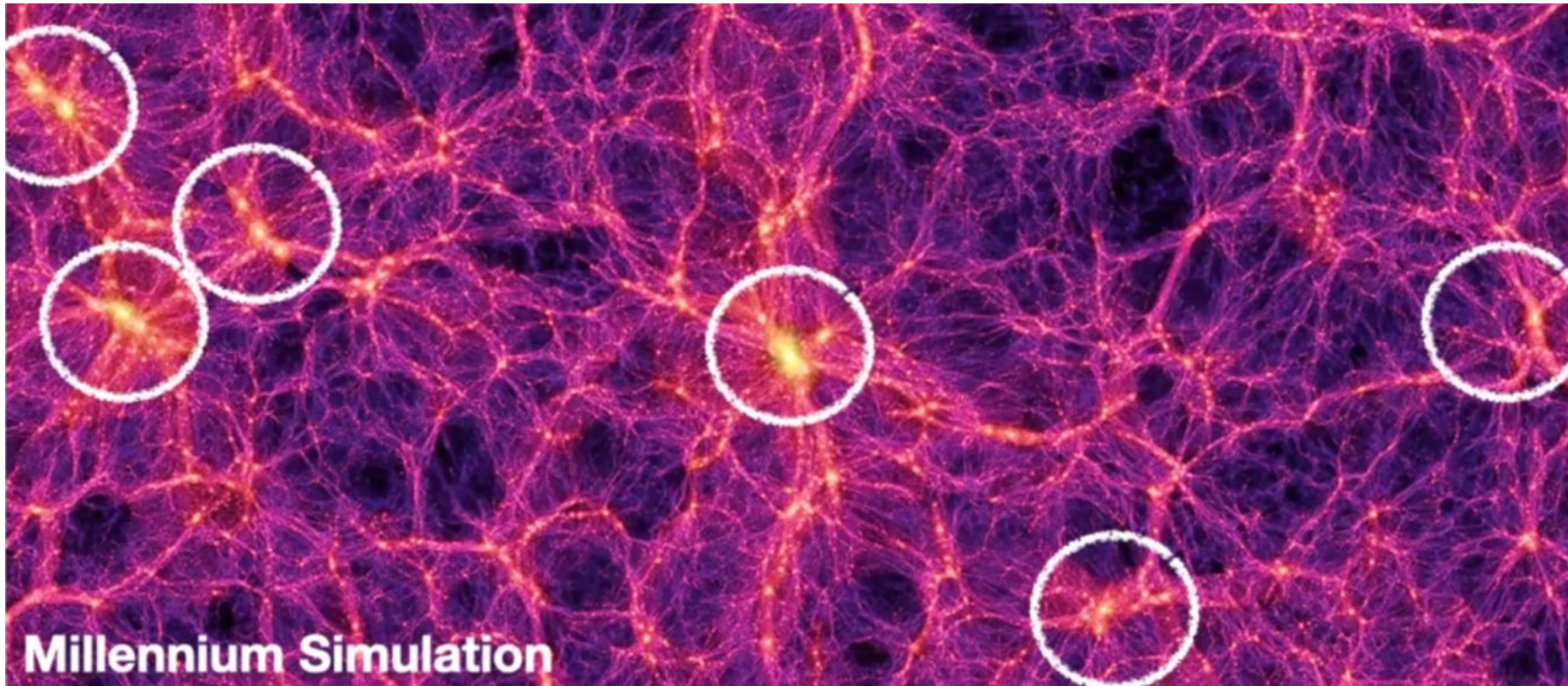


***Dark Matter and Baryons beyond
Equilibrium:
Cluster Outskirts and Infall***

Keiichi Umetsu (ASIAA)

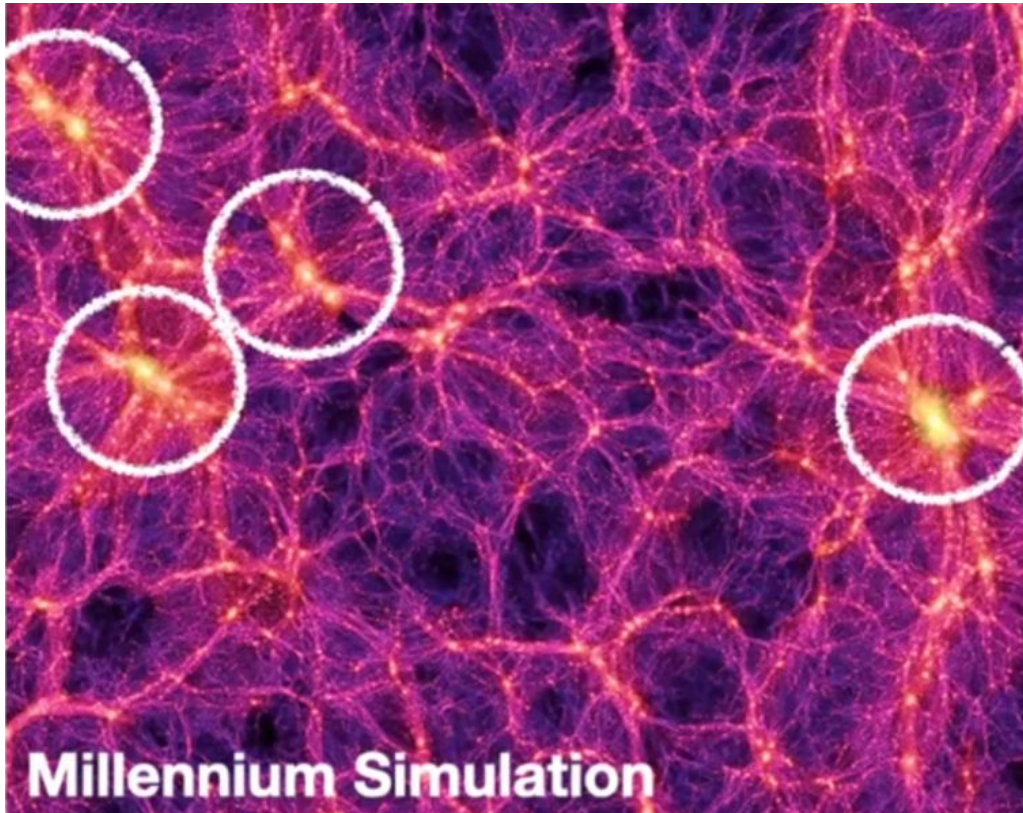
Cosmology and astrophysics with galaxy clusters

