibration is excited.
- Mirror surface moves along the laser axis.
- The optical path length changes.



## Evaluation of mirror thermal noise

Fluctuation-Dissipation Theorem(FDT)

$$G_{\text{thermal noise}} \propto \sqrt{T\phi_{\text{loss}}(\omega)}$$

Mirror thermal noise  
(Power spectrum density)

Temperature

Mechanical loss

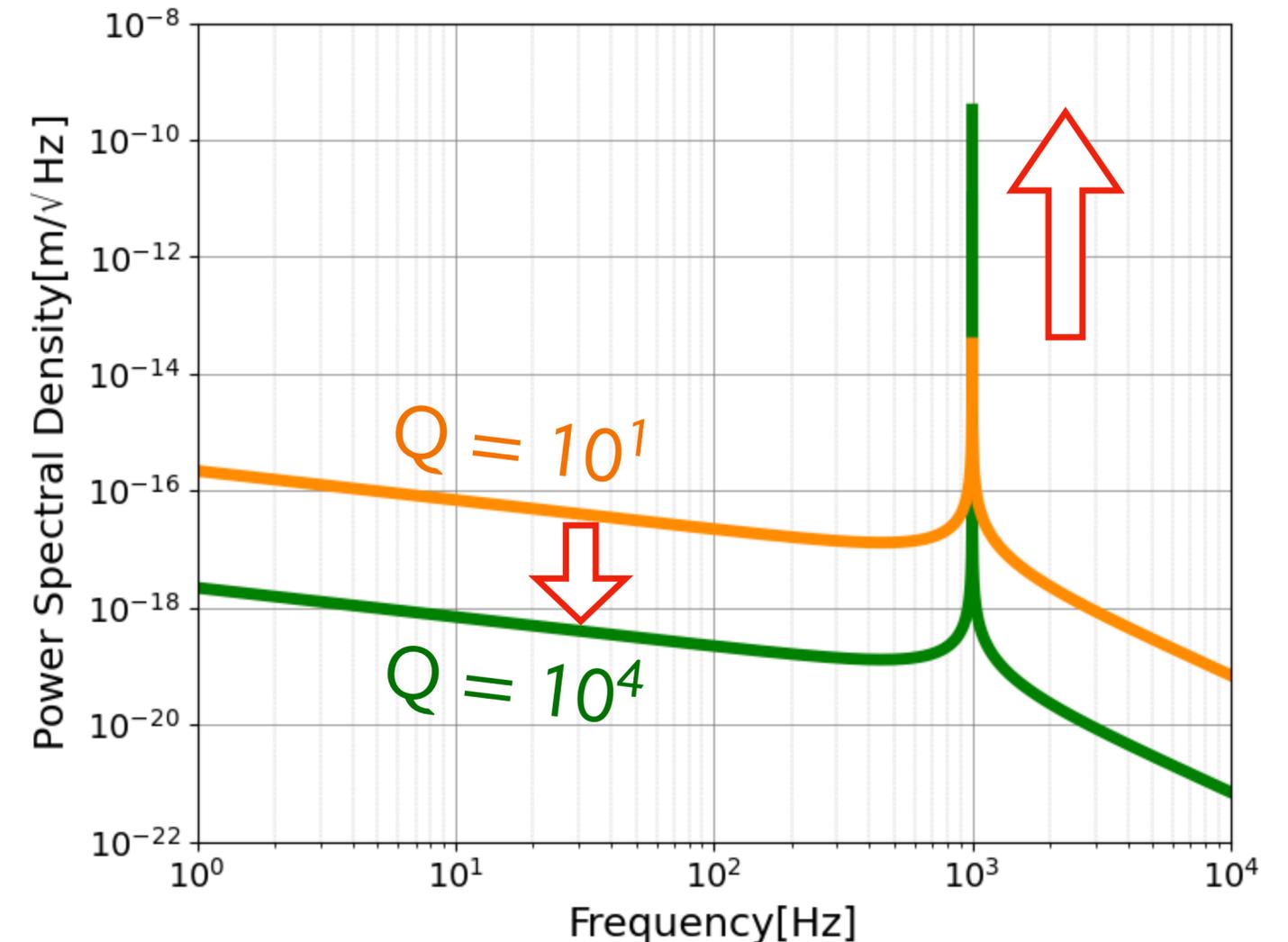
# Mechanical loss

## Mechanical loss

- Due to the loss of the elastic energy inside the mirror.
- The ratio of the dissipated energy per cycle to total stored energy.

$$\phi = \frac{E_{\text{lost per cycle}}}{2\pi E_{\text{total stored}}} = \frac{1}{Q}$$

Peak sharpness  
at resonant frequency

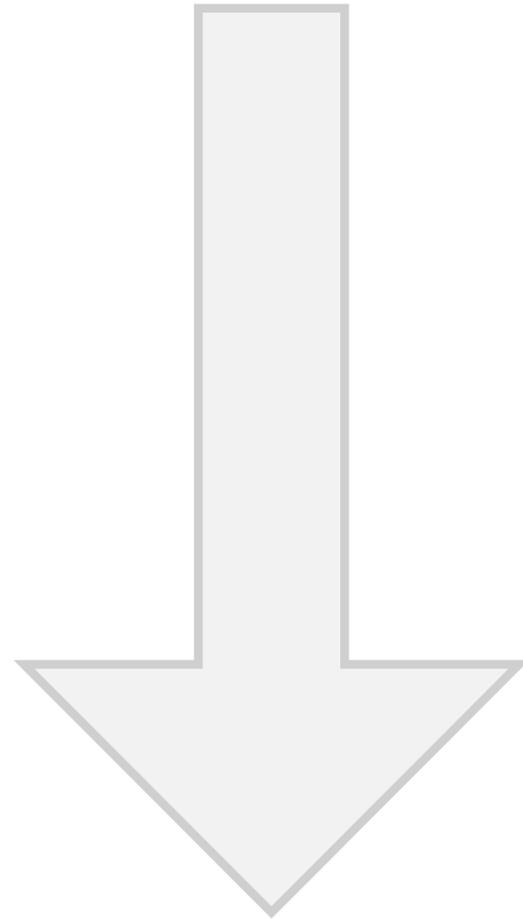


Reduce the coating thermal noise

→ Use a material with **small mechanical loss in the coating**

# Purpose of measurement

The  $\text{TiO}_2$  doped coating has a smaller mechanical loss at 300 K.



	Substrate	Coating	Temperature
LIGO and Virgo	Fused silica	$\text{SiO}_2/\text{Ta}_2\text{O}_5$ doped $\text{TiO}_2$	300 K
KAGRA	Sapphire	$\text{SiO}_2/\text{Ta}_2\text{O}_5$ undoped $\text{TiO}_2$	about 20 K

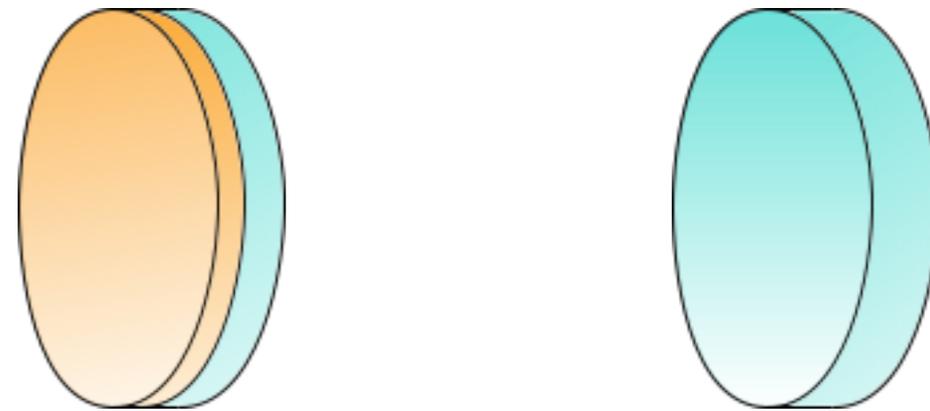
Comparison of the mechanical loss of coating of  $\text{TiO}_2$  doped and undoped on sapphire at low temperature.

# Estimation of coating mechanical loss $\phi$

Coating is extremely thin.  $\longrightarrow$  We prepare two kind of sapphire disks.

The one sapphire disk is **with coating**, and the other one is **without coating**.  
We measure each mechanical loss and take the difference between the two disks.

$$\phi_{\text{coating}} \simeq \frac{E_{\text{sapphire}}}{E_{\text{coating}}} \left( \phi_{\text{with coating}} - \phi_{\text{without coating}} \right)$$



