

Antideuteron Analysis

(Velocity Reconstruction with Deep Learning)

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RICH Velocity Reconstruction with Deep Learning (Old Version)

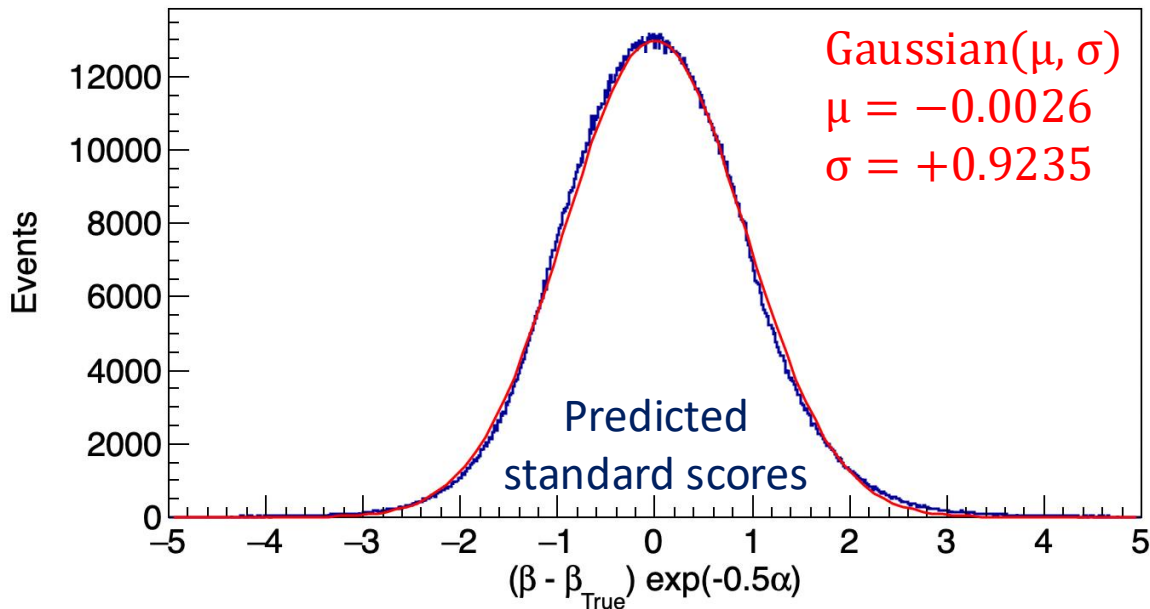
Inputs: hit information + others

Outputs:

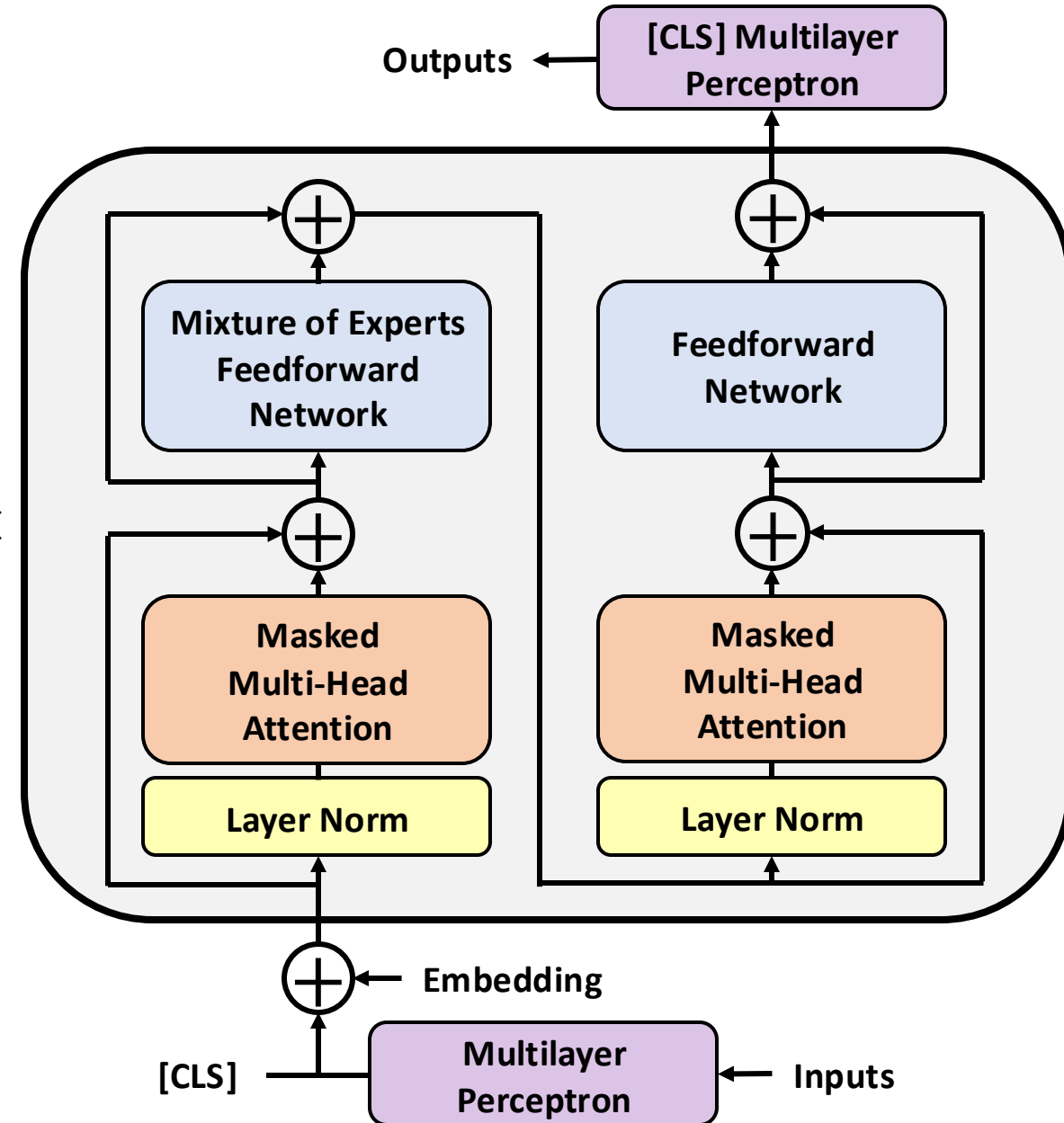
- 1) β , predicted velocity
- 2) $\alpha = \ln \sigma^2$, predicted velocity log variance (uncertainty)

Heteroscedastic Loss (Gaussian Negative Log-Likelihood):

$$\mathcal{L} = \frac{1}{N} \sum \left[(\beta_i - \beta_{i,\text{True}})^2 e^{-\alpha_i} + \alpha_i \right]$$



$L \times$



Length of Sequence:

- Inputs N = 512
- Latents M = 8
- Outputs
 - 1) Gaussian Q = 2
 - 2) Student's t Q = 3

Number of Layers:

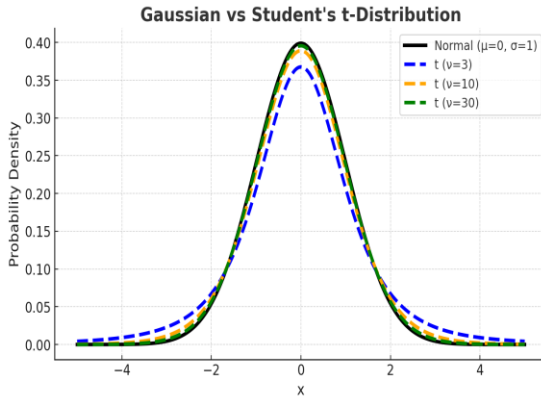
- L = 3

Number of Experts:

- E = 8

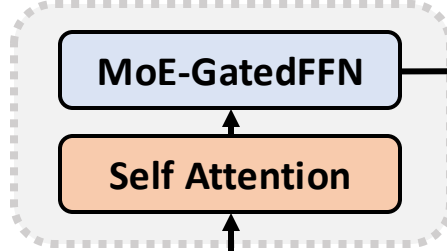
Hidden Dimension:

- D = 256

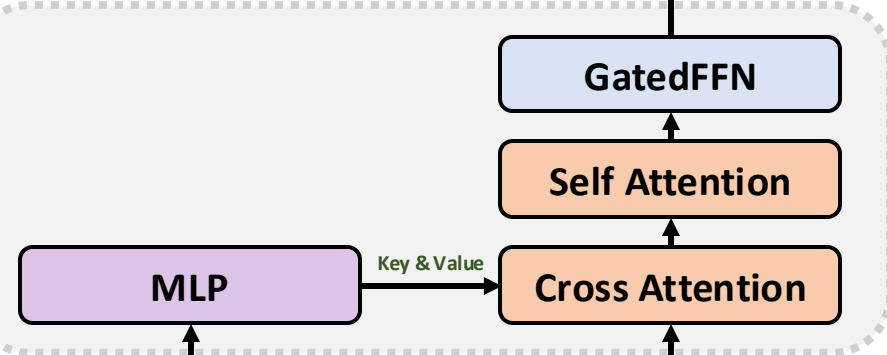


Latent Transformer

L
×

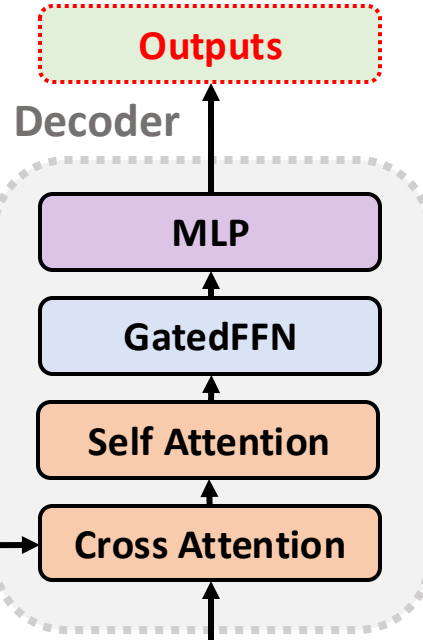


Encoder



length of sequence = N
(Maximum Number of Hits)

Latents (Query)
length of sequence = M
(M << N)



Outputs (Query)
length of sequence = Q
(Q ≤ M)

Outputs

Physical Variable Reconstruction with Deep Learning

- Inputs:**
hit relation information
- Outputs:**
 - Gaussian Distribution
 - 1) β_G , predicted mean
 - 2) $\alpha_G = \ln \sigma^2$, predicted log variance (uncertainty)
 - Student's t Distribution
 - 1) β_T , predicted mean
 - 2) $\alpha_T = \ln \sigma^2$, predicted log variance (uncertainty)
 - 3) $\gamma_T = \ln v$, predicted tail heaviness (robustness to outliers)

Physics-informed Objective Function:

Gaussian NLL

$$\mathcal{L}_G = -\frac{2}{N} \sum \ln p_{G,i} = \frac{1}{N} \sum (C_{G,i} + E_{G,i})$$

$$C_G = \ln 2\pi + \alpha_G$$

$$E_G = (\beta_G - \beta_{\text{True}})^2 e^{-\alpha_G}$$

$$p_G = (2\pi \cdot e^{\alpha_G})^{-1/2} \cdot e^{(-1/2) \cdot (\beta_G - \beta_{\text{True}})^2 e^{-\alpha_G}}$$

Student's t NLL

$$\mathcal{L}_T = -\frac{2}{N} \sum \ln p_{T,i} = \frac{1}{N} \sum (C_{T,i} + E_{T,i})$$

$$C_T = 2 \cdot [\ln \Gamma(e^{\gamma_T}/2) - \ln \Gamma((1 + e^{\gamma_T})/2)] + (\ln \pi + \alpha_T + \gamma_T)$$

$$E_T = (1 + e^{\gamma_T}) \cdot \ln[1 + (\beta_T - \beta_{\text{True}})^2 e^{-(\alpha_T + \gamma_T)}]$$

$$p_T = \frac{\Gamma((1 + e^{\gamma_T})/2)}{\Gamma(e^{\gamma_T}/2)} (\pi \cdot e^{\alpha_T + \gamma_T})^{-1/2} [1 + (\beta_T - \beta_{\text{True}})^2 e^{-(\alpha_T + \gamma_T)}]^{-(1 + e^{\gamma_T})/2}$$

p_T follows a Gaussian distribution when $\gamma_T \rightarrow \infty$

$$\text{Distribution Variance} = \begin{cases} e^{\alpha_T + \gamma_T} / (e^{\gamma_T} - 2) & , \gamma_T > \ln 2 \\ \infty & , 0 < \gamma_T \leq \ln 2 \\ \text{undefined} & , \gamma_T \leq 0 \end{cases}$$

