

The F_2^n / F_2^p measurement in the BONuS12 experiment

Yu-Chun Hung
Old Dominion University



Outline

- Physics Motivations
- BONuS12 experiment with CLAS12 at Jefferson Lab
 - Experimental Setup
 - RTPC features
- Data analysis & Preliminary Results
- Summary

Probing the inner structure particles

- Scattering/Collision → Probe the internal structure of particles

- Elastic scattering:

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4E^2 \sin^4\left(\frac{\theta}{2}\right)} \frac{E'}{E} \left(\frac{G_E^2 + \tau G_M^2}{1 + \tau} \cos^2\left(\frac{\theta}{2}\right) + 2\tau G_M^2 \sin^2\left(\frac{\theta}{2}\right) \right) \quad \tau = \frac{Q^2}{4m_p^2}$$

G_E : Electric form factor
→ charge distribution of the nucleon.

G_M : Magnetic form factor
→ magnetic moment distribution of the nucleon

- Deep Inelastic Scattering (DIS, large Q^2 , large ν):

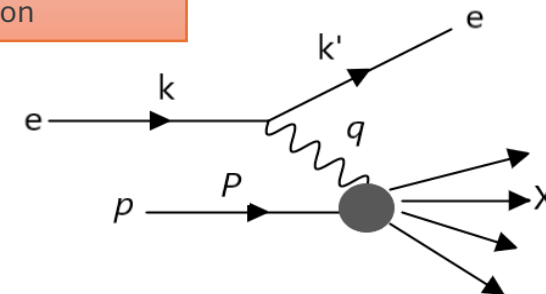
$$\frac{d\sigma}{d\Omega dE'} = \frac{\alpha^2}{4E^2 \sin^4\left(\frac{\theta}{2}\right)} \left(\frac{F_2(x, Q^2)}{\nu} \cos^2\left(\frac{\theta}{2}\right) + \frac{2F_1(x, Q^2)}{M_p} \sin^2\left(\frac{\theta}{2}\right) \right)$$

$F_1(x, Q^2), F_2(x, Q^2)$ are structure functions

- Naïve Quark-Parton Model

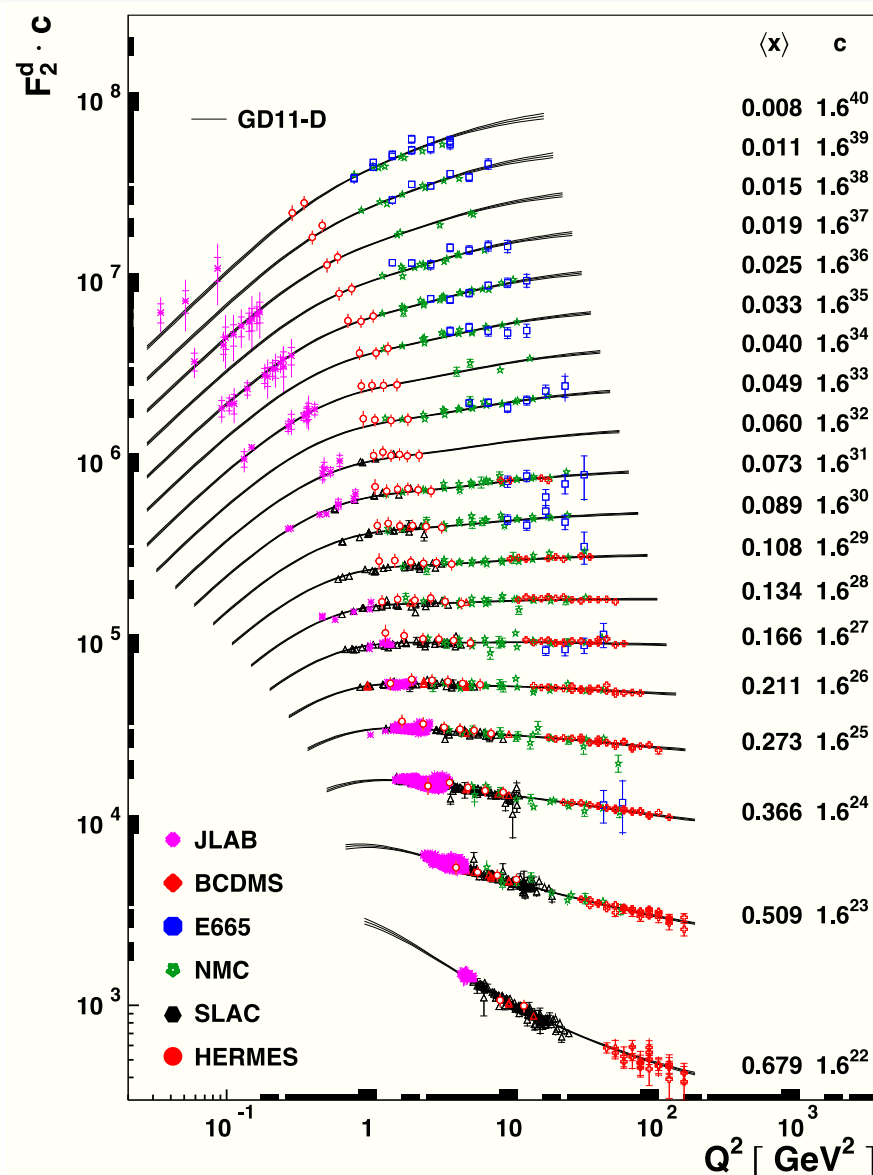
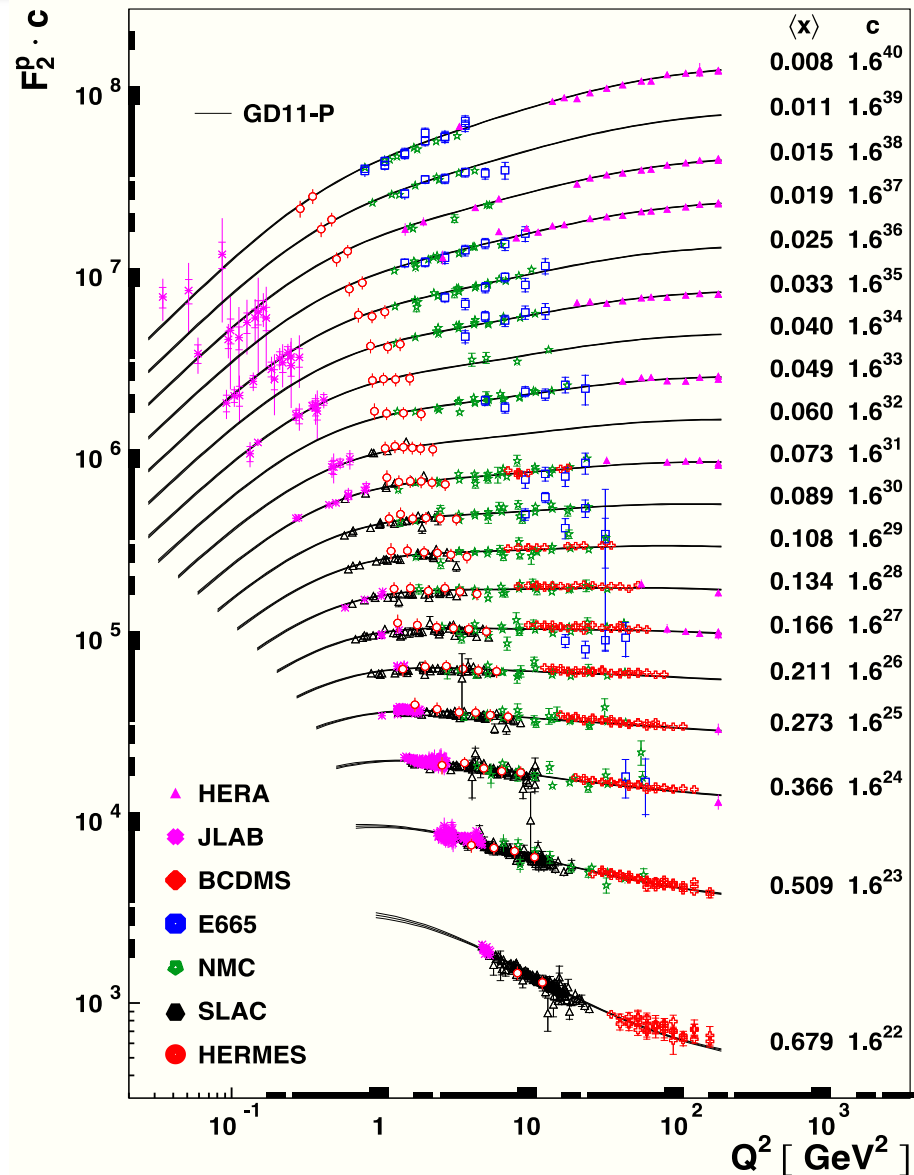
$$F_1(x) = \frac{1}{2} \left(\frac{4}{9} [u(x) + \bar{u}(x)] + \frac{1}{9} [d(x) + \bar{d}(x) + s(x) + \bar{s}(x)] + \dots \right)$$

$$F_2(x) = 2xF_1(x) \quad (\text{Callan-Gross relation})$$



Electron scatter off a proton in DIS region

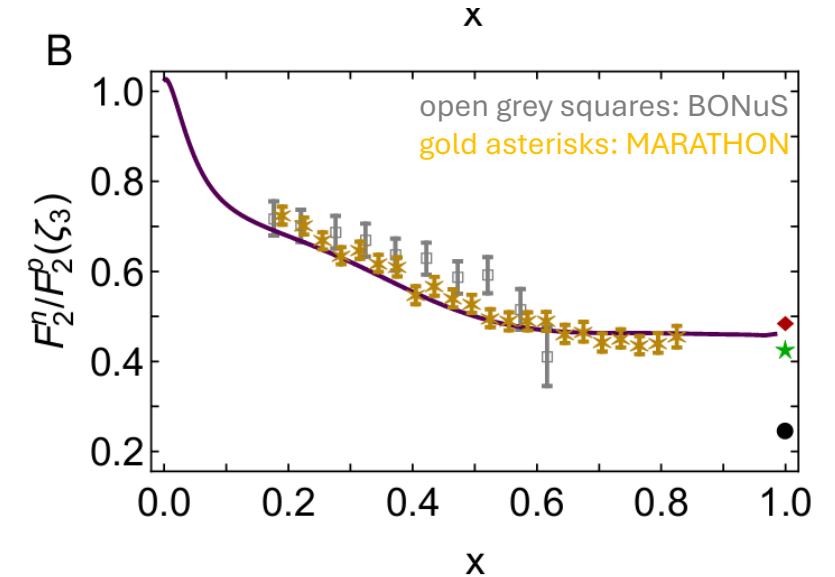
Structure Function — Existing data for p and D



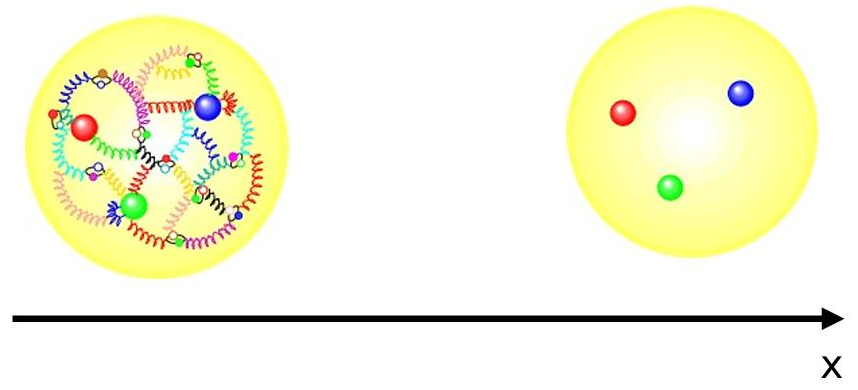
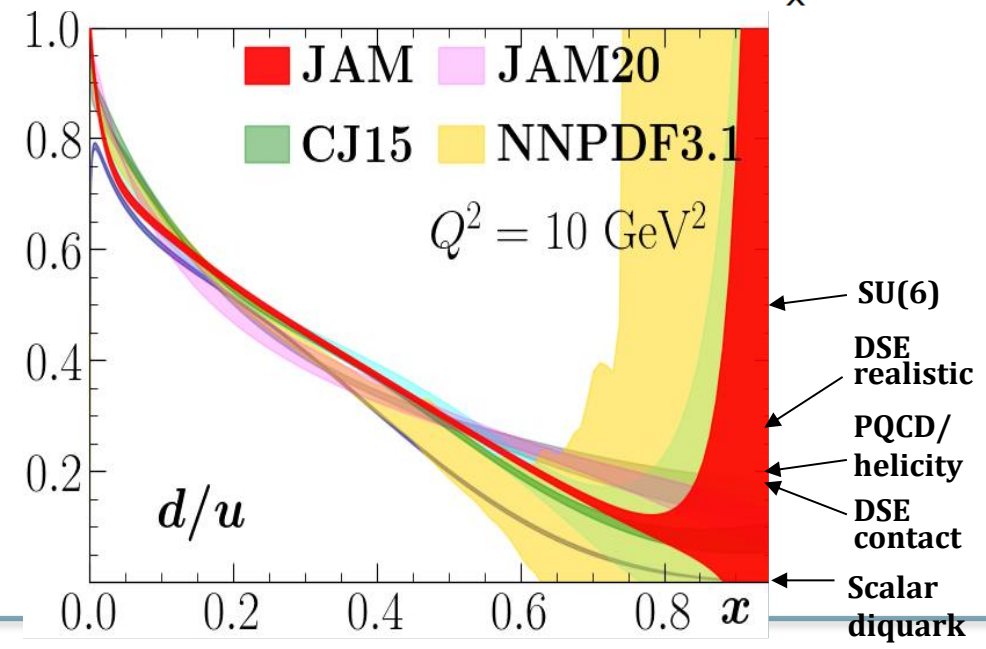
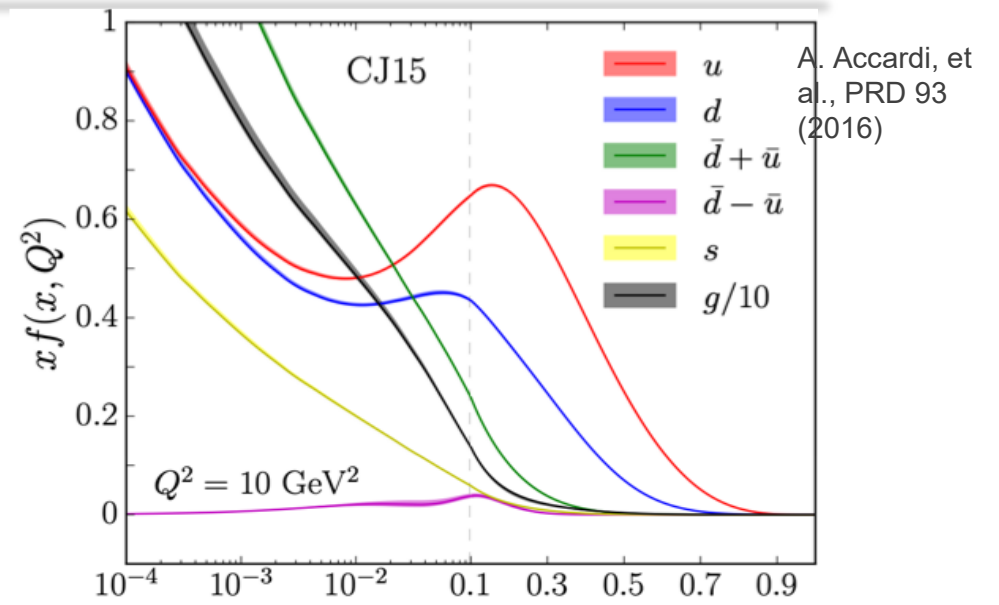
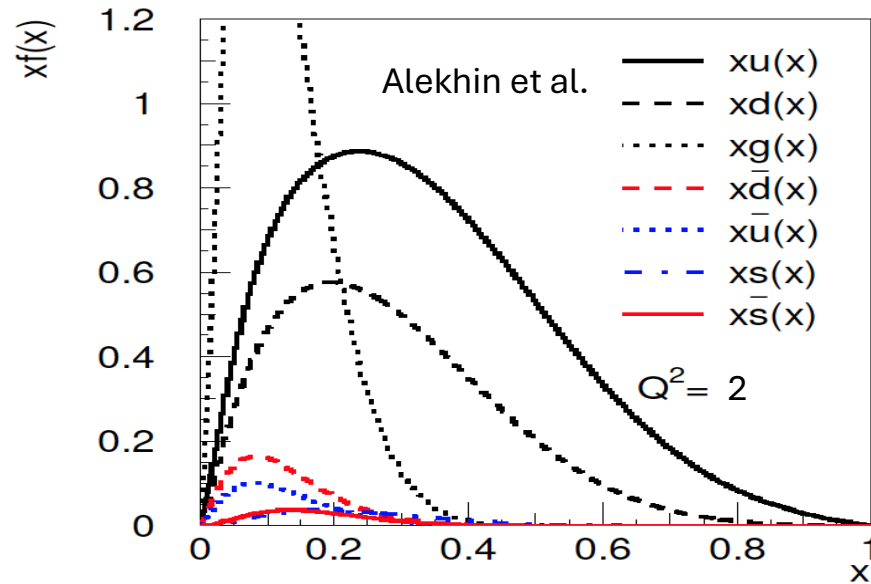
Rich results for F_2^p and F_2^d !