Elastic strain energy  $E$

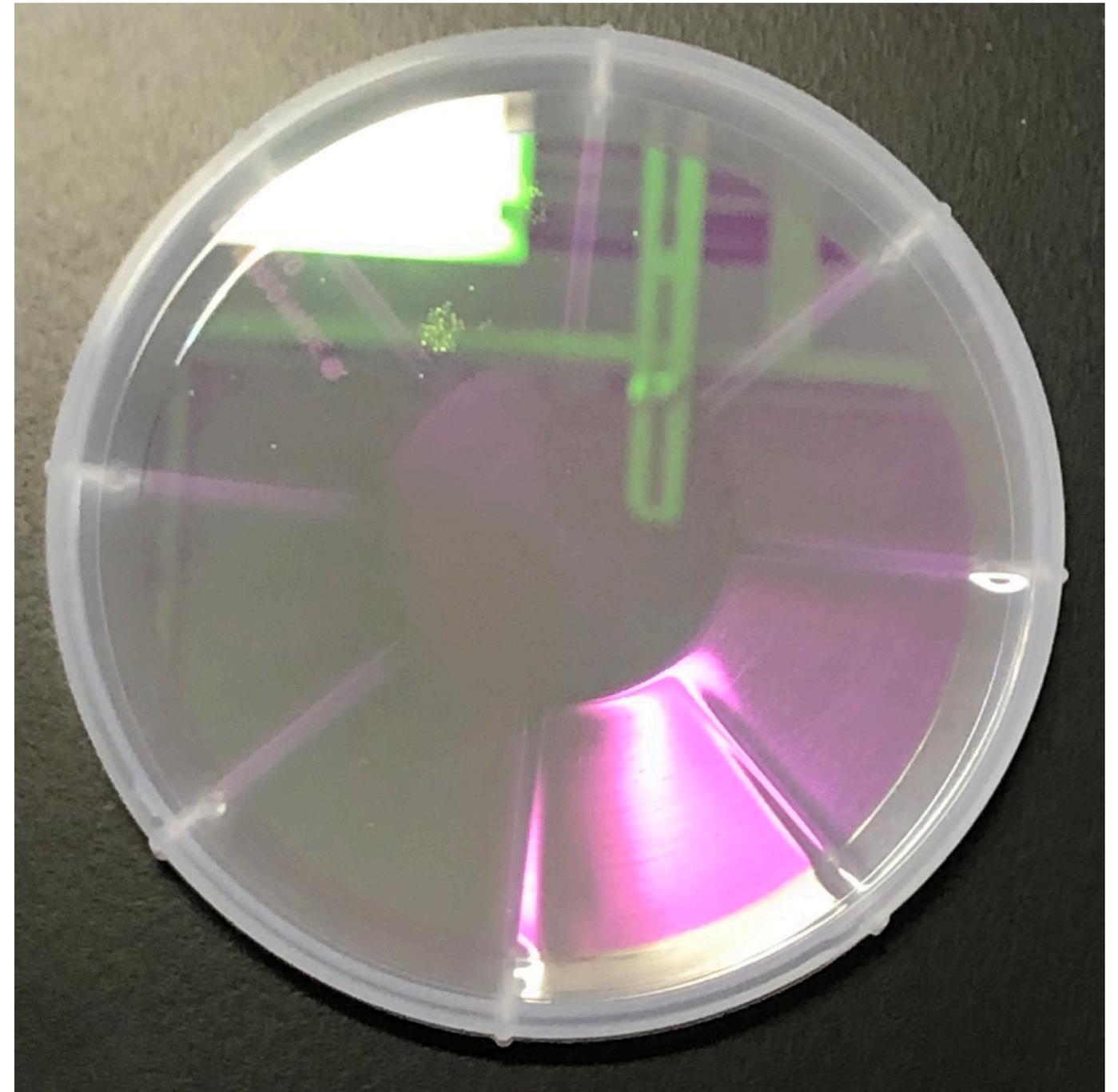
- Stored energy in deformed material.
- The value is calculated using FEM : COMSOL

# Sample

Sapphire disk : 100 mm diameter and 0.5 mm thickness

Substrate	Coating
Sapphire	SiO <sub>2</sub> /Ta <sub>2</sub> O <sub>5</sub> doped TiO <sub>2</sub> (38 layers)
Sapphire	SiO <sub>2</sub> /Ta <sub>2</sub> O <sub>5</sub> undoped TiO <sub>2</sub> (40 layers)
Sapphire	Nothing

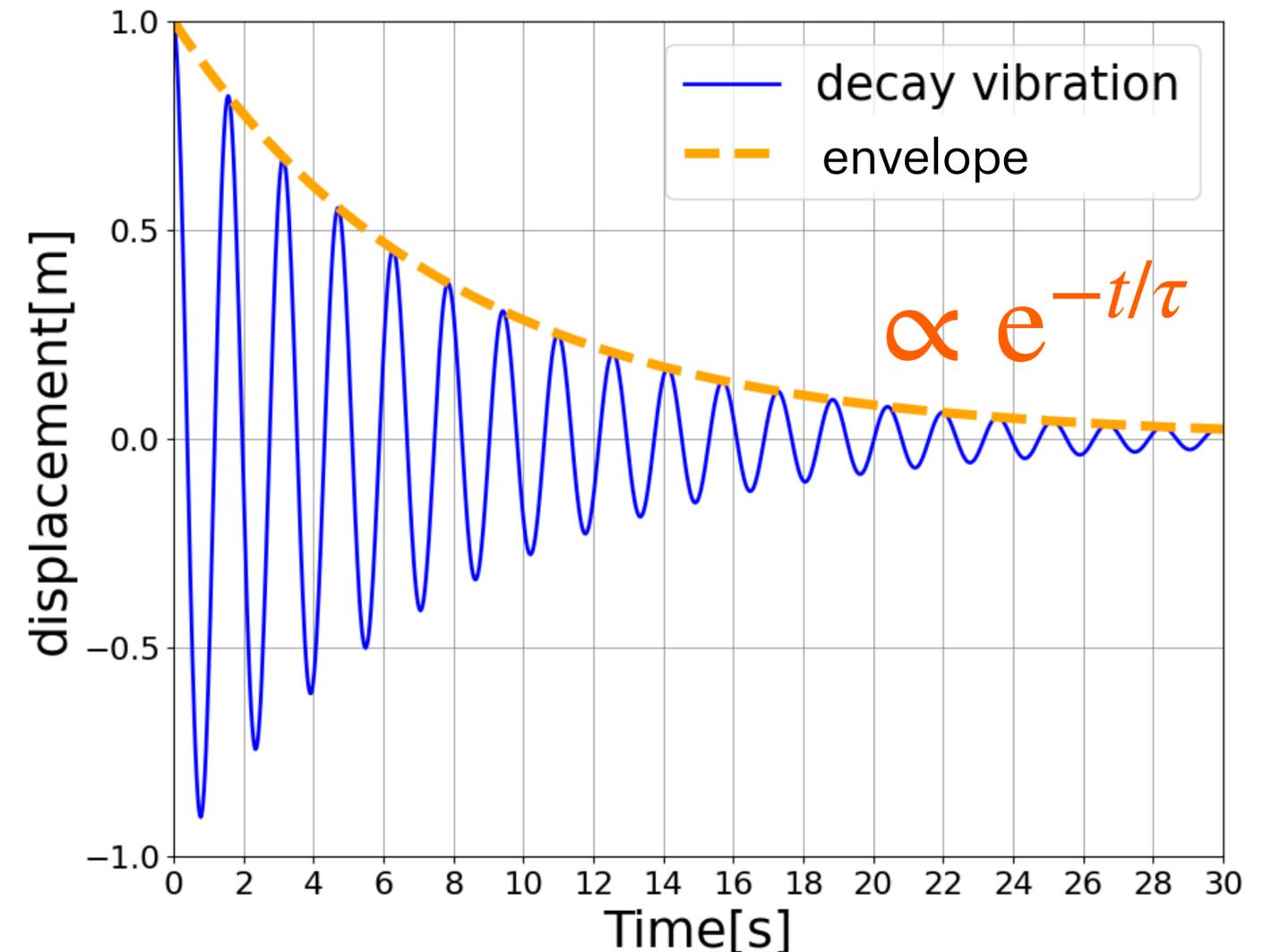
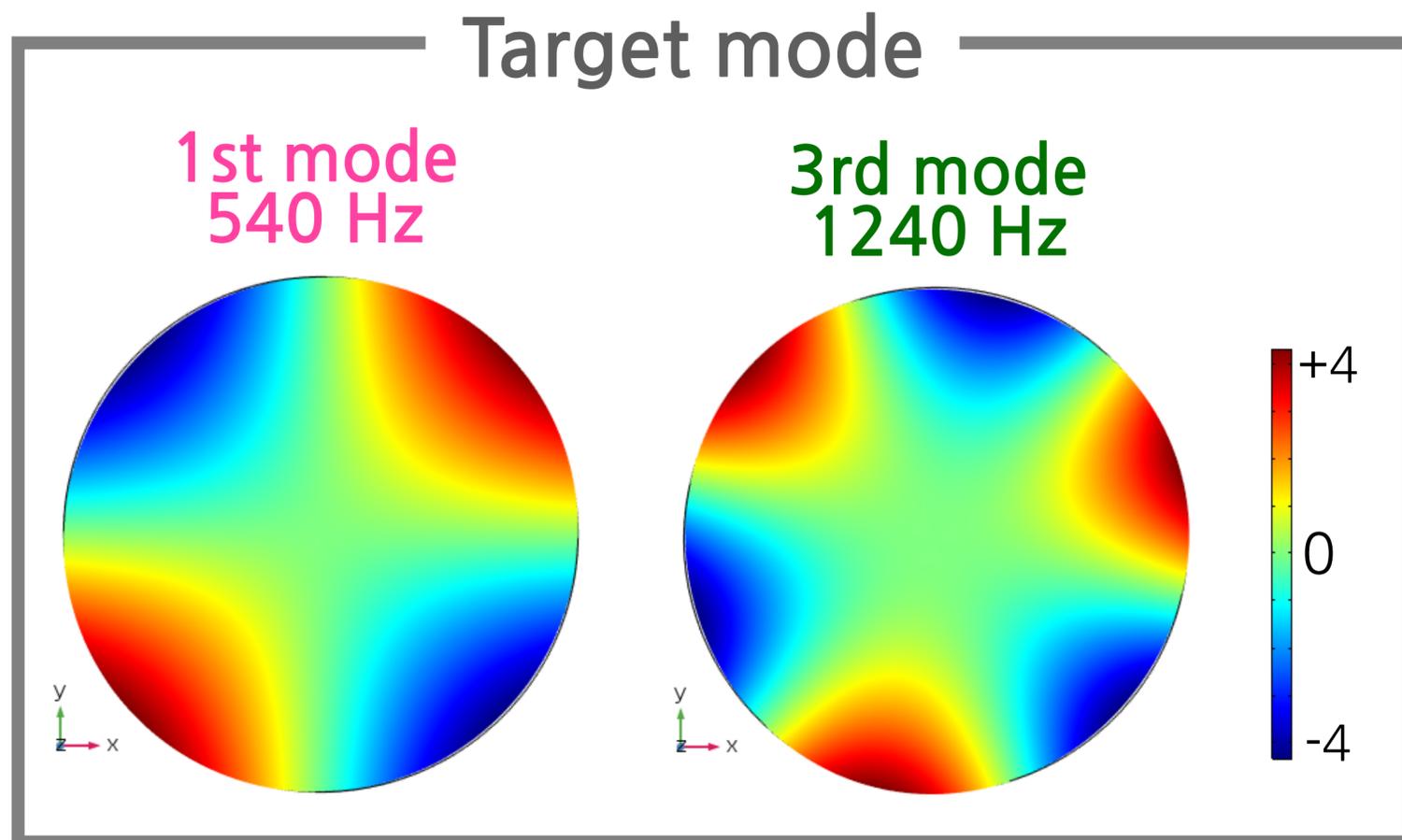
Deposited at LMA(France),  
which deposit coating LIGO, Virgo and KAGRA mirrors



# Measurement method

## Ring down method

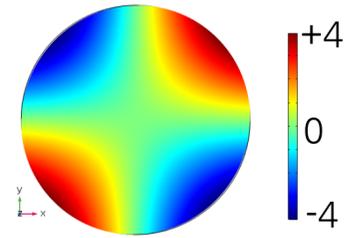
1. Exciting the disk at a resonant frequency using an electrostatic actuator.
2. Stop the excitation of the actuator.
3. Measuring the decay time  $\tau$  by an electrostatic transducer.
4.  $\phi$  is derived from  $\phi = 1/f\pi\tau$  ( $f$ : resonant frequency).



