

Experimental approach to observe wide-band Stochastic Gravitational Wave Background

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Taiwan-LIGO instrumentation group

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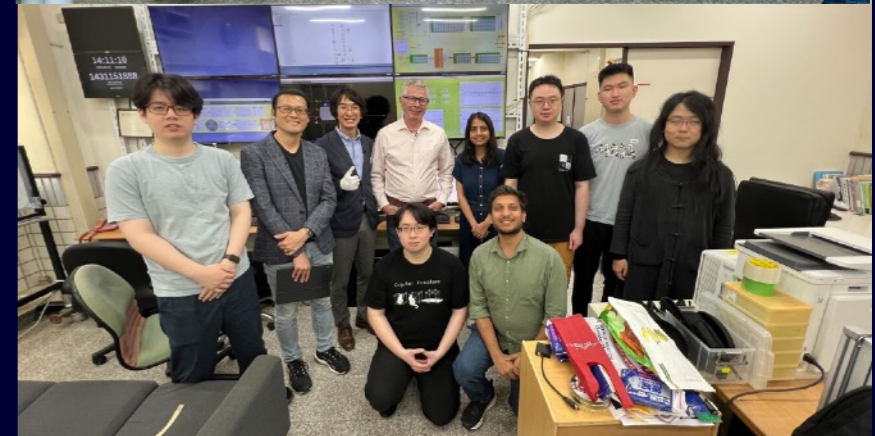
University of Philippine, Diliman

Mario Organo

NCU-CMB group (from 2025 April)