Structure Function — Existing data for n

- There are many experiments provide precise measurements on F_2^p and F_2^d , but less precise for F_2^n , especially at large x , where different theoretical models have different predictions
- Neutron as the target
→ Decay in ~ 15 mins.
→ difficult to prepare a free neutron in the experiment
- Obtained F_2^n from a bound neutron inside the nucleon.
→ The nuclear corrections will have theoretical model dependence at large Bjorken- x



Unpolarized PDFs



Valence Region: Structure Functions for $x \rightarrow 1$

- Dominated by up and down valence quarks \Rightarrow quantum numbers of the nucleon
- Important for higher power x^n moments \Rightarrow Mellin Moments, LQCD
- Related to high- Q^2 , moderate x through DGLAP \Rightarrow relevant for LHC Physics
- MANY predictions based on models, pQCD, DS equation and Lattice QCD ^{*)}:

^{*)} Moments, quasi-PDFs, pseudo-PDFs

- With Isospin symmetry, at large x :

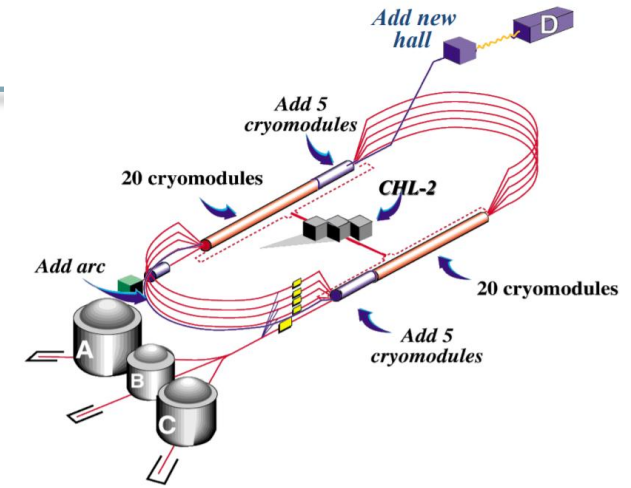
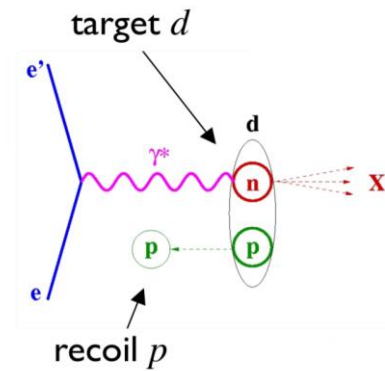
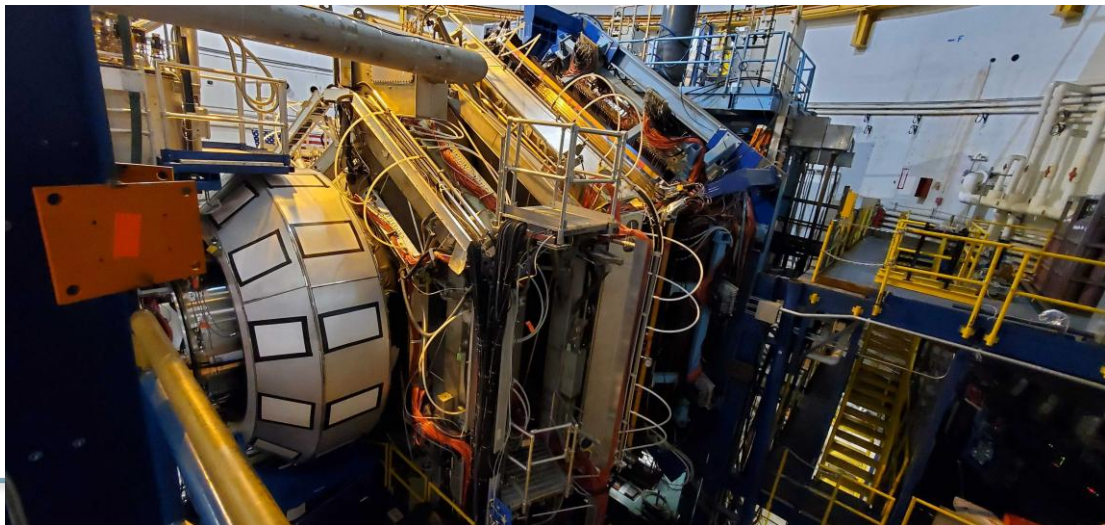
$$F_2^p \approx x \left(\frac{4}{9} u(x) + \frac{1}{9} d(x) \right)$$
$$F_2^n \approx x \left(\frac{4}{9} d(x) + \frac{1}{9} u(x) \right)$$

$$\rightarrow \frac{F_2^n}{F_2^p} \approx \frac{1+4d/u}{4+d/u}$$

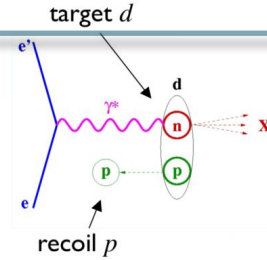
Nucleon Model	F_2^n/F_2^p	d/u
	$x \rightarrow 1$	$x \rightarrow 1$
SU(6) Symmetry	2/3	0.5
Scalar diquark dominance	1/4	0
DSE contact interaction	0.41	0.18
DSE realistic interaction	0.49	0.28
PQCD (helicity conservation)	3/7	0.2

BONuS12 Experiment at JLab

- BONuS12(Barely Offshell NUCleon Structure) is one of the experiments in the CLAS12 collaboration, completed at Jefferson Lab Hall B in 2020
- Extension program from previous BONuS with upgraded 12 GeV Continuous Electron Beam Accelerator Facility (CEBAF).
 - BONuS:
 - 5.3 GeV electron beam energy
 - DIS region: up to $x=0.56$ (at $W > 2(\text{GeV}/c^2)$)
 - BONuS12:
 - 11 GeV electron beam energy
 - DIS region: $x \sim 0.8$ (at $W > 1.8 (\text{GeV}/c^2)$)
- Use proton spectator tagging method which would reduce the model dependent of the $\frac{F_2^n}{F_2^p}$.



Nuclear Uncertainties in Deuteron



- **Final State Interaction**

- Struck neutron interacts with the spectator p
- Proton momentum is enhanced
- FSIs are small at low p_s and large θ_{pq}

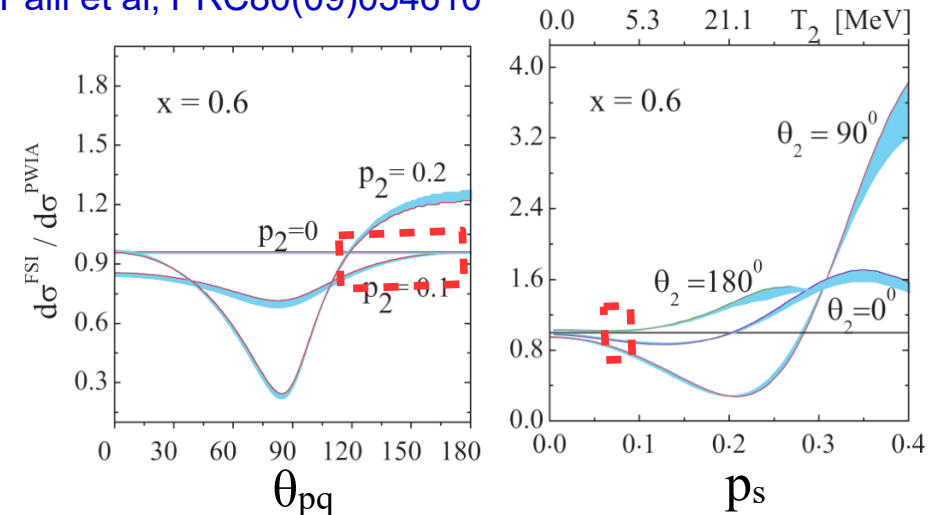
- **Target Fragmentation**

- $e n \rightarrow e p X$ (where $n \rightarrow \pi^- p$) and $e p \rightarrow e p X$ (where $p \rightarrow \pi^0 p$).
- TF enhances the proton yield only at forward angles ($\cos \theta_{pq} > 0.6$)

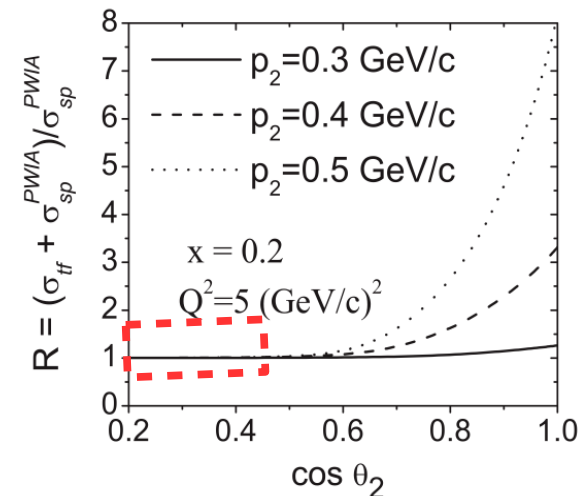
- **Off-Shell Corrections**

- Due to the neutron is bound in the deuteron
- Low p_s selection reduces this effect \rightarrow Less than 2% in our region

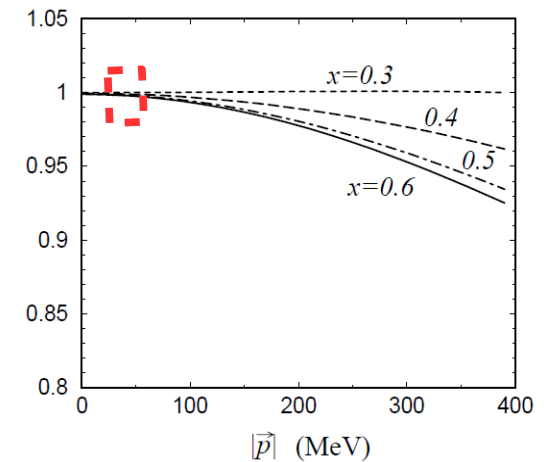
Palli et al, PRC80(09)054610



Palli et al, PRC80(09)054610



Melnitchoul et al, PRL B335,11(1994)



Extract the physics

$$D(e, e')X \quad R_{\text{inc}}(x, Q^2) = \frac{Y_{\text{inc}}^{\text{Data}}}{Y_{\text{inc}}^{\text{MC}}} \propto \frac{F_{2d}^{\text{true}}(x, Q^2)}{F_{2d}^{\text{Gen}}(x, Q^2)}$$

$$D(e, e'p_s)X \quad R_{\text{tag}}(x', Q^2) = \frac{Y_{\text{tag}}^{\text{Data}}}{Y_{\text{tag}}^{\text{MC}}} \propto \frac{F_{2n}^{\text{true}}(x', Q^2)}{F_{2n}^{\text{Gen}}(x', Q^2)}$$

$$SR = \frac{R_{\text{tag}}(x', Q^2)}{R_{\text{inc}}(x, Q^2)} = \frac{(Y_{\text{tag}}^{\text{Data}} / Y_{\text{tag}}^{\text{MC}})}{(Y_{\text{inc}}^{\text{Data}} / Y_{\text{inc}}^{\text{MC}})} = \frac{(Y_{\text{tag}}^{\text{Data}} / Y_{\text{inc}}^{\text{Data}})}{(Y_{\text{tag}}^{\text{MC}} / Y_{\text{inc}}^{\text{MC}})} = \text{Constant} \cdot \frac{\left(\frac{F_{2n}}{F_{2d}}\right)^{\text{true}}}{\left(\frac{F_{2n}}{F_{2d}}\right)^{\text{Gen}}}$$

$$\left(\frac{F_{2n}}{F_{2d}}\right)^{\text{true}} = \text{Constant} \cdot \left(\frac{F_{2n}}{F_{2d}}\right)^{\text{Gen}} * \frac{(Y_{\text{tag}}^{\text{Data}} / Y_{\text{inc}}^{\text{Data}})}{(Y_{\text{tag}}^{\text{MC}} / Y_{\text{inc}}^{\text{MC}})}$$

$$\left(\frac{F_{2n}}{F_{2p}}\right)^{\text{true}} = \left(\frac{F_{2n}}{F_{2d}}\right)^{\text{true}} * \left(\frac{F_{2d}}{F_{2p}}\right)^{\text{fit}} \quad \& \quad \frac{d}{u} \approx \frac{4F_{2n}/F_{2p} - 1}{4 - F_{2n}/F_{2p}}$$

$$Y_{\text{inc}}^{\text{Data}}(x, Q^2) \sim \mathcal{L} \left[A(x, Q^2) \cdot \eta(x, Q^2) \cdot \Delta\sigma_{\text{inc}}(x, Q^2) \right],$$

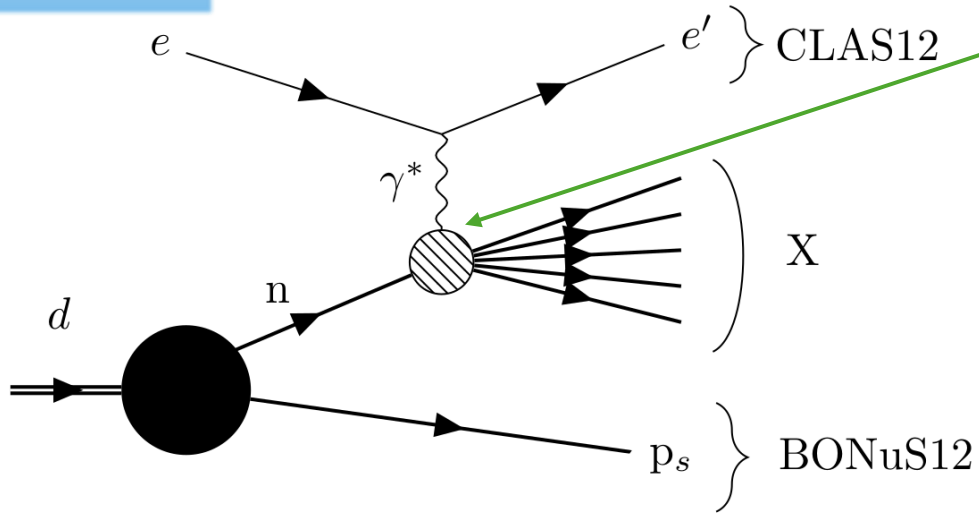
$$Y_{\text{inc}}^{\text{MC}}(x, Q^2) \sim \mathcal{L}_{\text{LUND}} \left[A(x, Q^2) \cdot \eta(x, Q^2) \cdot \Delta\sigma_{\text{inc}}^{\text{Sim}}(x, Q^2) \right],$$

of counts, with the assumption that $\Delta\sigma \propto F_2^d$

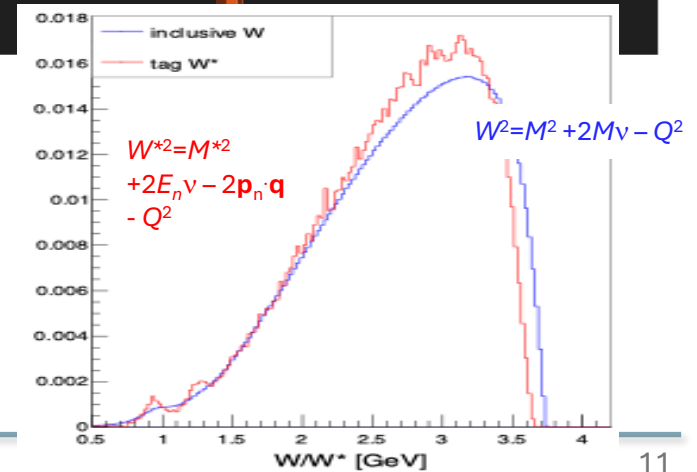
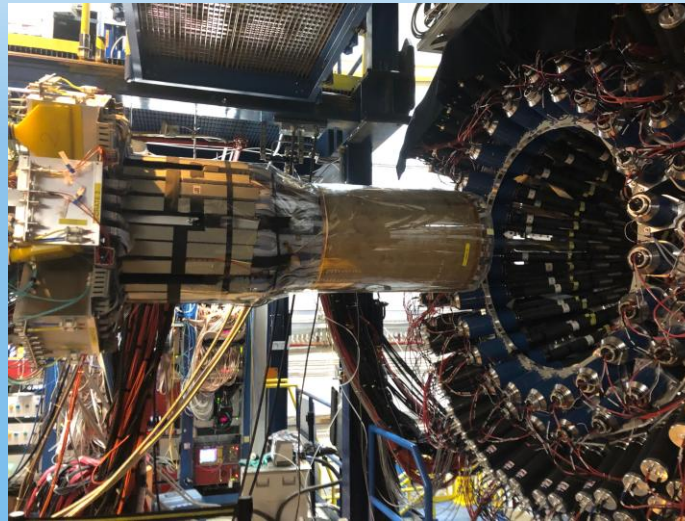
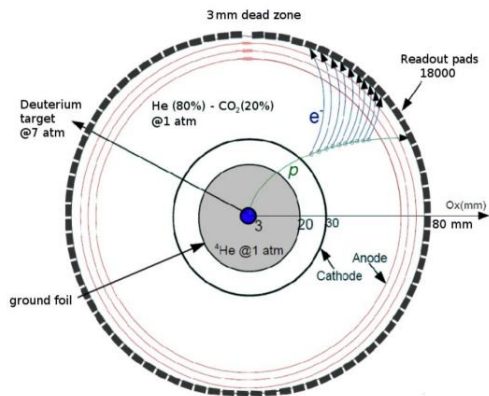
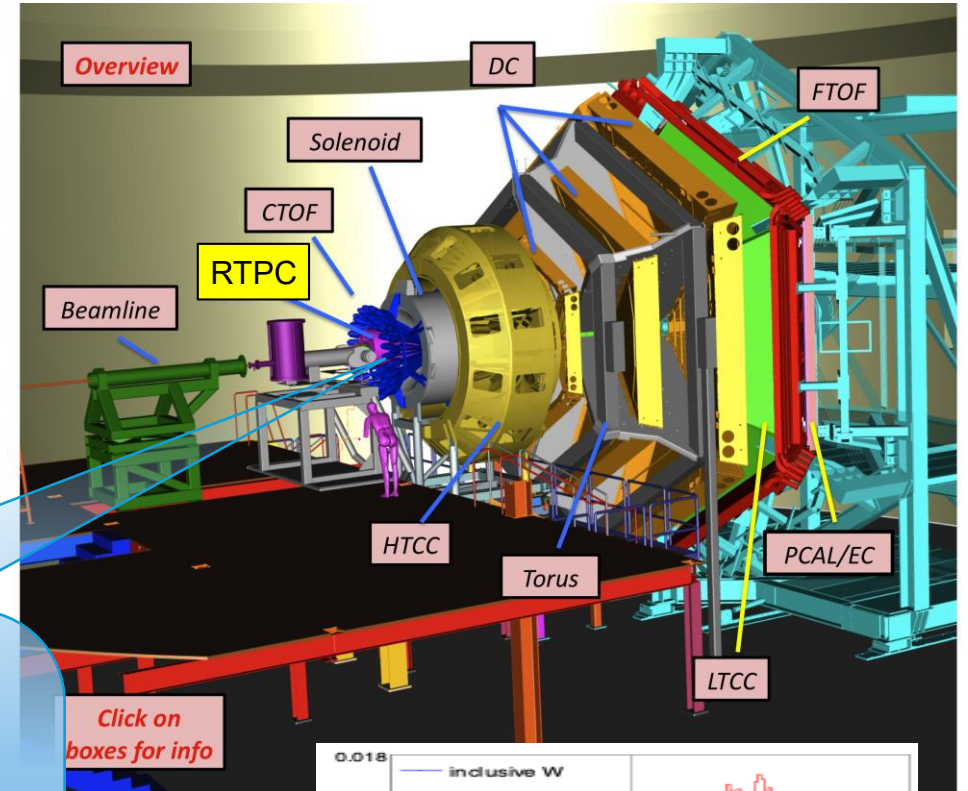
Acceptance and efficiencies