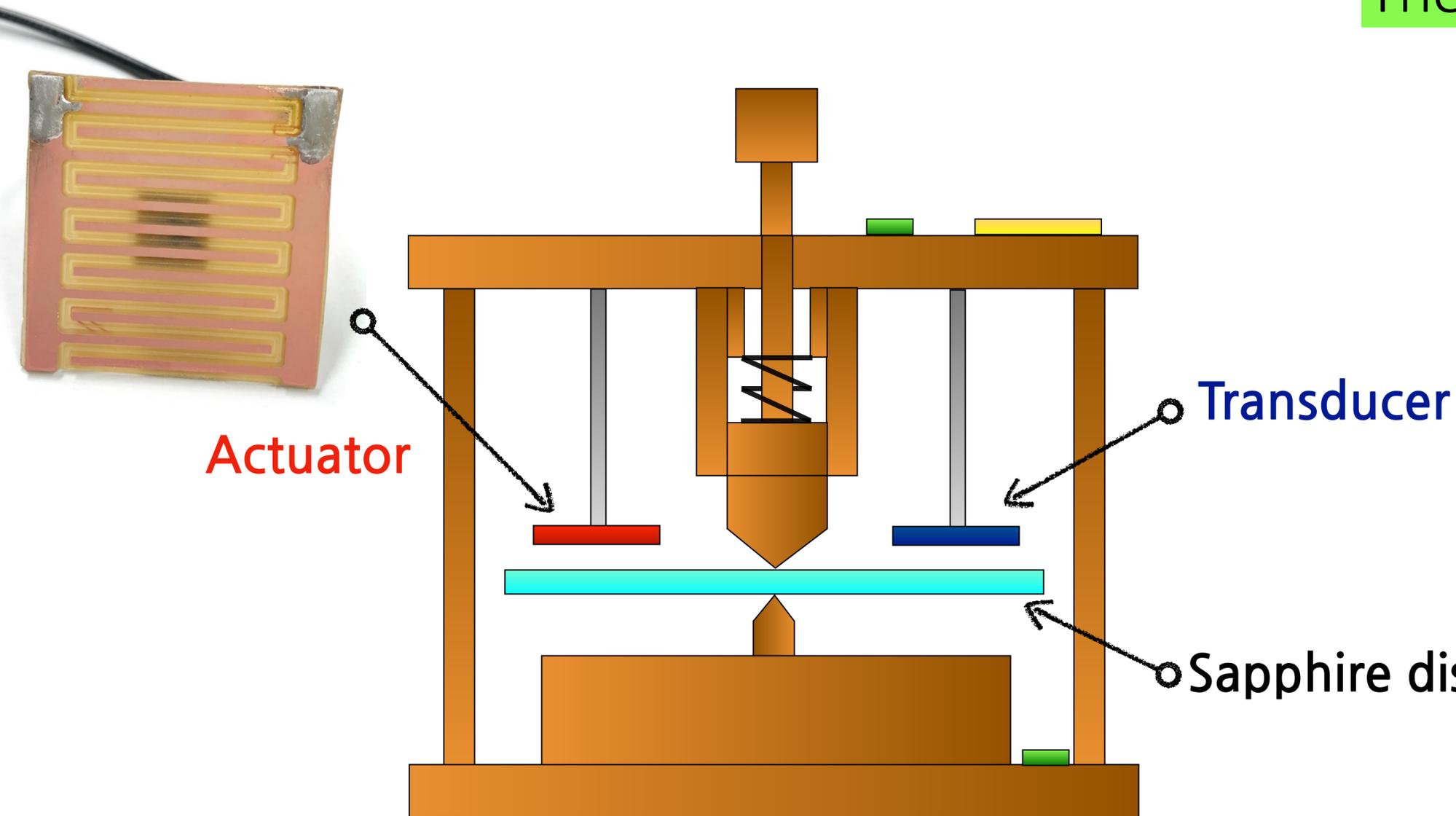
# Experiment apparatus in Univ. Toyama

## Nodal support system

Only the center of the disk is fixed.

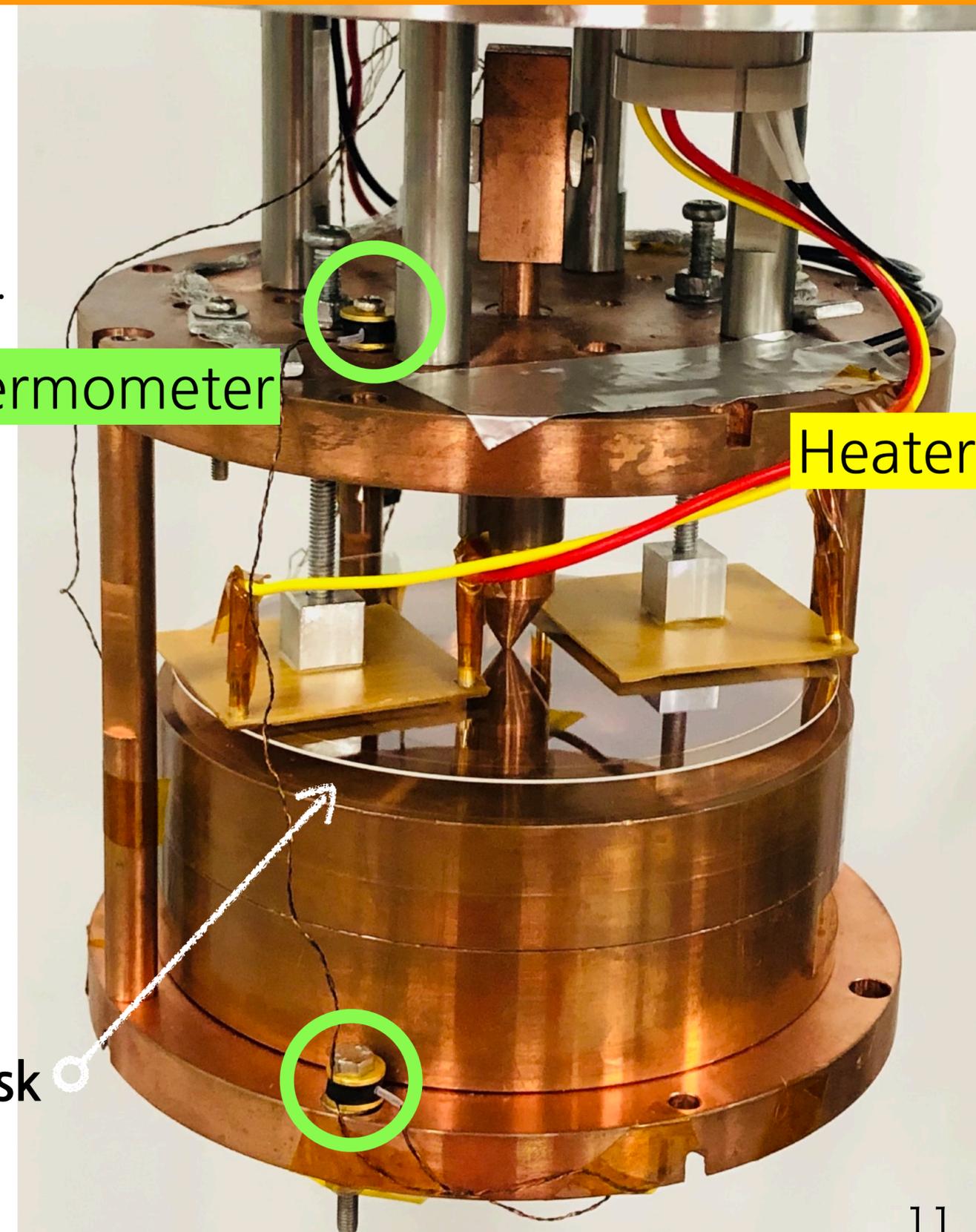


- The center in our measured resonant mode is the node.
- The effect of the loss in the support system is extremely small.