Galaxy clusters are massive cosmic-web nodes still growing under gravity

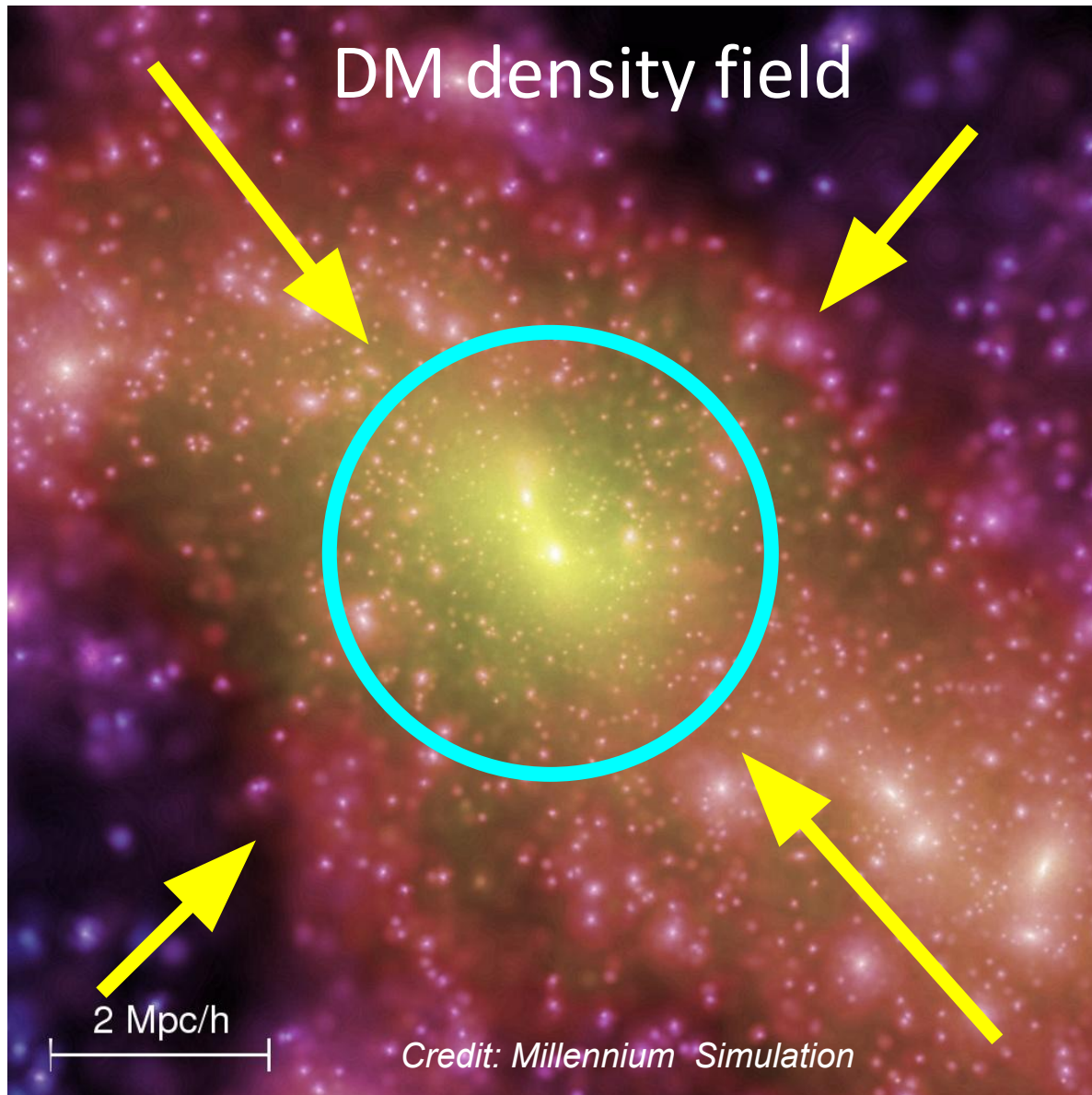


Cosmology and astrophysics with galaxy clusters

Galaxy clusters are massive cosmic-web nodes still growing under gravity



Cluster halo at a cosmic-web node

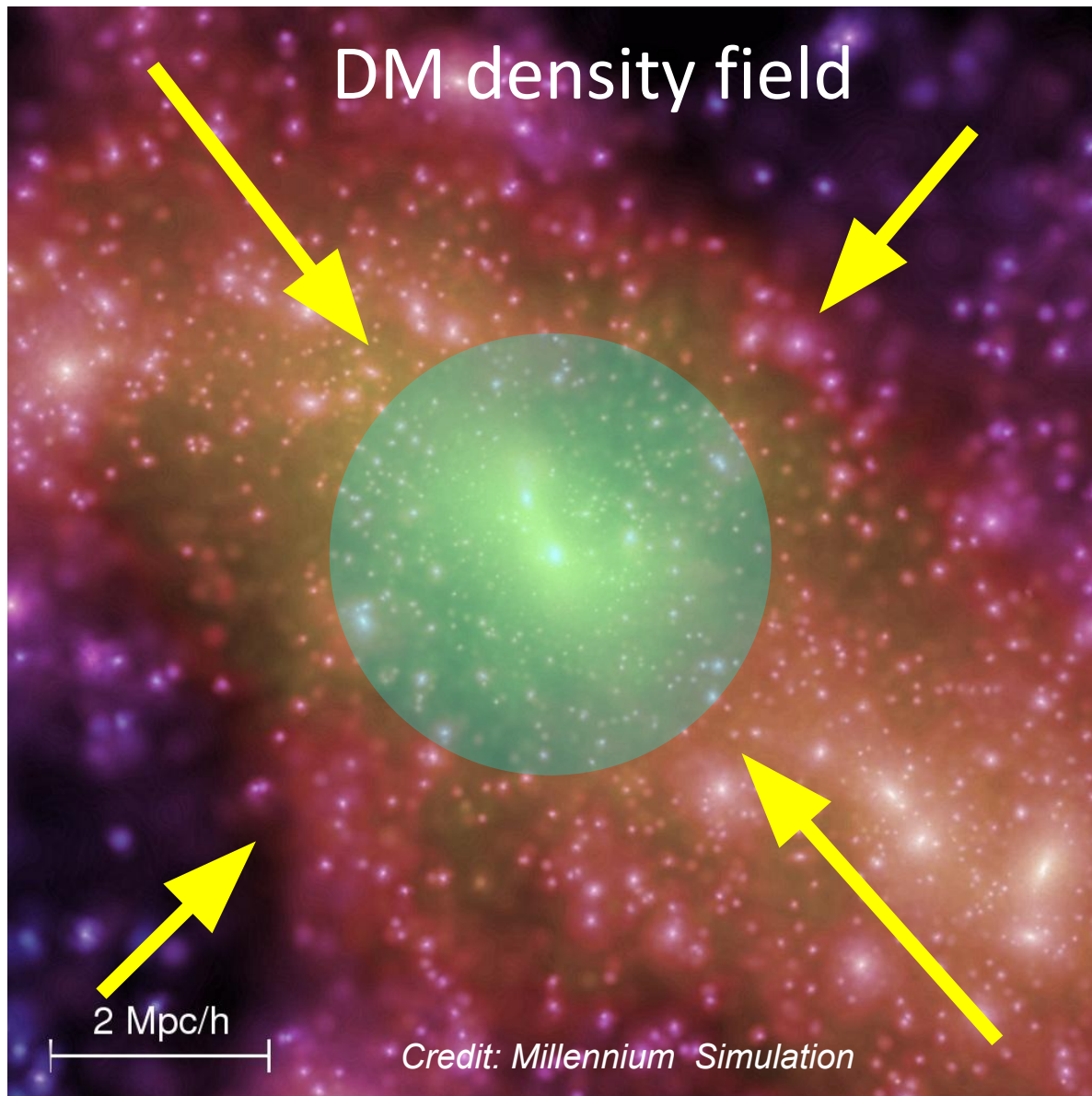


**Halo's dynamical
boundary @**
 $R_{sp} \approx 2 \text{ Mpc}/h$

Interior
= quasi-equilibrium

Exterior
= infall regions

Multi-tracers of the cluster potential



**Kinematic /
thermodynamic
tracers** (galaxies, gas)

$$U + 2T + \cancel{S} \simeq 0$$

$$U = \sum_i m_i \Phi(\mathbf{r}_i)$$

Geometric tracers
(weak lensing)

$$\nabla_i \nabla_j \psi = \kappa \delta_{ij} + \gamma_{ij}$$

$$\psi \propto \int \Phi_W(\mathbf{r}) dl$$

Cluster outskirts and infall: the nonlinear, non-equilibrium frontier

Outskirts are dynamically young and far from equilibrium.