BONuS12 Experimental Setup with CLAS12

10.4 GeV

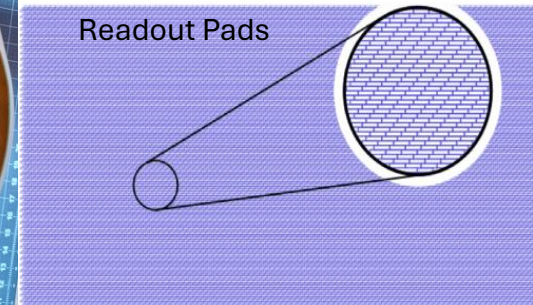
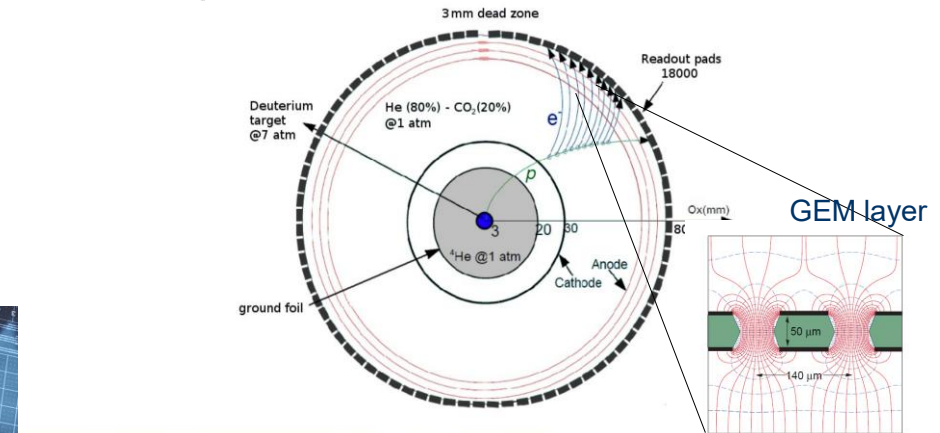
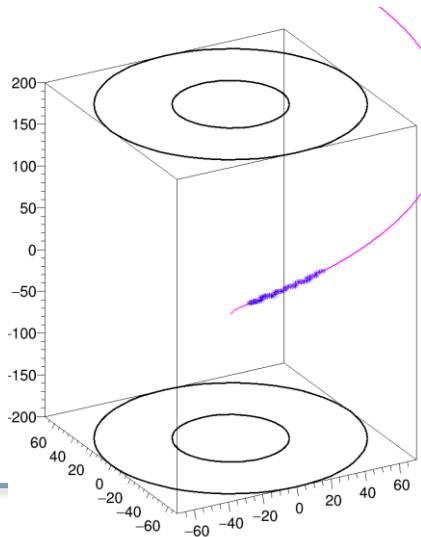
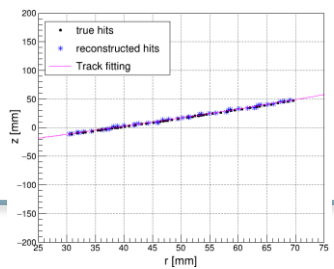
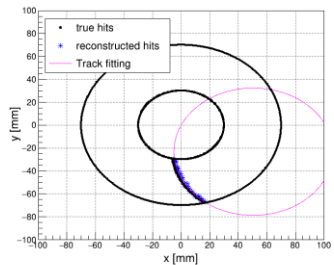
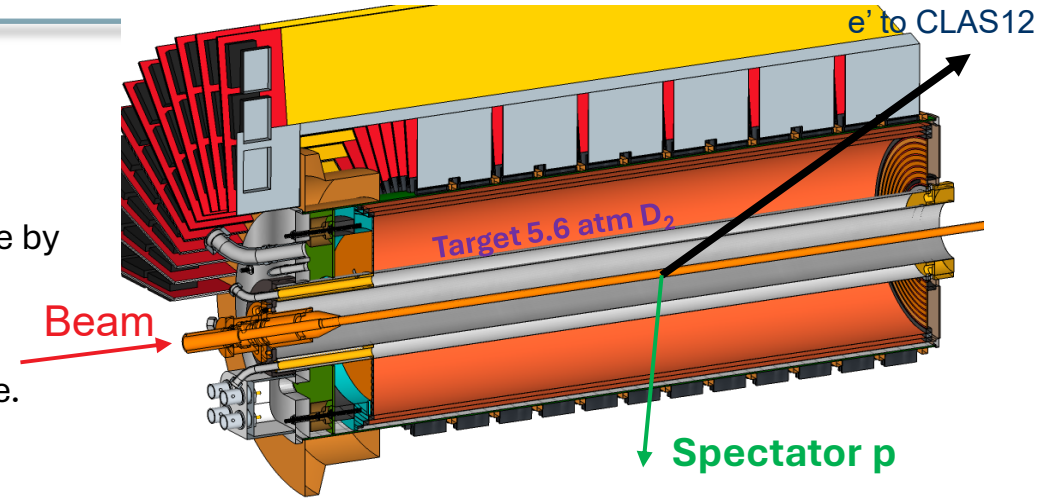


$$E_n = M_D - E_s$$
$$\mathbf{p}_n = -\mathbf{p}_s$$
$$M^{*2} = E_n^2 - \mathbf{p}_n^2$$



BONuS12 Radial Time Projection Chamber (RTPC)

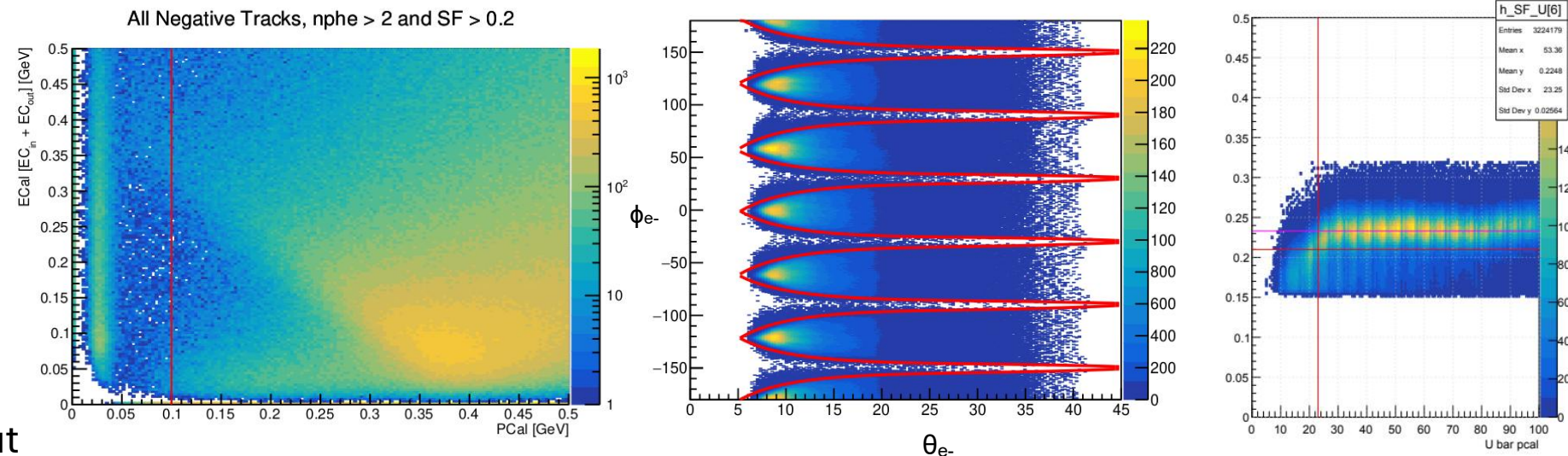
- Detector geometry and gas
 - 40 cm long , and 16 cm in diameter
 - He/CO₂ (80/20) gas mixture
 - Drift region (3 cm to 7 cm) and Transfer region (from 7 cm to 7.9 cm, 3mm space by the GEMs)
 - GEM (Gas Electron Multiplier): amplified the ionization electron.
 - Nearly 4 π angle coverage, 17,280 readout pads at outermost cylindrical surface.
- Work principle
 - Charged particle ionizes the gas atoms
 → Under EM field, released electrons follow their **drift paths** at a certain **drift speed**
 → Amplifications via the 3 GEM layers
 → Readout board → MVT FEU electronics → Signal height vs. Time bin
 - Construct 3D trajectory in the detector.



Event selection — DIS Electron at 10.4 GeV for D_2 target

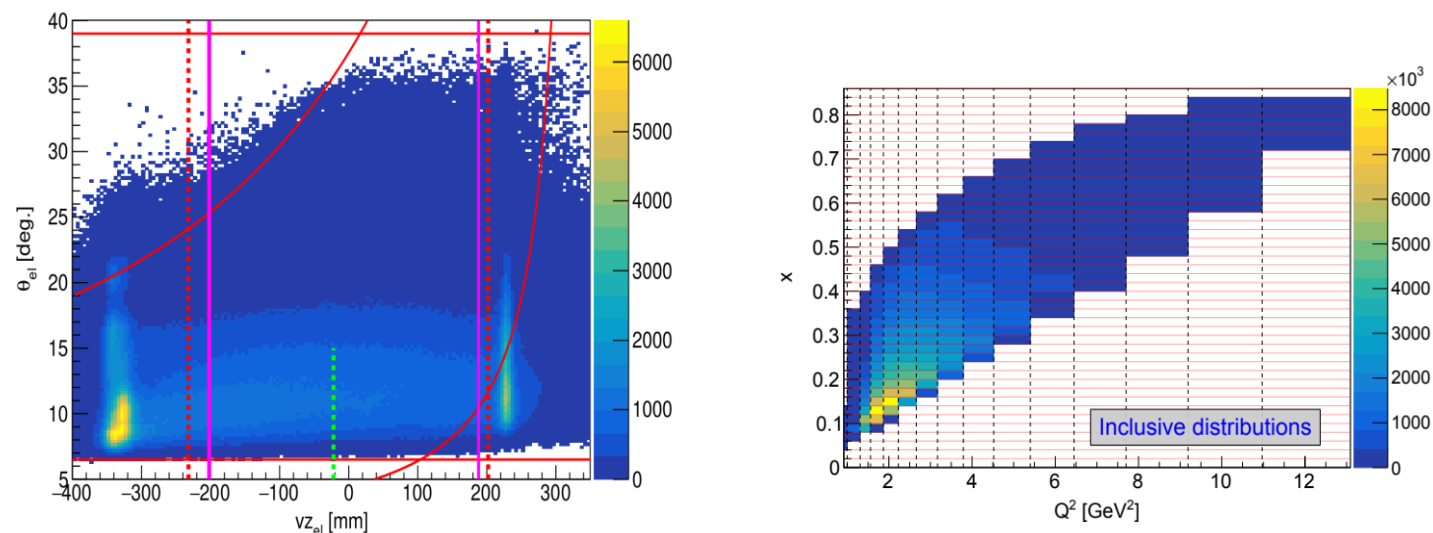
Electron selection cuts

- PID = 11
- nphe > 2
- $EC_{in} > 10$ [MeV]
- $E_{PCal} > 100$ [MeV]
- DC fiducial cuts
- $E' > 2.6$ [GeV]
- νZ_{e-}
- νZ_{e-} & θ_{e-} 2D geometric cut
- $\theta_{e-}^{local} > 7.0$ [Deg.]
- PCal SF and Fiducial cuts:



Additional DIS cuts

- $W > 1.8$ [GeV] (for Exp. And Sim.)
- $Q^2 > 1.56$ [GeV²]



Event selection — Spectator Proton in nDIS at 10.4 GeV for D_2 target

RTPC track quality cuts:

- The radius of curvature of tracks (< 0)
- Cut on χ^2 of helix fitter (< 5)
- Number of hits in a track (> 10)
- Cut on the maximum radius [67~72] [mm]
- Fiducial cut (v_z : [-210~180][mm])
- $35^\circ < \theta_{ps} < 145^\circ$

PID Cuts:

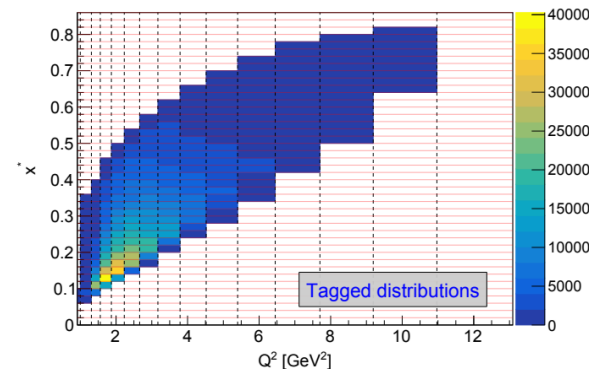
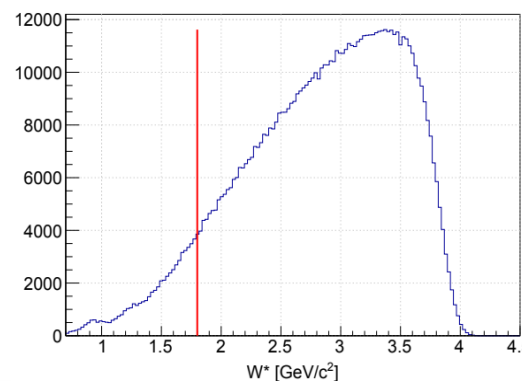
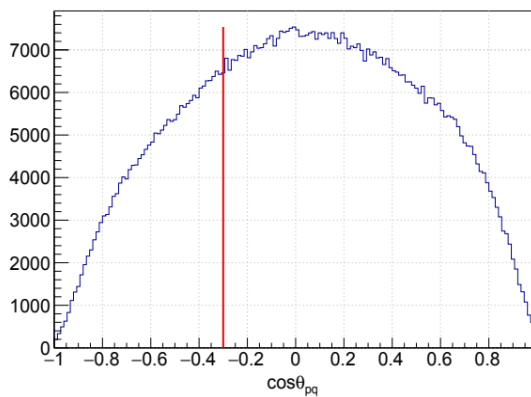
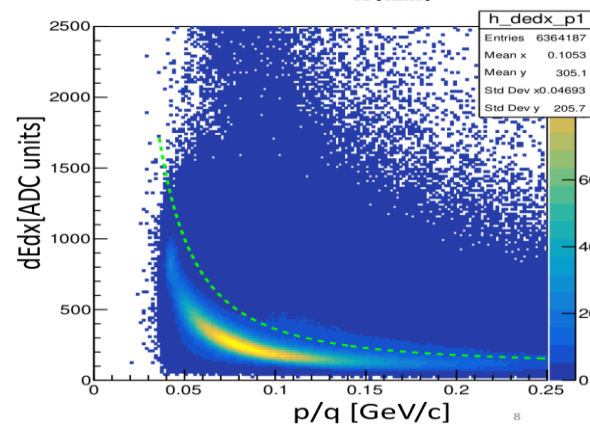
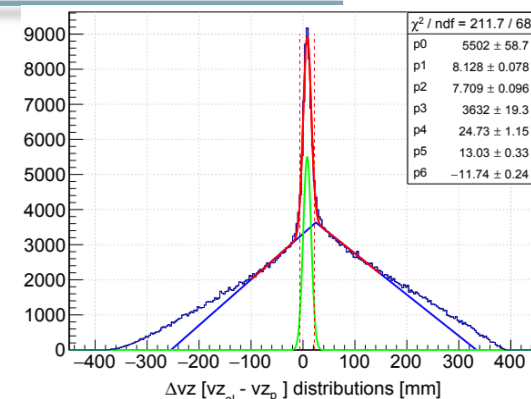
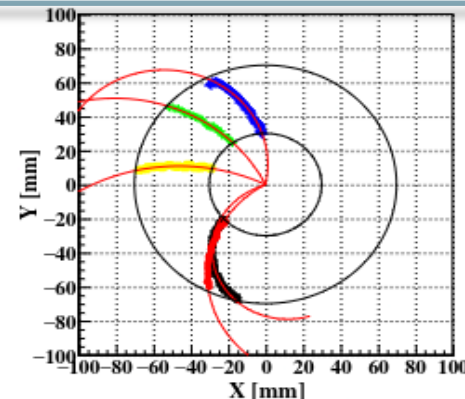
- Run-dependent Cuts on dEdx vs. p/q band for proton selection

ep Coincidence cuts

- Vertex coincidence cuts
- Timing coincidence

DIS & VIP cuts — To minimize the nuclear uncertainties (e.g. FSIs, Target Fragmentation, etc.)