National Central University

Yuki Inoue
Masashi Hazumi



Calibration Analysis

Data analysis and pipeline development for Ongoing Observation

Core-Optics R&D

R&D for the new technology of GW with Taiwan semiconductor technology

Experimental Cosmology

Landscape of Gravitational wave stochastic background study with GW and CMB data

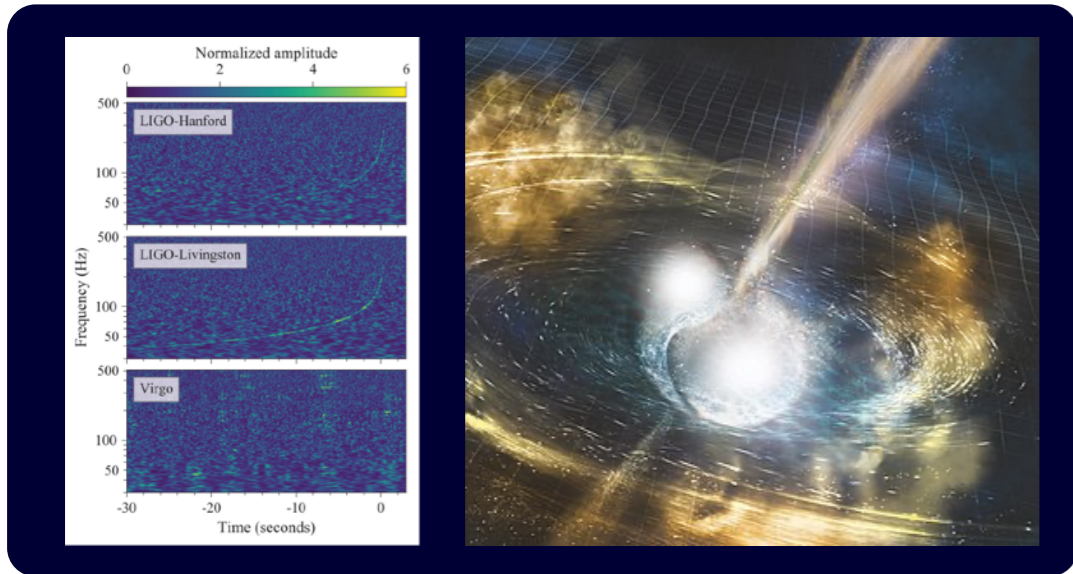
13 staffs and students join our group

Outline

- Introduction
 - Science
 - Project Overview
 - Schedule
 - Summary
-

Introduction

10 years anniversary from the first detection of Gravitational wave



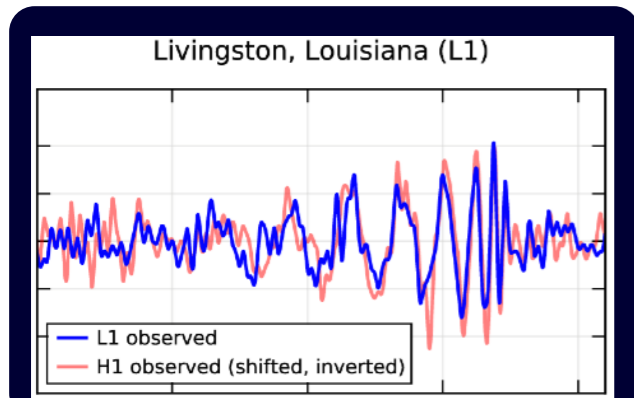
Main topics

2025 Aug. 04-a Data release

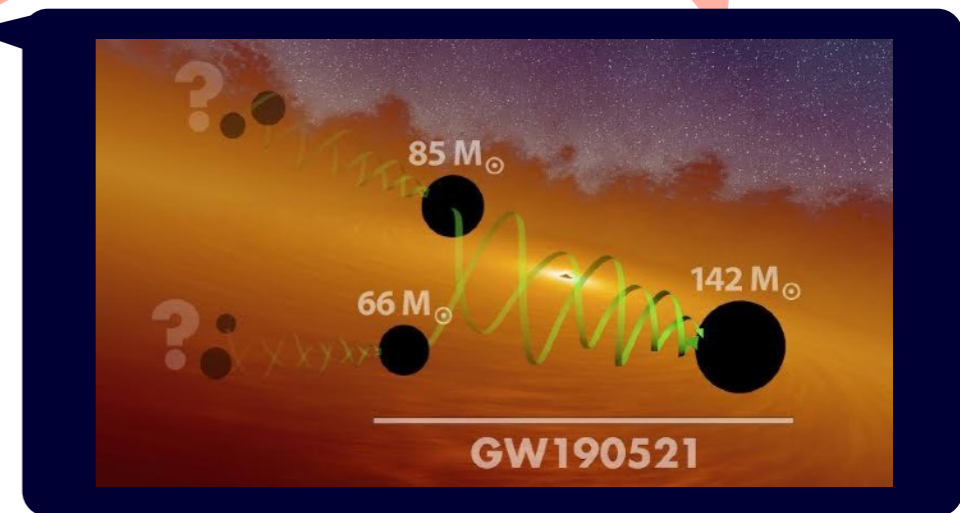
2023 May.24 Observation 4 start

2019 May. 21 IMBH

2017 Aug. 17 BNS



2015 Sep.14 The first detection



Introduction

10 years anniversary from the first detection of Gravitational wave

Main message of This talk!

OX = Observation X

Previous works

O1, O2, O3

The first detection era!

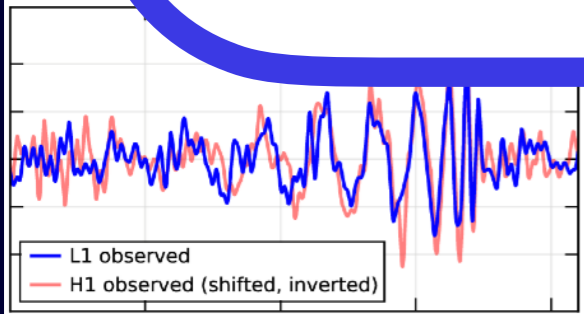
~400 events

This Talk!

O4

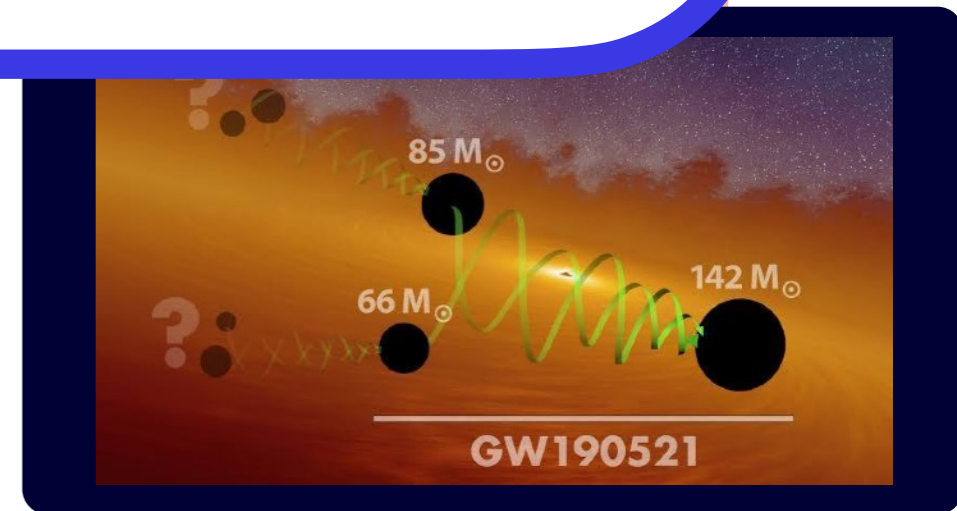
The statistical evaluation era!

It's kind of phase transition to new era of GW observation!