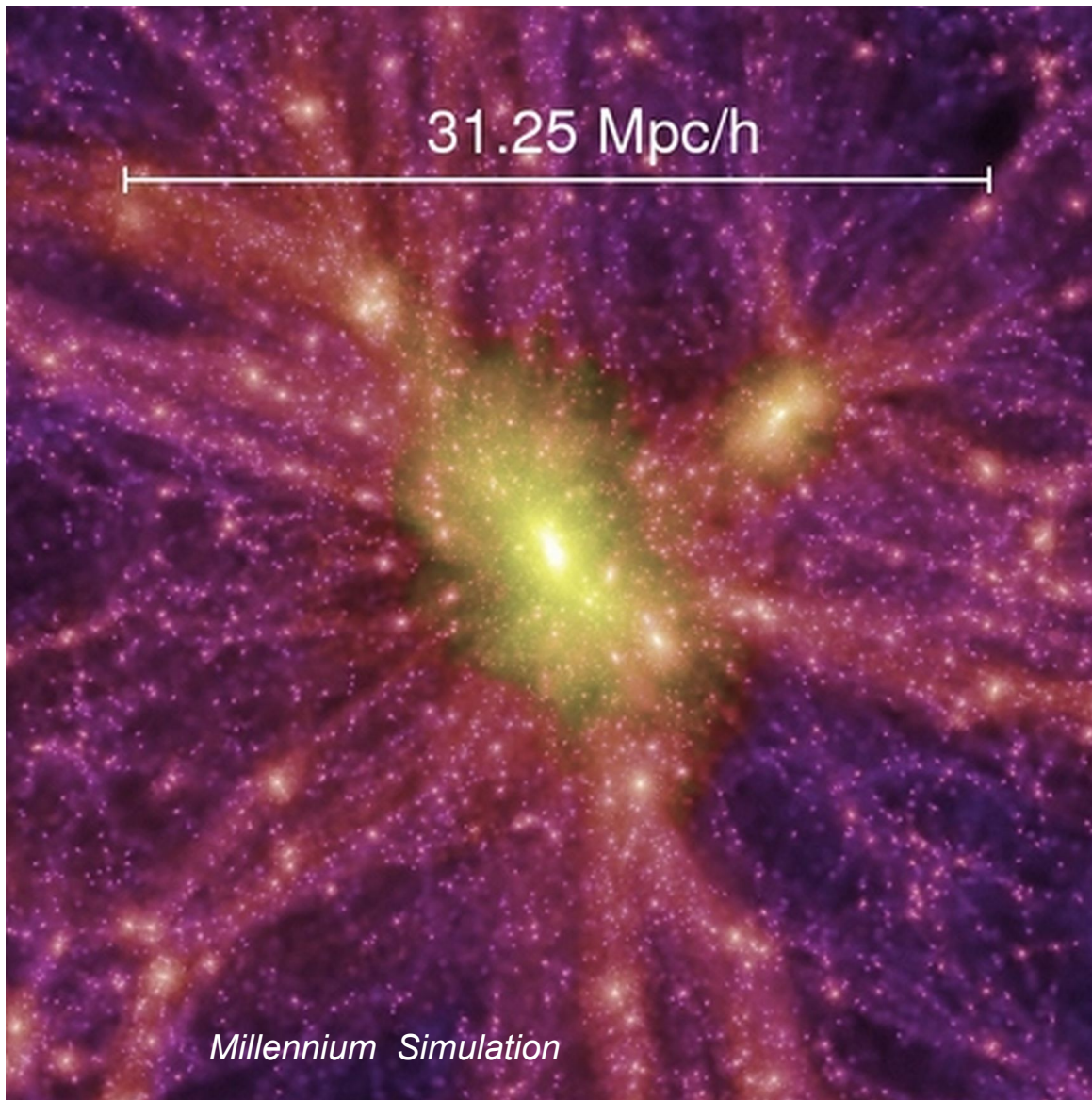
Maximum turnaround radius: $r_{\text{eq}} \approx 10 \text{ Mpc}/h$ at $z = 0$

Weak lensing

$$\nabla_i \nabla_j \psi = \kappa \delta_{ij} + \gamma_{ij}$$

Phase-space kinematics

$$v_{\text{esc}}^2 = -2 [\Phi(r) - \Phi(r_{\text{eq}})] - qH^2(r^2 - r_{\text{eq}}^2)$$



Key questions:

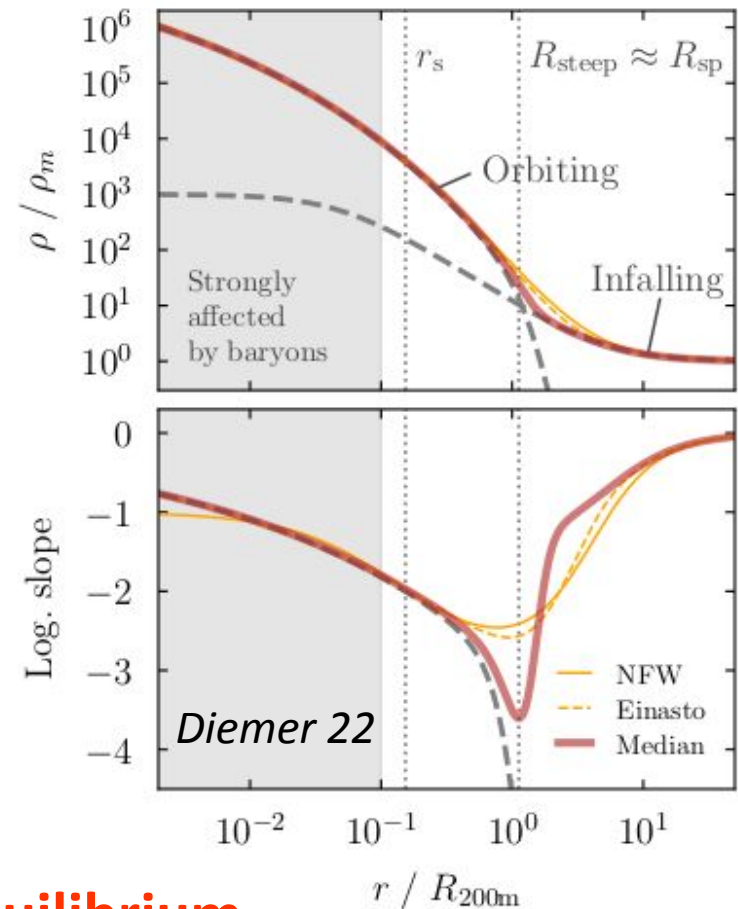
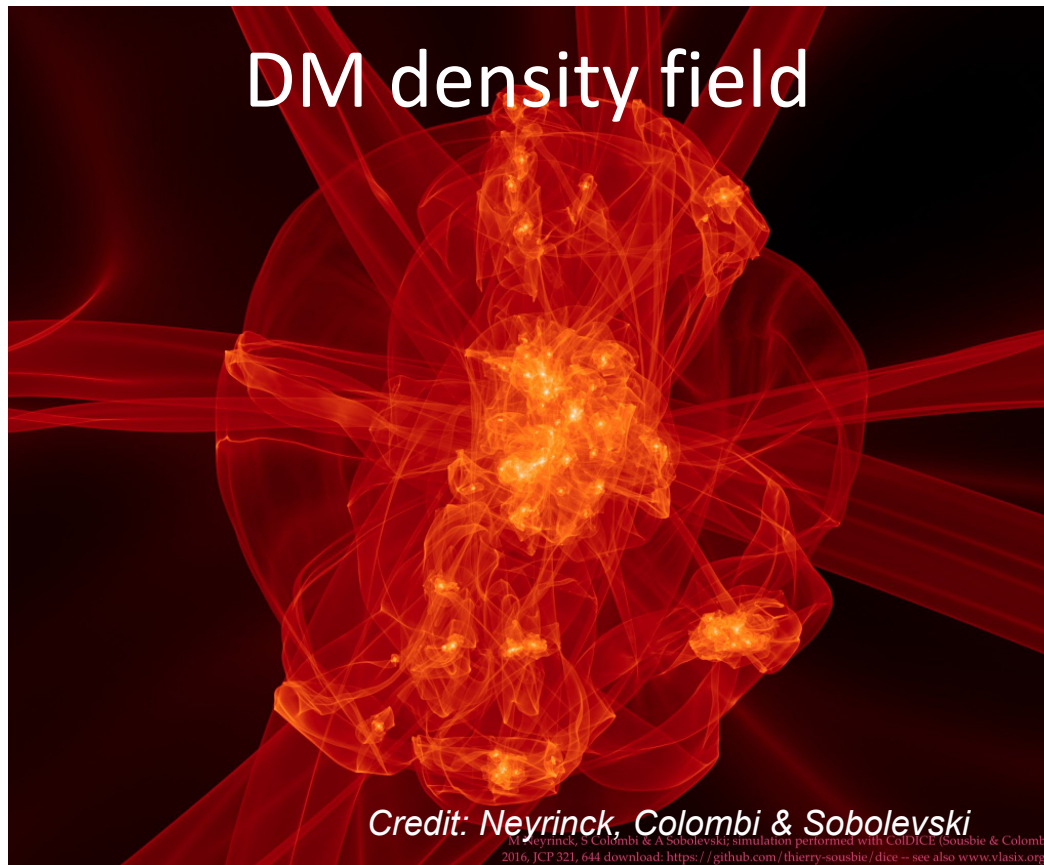
DM and baryons beyond equilibrium

- **How does matter flow from the cosmic web into massive halos?**
 - Reveals how halos grow and evolve in the nonlinear regime.
- **How do dark matter and diffuse baryons respond differently to gravity?**
 - Their mass and velocity structure is key to probing the nature of DM and gravity.
- **Where do the boundaries of collisionless and collisional matter emerge?**
 - Identifies the dynamical (splashback) and hydrodynamic (accretion shock) edges of halos.

Non-equilibrium structure formation on megaparsec scales



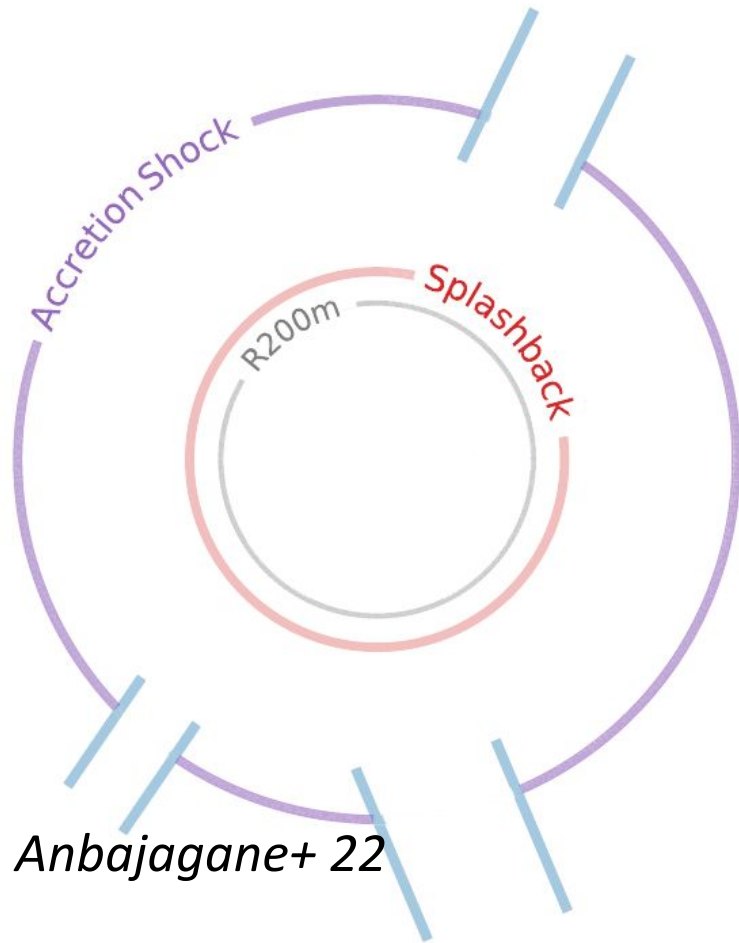
Dynamical halo boundary: splashback radius