- $W^* > 1.8$ [GeV]
- $0.075 < p_{ps} < 0.1$ [GeV/c]
- $\cos(\theta_{pq}) < -0.3$



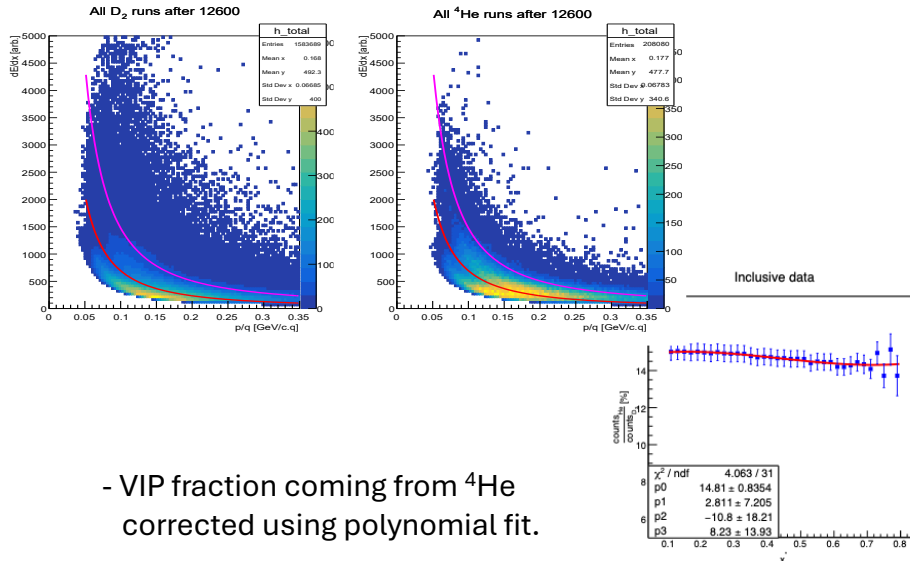
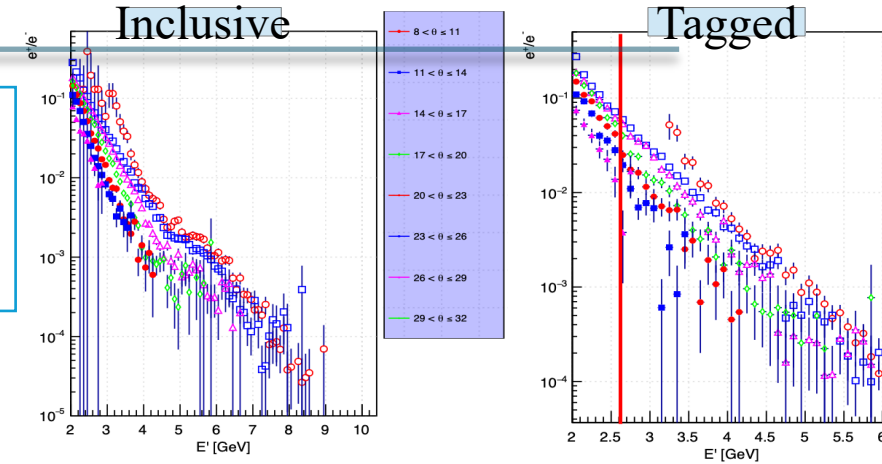
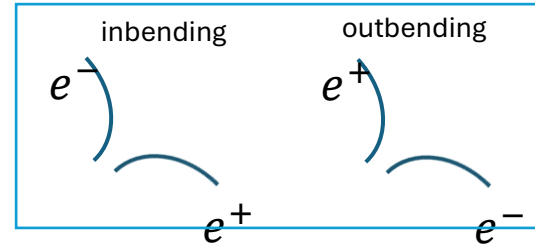
Background evaluation for experimental data

Electron

- Pair Symmetric Background: $\pi^0 \rightarrow e^+ e^- \gamma$
 - Secondary electron as trigger particle

Proton

- Accidental Background
 - Due to ionization electron inside RTPC drift slowly, the coincidence cuts are wider
 - Evaluated the combinatorics backgrounds by event mixing
- Deuterium Target Contamination



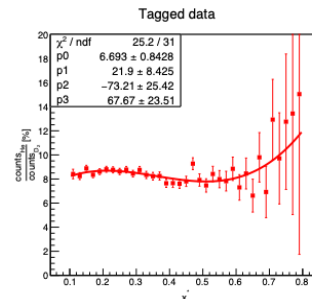
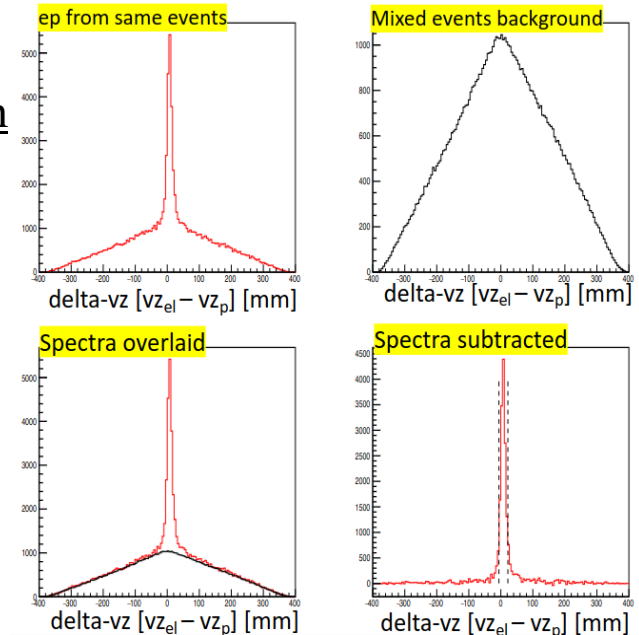
- VIP fraction coming from ^4He corrected using polynomial fit.

Electron

E1
E2
E3
.
.
.
E15

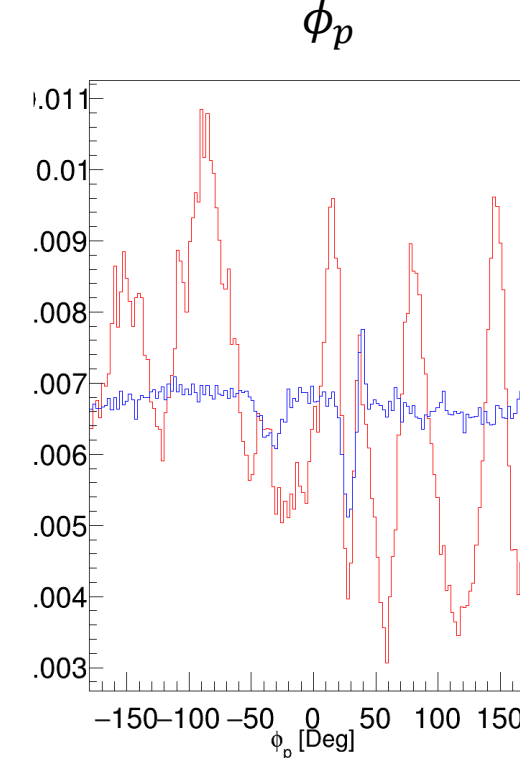
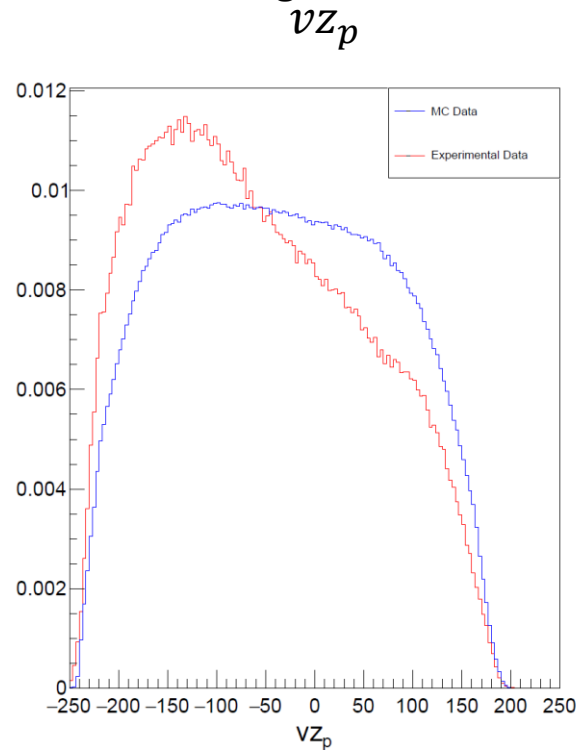
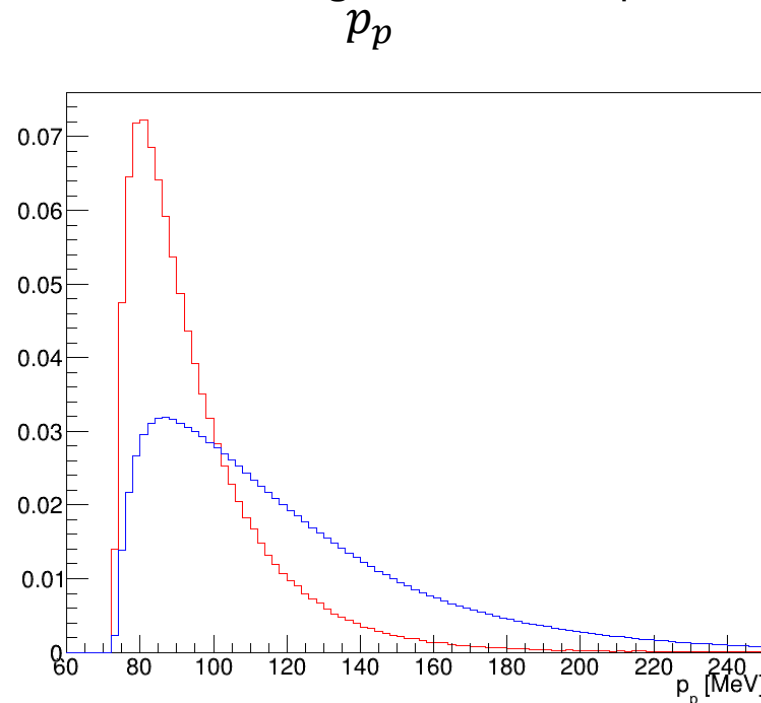
Proton

P1
P2
P3
.
.
.
P15



Simulation for BONuS12

- **Generator:** PWIA spectator model with 2014 Bosted/Christy fit to world data for F2n and F2d, AV18 D wave function, relativistic motion of struck nucleon, and equivalent radiator method for internal rad. Effects.
- Process the generated events through the full GEMC simulation chain with RTPC implementation and reconstruct them as real data. → For both tagged and inclusive cases.
- A realistic efficiency of RTPC is still needed to implement it into the simulation.
- Introduce weighting factors for each selected event to ensure the final distributions match the real data.
- The weight factors are evaluated from proton momentum, v_z , and ϕ_p
- The total weight factor is the product of all individual weight factors.