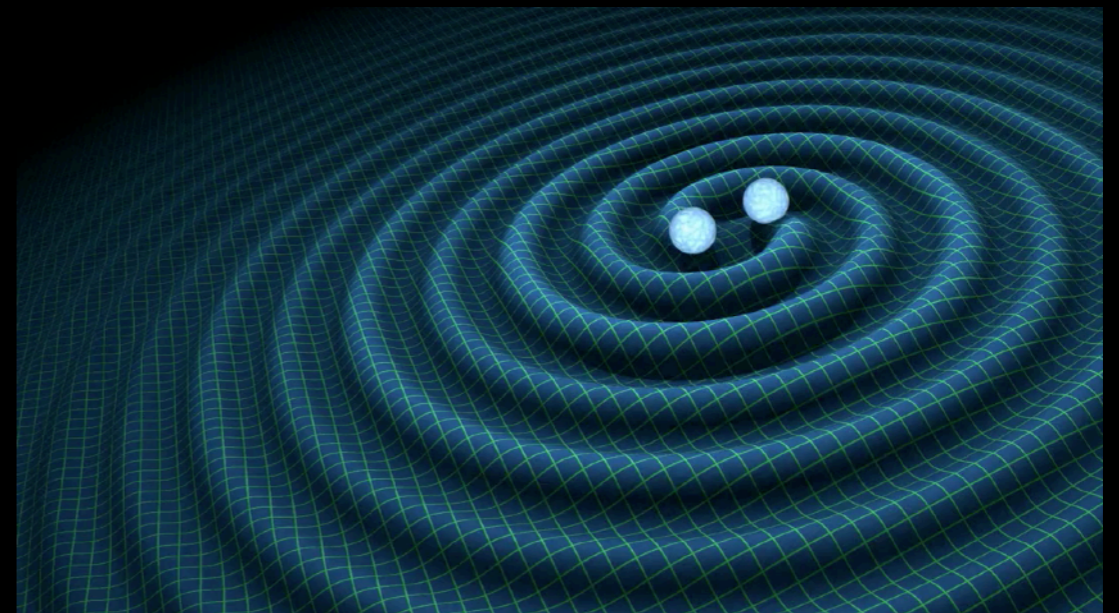
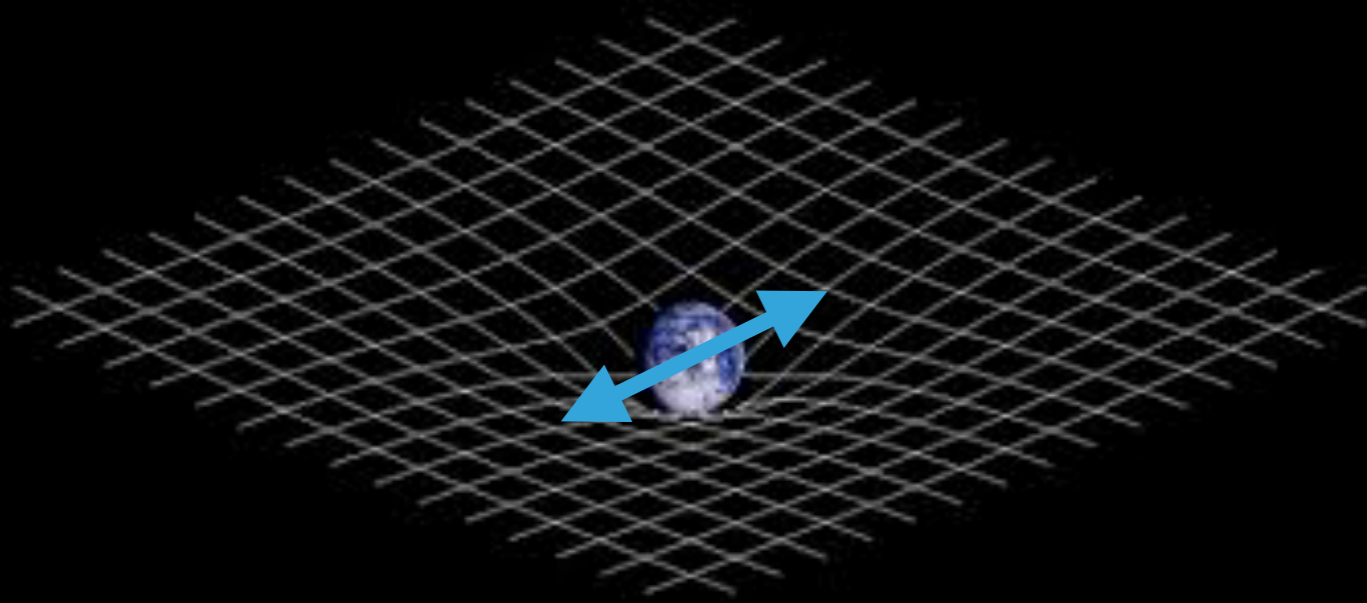


2017 Aug. 17 BNS

2015 Sep.14 The first detection



How to generate Gravitational Waves



- Science target is observation of gravitational waves.
- GW is generated by the oscillation of the massive object.