Gravitational potential tracers beyond equilibrium

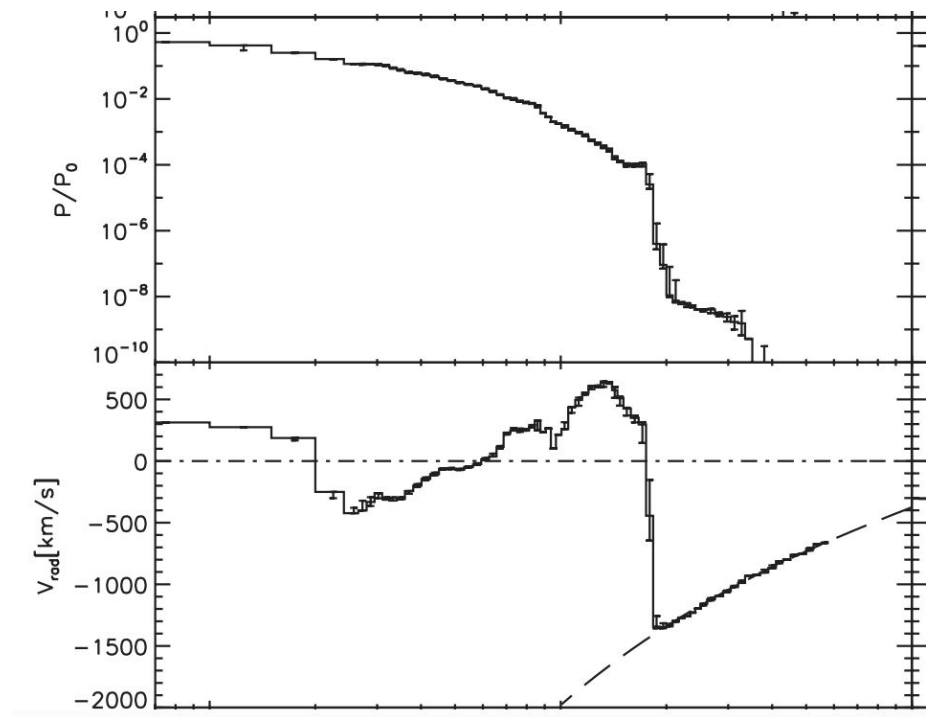
- Gravitational lensing (e.g., Umetsu & Diemer 2017)
- Escape velocity from phase-space galaxy kinematics (Pizzardo+ 2024)
- CLUMI+: joint weak lensing + escape velocity (Umetsu, Pizzardo+ 2025)

Hydrodynamic halo boundary: accretion shock radius



tSZ + kSZ $\rightarrow$ pressure & momentum
diagnostics across the shock

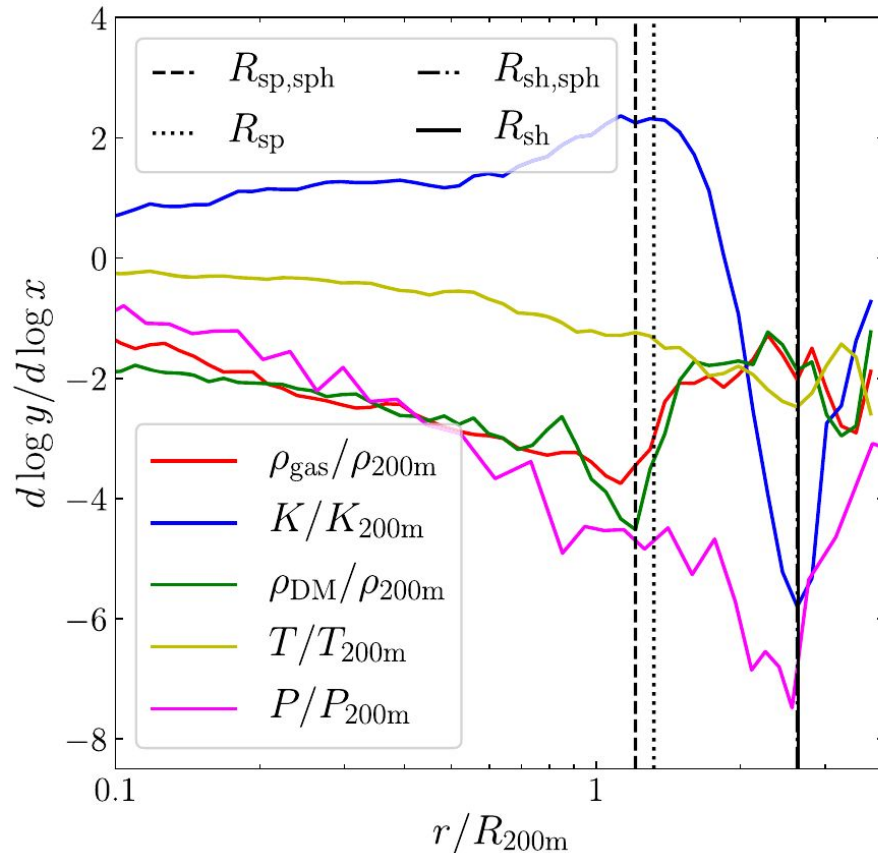
Pressure & velocity jumps at $r \approx 2 R_{sp}$
(Molnar+10, Lau+15, Avestruz+15, Shi 16)