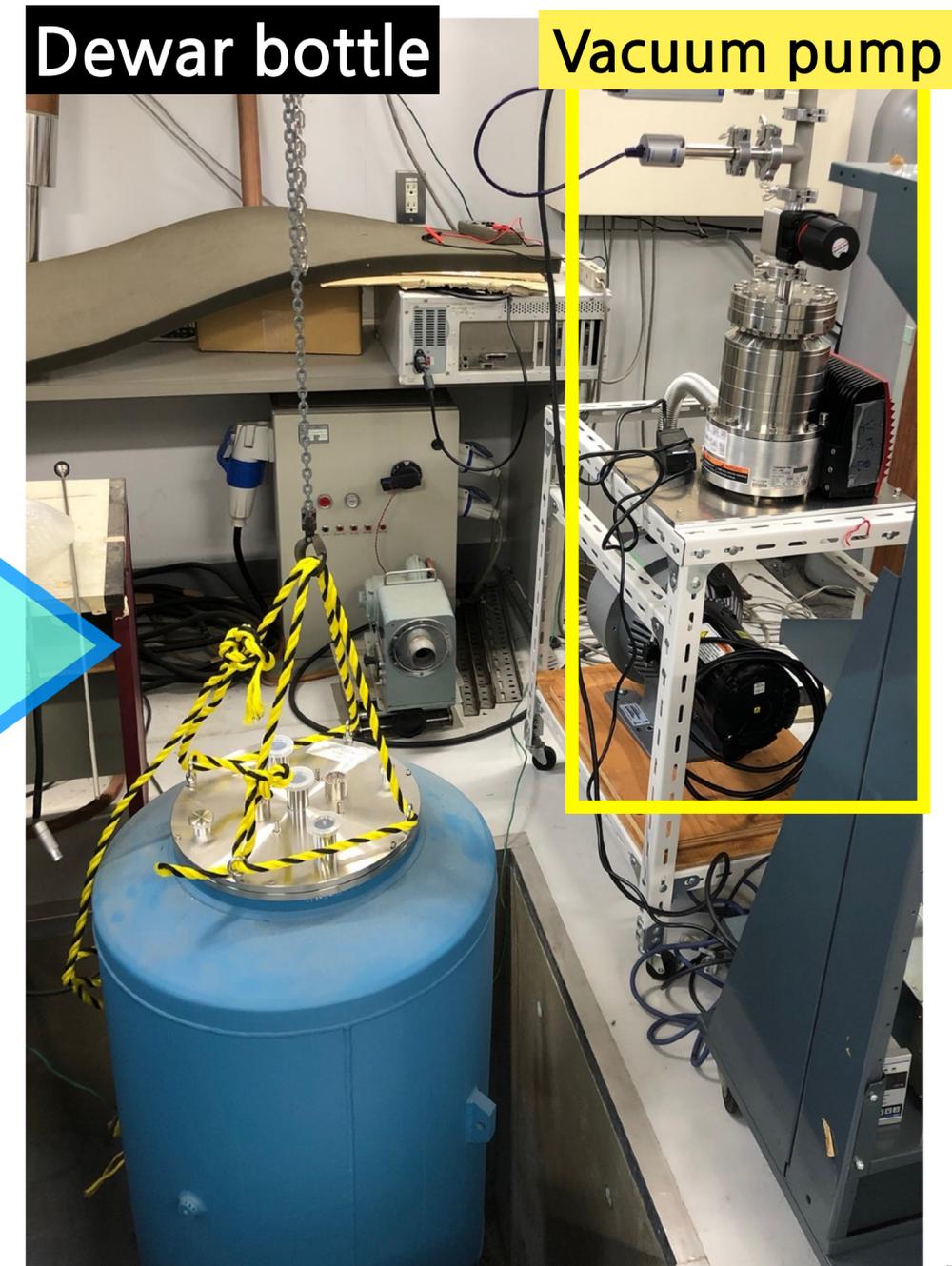
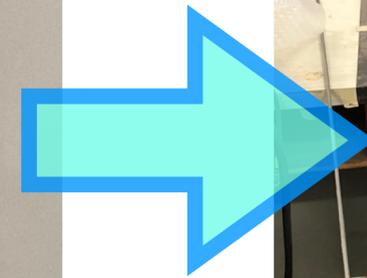
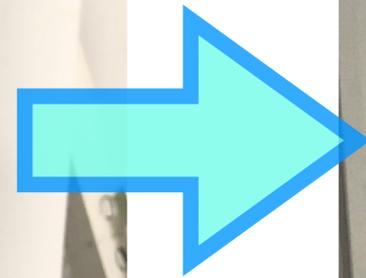
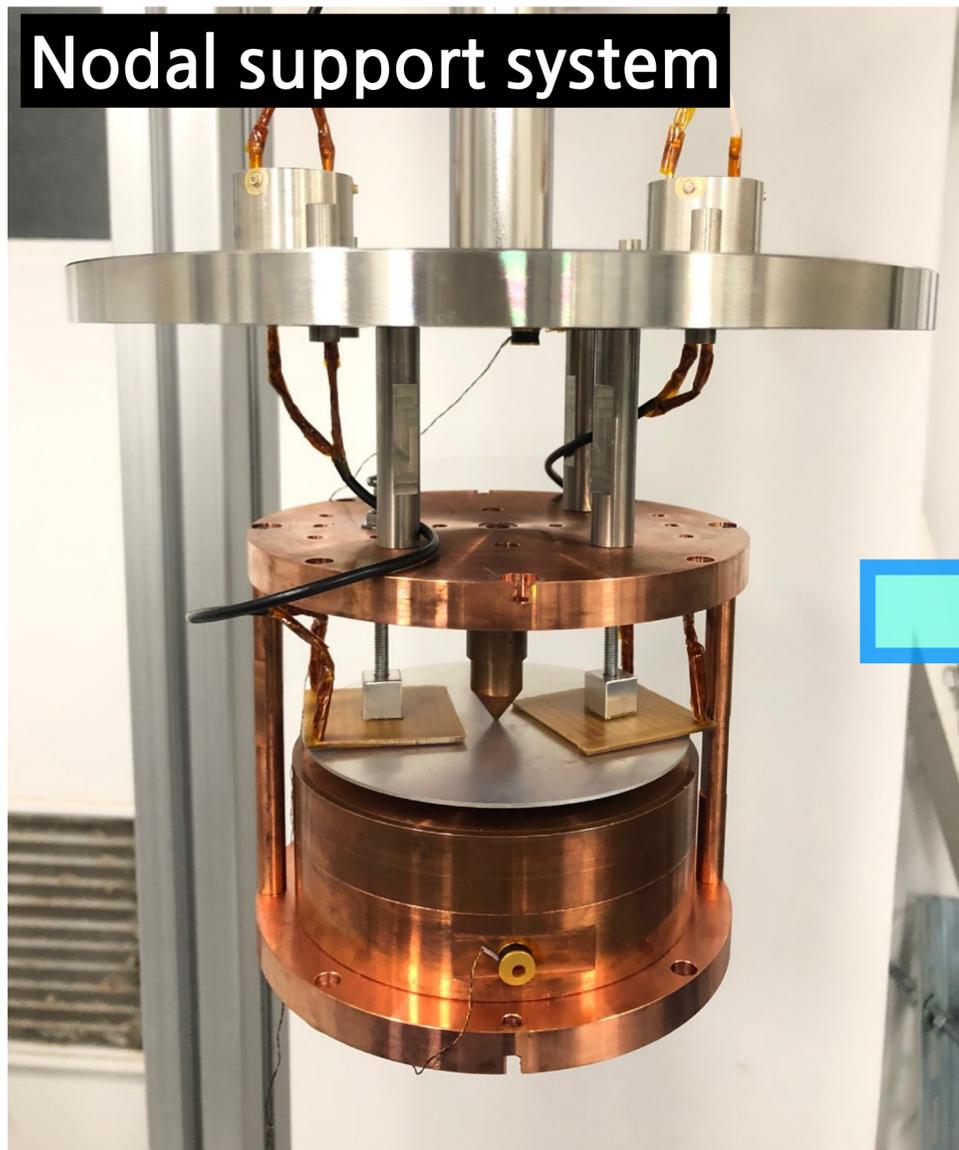
Thermometer

