

SEARCHING GRAVITATIONAL WAVE WITH AUTOREGRESSIVE APPROACH

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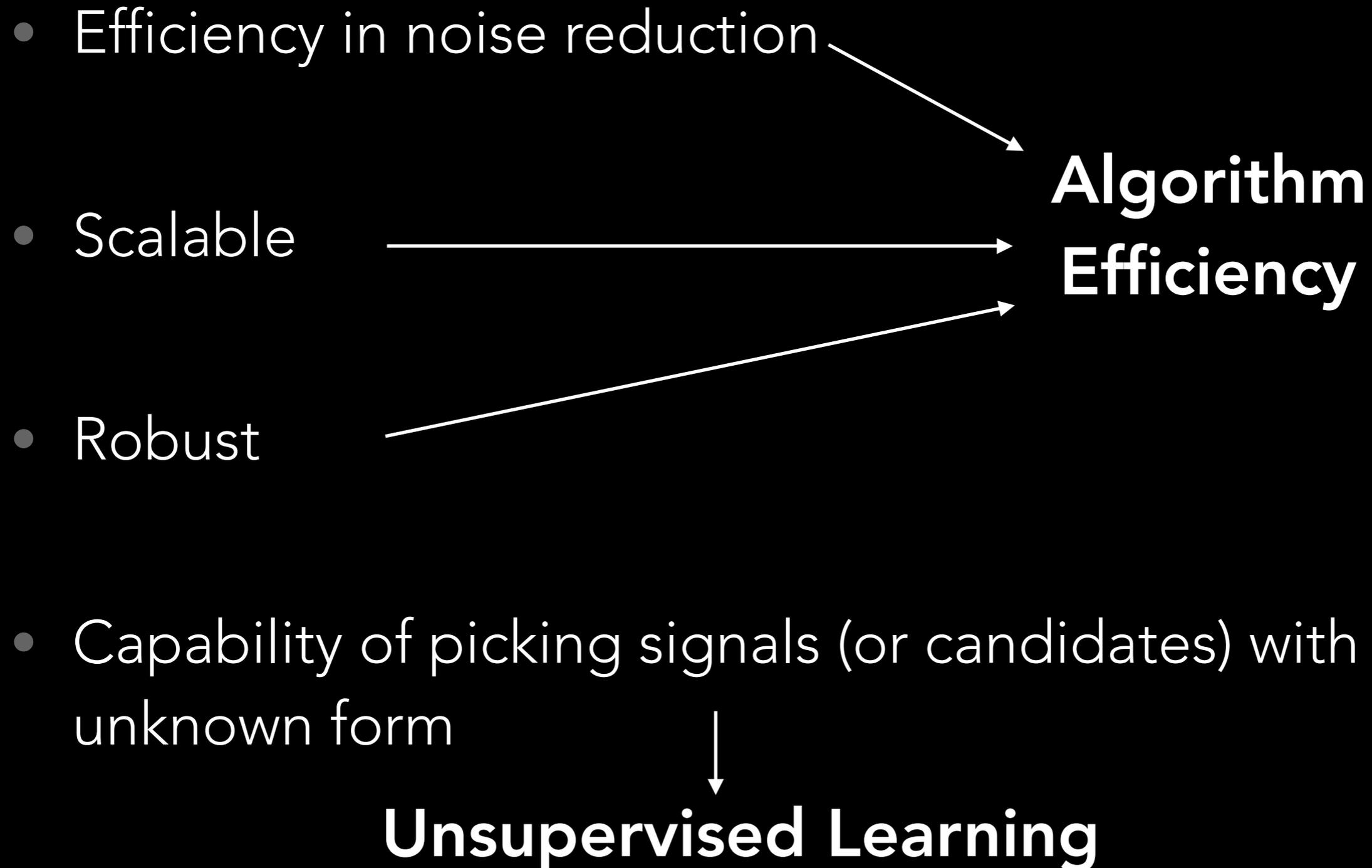
DATA CHALLENGES IN GRAVITATIONAL WAVE ASTRONOMY

- Presence of non-Gaussian noise (instrumental + environmental) that are far larger than the astrophysical signal.

$$h_{\text{noise}} \sim 10^{-19} \quad \text{vs.} \quad h_{\text{signal}} \lesssim 10^{-21}$$

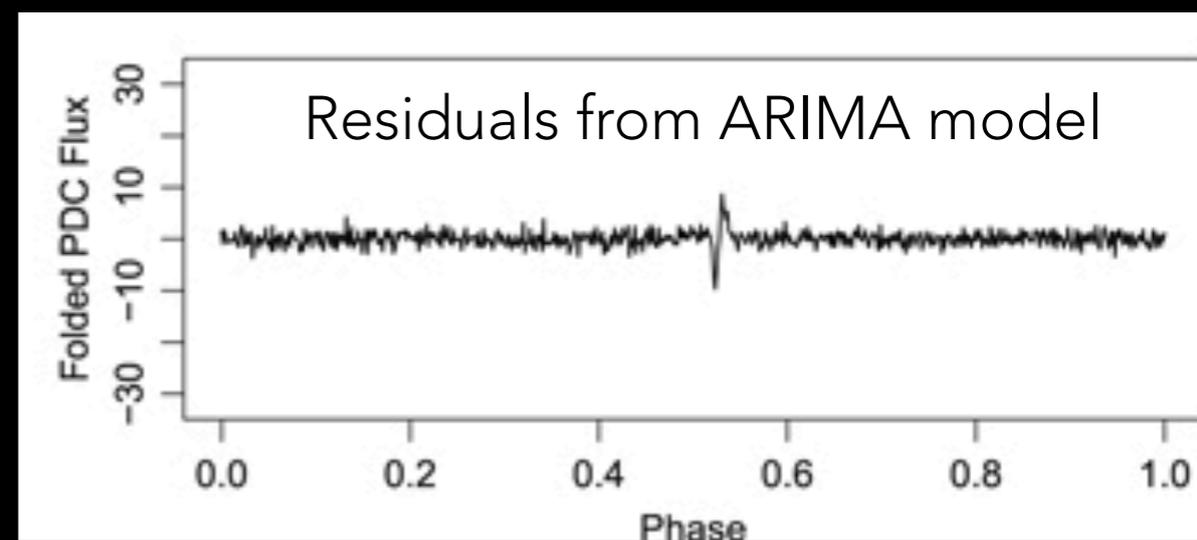
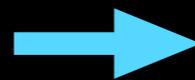
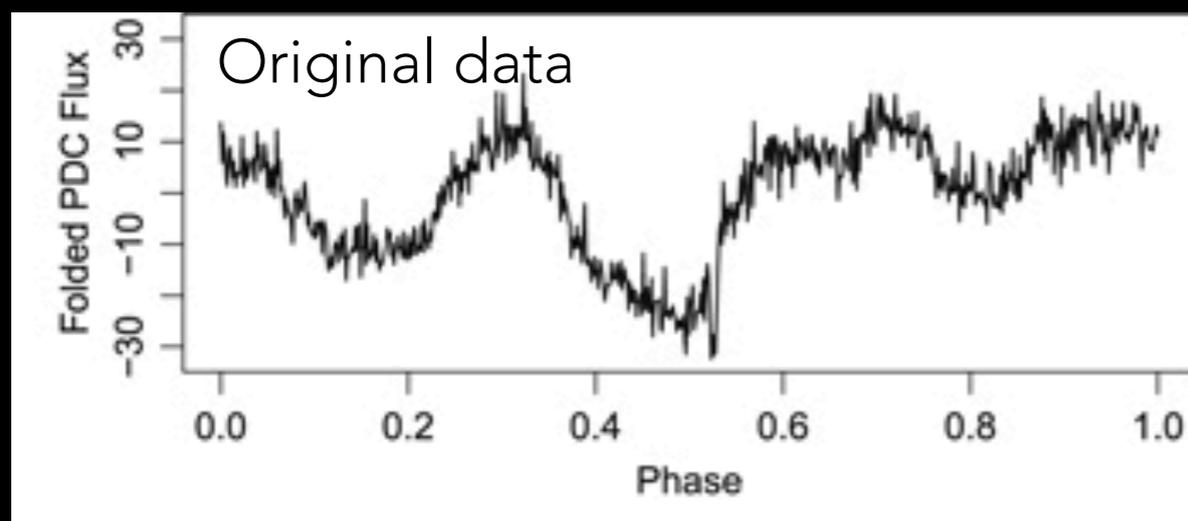
- Conventional detection algorithm (e.g. matched filtering) cannot pick the signal without the knowledge of its form.
- Large data volume

WISH LIST FOR DETECTION PIPELINE



NOISE REDUCTION WITH STOCHASTIC AUTOREGRESSIVE MODELING

- Simple approach of analysis in time domain
- Capable to handle various kinds of noise from non-stationary autocorrelated stochastic processes.
- Not much application in astronomy until recently (e.g. exoplanet search)



AUTOREGRESSIVE INTEGRATED MOVING AVERAGE (**ARIMA**) MODEL

- ARIMA model comprises 3 components:
 1. If the value of a variable at a given time is influenced by its *past values*, the process is **autoregressive (AR)** which can be regarded as a simple regression problem. An AR process of order p is modeled by:

$$x_t = a_1x_{t-1} + a_2x_{t-2} + \dots + a_px_{t-p} + \epsilon_t + c$$

ϵ_t is normally distributed random error with zero mean and unknown variance (i.e. white noise). c is a constant.