Cosmological hydro simulations
(off-filament directions) by Molnar+10

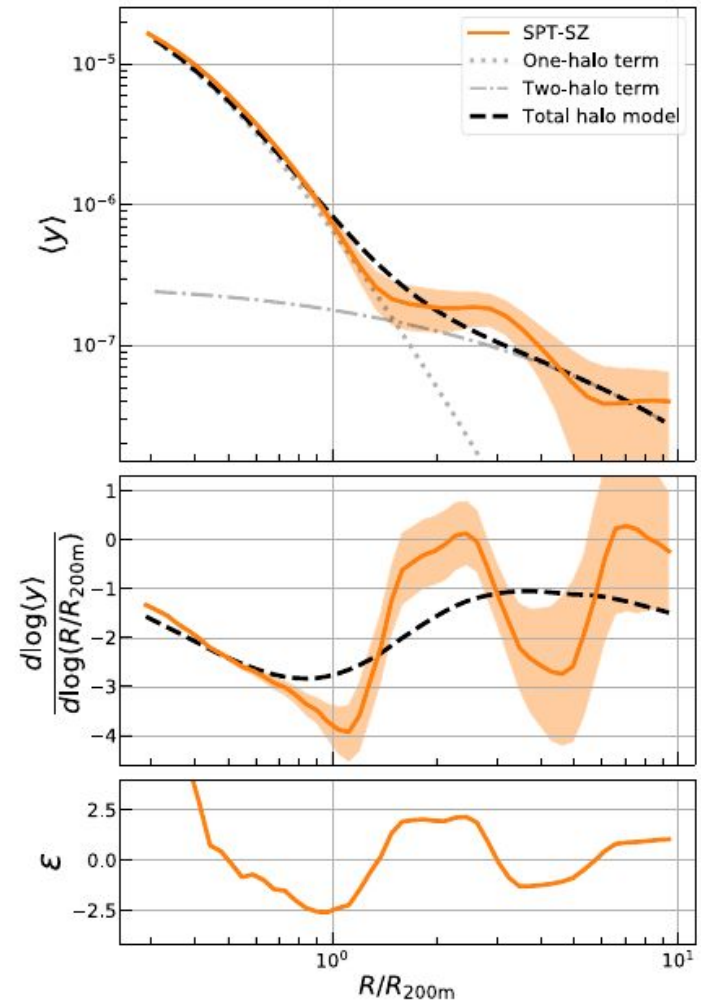
Simulations vs. current measurements

Zoom-in cosmological hydro simulations (65 clusters)



Aung, Nagai, & Lau 21

SPT + Planck tSZ (516 clusters)