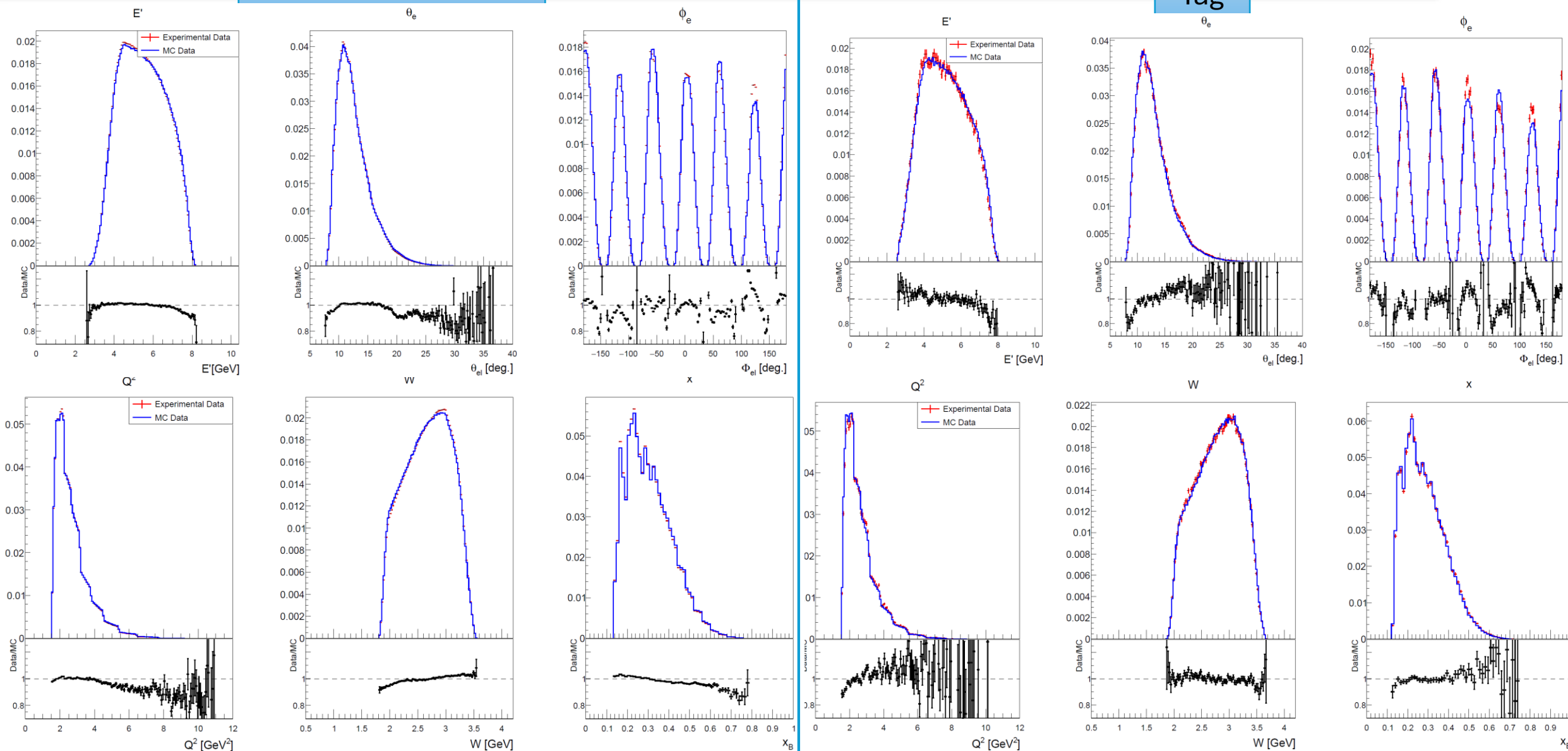


- MC. Data
- Experimental Data

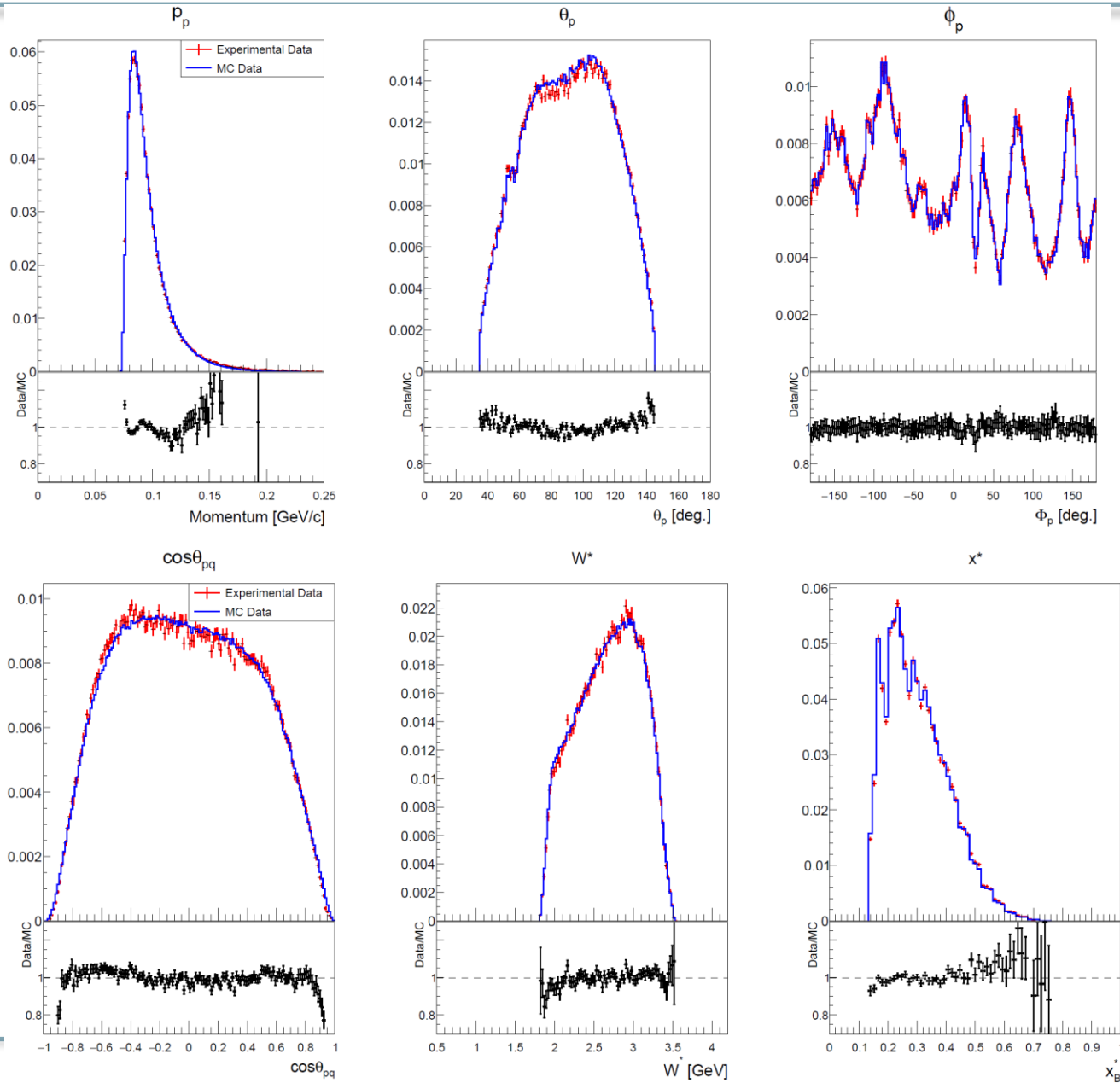
Data & MC comparison — Electron

Inclusive

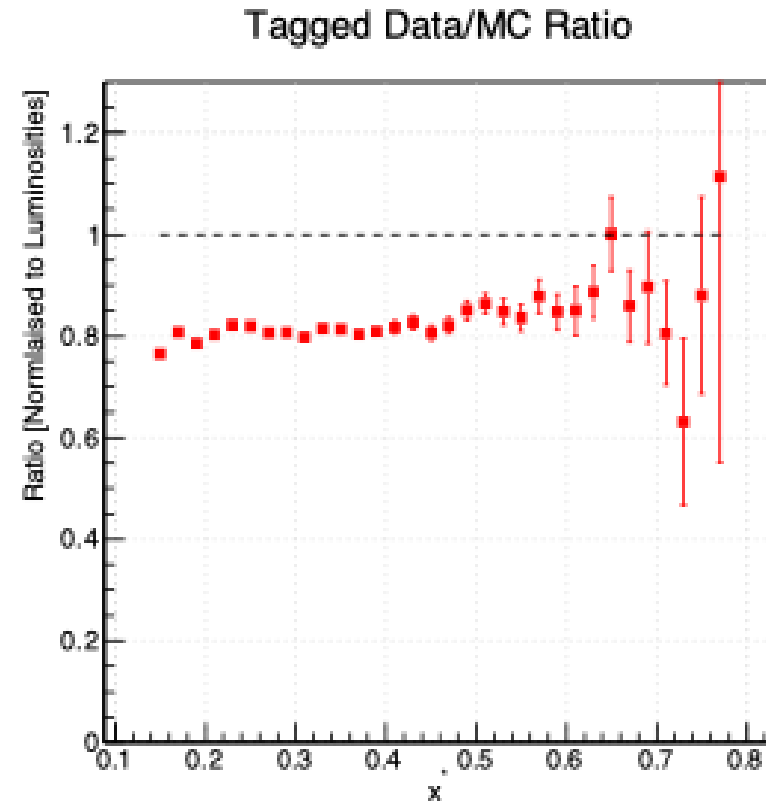
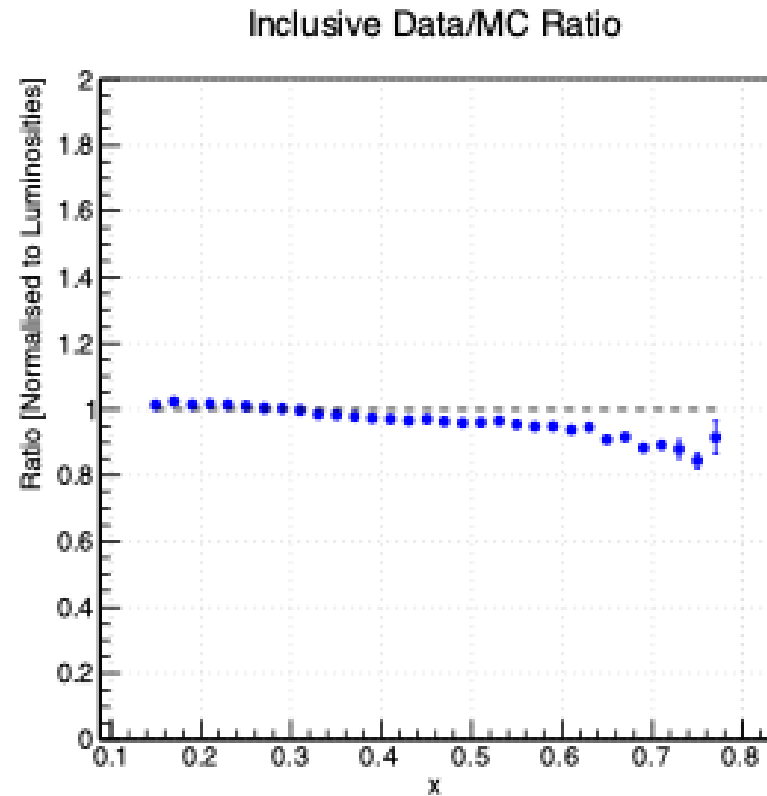
Tag



Data & MC comparison — Proton



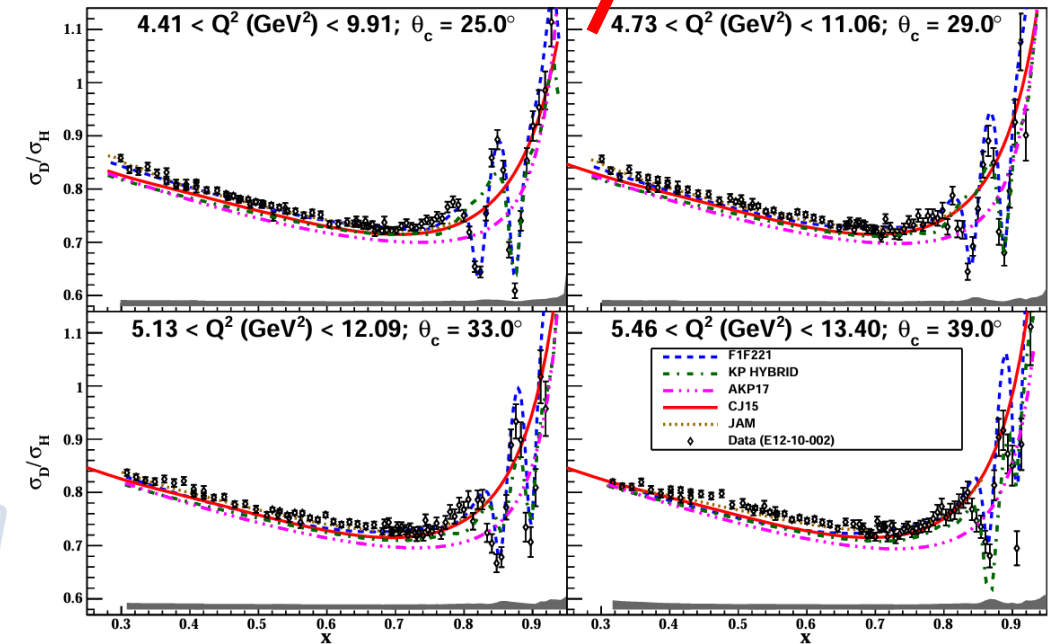
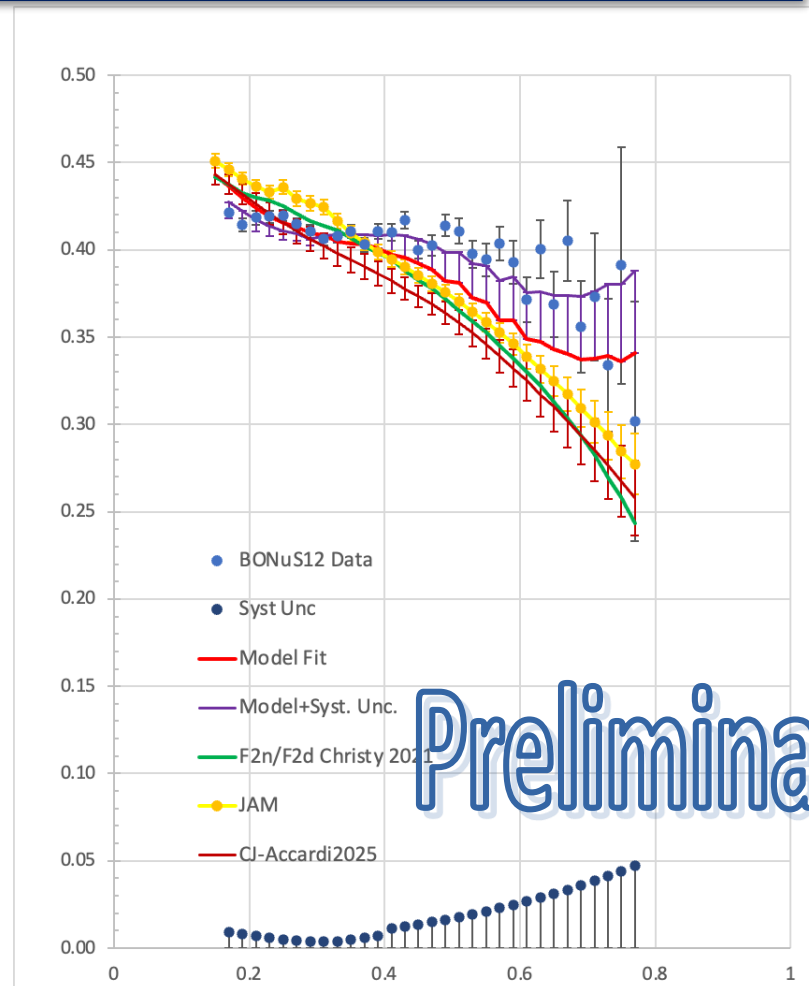
Data/MC ratio with Normalized Luminosities — $D(e, e')X$ and $D(e, e'p_s)X$



BONuS12 Preliminary Results — F_2^n / F_2^d

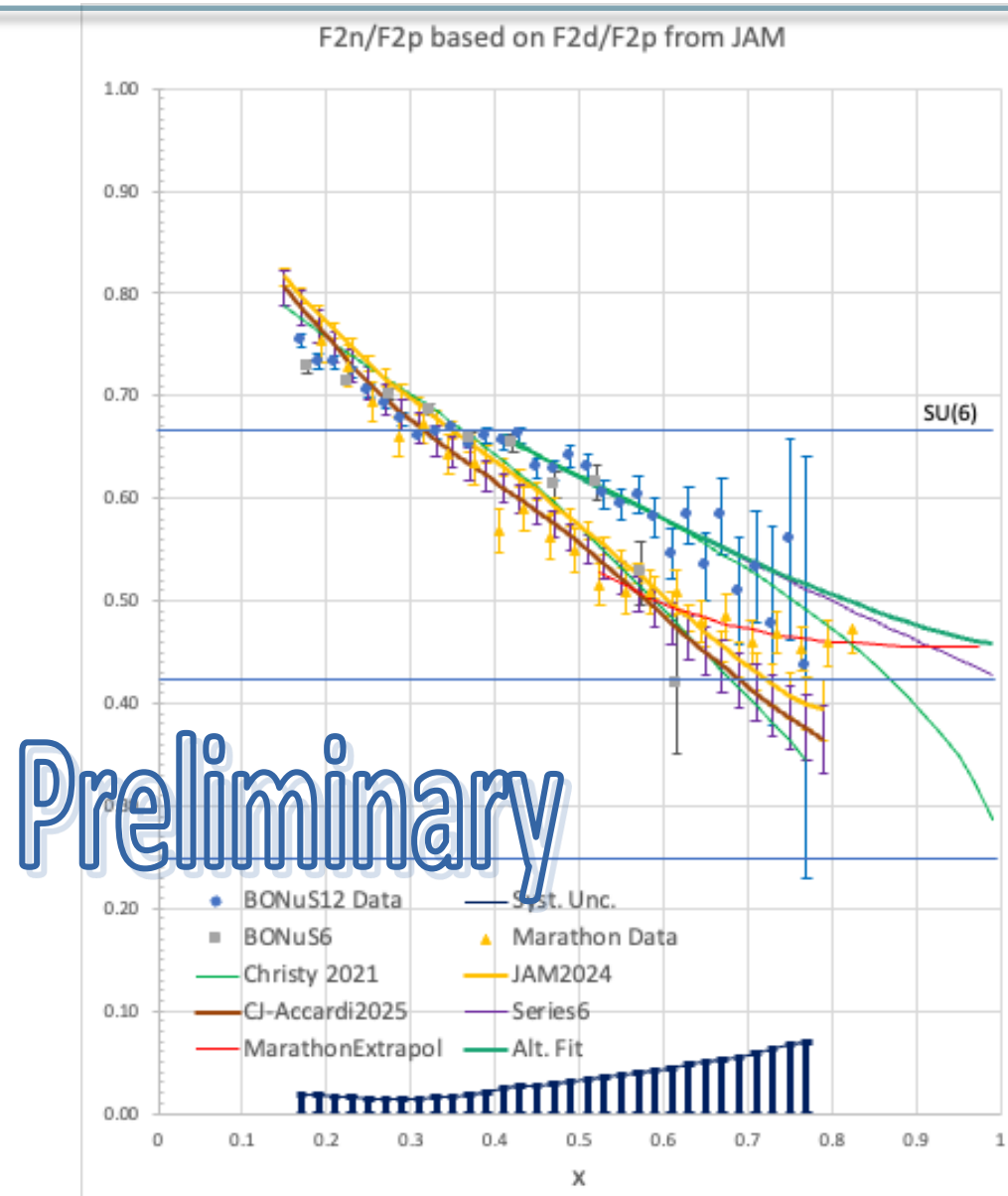
$$\left(\frac{F_{2n}}{F_{2d}}\right)^{\text{true}} = \text{Constant} \cdot \left(\frac{F_{2n}}{F_{2d}}\right)^{\text{Gen}} * \frac{\left(\gamma_{\text{tag}}^{\text{Data}} / \gamma_{\text{inc}}^{\text{Data}}\right)}{\left(\gamma_{\text{tag}}^{\text{MC}} / \gamma_{\text{inc}}^{\text{MC}}\right)}$$

$$\left(\frac{F_2^n}{F_2^p}\right)^{\text{true}} = \left(\frac{F_{2n}}{F_{2d}}\right)^{\text{true}} * \left(\frac{F_{2d}}{F_{2p}}\right)^{\text{fit}}$$

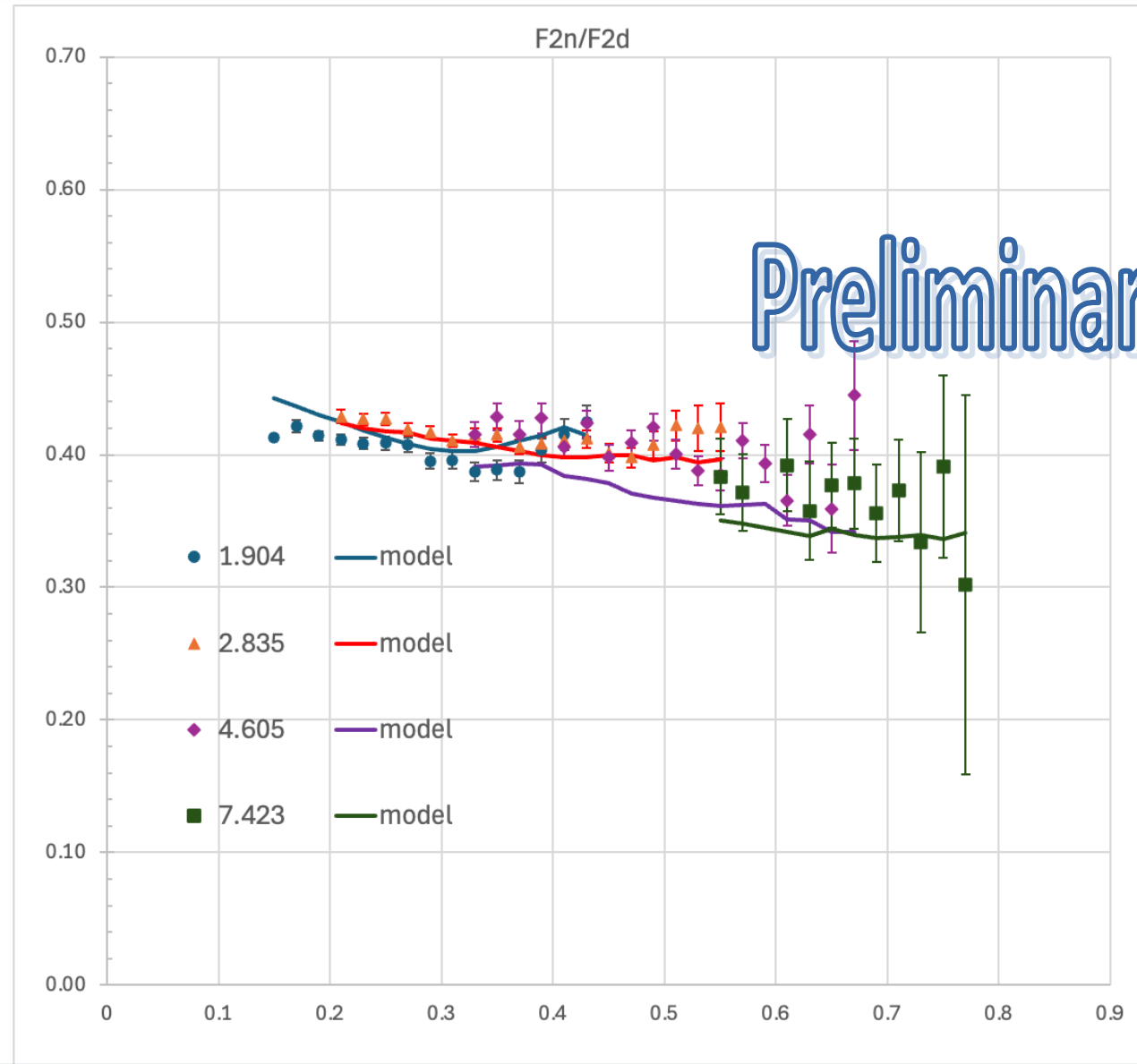


D. Biswas et al., arXiv hep-ex 2409.15236
PHYSICAL REVIEW LETTERS 135, 151902 (2025)

BONuS12 Preliminary Results — F_2^n / F_2^p



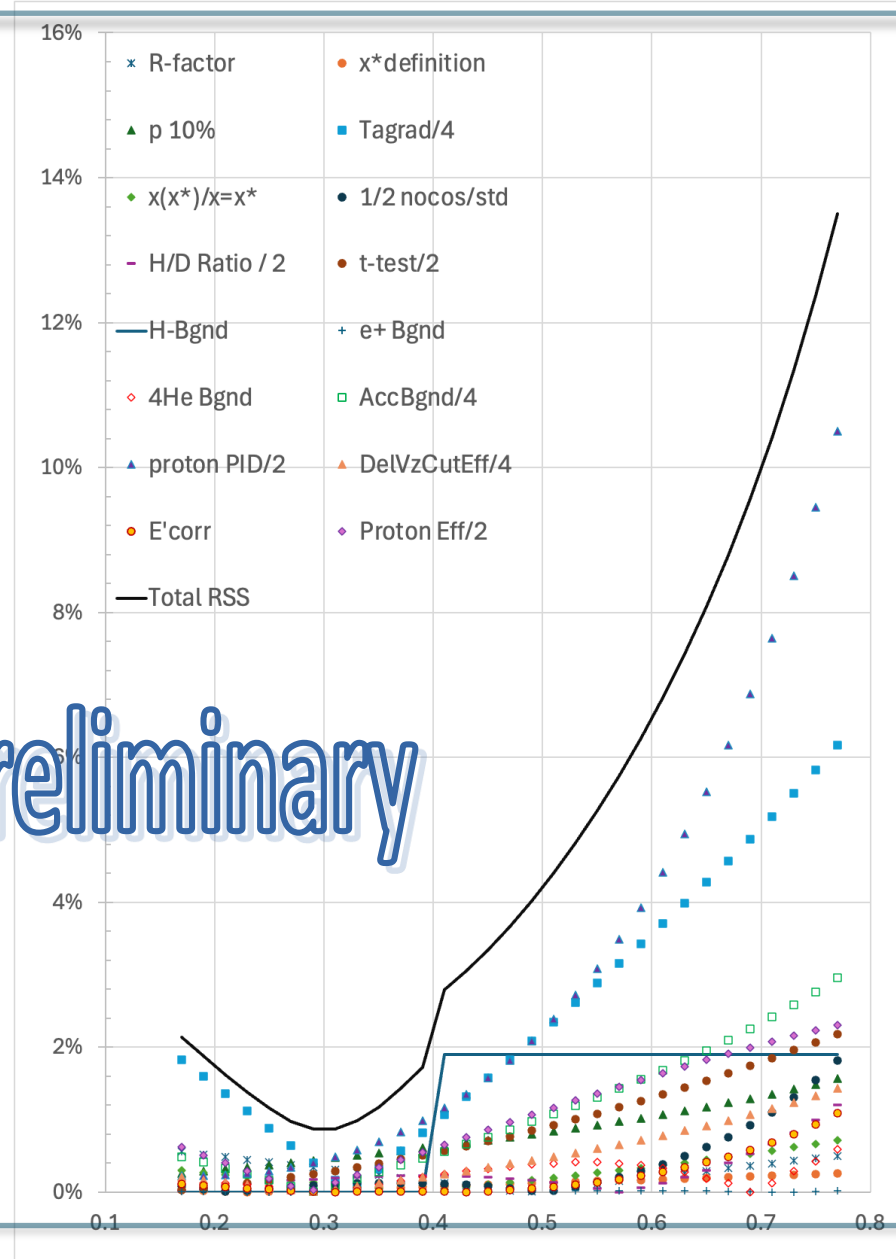
BONuS12 Preliminary Results — Q^2 -dependence F_2^n / F_2^d