AUTOREGRESSIVE INTEGRATED MOVING AVERAGE (**ARIMA**) MODEL

- ARIMA model comprises 3 components:
 1. If the variable has its current value depends on the *noise terms* in the previous q time steps, the process is described as a **moving average (MA)** model with order q :

$$x_t = b_1\epsilon_{t-1} + b_2\epsilon_{t-2} + \dots + b_q\epsilon_{t-q} + \epsilon_t + c$$

Combining both we have ARMA model which predicts the value at a given time by both lagged values and lagged errors.

AUTOREGRESSIVE INTEGRATED MOVING AVERAGE (**ARIMA**) MODEL

- ARIMA model comprises 3 components:
3. For a non-stationary process, an approximately stationary time series can be obtained by *differencing operation*:

$$x'_t = x_t - Bx_t = x_t - x_{t-1}$$

To restore the original light curve, one has to reverse this operation (i.e. *integrate* the series back). An **integrated (I)** process is modeled as:

$$(1 - B)^d x_t = \epsilon_t$$

AUTOREGRESSIVE INTEGRATED MOVING AVERAGE (**ARIMA**) MODEL

Combining the aforementioned three processes together into a single regression procedure, we have

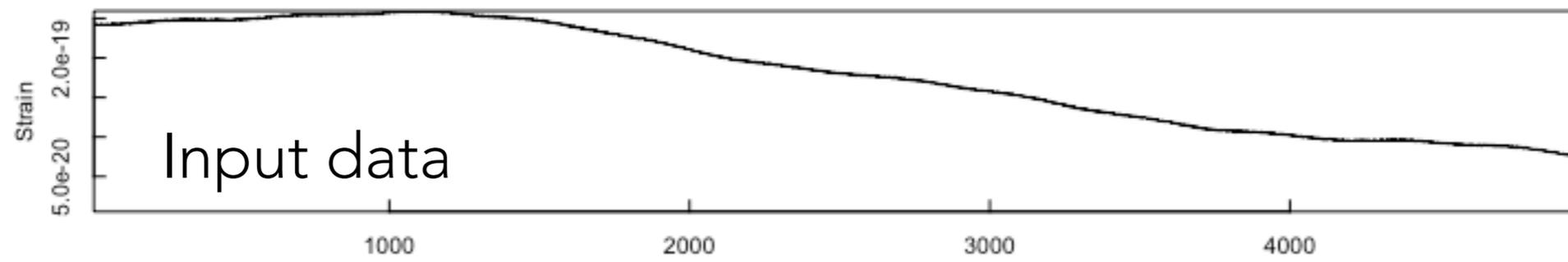
ARIMA(p,q,d) model:

$$(1 - B)^d x_t = \sum_{i=1}^p a_i x_{t-i} + \sum_{j=1}^q b_j \epsilon_{t-j} + \epsilon_t + c$$

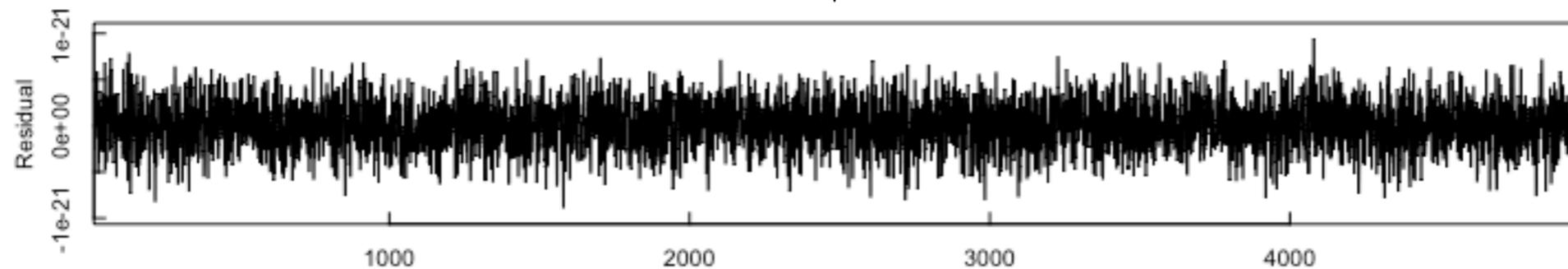
The model parameters can be determined by maximum likelihood estimation with the orders p and q determined through certain information criterion (e.g. BIC, AIC).

TEST CASE#1 SIMULATED DATA

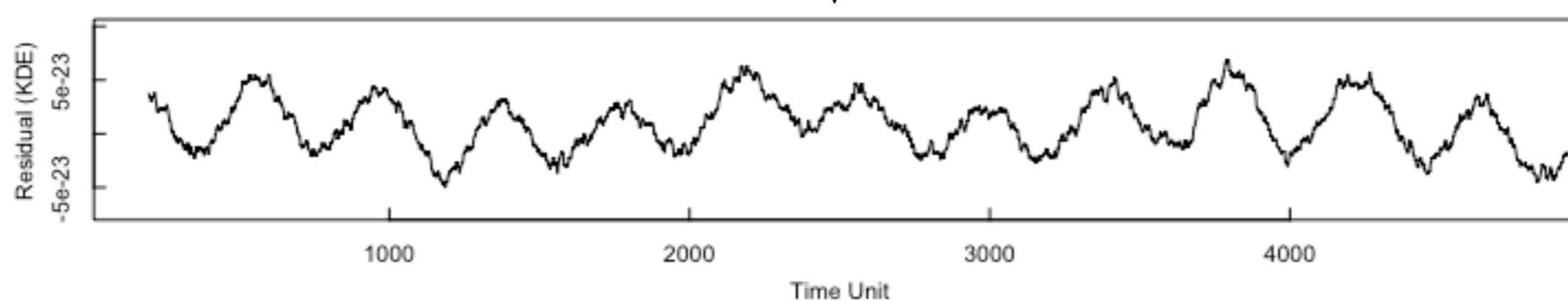
- The simulated LIGO strain series with a constant 10 Hz sinusoidal signal of $h \sim 10^{-21}$ injected.



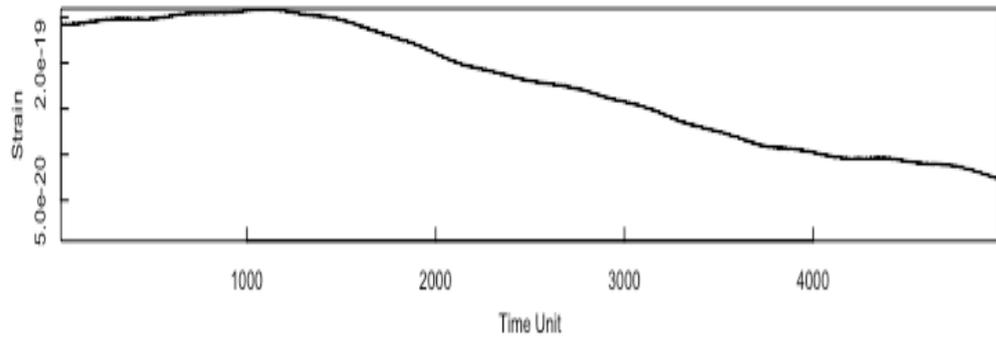
↓ Subtract AR(45)