Heater



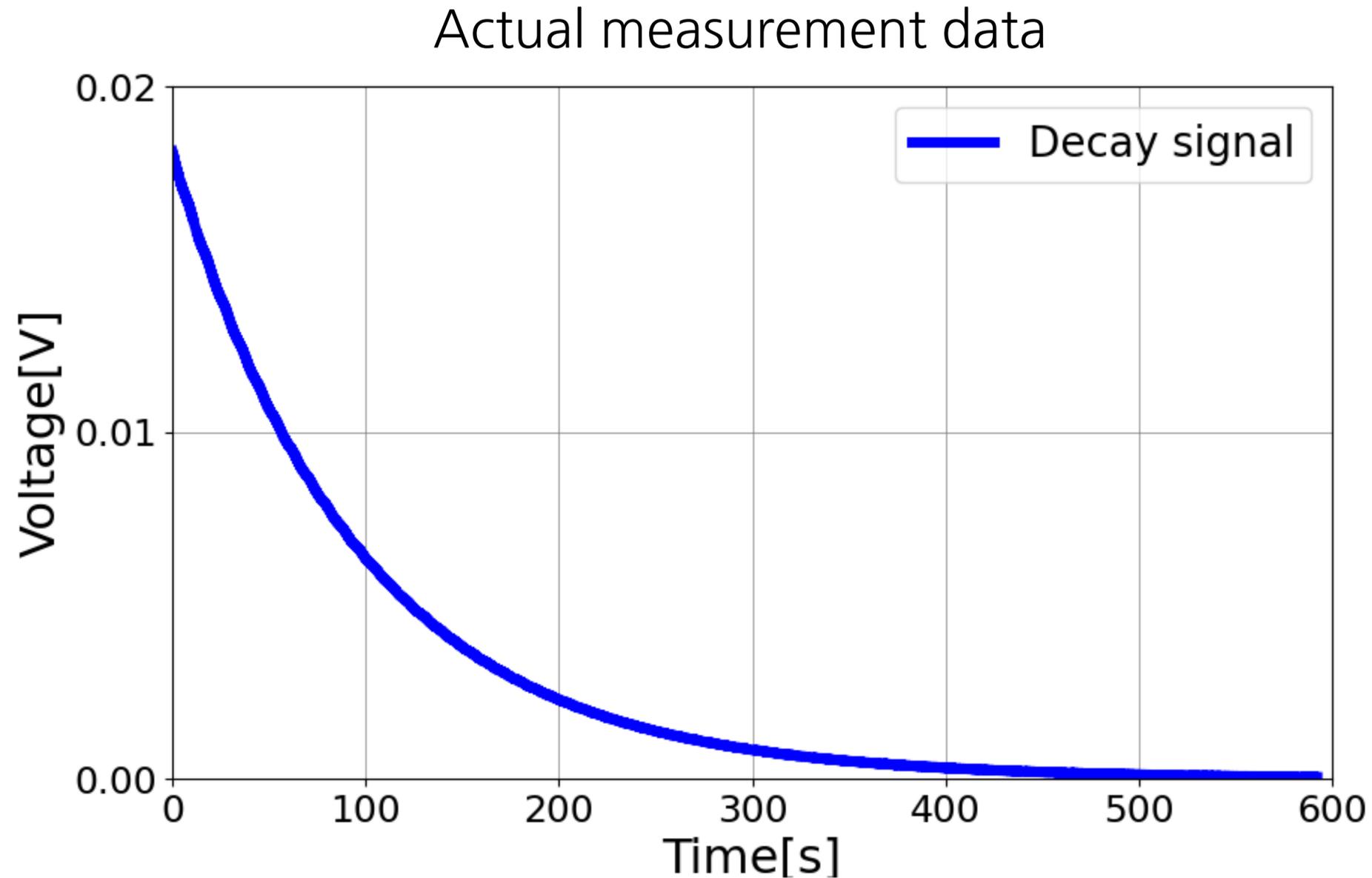
# Cooling method

We use liquid nitrogen and liquid helium to cool down our experimental apparatus.



# Actual measurement data : $\phi_{\text{with}}$ and $\phi_{\text{without}}$

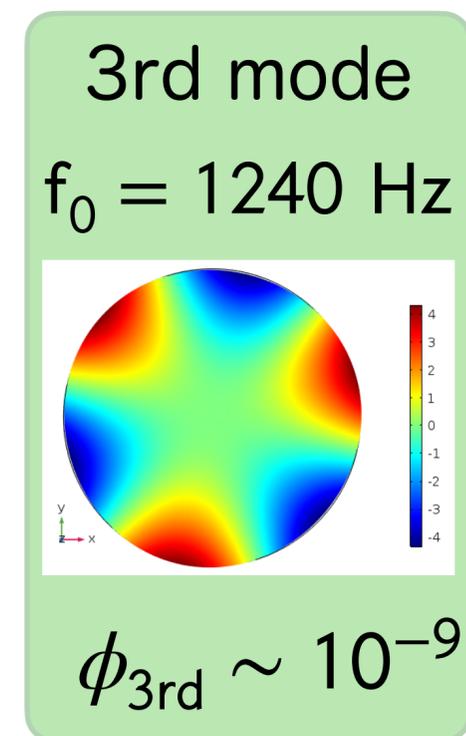
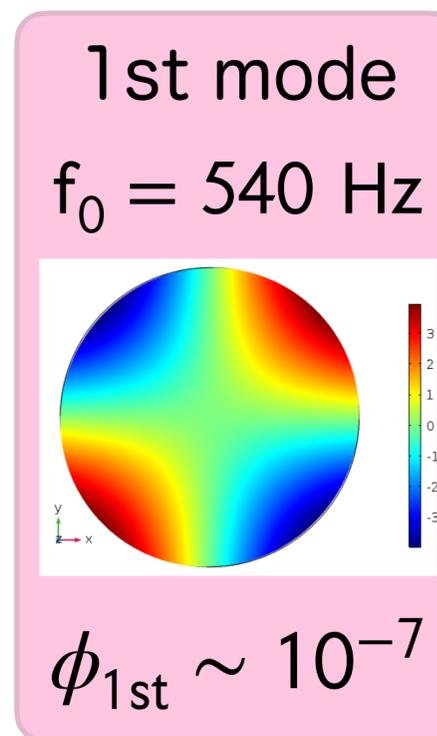
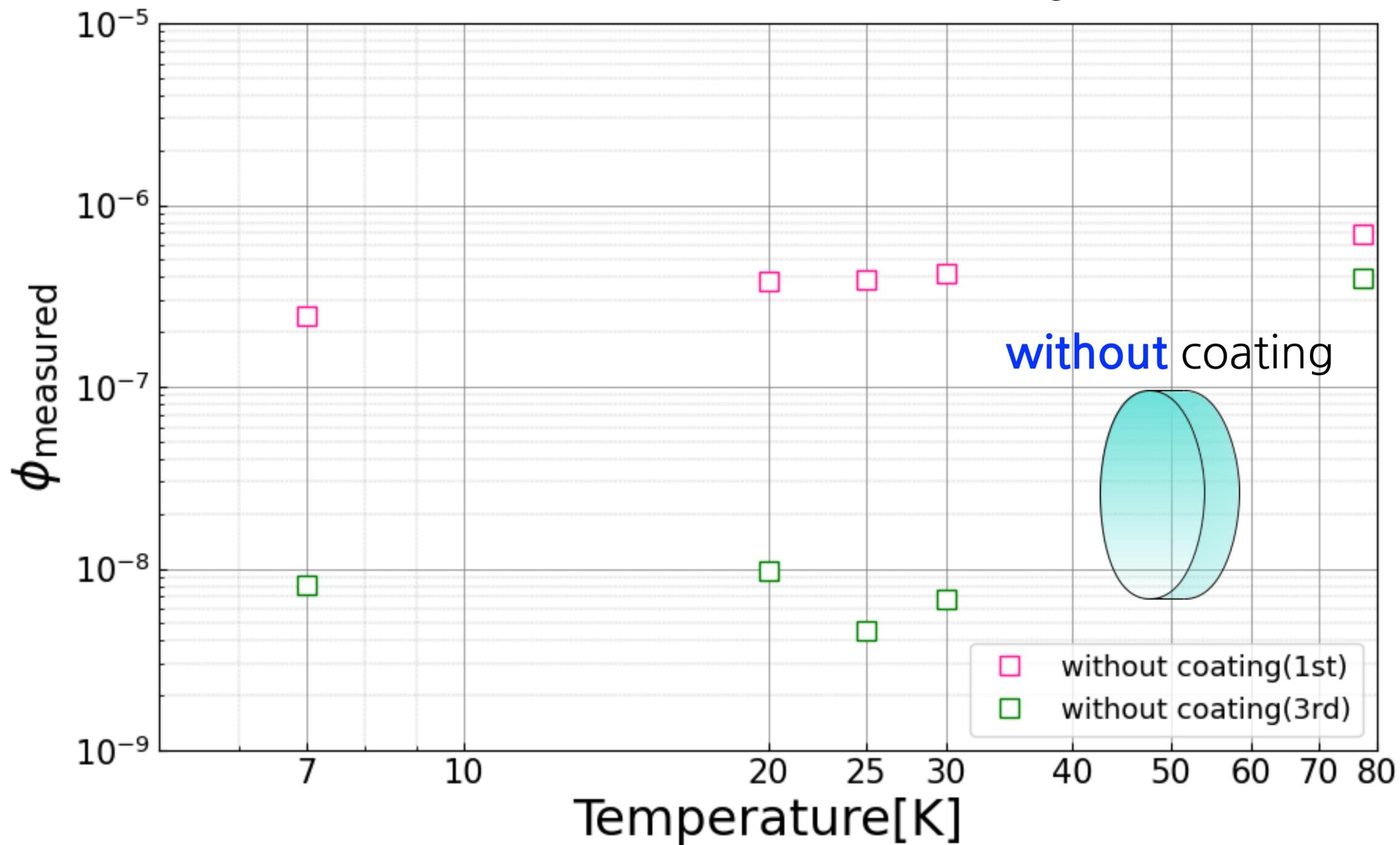
We extract only the resonant frequency components by the lock-in amplifier.



We measure the decay time and estimate the mechanical loss for each disk between 6 K and 77 K.

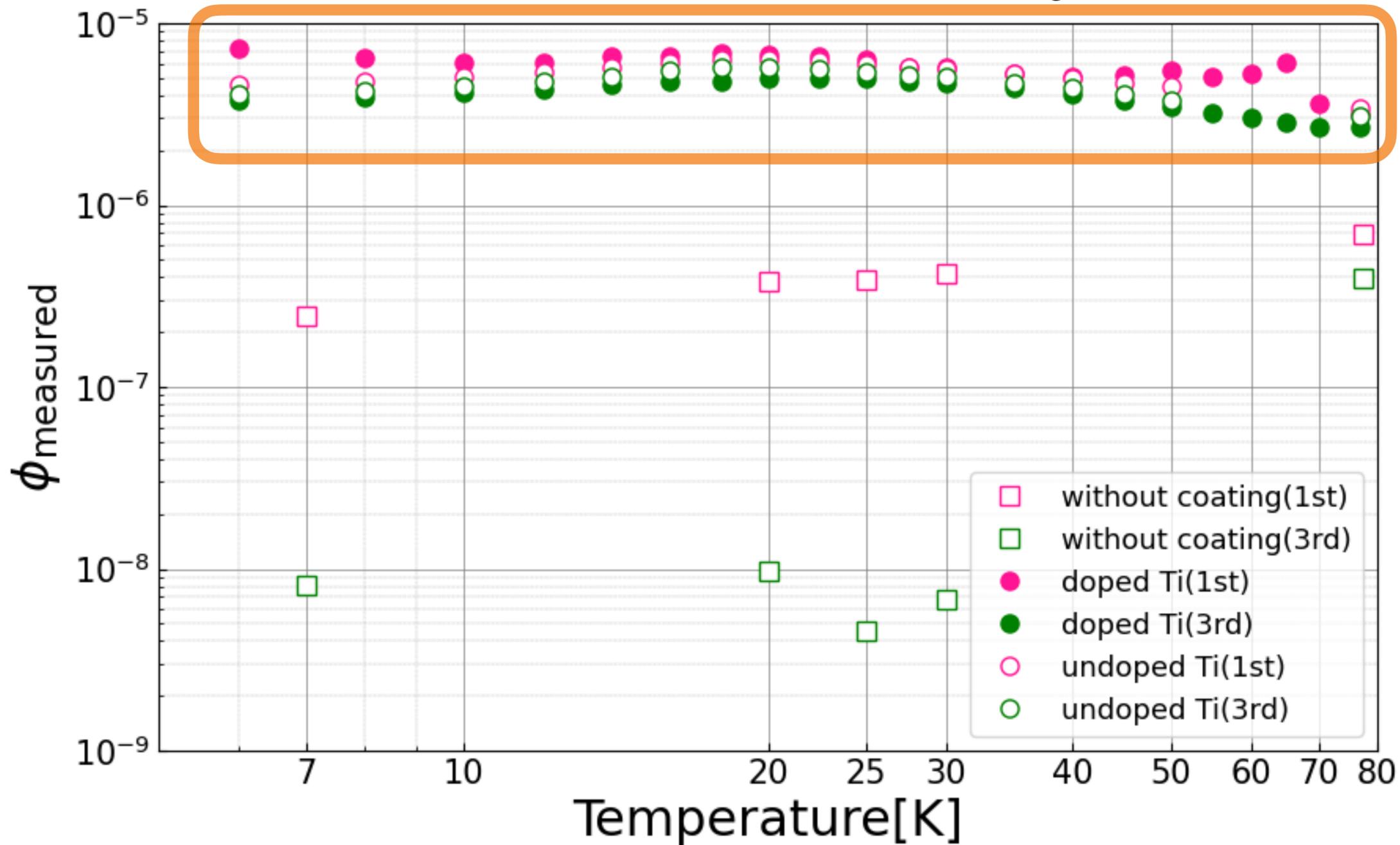
# Result : Measured mechanical loss $\phi_{\text{with}}$ and $\phi_{\text{without}}$