Systematic Uncertainty Budget

- Correction for $R = \sigma_L / \sigma_T$
- Ambiguity in definition of x^* / n off-shellness
- Momentum misreconstruction
- **Radiative corrections**
- Mismatch between inclusive and tagged electron acceptance (different E' , q if $x^* = x$)
- Effect of dropping $\cos(\theta_{pq})$ VIP cut
- Sanity check: Can we extract F2p/F2D?
- Effect of different RTPC efficiency for 2nd half of run
- Background subtraction from tagged events:
 - “H background” ($A > 4$ target components)
 - Pair symmetric background
 - 4He background ($A=4$ target components)
 - Accidental background
- **Difference between low dE/dx and high dE/dx in the proton PID band**
- Coincidence cut efficiency
- E' correction in data and MC
- Efficiency correction for RTPC
- TOTAL RELATIVE SYSTEMATIC ERROR (Square root of sum of squares)

Preliminary



Summary

- Nucleon Structure functions provide fundamental information about bound-state QCD and continue to be actively studied (experimentally, theoretically, and phenomenologically)
- Structure functions in the valence region remain of high theoretical interest and provide crucial input to precision experiments (A1n, LHC,...)
- Results from MARATHON and, even more so, BONuS12 indicate higher than expected $F2n/F2p$ ratio at large x
- Essential ingredient: To extract neutron (polarized) structure functions from measurements on nuclei (d, ^3He) \Rightarrow we must understand the EMC effect in detail. Vice versa, only precise data on the free neutron can help us pin down nuclear binding effects across the table of isotopes
 \Rightarrow We need ALL the different data on $F2n$ we can get

Backup

BONuS12 Corr. V: Culling Partially Filled Bins

Ratio Tagged/Inclusive from MC show smooth dependence on x and Q^2 except for a few bins at the edge of the acceptance (very sensitive to precise simulation of physical boundaries), as well as bins only partially filled due to W^* / W cut \Rightarrow These bins have been removed from final results...

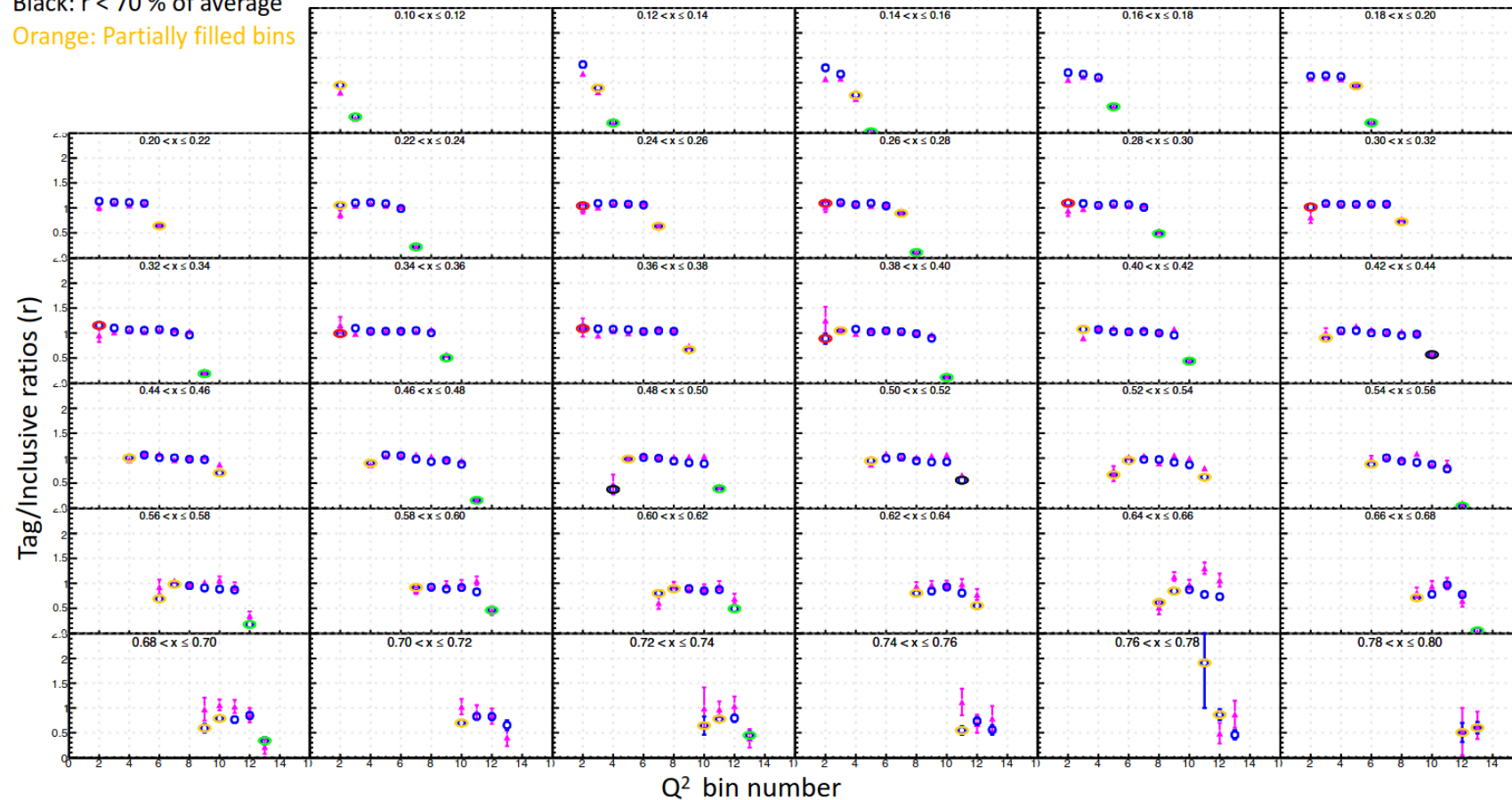
Green: $r < 0.5$

Red: Statistical uncertainty > 2.5 times the average

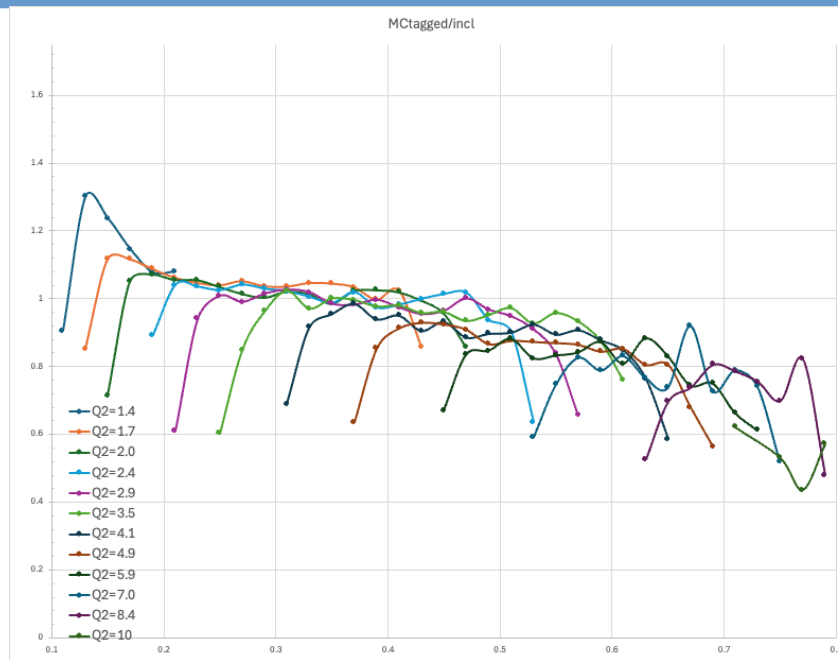
Black: $r < 70\%$ of average

Orange: Partially filled bins

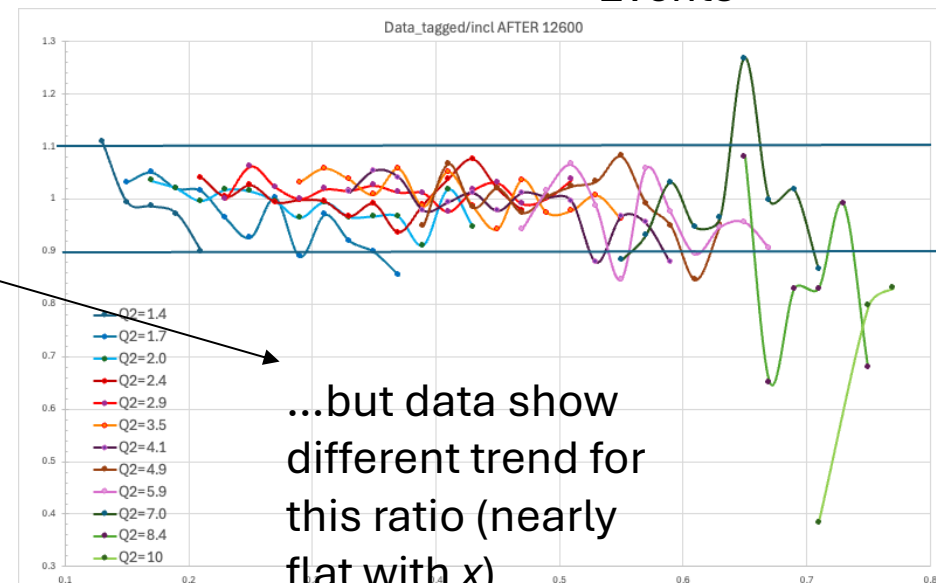
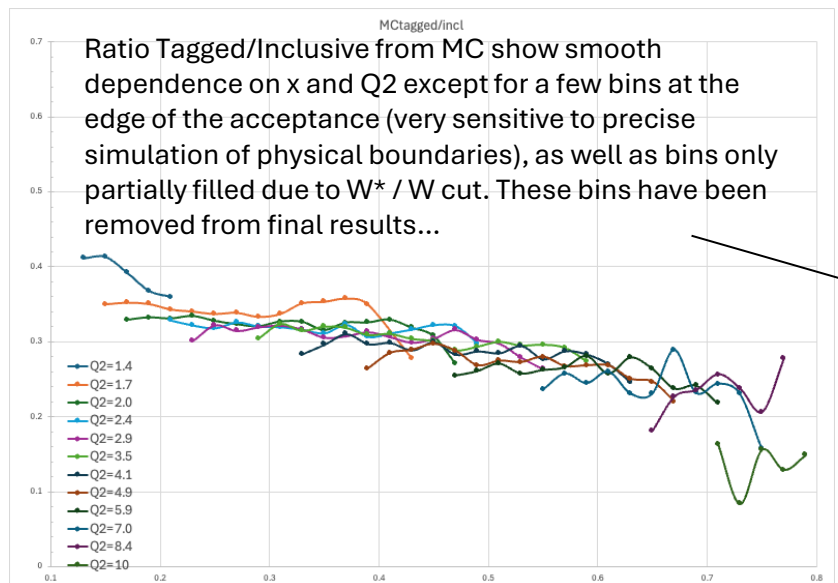
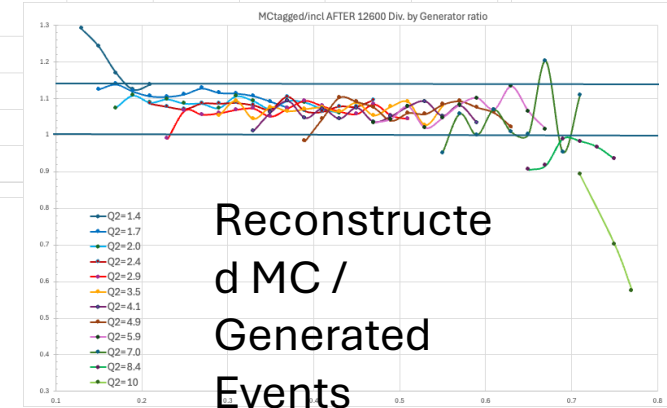
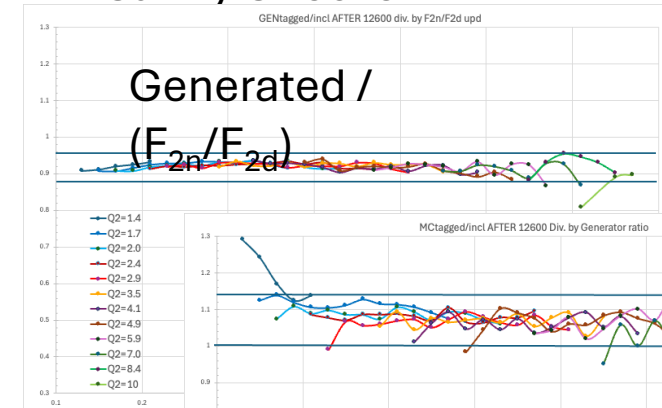
Magenta: Data : Blue: MC



BONuS12 Corr. V: Culling Partially Filled Bins

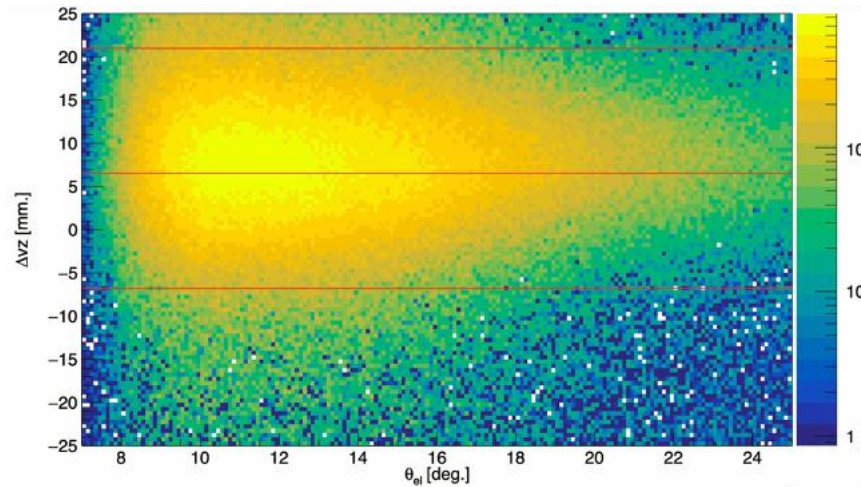


Sanity Checks:



...but data show different trend for this ratio (nearly flat with x)

Event selection — Vertex coincidence cuts ($\Delta v_z = v_{z,e} - v_{z,p}$)



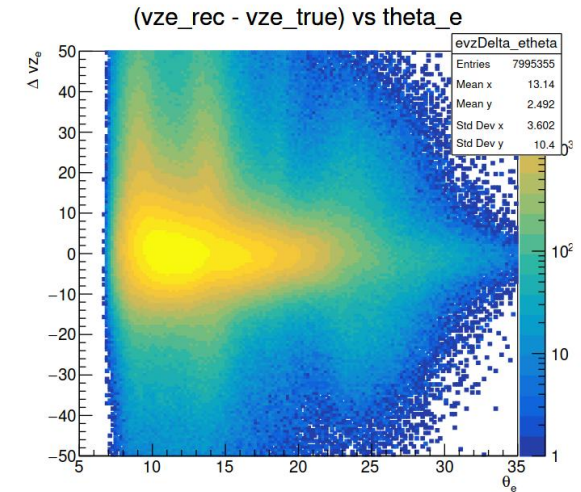
Δv_z cut for **data** is 2σ around μ , separately for each sector \rightarrow

θ -dependence of μ and σ leads to θ -dependent inefficiency (Gaussian tails outside the cut)

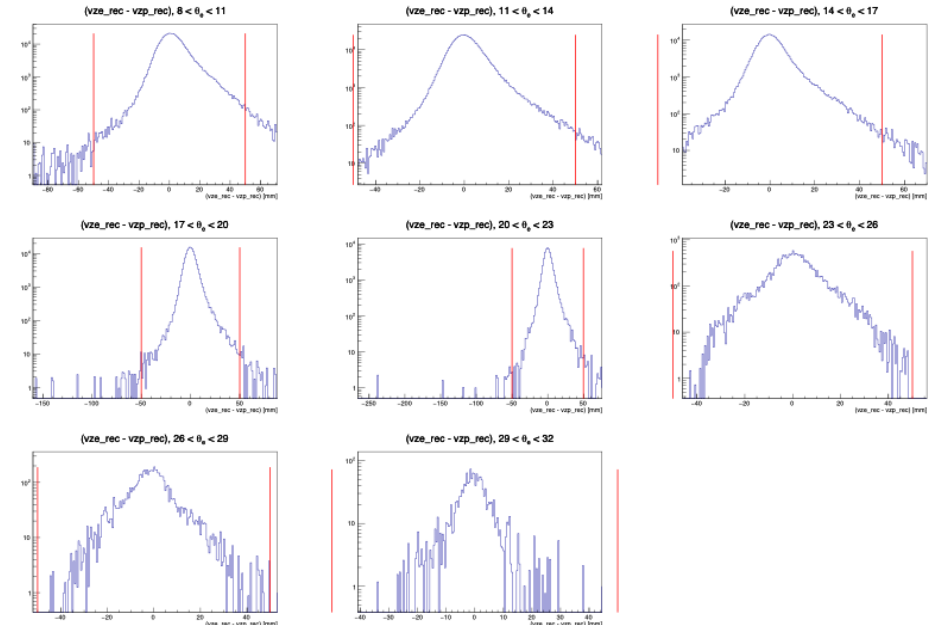
\rightarrow Correct yield for the cut efficiency

For **MC**, we had to use much wider Δv_z cuts (± 5 cm) due to distortion in tracking leading to mis-reconstructed θ_e and Δv_z .