↓ Low-pass filter



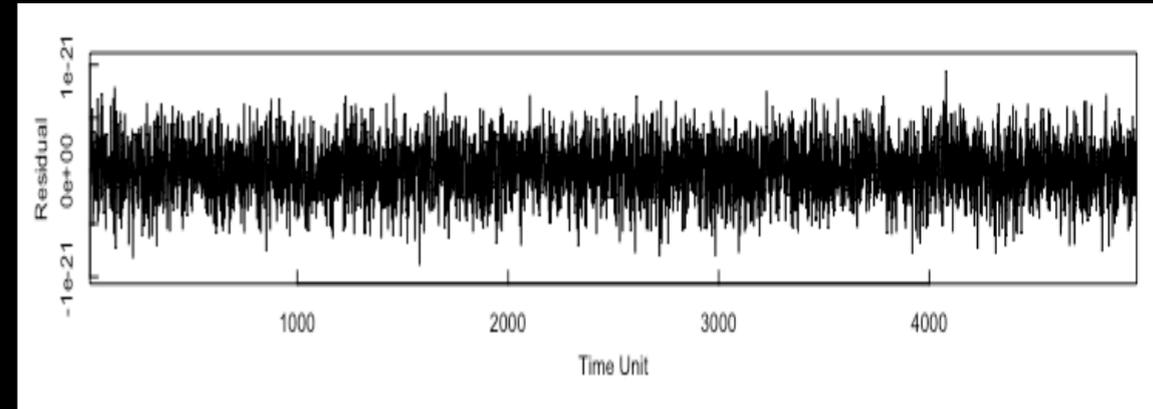
TEST CASE#1 SIMULATED DATA



Original data

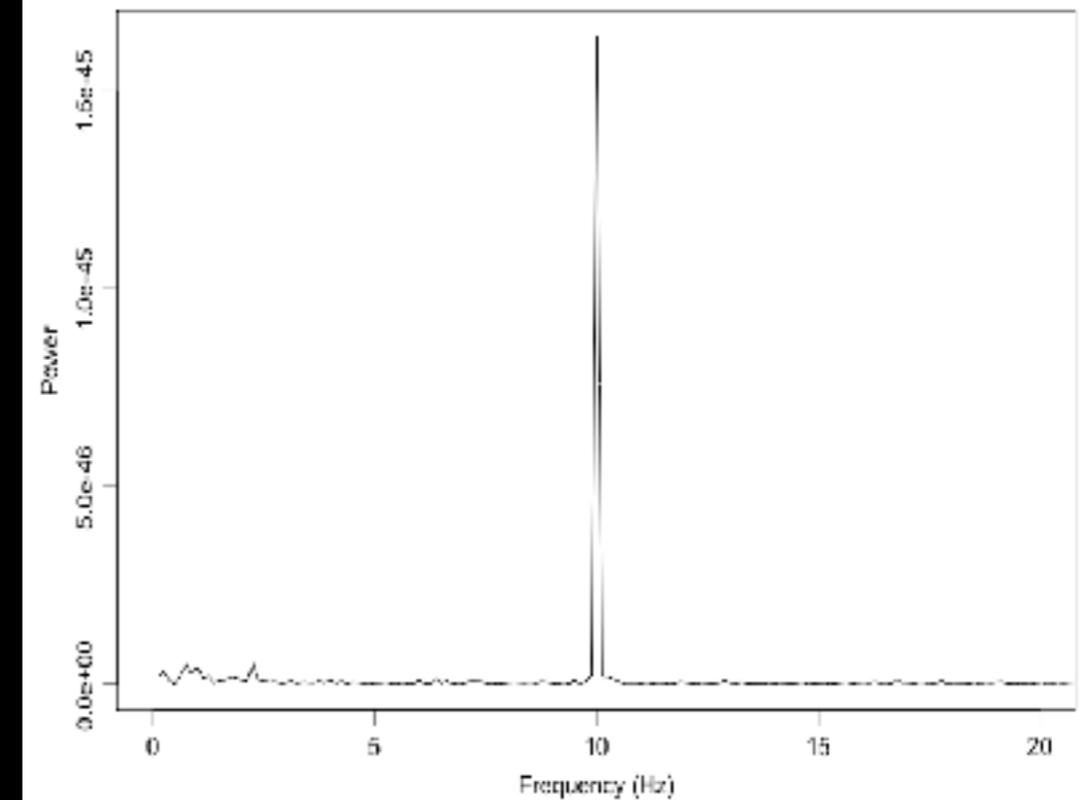
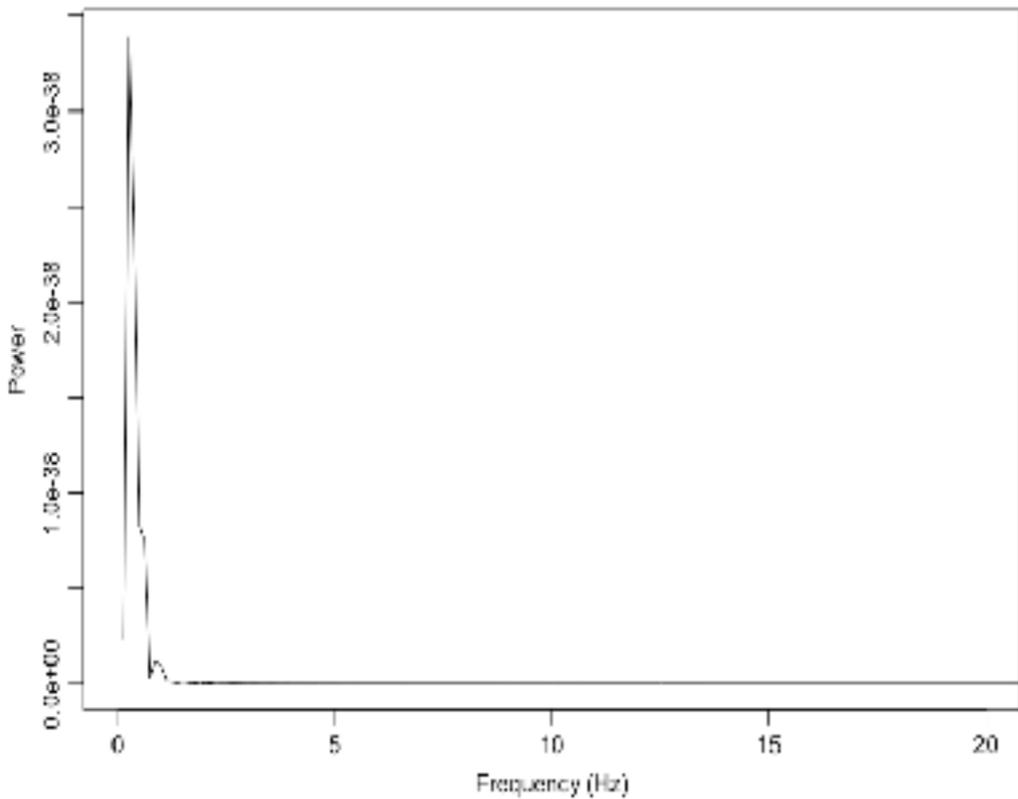
FFT

Subtract
AR(45)