$$\phi_{\text{coating}} \simeq \frac{E_{\text{sapphire}}}{E_{\text{coating}}} \left( \phi_{\text{with}} - \phi_{\text{without}} \right)$$

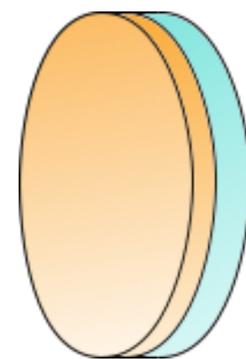


# Result : Measured mechanical loss $\phi_{\text{with}}$ and $\phi_{\text{without}}$

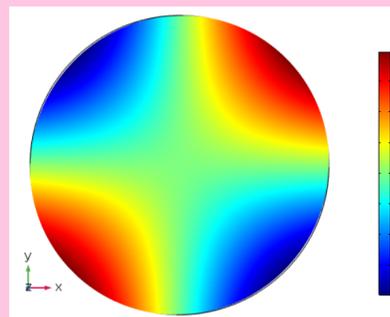
$$\phi_{\text{coating}} \approx \frac{E_{\text{sapphire}}}{E_{\text{coating}}} \left( \phi_{\text{with}} - \phi_{\text{without}} \right)$$



with coating

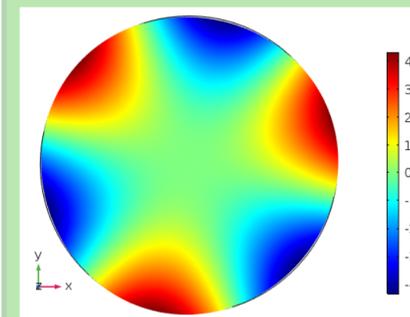


1st mode  
 $f_0 = 540 \text{ Hz}$



$\phi_{1\text{st}} \sim 10^{-6}$

3rd mode  
 $f_0 = 1240 \text{ Hz}$



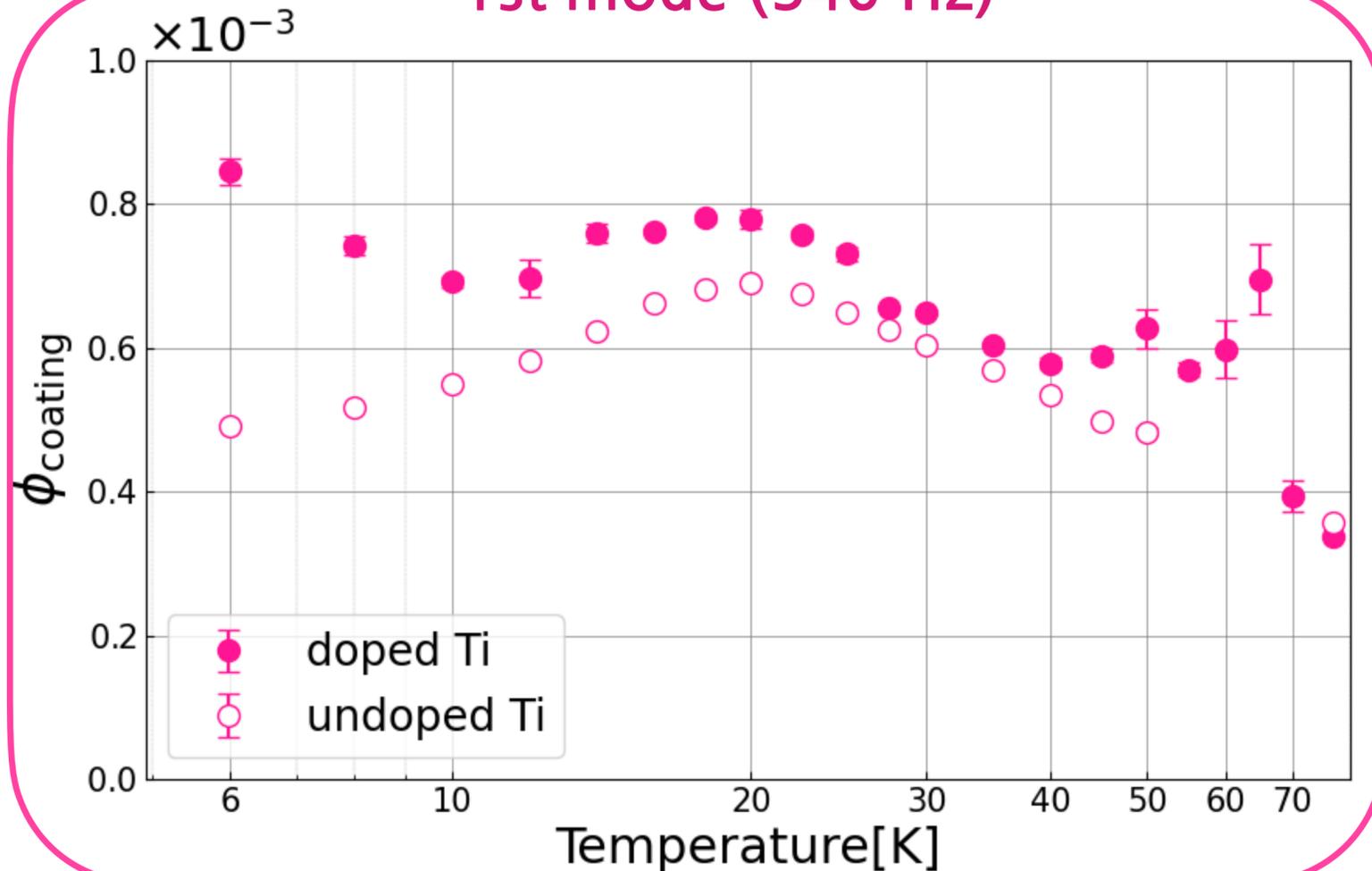
$\phi_{3\text{rd}} \sim 10^{-6}$

We can measure  $\phi_{\text{with}}$  clearly.

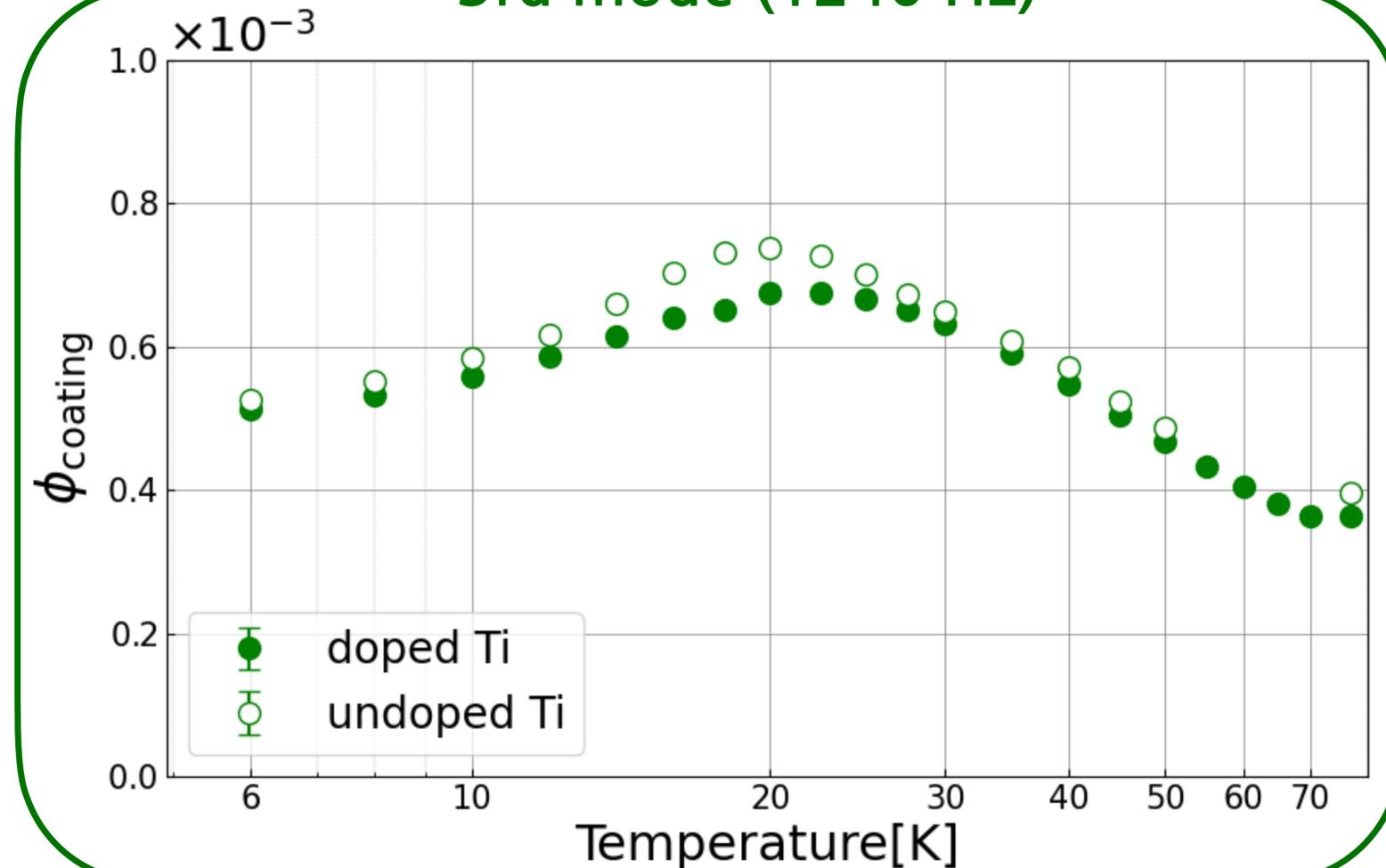
# Estimation : Coating mechanical loss $\phi_{\text{coating}}$