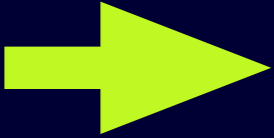
Metric

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu$$

Metric

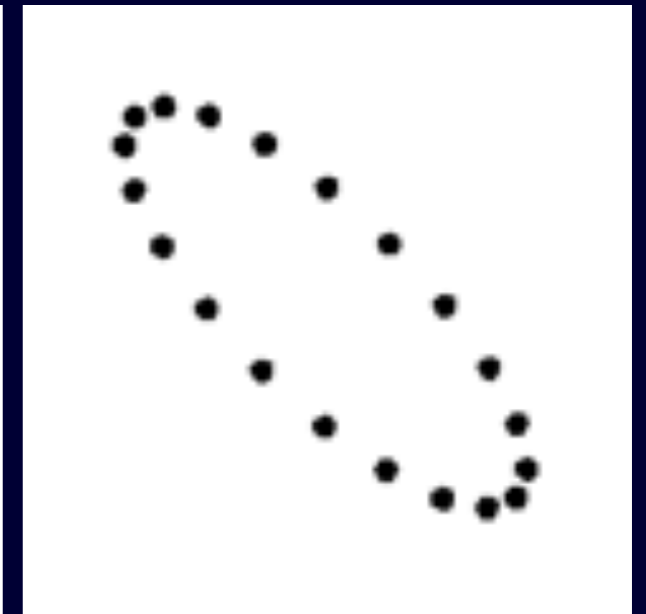
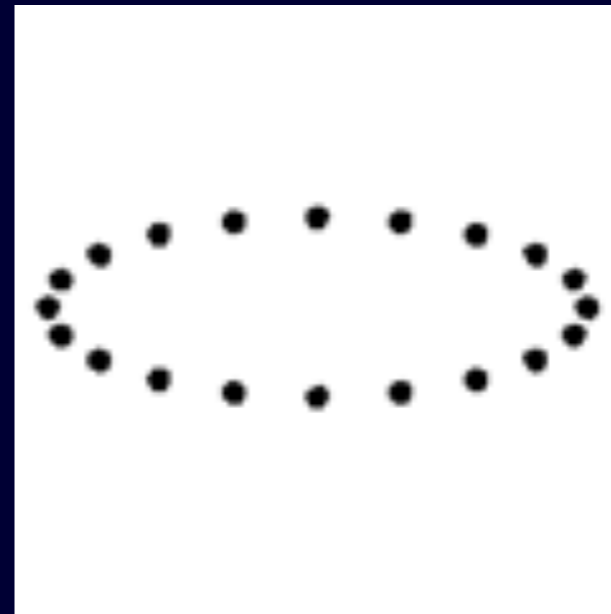
$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

Perturbation


$$\left(\frac{\partial^2}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2}{\partial t^2} \right) h = 0$$

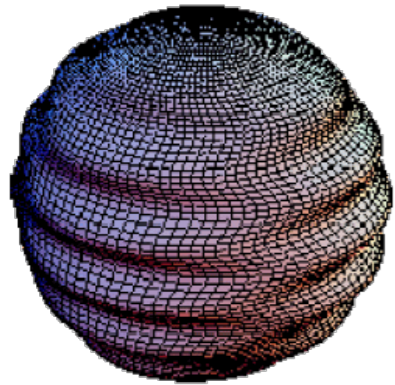
$$h_{ij} = A_{ij} \times \exp [i(\omega t - kz)]$$

$$A_{ij} = \begin{bmatrix} h_+ & h_\times & 0 \\ h_\times & -h_+ & 0 \\ 0 & 0 & 0 \end{bmatrix}$$