Anbajagane+ 22

Non-equilibrium cluster outskirts with SO+

Weak lensing +
phase-space to anchor
the underlying potential

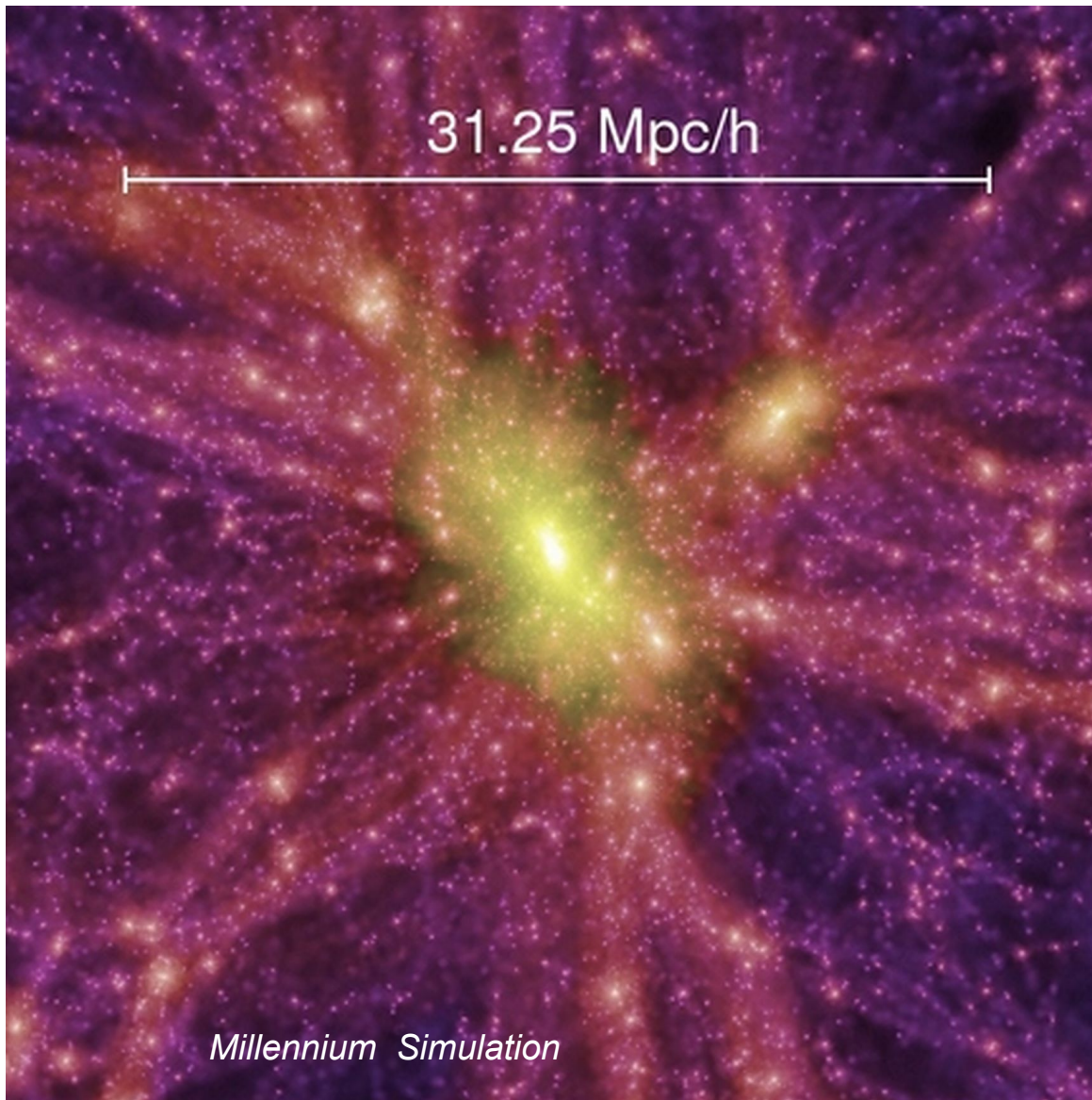
$$\nabla_i \nabla_j \psi = \kappa \delta_{ij} + \gamma_{ij}$$

$$v_{\text{esc}}^2 = -2 [\Phi(r) - \Phi(r_{\text{eq}}) - qH^2(r^2 - r_{\text{eq}}^2)]$$

Thermal and kinetic SZ
signals in the CMB

$$y \propto \int P_e dl$$

$$\frac{\Delta T_{\text{kSZ}}}{T_{\text{CMB}}} = - \int \frac{v_{\parallel}}{c} d\tau_e$$



Key objectives with SO+ (initial ideas)

Case A: Dark matter vs. gas boundaries

- WL + redshifts (CLUMI+) measures the collisionless boundary (splashback).
- SO's tSZ (thermal pressure) + kSZ (LOS momentum) measures the collisional boundary (accretion shock).
- Combining tSZ and kSZ + redshifts yields the radial entropy profile, whose jump is a robust signature of the shock.

Case B: Infall kinematics in the transition region

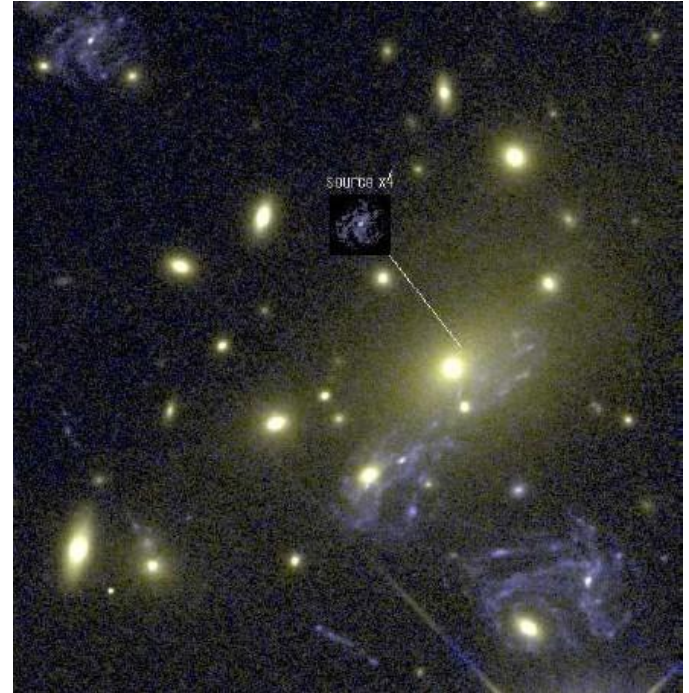
- Compare collisionless infall velocities (from CLUMI+) with LOS electron momentum (from velocity-weighted cluster–satellite kSZ) to study where and how gas slows relative to the collisionless infall flow.

Weak lensing in galaxy clusters

Shape distortions (shear)



Magnification



- **Gravitational shear**
 - ✓ Shape distortion: $\delta e \sim \gamma$
- **Magnification bias**
 - ✓ Flux amplification: μF
 - ✓ Area distortion: $\mu \Delta\Omega$

Sensitive to “excess” mass density

$$\Sigma_{\text{cr}} \gamma_{+} = \Delta \Sigma(r_{\perp}) \equiv \Sigma(< r_{\perp}) - \Sigma(r_{\perp})$$

Sensitive to “total” matter density

$$\mu \simeq 1 + 2\kappa; \quad \Sigma_{\text{cr}} \kappa = \Sigma(r_{\perp})$$