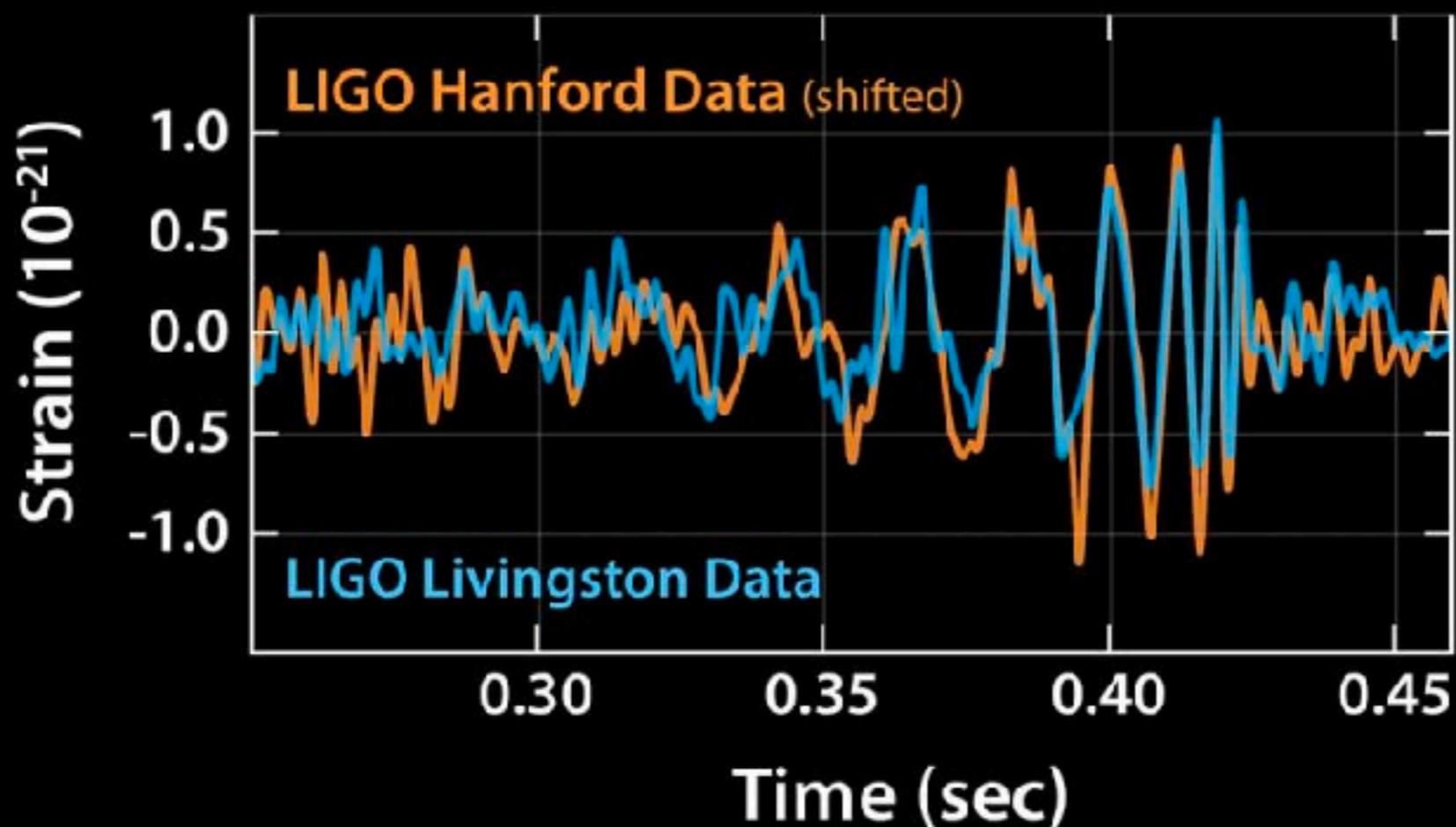


Residual (without low-pass filter)

FFT

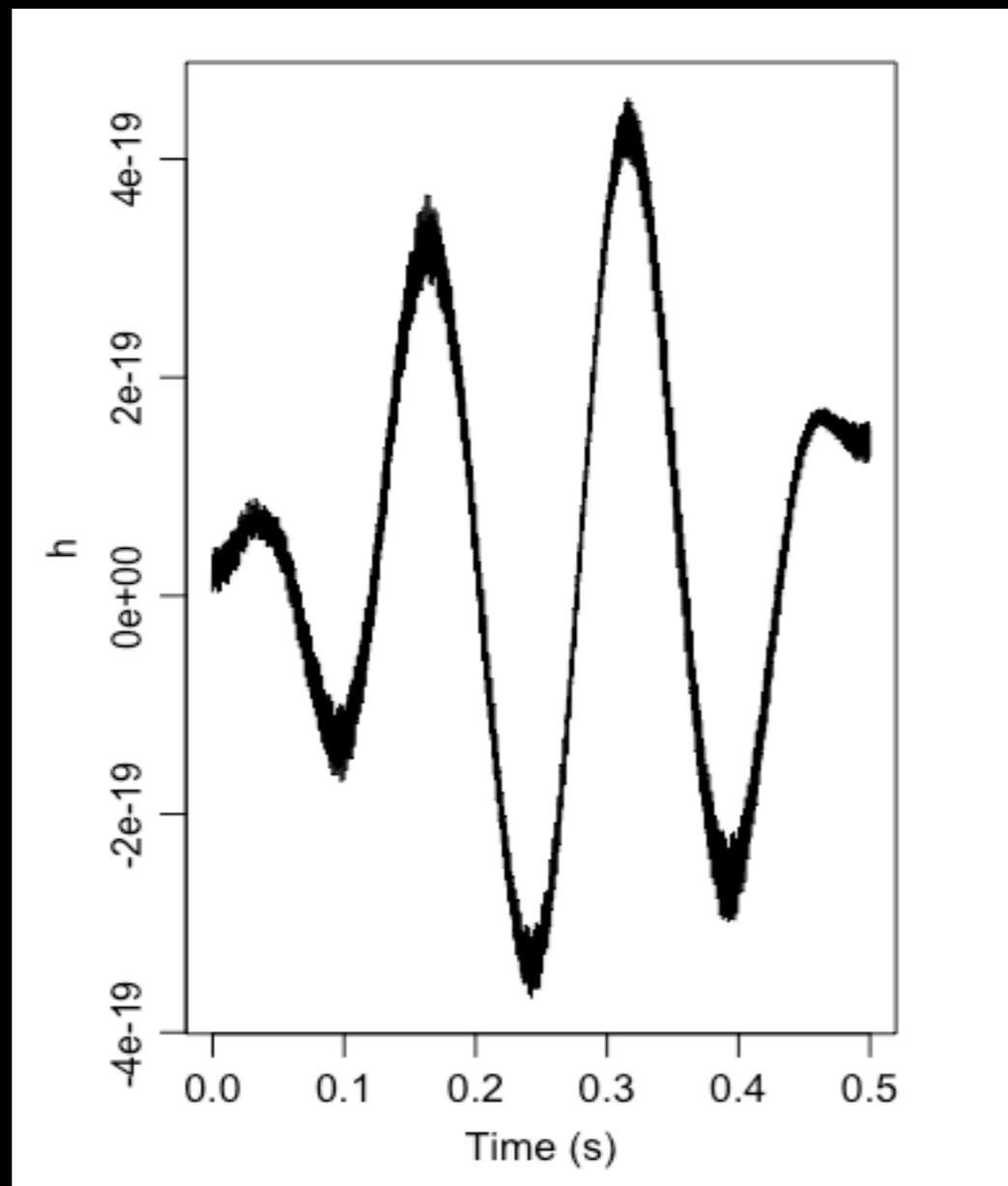


TEST CASE#2: LIGO DATA OF GW150914



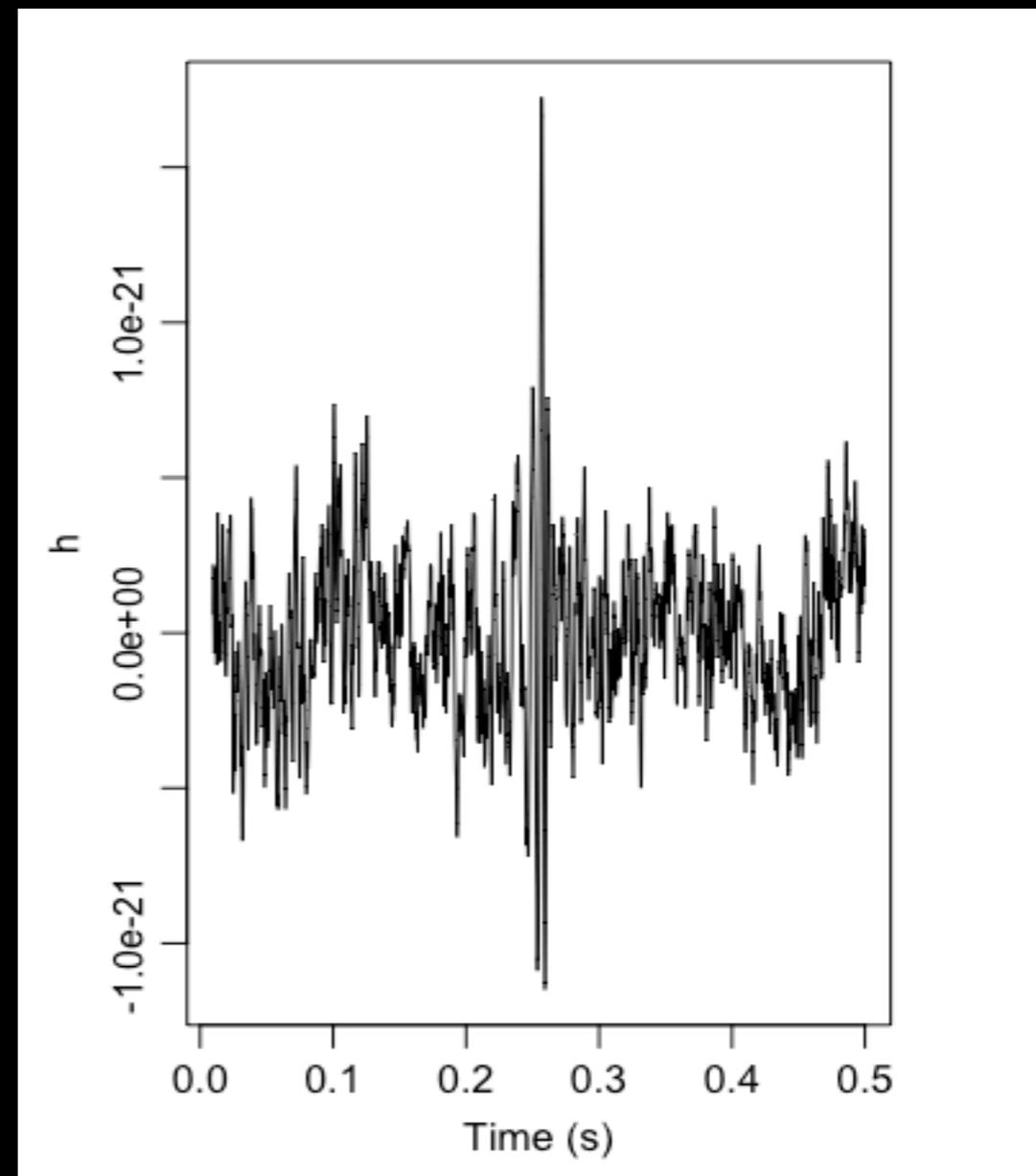
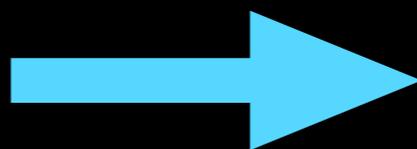
TEST CASE#2: LIGO DATA OF GW150914