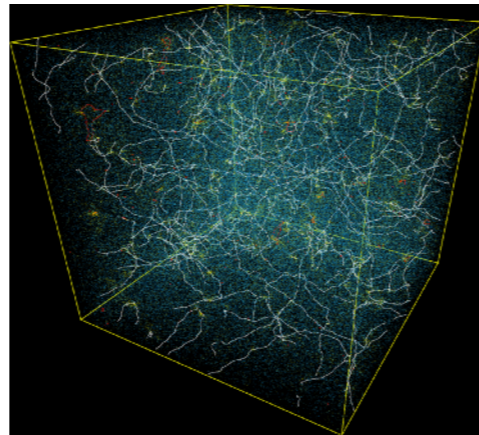
Stochastic background source

Primordial



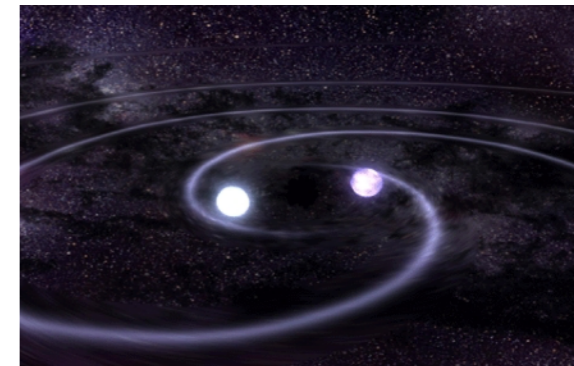
- Initial fluctuation with Inflation

Phase transition

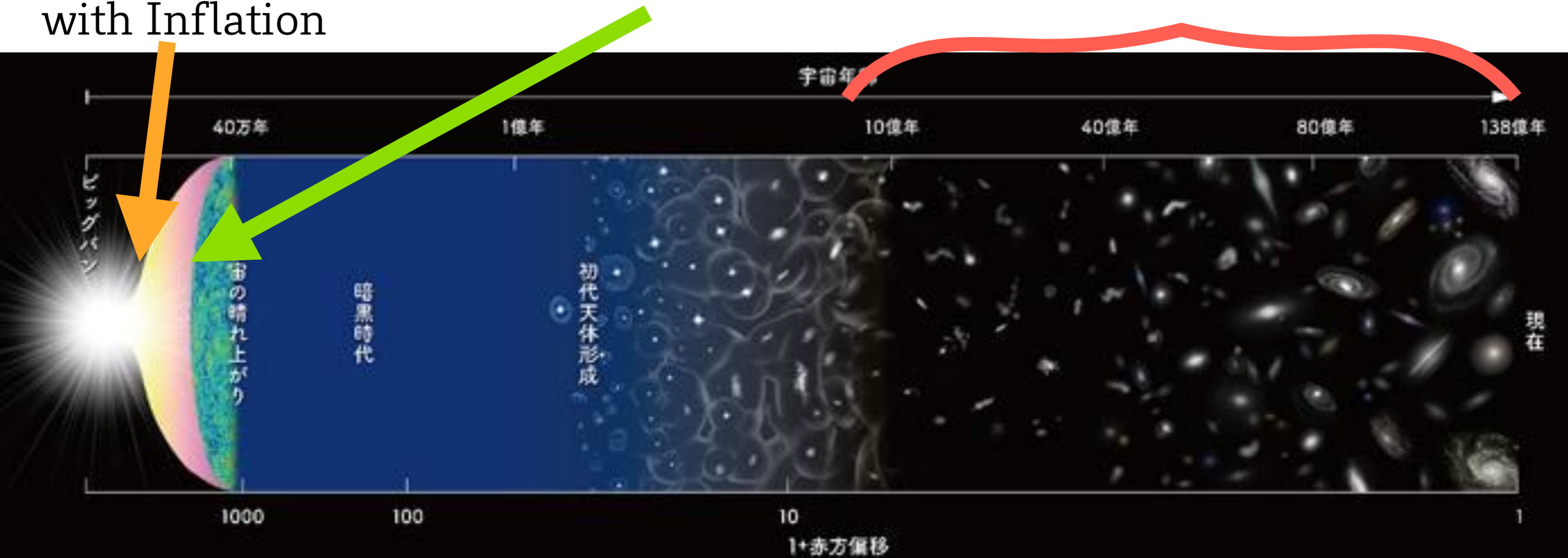


- Cosmic string

Astronomical



- BBH and BNS



Astronomical Stochastic background

1. Astrophysical Sources

Many compact objects and transients throughout cosmic history.



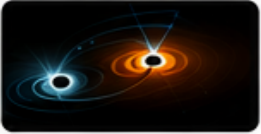
Binary Black Holes (BBH)

- Most numerous
- Dominant at 10^{-2} – 10^2 Hz
- Merger and ringdown cutoff



Binary Neutron Stars (BNS)

- Extend to higher frequency
- Cutoff \sim few kHz
- Important EM counterparts



Neutron Star–Black Hole Binaries (NSBH)

- Intermediate contribution
- Cutoff \sim few 10^2 – 10^3 Hz

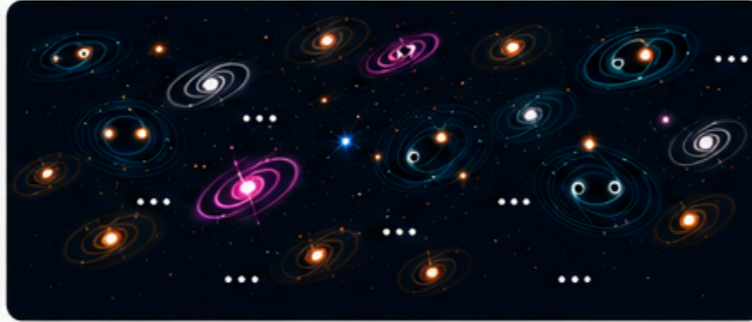


Other transients

- Core-collapse supernovae, magnetars, etc.
- Subdominant background

2. Stochastic Superposition

The SGWB arises from the superposition of a large number of unresolved sources with different redshifts, masses, and orientations.



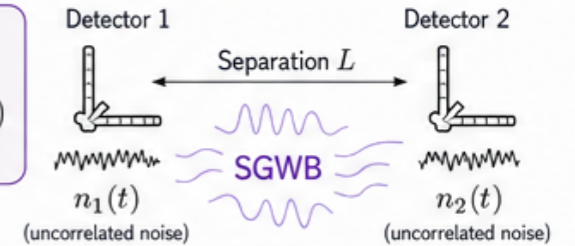
Random phases + independent locations
 \Rightarrow Gaussian, stationary, isotropic (to good approx.)

3. Statistical Description: Estimating $\Omega_{\text{GW}}(f)$ from Two Detectors

From the cross-correlation of two detectors 1 and 2 separated by L , an unbiased estimator of the dimensionless energy density $\Omega_{\text{GW}}(f)$ is (Allen & Romano 1999, Phys. Rev. D 59, 102001)

Cross-correlation estimator

$$\hat{Y} = \int_{-\infty}^{\infty} df \tilde{s}_1^*(f) \tilde{s}_2(f) \hat{Q}(f)$$



Expectation value

$$\langle \hat{Y} \rangle = T \int_0^{\infty} df \gamma(f) S_h(f) \tilde{Q}(f)$$

where

- $\tilde{s}_i(f)$: Fourier transform of strain data from detector i
- T : observation time
- $\tilde{Q}(f)$: optimal filter (see below)
- $\gamma(f)$: overlap reduction function (depends on L and f)
- $S_h(f)$: one-sided strain PSD of the SGWB

Relation to $\Omega_{\text{GW}}(f)$

$$\Omega_{\text{GW}}(f) = \frac{10\pi^2}{3H_0^2} f^3 S_h(f)$$

Optimal filter and variance

$$\hat{Q}(f) = \mathcal{N} \frac{\gamma(f) S_h(f)}{P_1(f) P_2(f)}$$

$$\sigma_{\hat{Y}}^2 = \frac{T}{2} \left[\int_0^{\infty} df \frac{\gamma^2(f) S_h^2(f)}{P_1(f) P_2(f)} \right]^{-1}$$