\rightarrow Remaining inefficiency is small ($< 0.45\%$) but also corrected for.



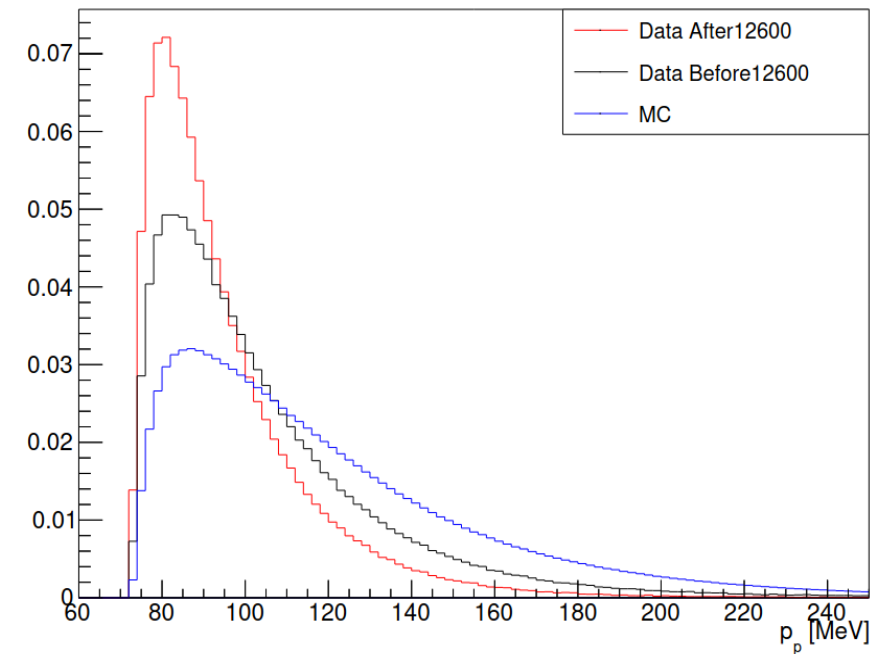
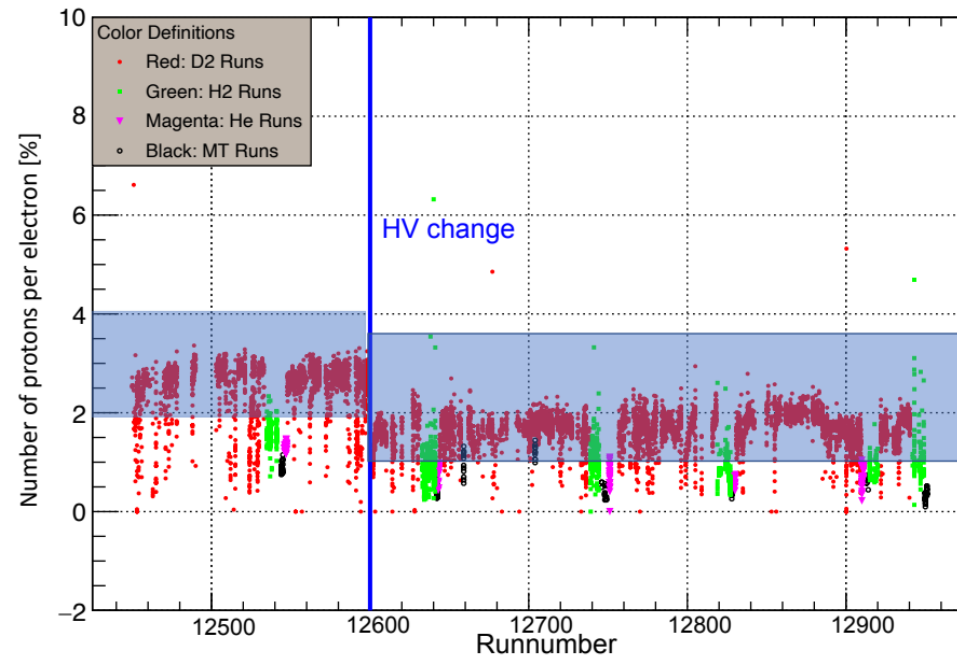
Δv_z in different θ_e bins



GEMs HV reduced of in RTPC after run 12600

In the middle of RGF-Summer2020 run, the RTPC GEMs HV were reduced from 385V to 375V.

This change has made the RTPC blinder to the high-energy recoils and more sensitive to the low-energy recoils of interest.

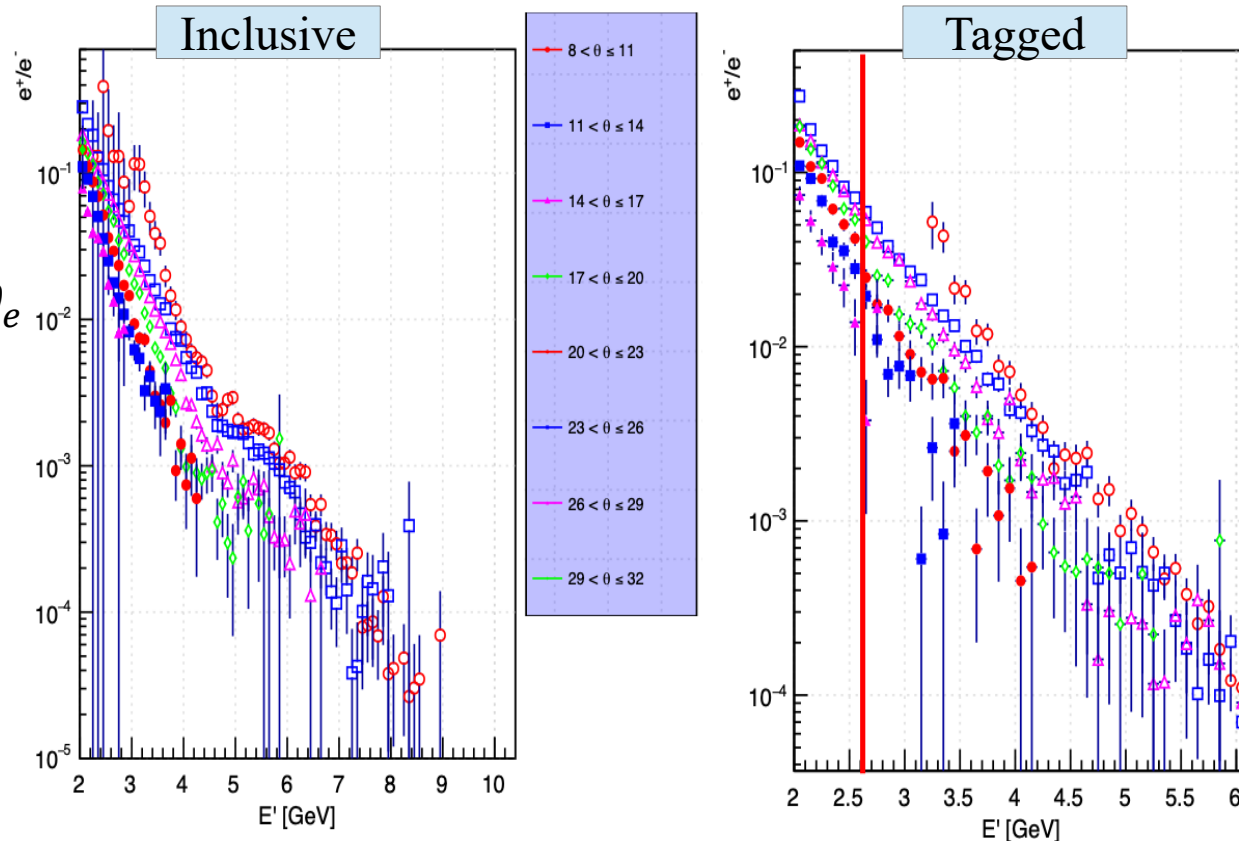
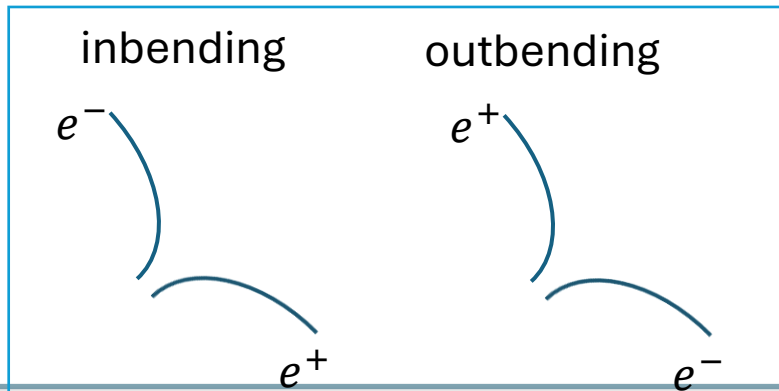


Background evaluation for experimental data — Pair Symmetric Background

There are still a number of events, but not the true ones, that passed the criteria as the background.

Electron

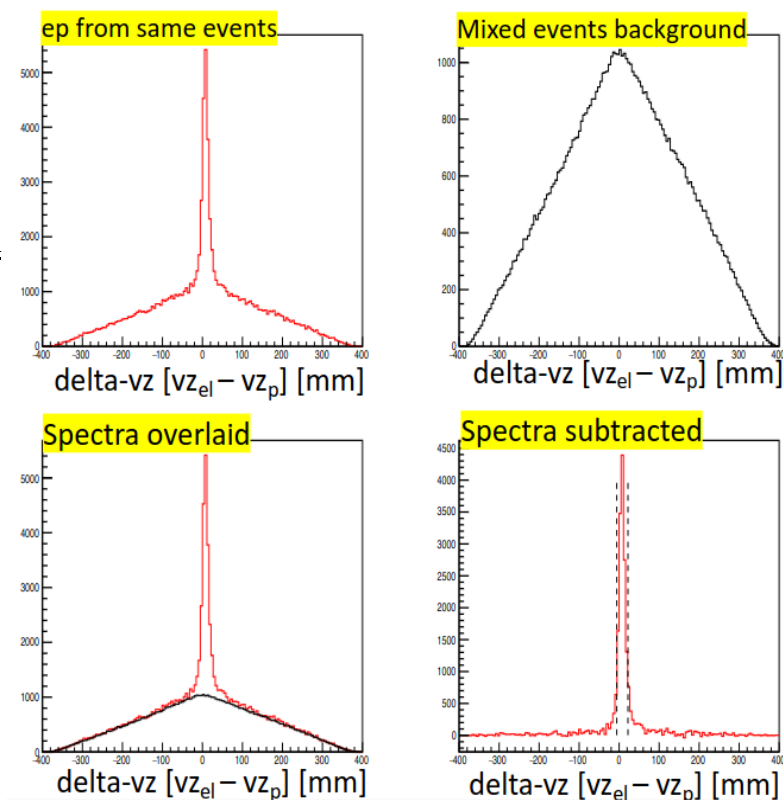
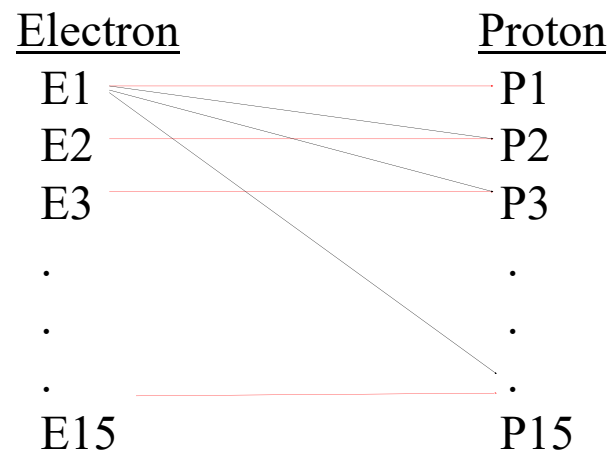
- Pair Symmetric Background: $\pi^0 \rightarrow e^+ e^- \gamma$
 - Secondary electron as trigger particle
 - Electron and positron have same behavior in the opposite direction of the magnetic field
 - Look at the ratio of the outbending position to the inbending electron $\frac{e^+}{e^-}$ as function of E' in different θ_e bins.
- $N_{e-,scattered} = N_{e-,measured} \left(1 - \frac{N_{e+,measured}}{N_{e-,measured}}\right)$



Background evaluation for experimental data — Accidentals

Proton

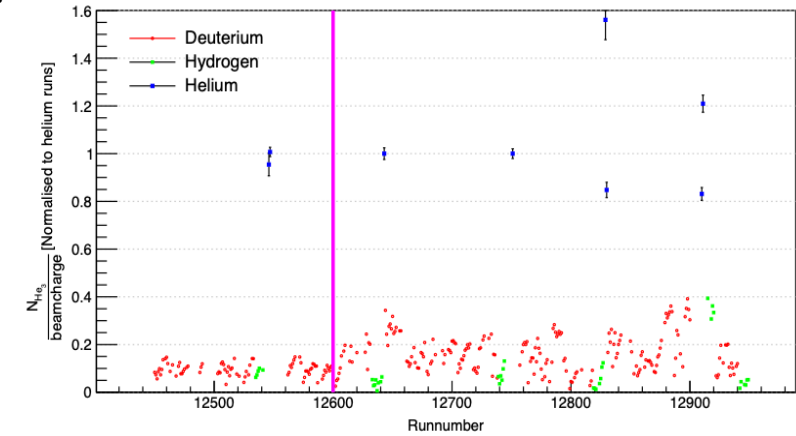
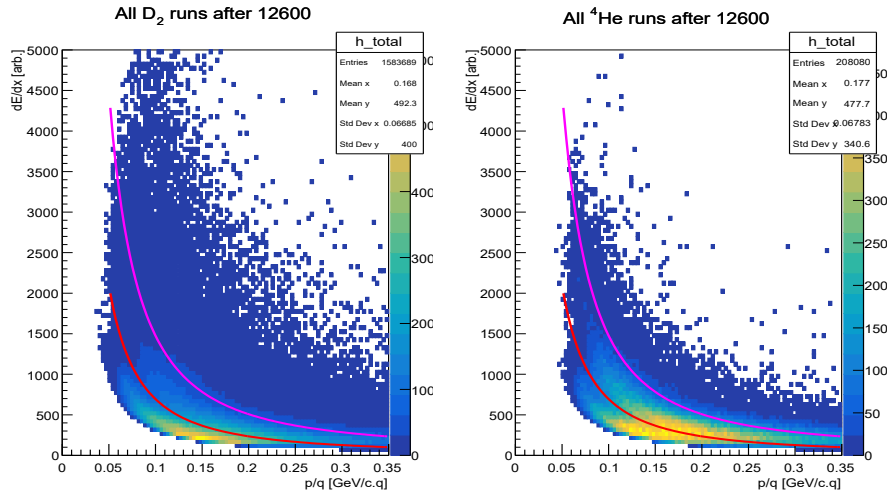
- Accidental Background
 - Due to ionization electron inside RTPC drift slowly, the coincidence cuts are wider
 - A significant number of accidental coincidence is included
- Procedure: For every **15 consecutive events** passing all selection criteria:
 - Perform event mixing and form 15x15 ep pairs
 - 15 ep pairs** [Red in fig.] from the same event
 - 210 combinatorics backgrounds** [Black in fig.].
 - Scale background count by **14**.



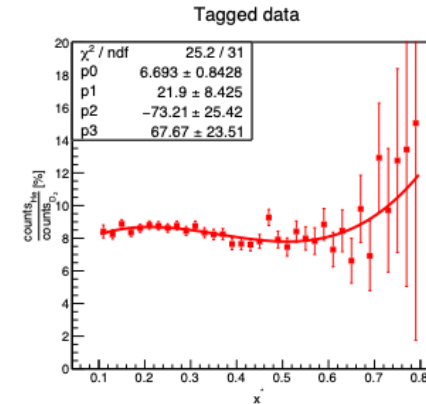
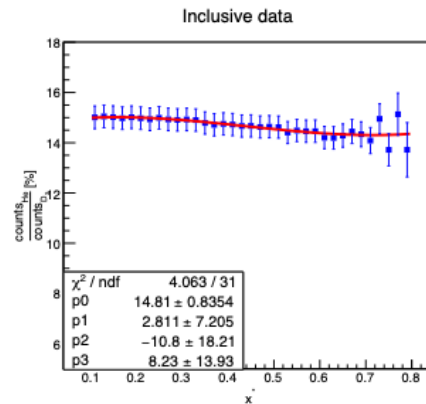
Background evaluation for experimental data — ^4He Contamination

Proton

- Deuterium Target Contamination
 - ^4He could diffuse into the target straw from the surrounding buffer gas region
 - Estimated using $^3\text{H}/^3\text{He}$ band in dE/dx vs. p/q from D_2 runs and ^4He runs.