I. LIGO Hanford



Raw data

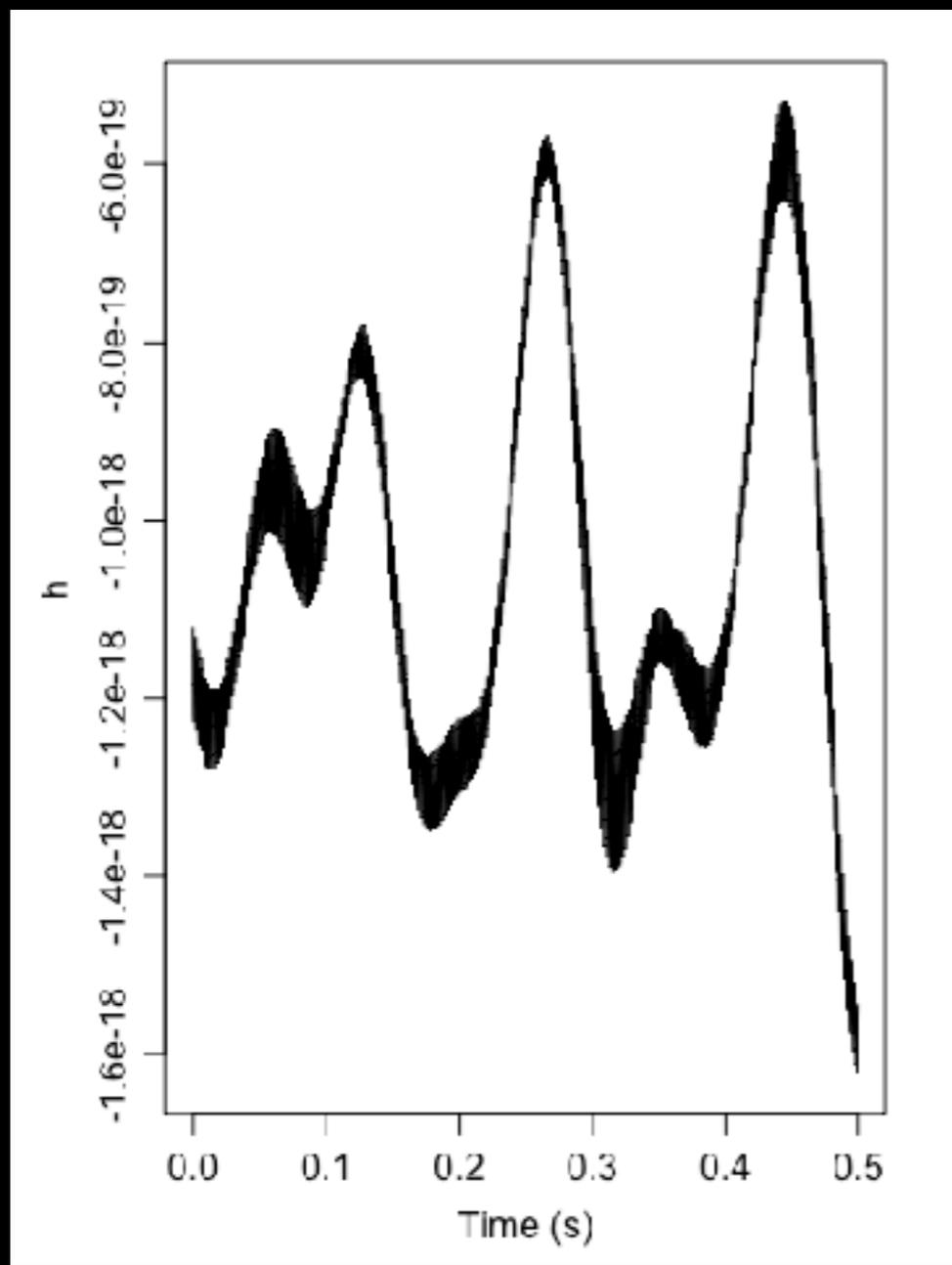
Subtract
AR(31)
+
Low-Pass
filter



Residuals

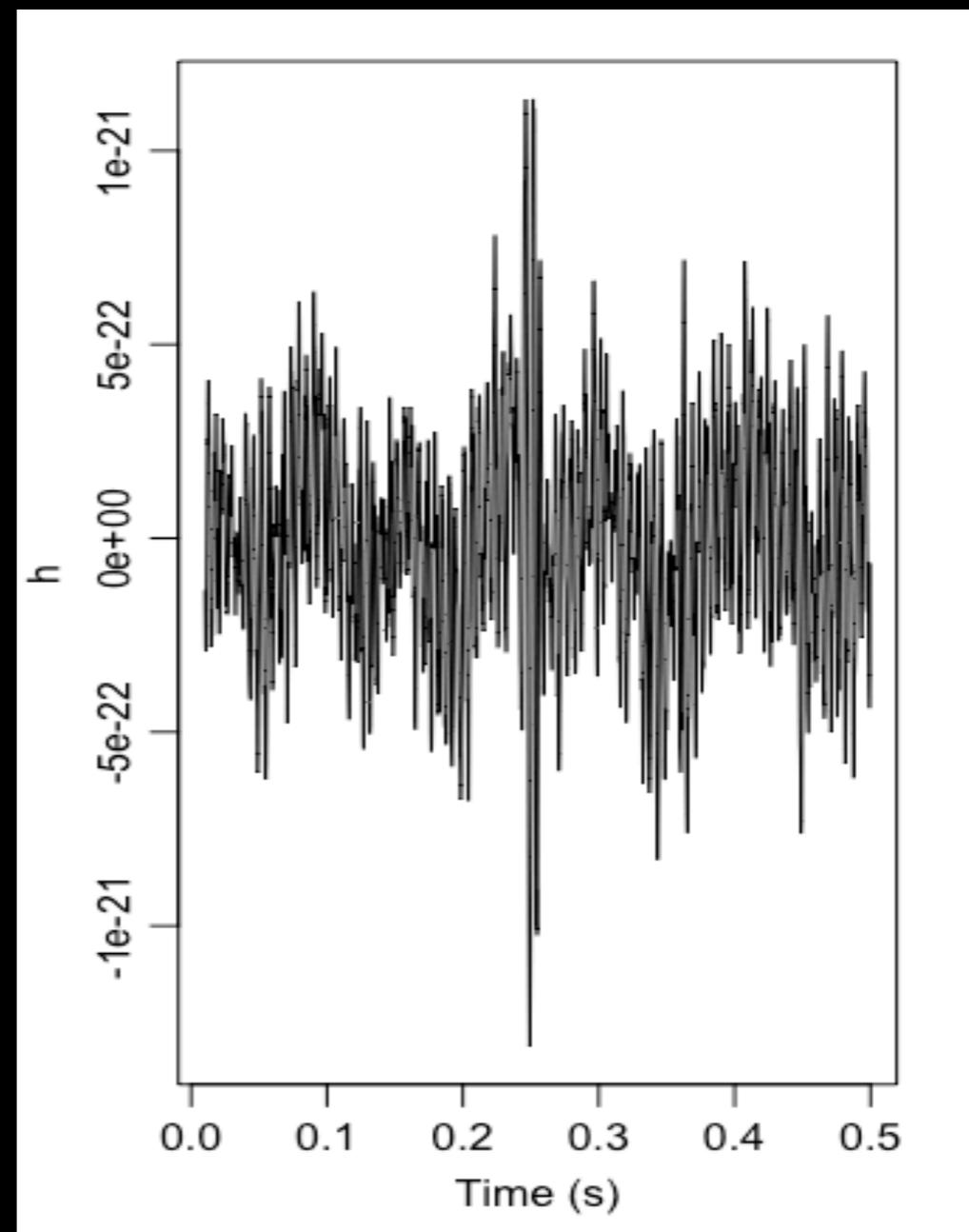
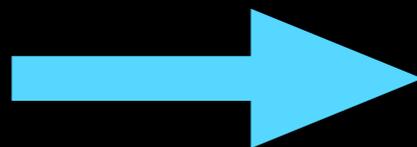
TEST CASE#2: LIGO DATA OF GW150914