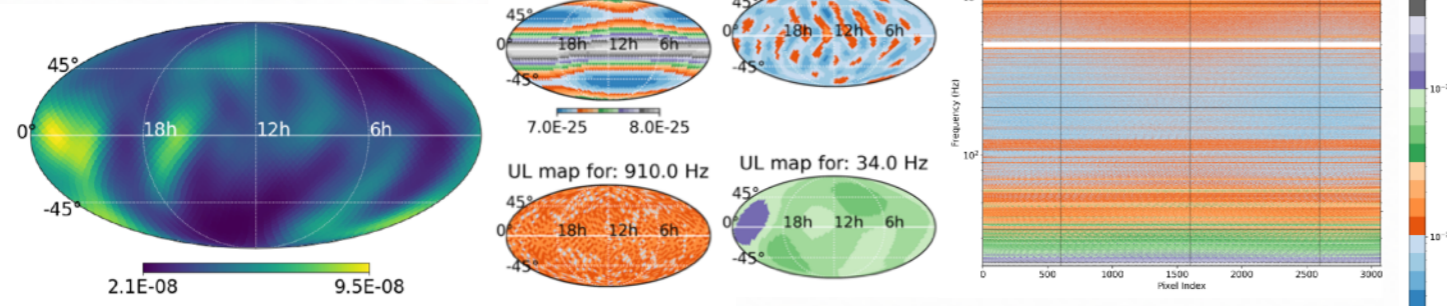
Estimator for $\Omega_{\text{GW}}(f)$

$$\hat{\Omega}_{\text{GW}}(f) = \sigma_{\hat{Y}}^2 \frac{10\pi^2}{3H_0^2} f^3 \hat{Y}$$

- $P_i(f)$: one-sided noise PSD of detector i
- H_0 : Hubble constant
- \mathcal{N} : normalization constant

4. Anisotropy

The SGWB may have angular structure.

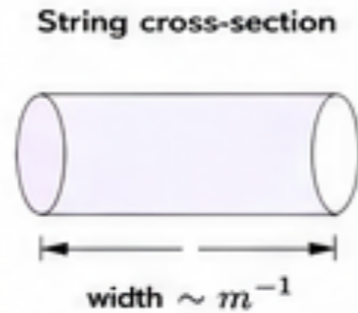


R. Abbott et al. (LVK) Phys.Rev.D 105 (2022)

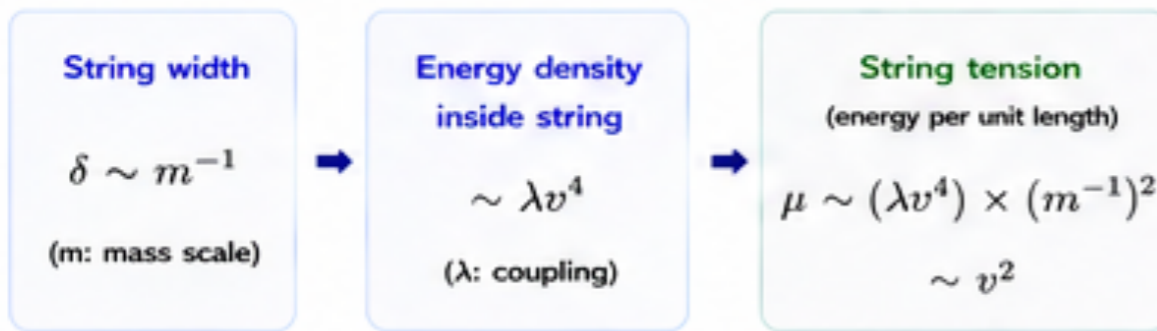
Cosmic string origin of SGWB

What are cosmic strings?

Topological line defects formed in spontaneous symmetry breaking in the early Universe. Characterized by the tension μ (energy per unit length).