- VIP fraction coming from ^4He corrected using polynomial fit.



Background evaluation for experimental data — “H Background”

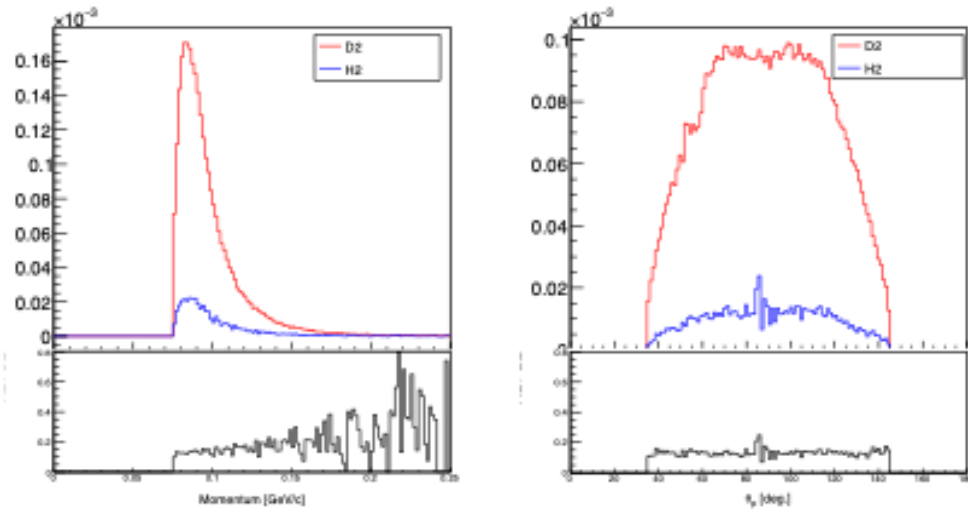
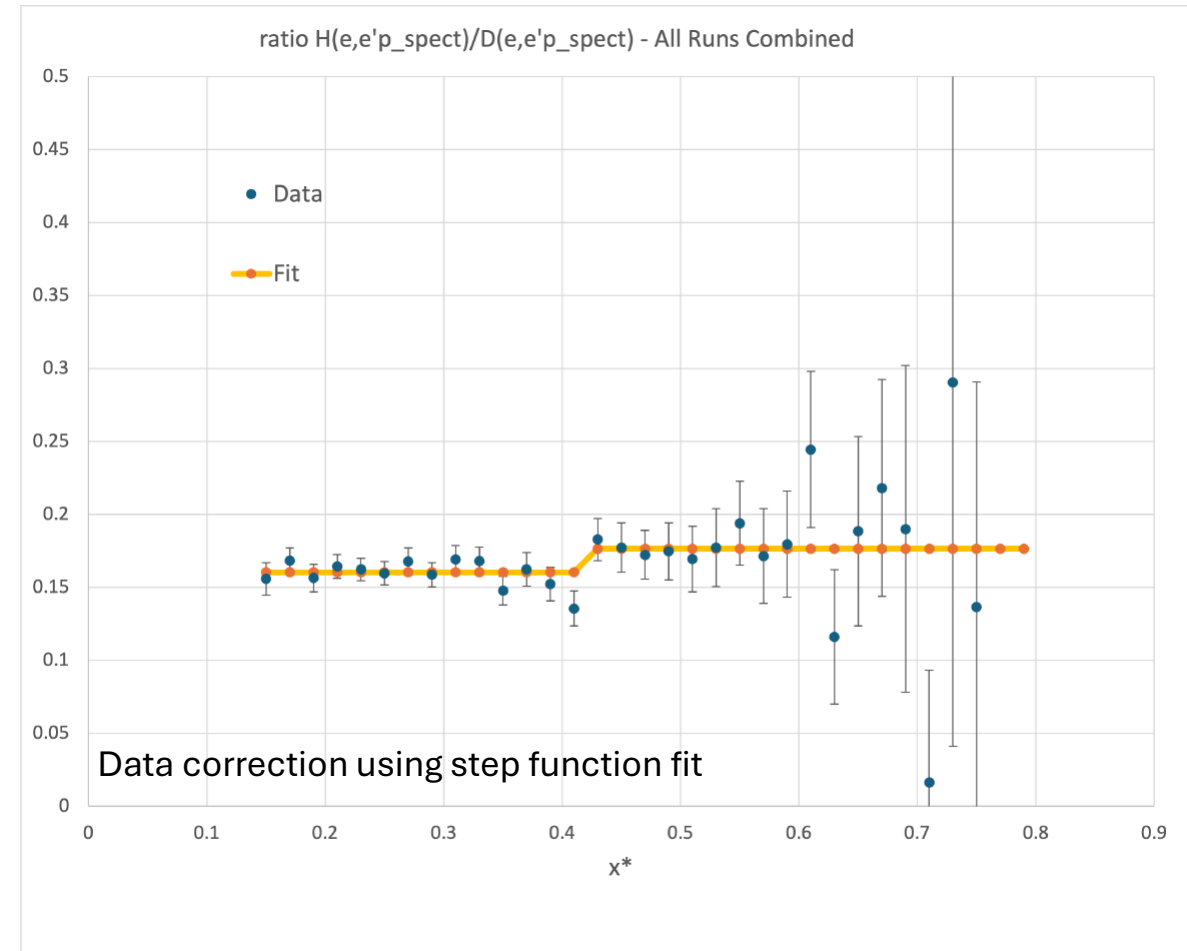


Figure 5.8: The distributions of momentum and θ_p for hydrogen and deuterium runs normalized to the beam charge after all backgrounds subtracted.

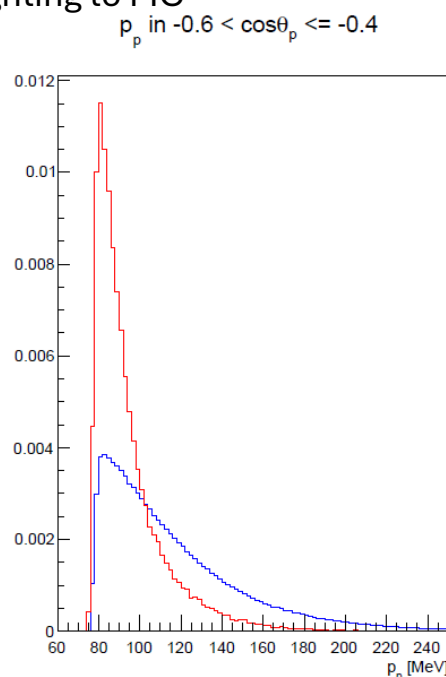


Momentum weighting on MC

Procedures

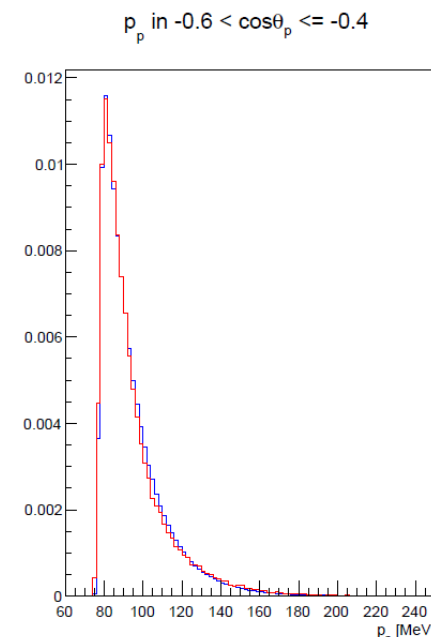
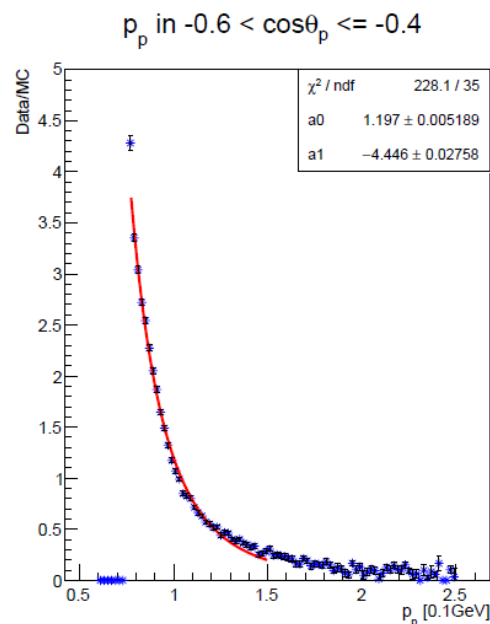
- Divided the tagged data in 10 $\cos \theta_p$ bins
- Calculate the Data/MC ratio, made plots as function of p
- Fit the Data/MC vs. p
- Extract the fitting parameters in the individual θ_p bins and fit them as a function of $\cos \theta_p$.
- Implement the weighting on MC to Match experimental data

Before weighting to MC



After weighting to MC

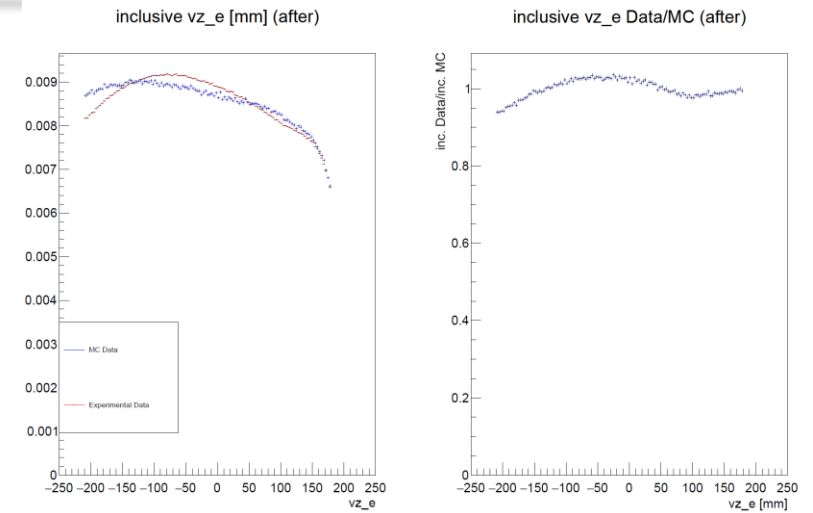
- MC. Data
- Experimental Data



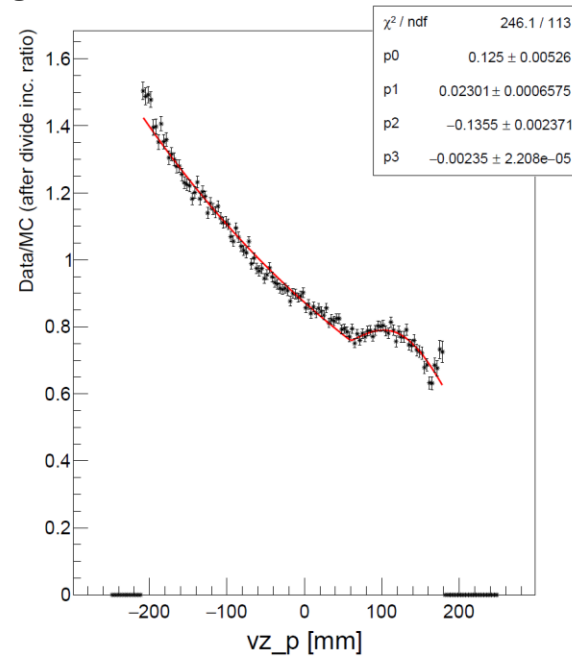
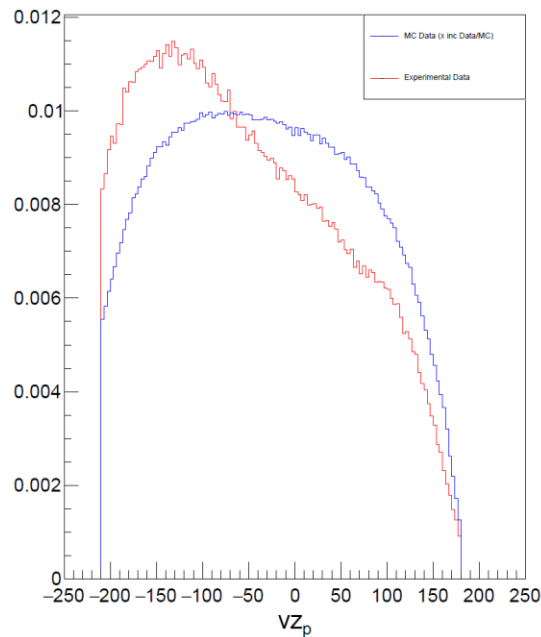
z-vertex weighting on MC

Procedures

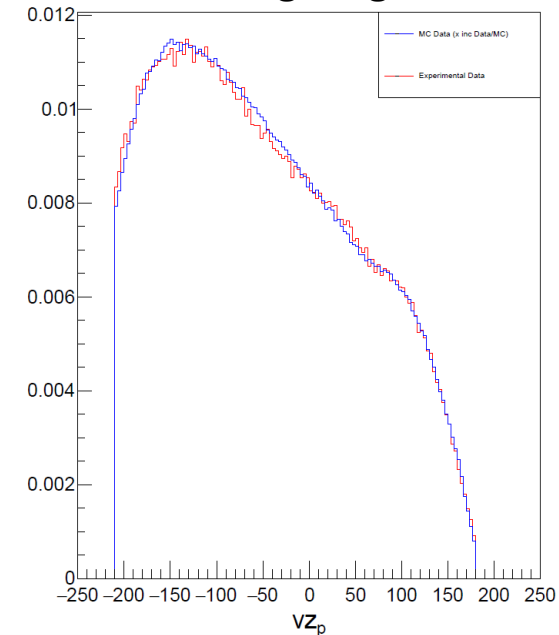
- Calculate the Data/MC ratio of νz_p , with eliminating the effect come from νz_e by dividing the inclusive νz_e ratio
- Fit the Data/MC vs. νz_p
- Parameterize the weight factor as a function of νz_p .



Before weighting to MC



After weighting to MC



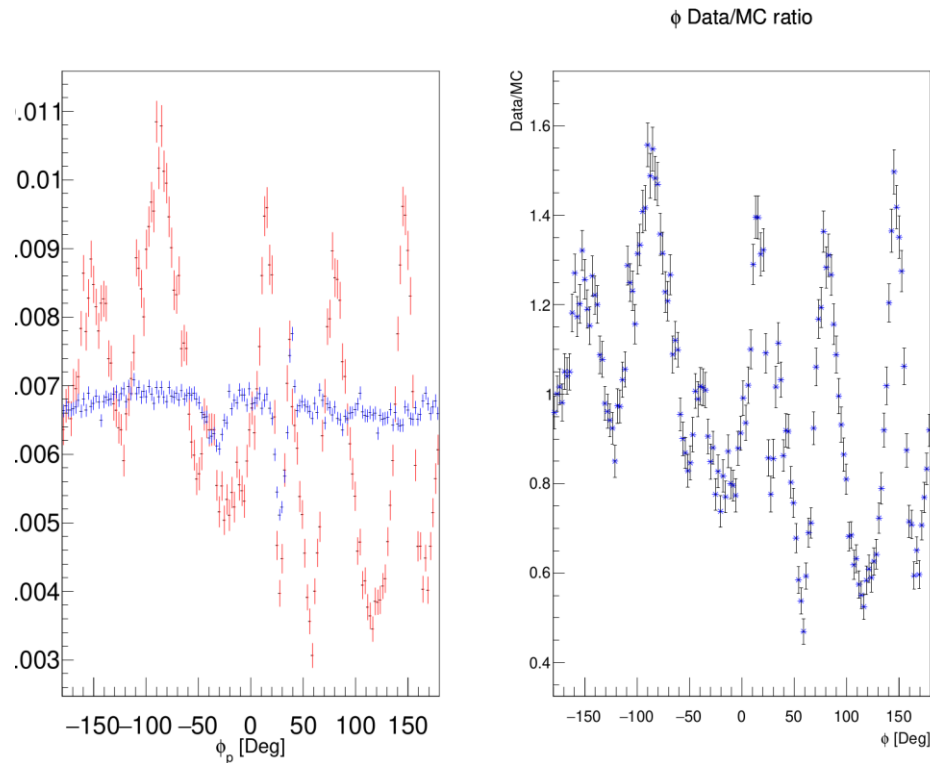
- MC. Data
- Experimental Data

ϕ_p weighting on MC

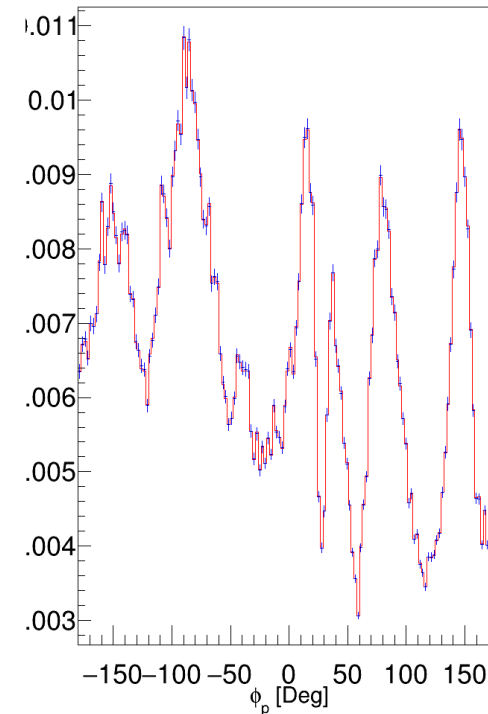
Procedures

- Calculate the Data/MC ratio for each bin from the histogram, made a table of the ratio in ϕ_p
- The weight factor is the ratio if ϕ_p is filled within that bin.

Before weighting to MC



After weighting to MC



- MC. Data
- Experimental Data