II. LIGO Livingston



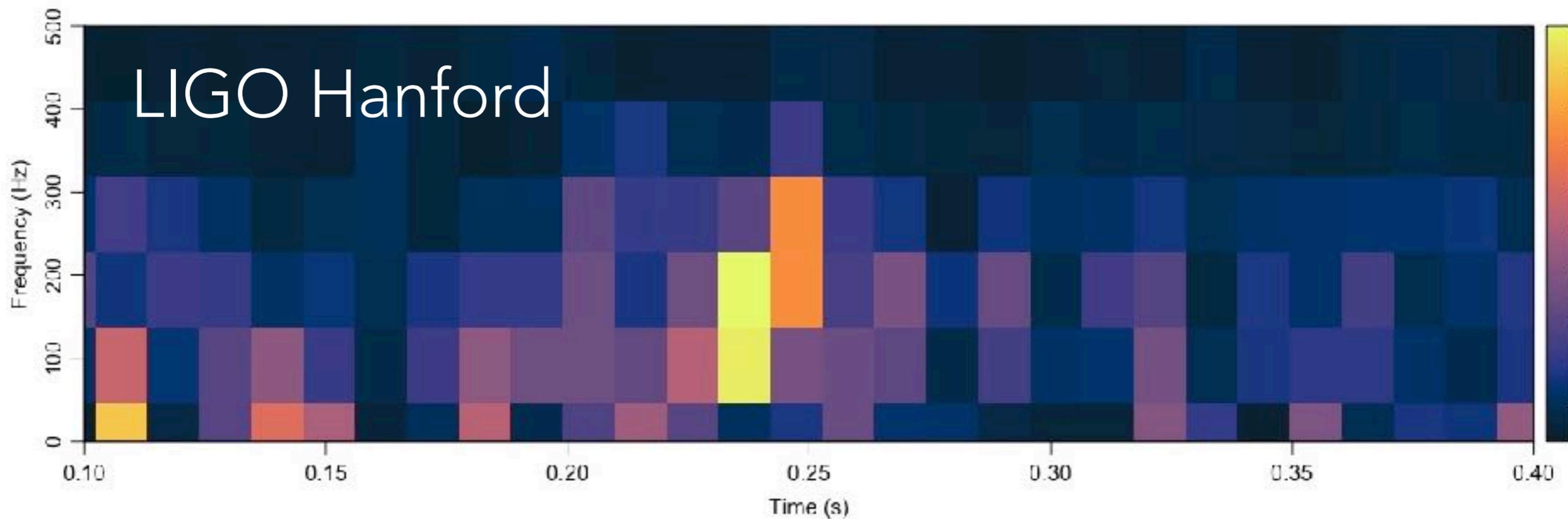
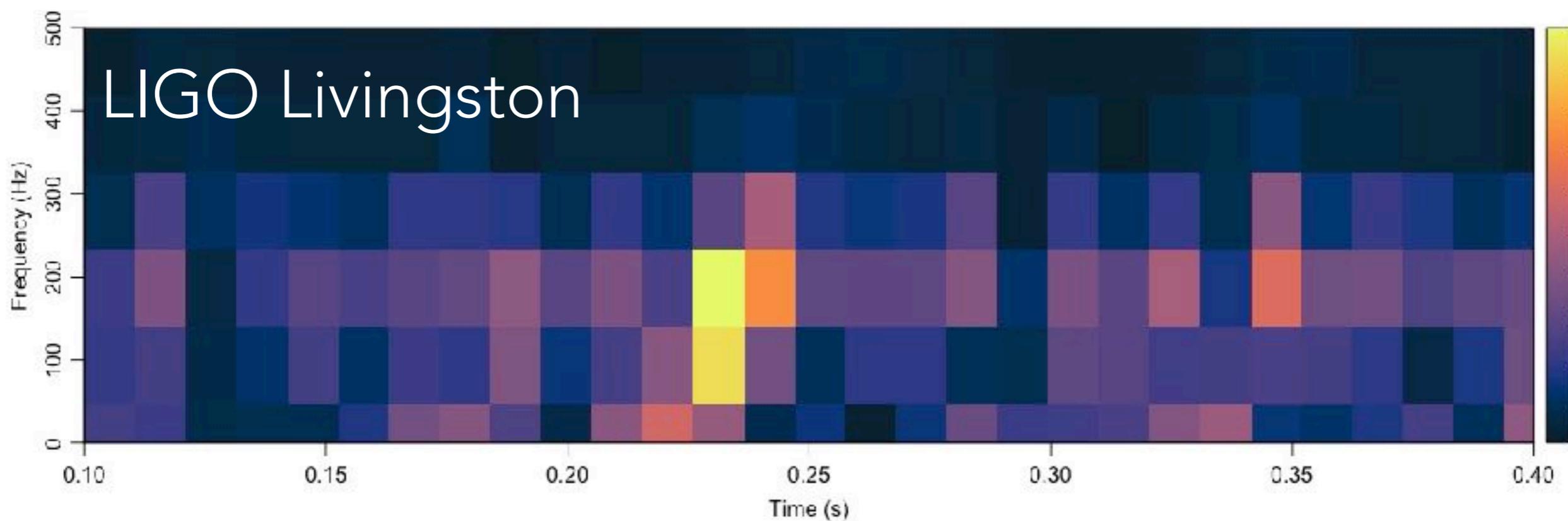
Raw data