Order of the tension μ



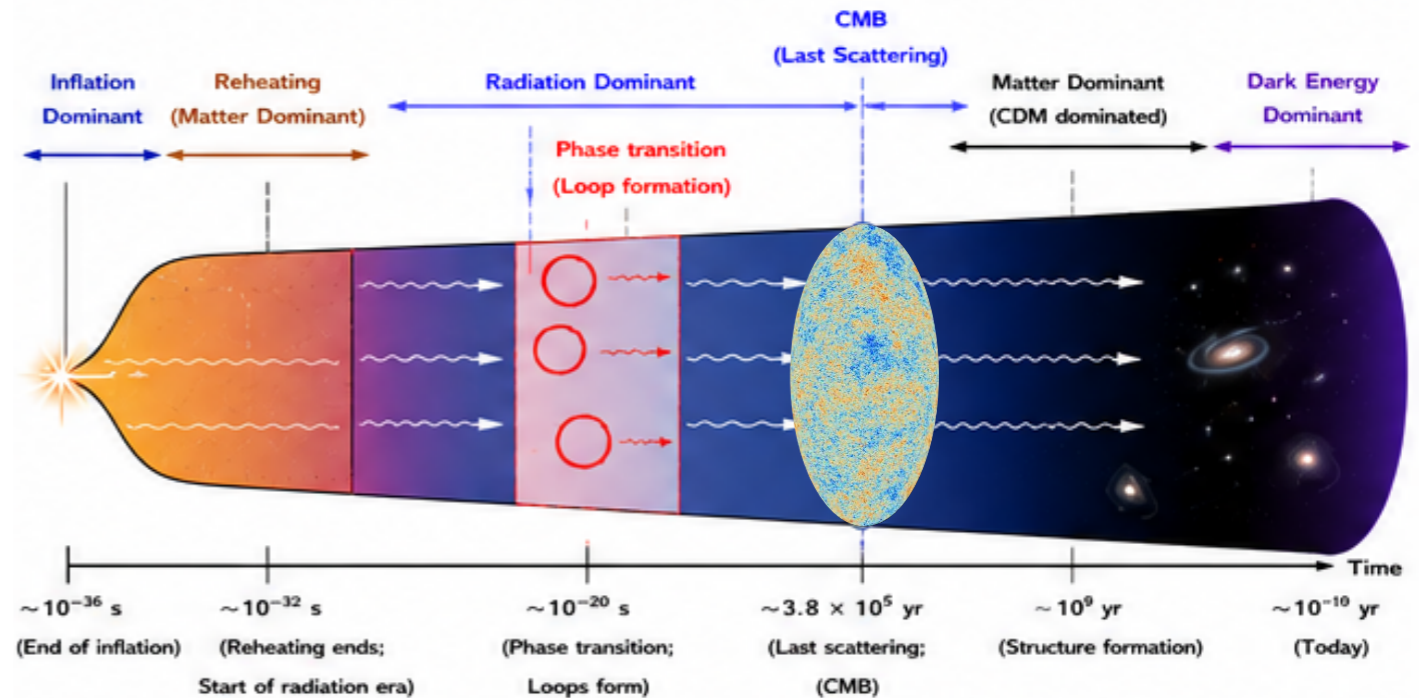
Key parameter: $G\mu$ (dimensionless)

$$G\mu = 10^{-6} \left(\frac{v}{10^{16} \text{ GeV}} \right)^2$$

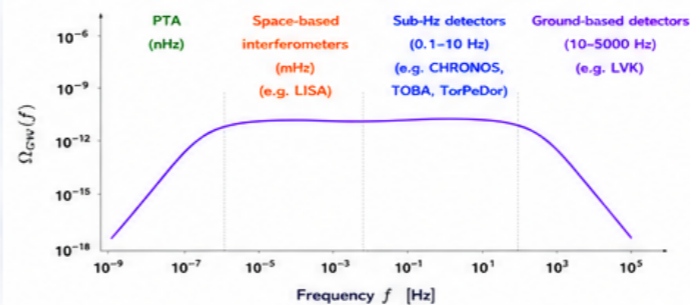
G : Newton's constant
 v : symmetry breaking scale

Measuring $G\mu$ directly probes the energy scale of symmetry breaking!

Cosmic strings exist only for a short period in the early Universe. They form loops at a phase transition and then decay, emitting gravitational waves.



The SGWB from cosmic strings has a broad and characteristic spectrum.



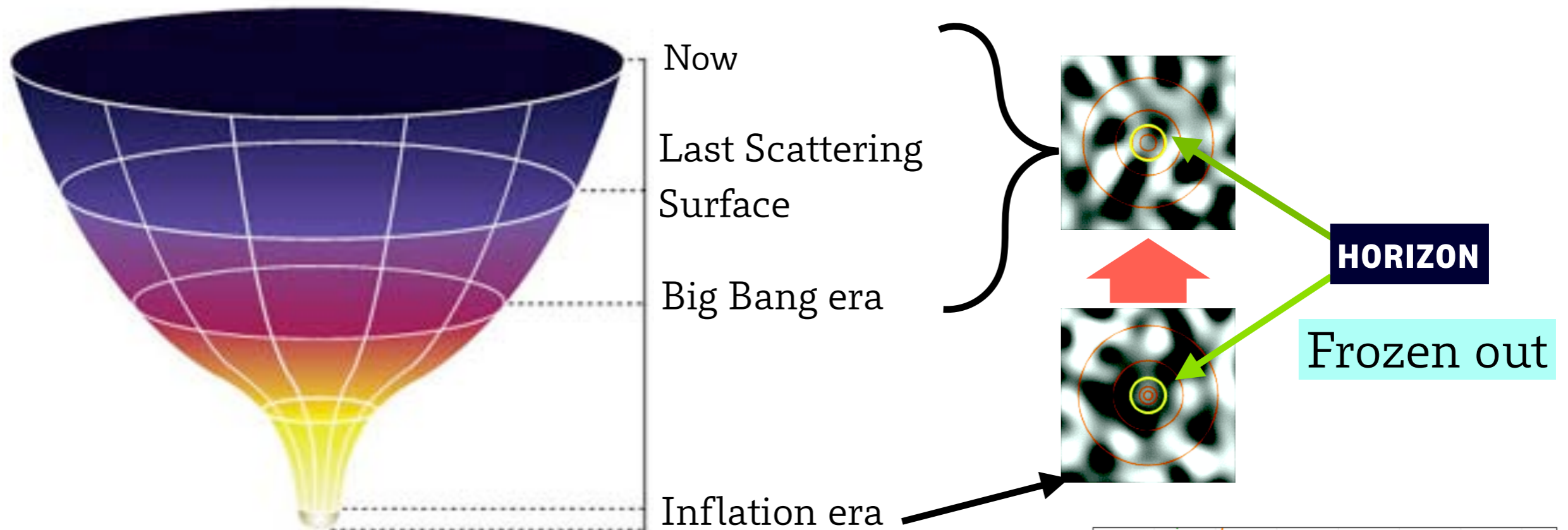
Spectral features

- Low frequency: large loops and cusps
- Mid frequency: loop oscillations and kinks
- High frequency: small loops and high harmonics
- Overall: broadband power-law-like spectrum (broken power law)