$$\phi_{\text{coating}} \approx \frac{E_{\text{sapphire}}}{E_{\text{coating}}} (\phi_{\text{with}} - \phi_{\text{without}})$$

1st mode (540 Hz)



3rd mode (1240 Hz)



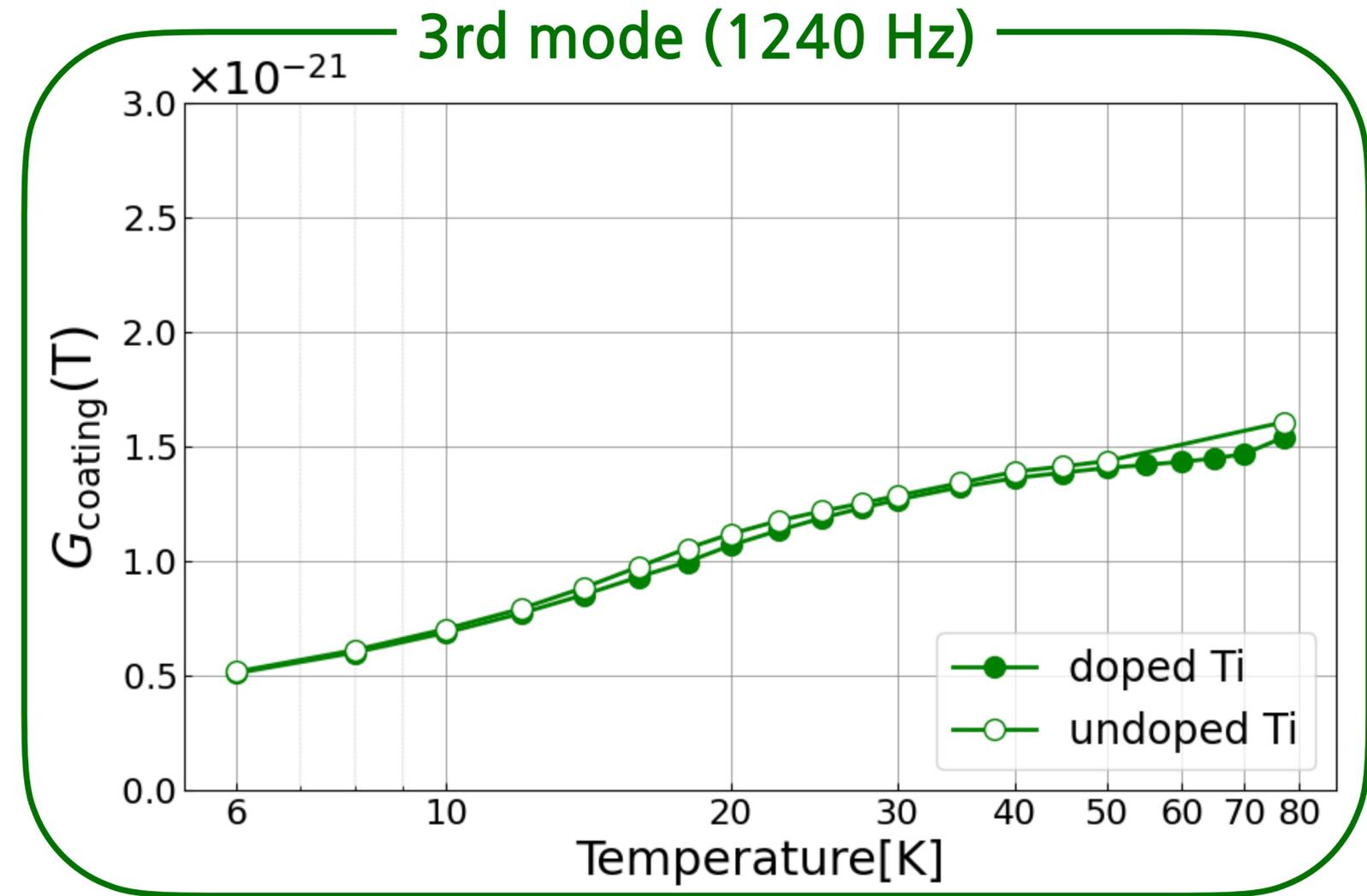
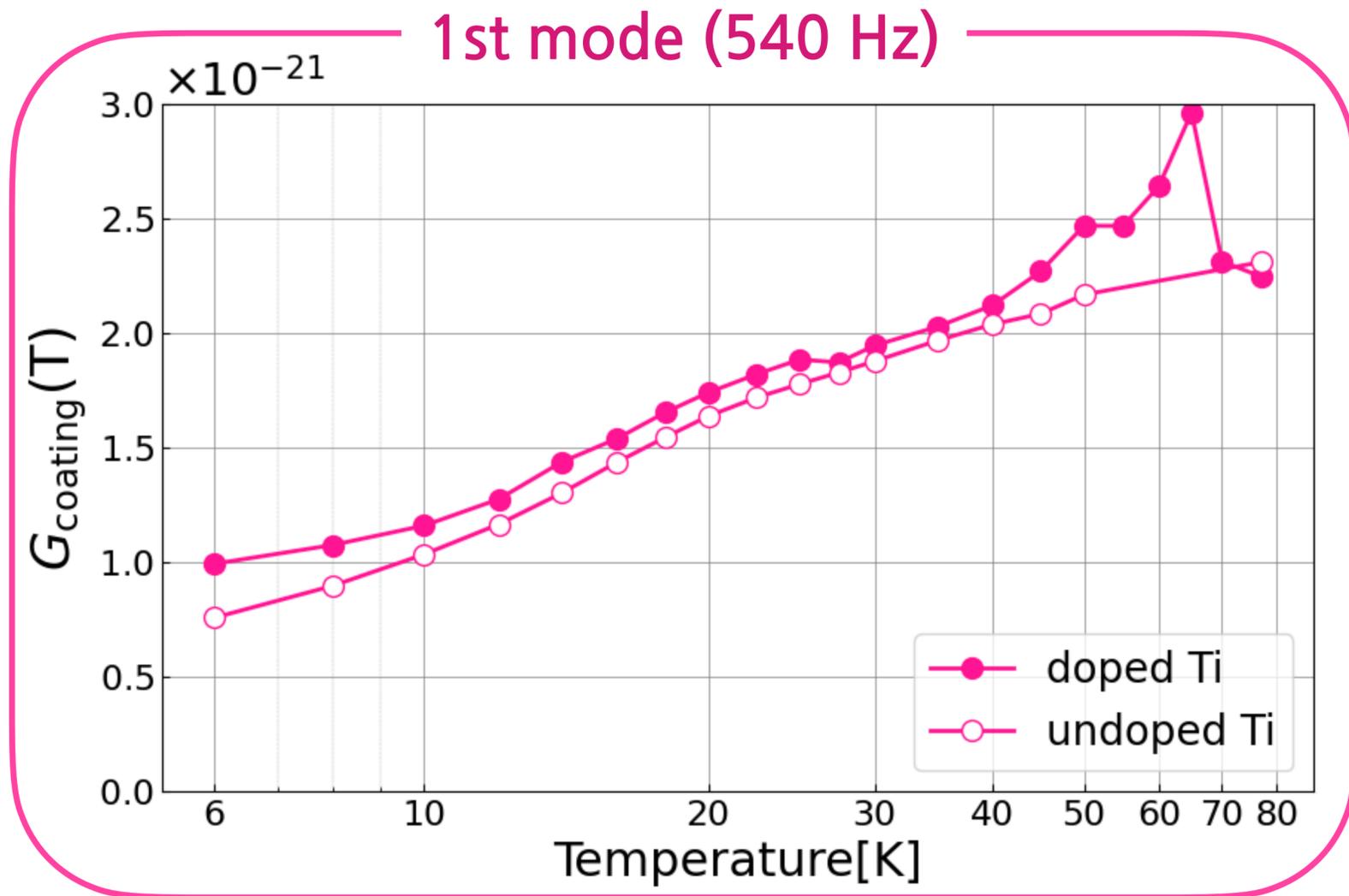
Temperature dependence : Peak at around 20 K

We derive the thermal noise from our result.

- Temperature dependence of coating thermal noise.
- The contribution of  $\text{TiO}_2$  doped and undoped coating.