Subtract
AR(33)
+
Low-Pass
filter



Residuals

TEST CASE#2: LIGO DATA OF GW150914

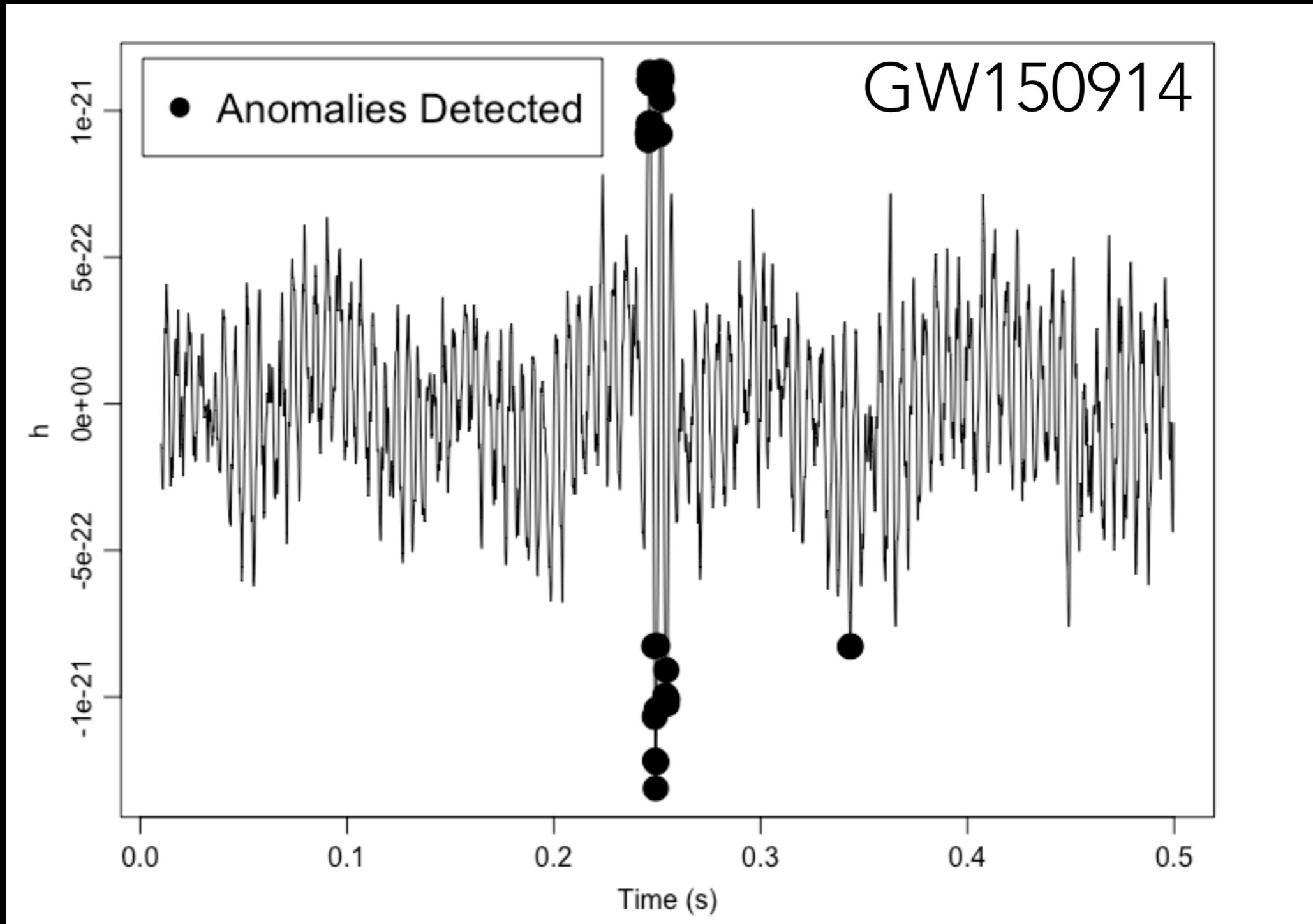


UNSUPERVISED ANOMALY DETECTION

- After the noise subtraction, events candidates can be identified as anomalies, which differ from normal instances significantly.
- Anomalies detected from different detectors (LIGO-H, LIGO-L, KAGRA, VIRGO) can be cross-correlated and analysed with clustering technique.
- The shortlisted anomalies can be taken as event candidates for further analysis.

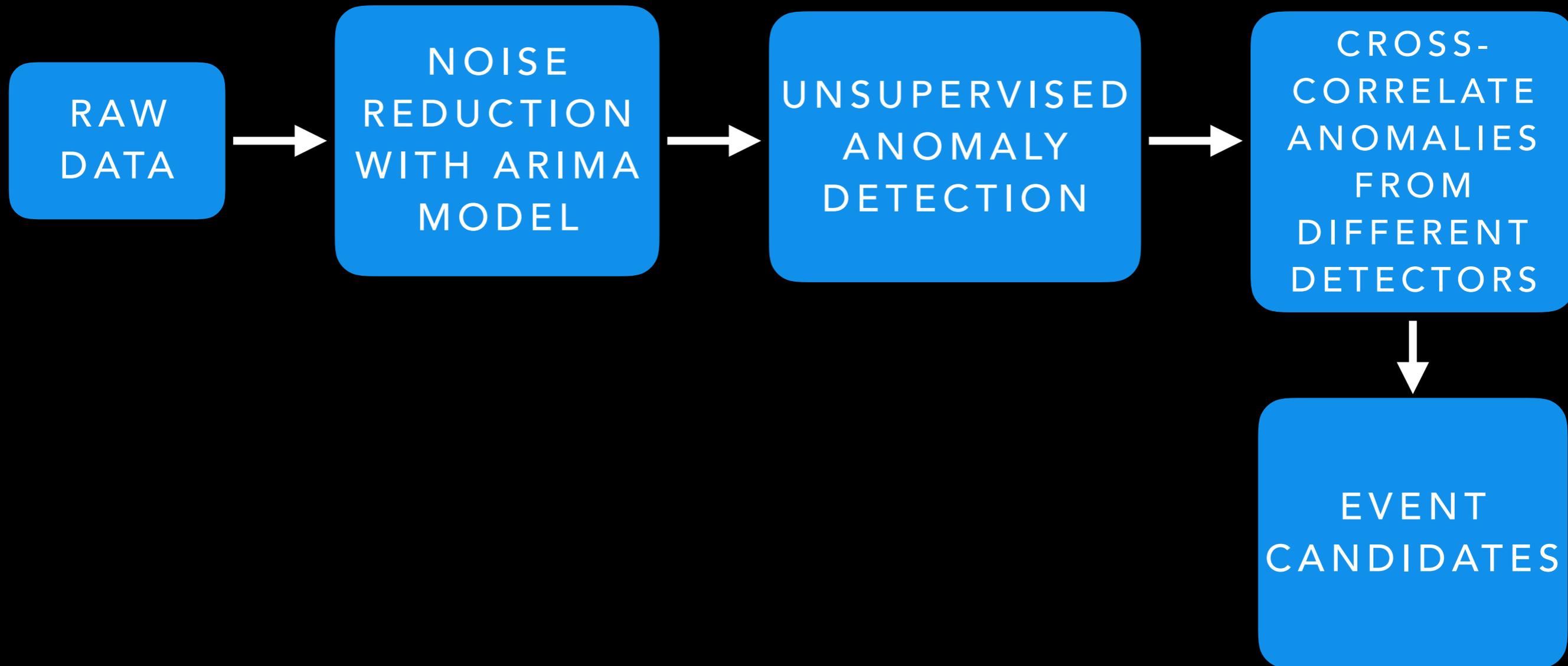
UNSUPERVISED ANOMALY DETECTION

II. LIGO Livingston



SUMMARY & OUTLOOK

We propose a computationally efficient pipeline for handling GW data.

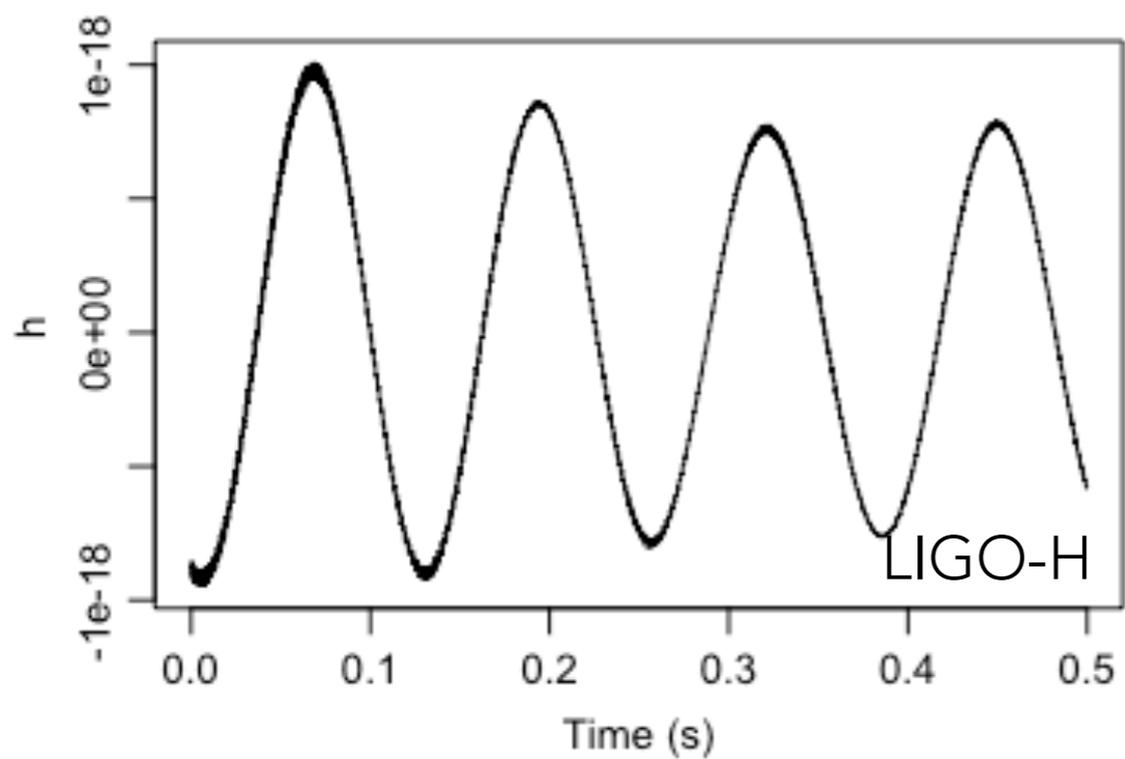


Further work will be devoted to improve the performance of anomaly detection with machine learning techniques (e.g. autoencoder).

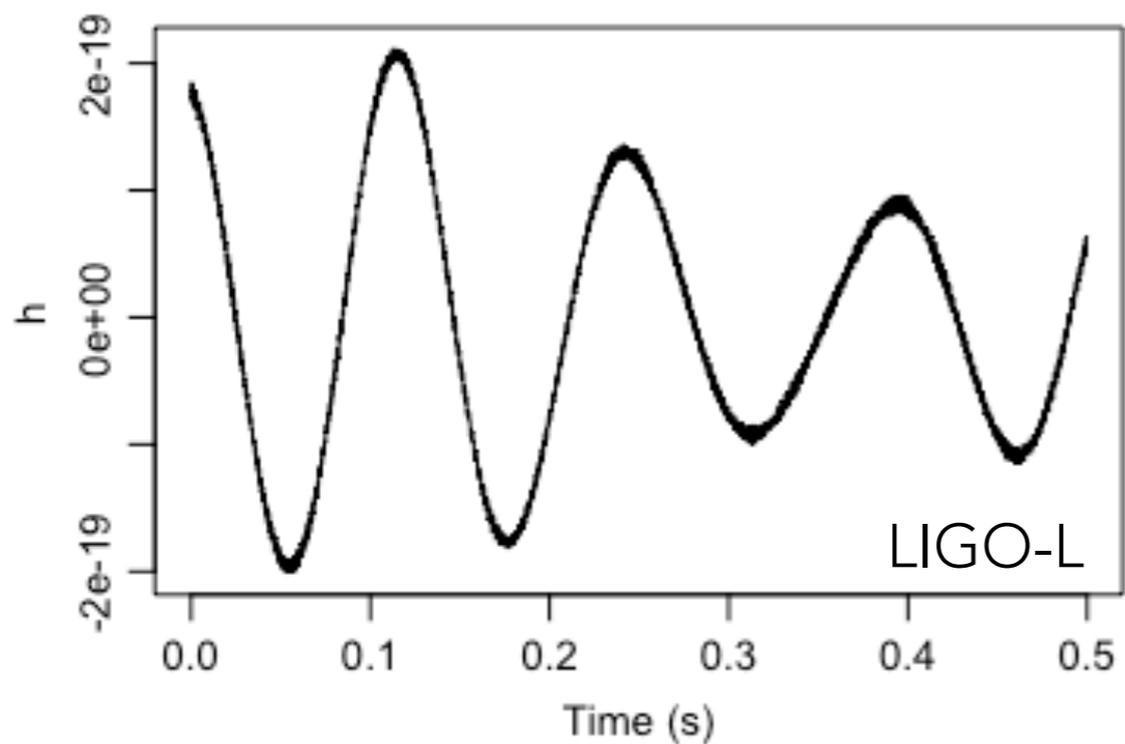
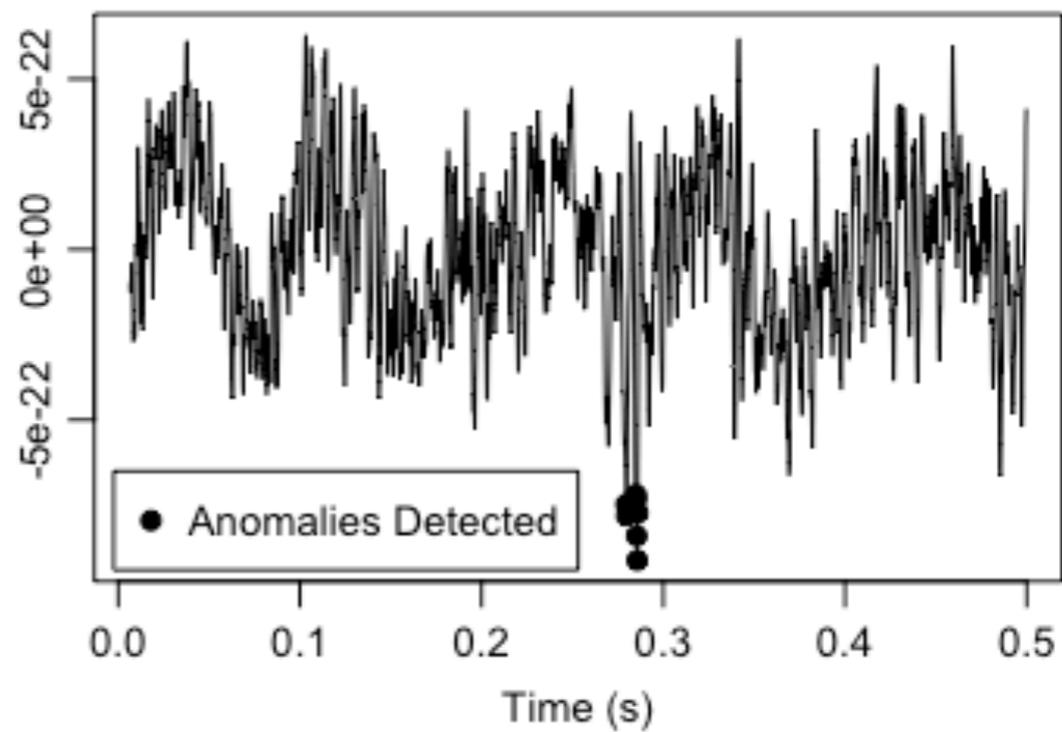
THANK YOU VERY MUCH

ADDITIONAL SLIDE:
TEST CASE #3

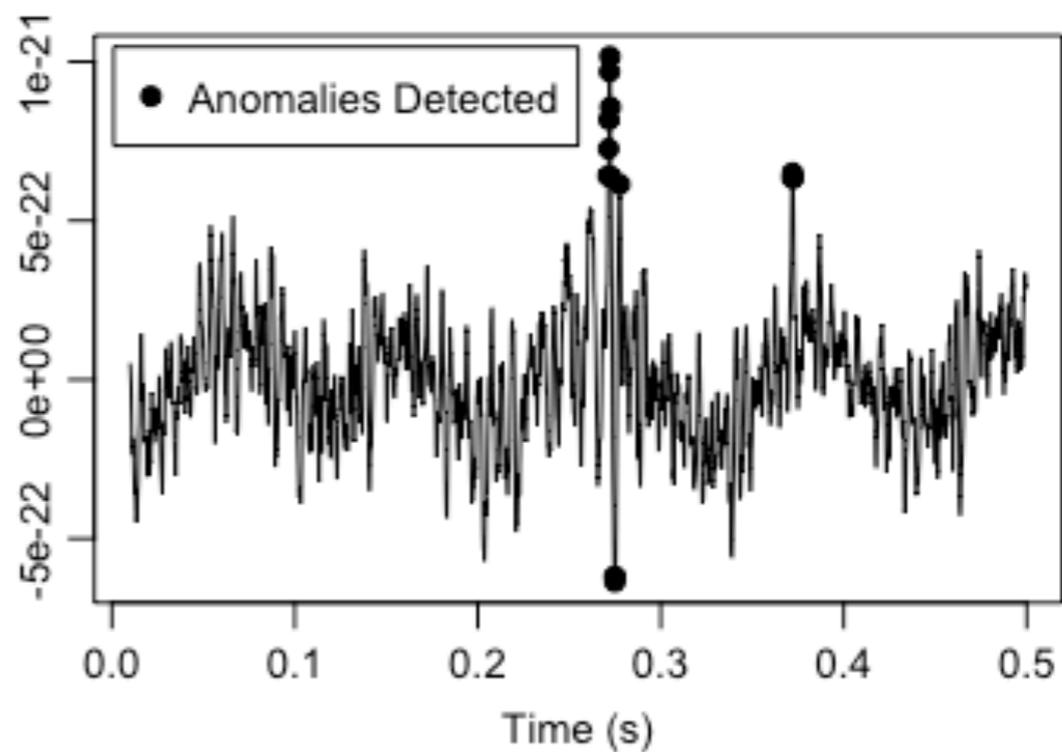
GW170814



$-AR(18)$
→



$-AR(32)$
→



GW170814