# Estimation : Coating thermal noise $G_{\text{coating thermal noise}}$

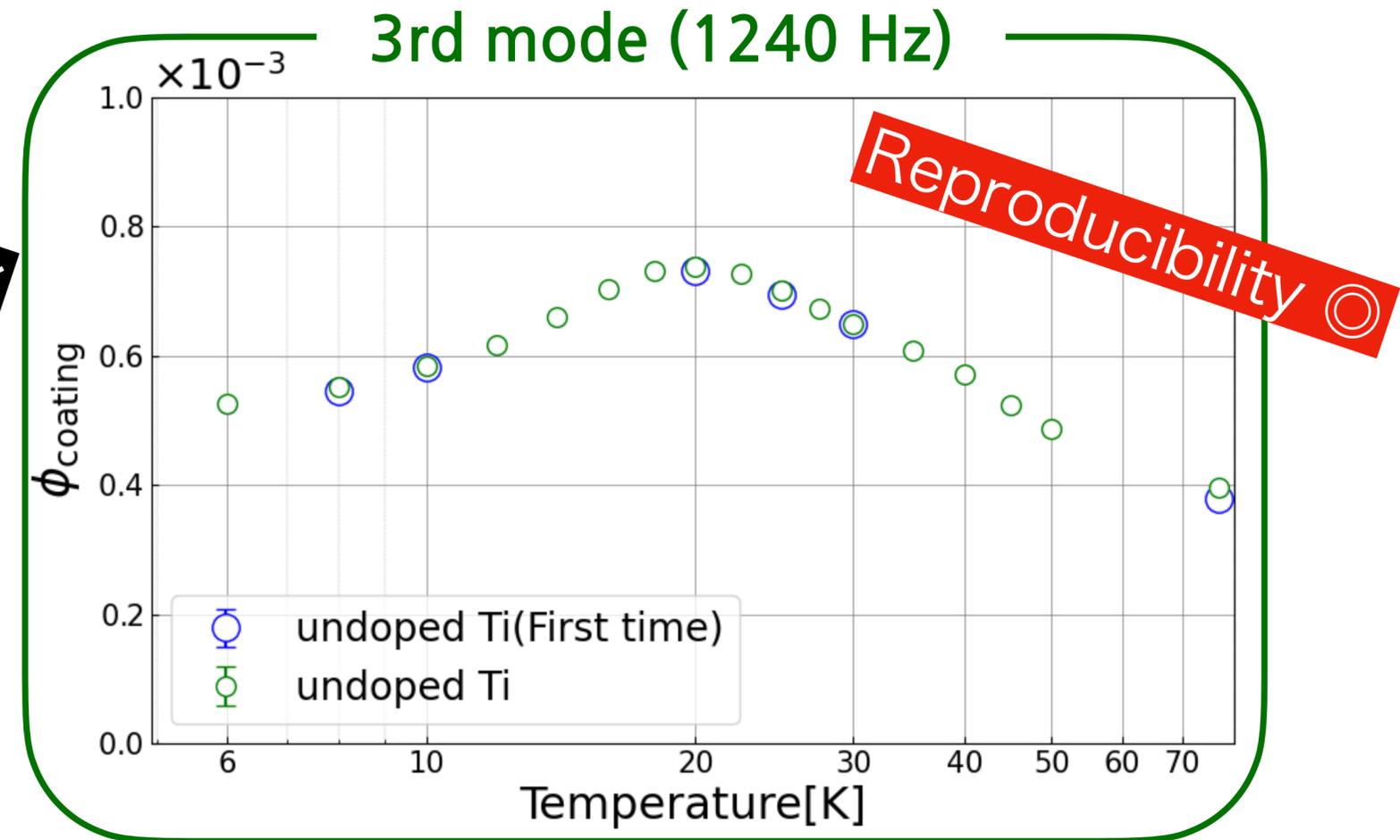
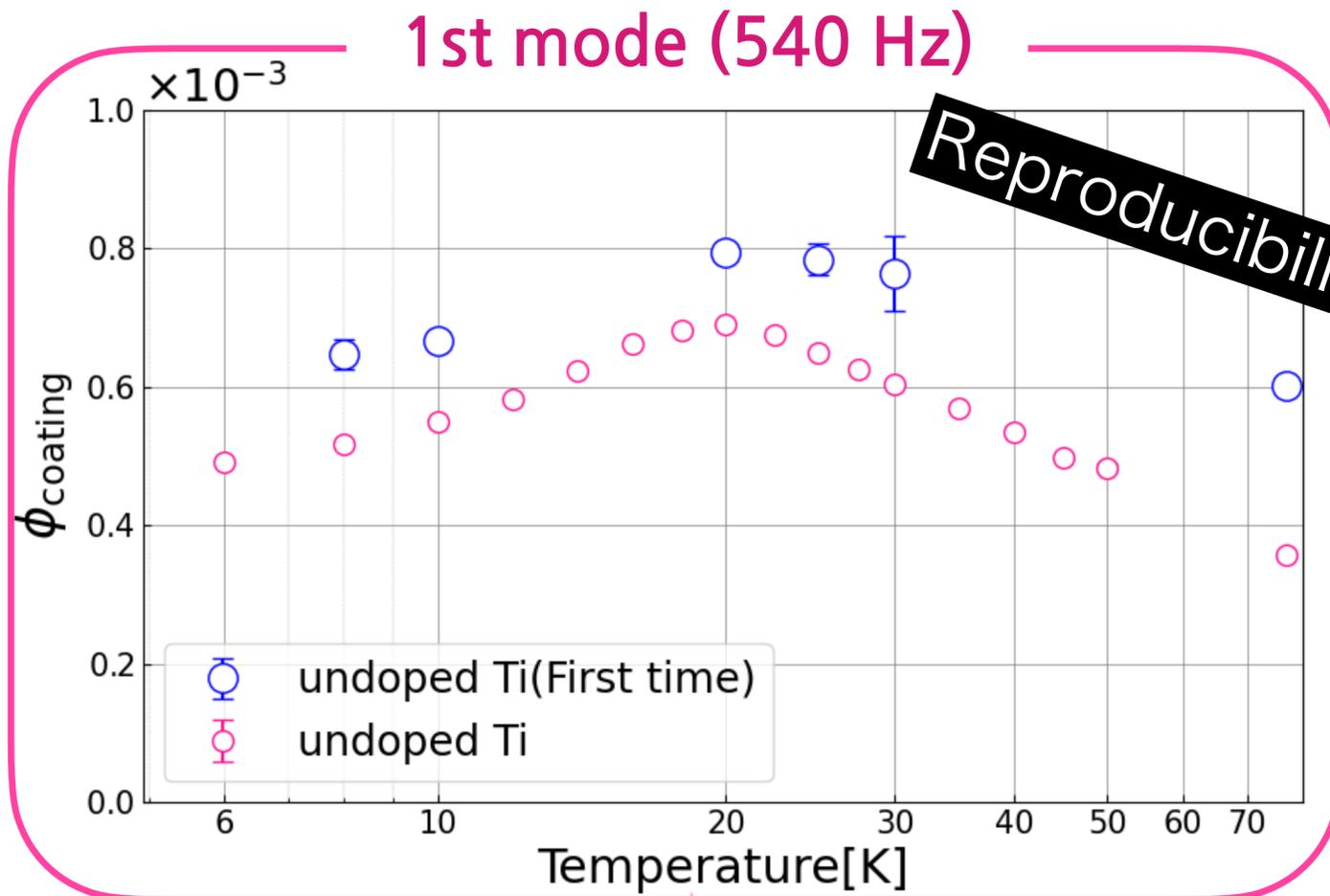
$$G_{\text{thermal noise}} \approx \sqrt{\frac{2k_B T}{\pi^2 f} \frac{d}{\omega^2 Y_{\text{sapphire}}} \phi \left( \frac{Y_{\text{coating}}}{Y_{\text{sapphire}}} + \frac{Y_{\text{sapphire}}}{Y_{\text{coating}}} \right)}$$



- The coating thermal noise is smaller at lower temperatures.
- Contribution to thermal noise : No large difference between  $\text{TiO}_2$  doped and undoped coating.

# Discussion

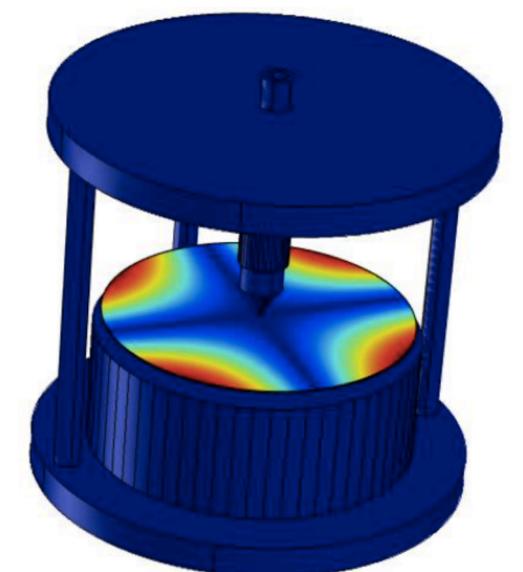
The reproducibility of the measurement of  $\phi$   $\longrightarrow$  We measure the same sample twice



Due to the nodal support system..?

- The amplitude near the center is larger in 1st mode than that in 3rd mode.
- The 1st mode has a large loss originating from the support system (The 3rd mode is flatter near the center.)

The  $\phi$  depends on how to set the disk to the support system.  
**This needs further research.**



## Summary

- The mirror thermal noise mainly comes from the coating around 100 Hz.
- We constructed experimental apparatus at the Univ. Toyama to evaluate the mechanical loss of the coating over a wide temperature range.
- We measure the mechanical loss of the  $\text{TiO}_2$  doped and undoped coating on sapphire from 6 K to 77 K.
- Mechanical loss of the coating depends on the temperature : local maximum around 20K
- Contribution to thermal noise :

No large difference between the  $\text{TiO}_2$  doped and undoped coating on sapphire.

The thermal noise is smaller at lower temperatures.

## Future plan

- Check reproducibility.
- Investigation to reduce the coating mechanical loss.



Thank you for your attention