Parameter	Meaning / Role	Impact on observations
$G\mu$	String tension (strength of gravity)	Sets overall amplitude of SGWB: $\Omega_{\text{SGWB}}(f) \propto (G\mu)^2$ Main target of observations
α	Loop size parameter (correlation length)	Affects energy density $\rho_s / \rho_{\text{tot}} \sim \alpha G\mu$
Loop size distribution	Initial loop size and production efficiency	Affects spectral shape and peak frequency
Emission mechanisms (spectrum)	Loop oscillation modes, cusps, kinks	Determine spectral slope and features
Loop reconnection probability p	Reconnection probability of string intersections	Affects loop production rate (and thus amplitude)

Primordial Gravitational wave

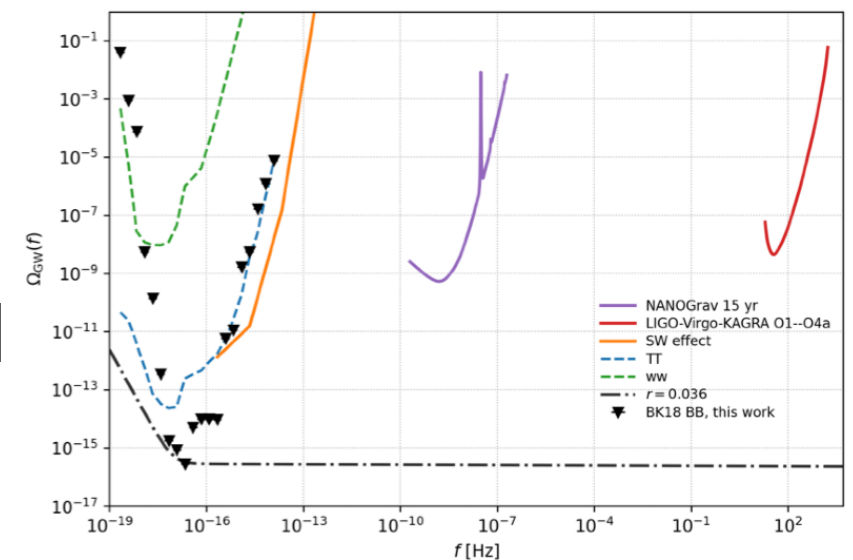
Primordial GW come back to observable universe



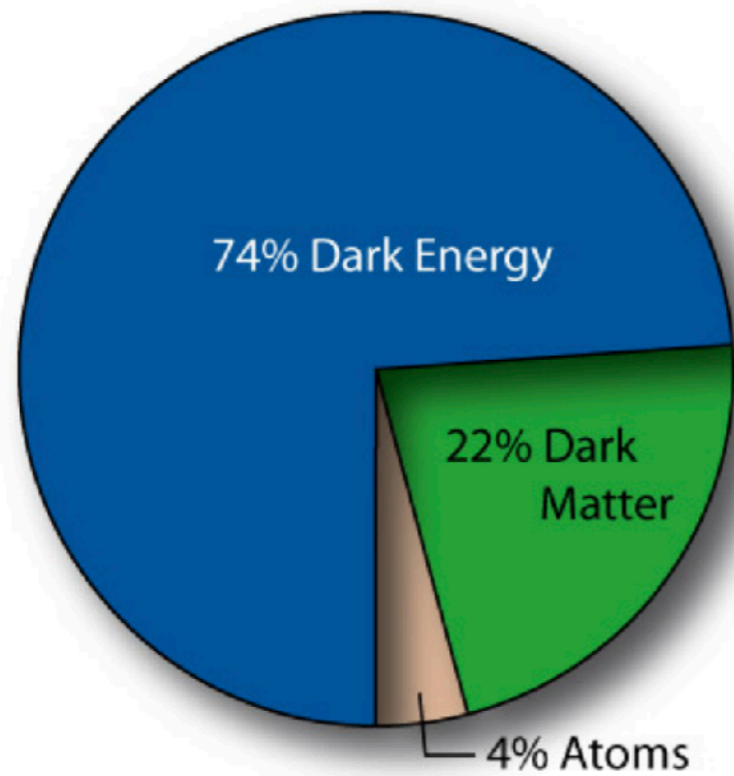
$$\Omega_{GW}(k, \tau_0) = \frac{\mathcal{P}_T(k)}{12H_0^2} k^2 \cdot \begin{cases} \frac{\tau_*^2}{\tau_0^2} [A(k)j_2(k\tau_0) + B(k)y_2(k\tau_0)]^2, & \text{if } k > k_*, \quad \propto f^0 \\ \left[\frac{3j_2(k\tau_0)}{k\tau_0} \right]^2, & \text{if } k < k_*, \quad \propto f^{-2} \end{cases}$$

Matter dominant

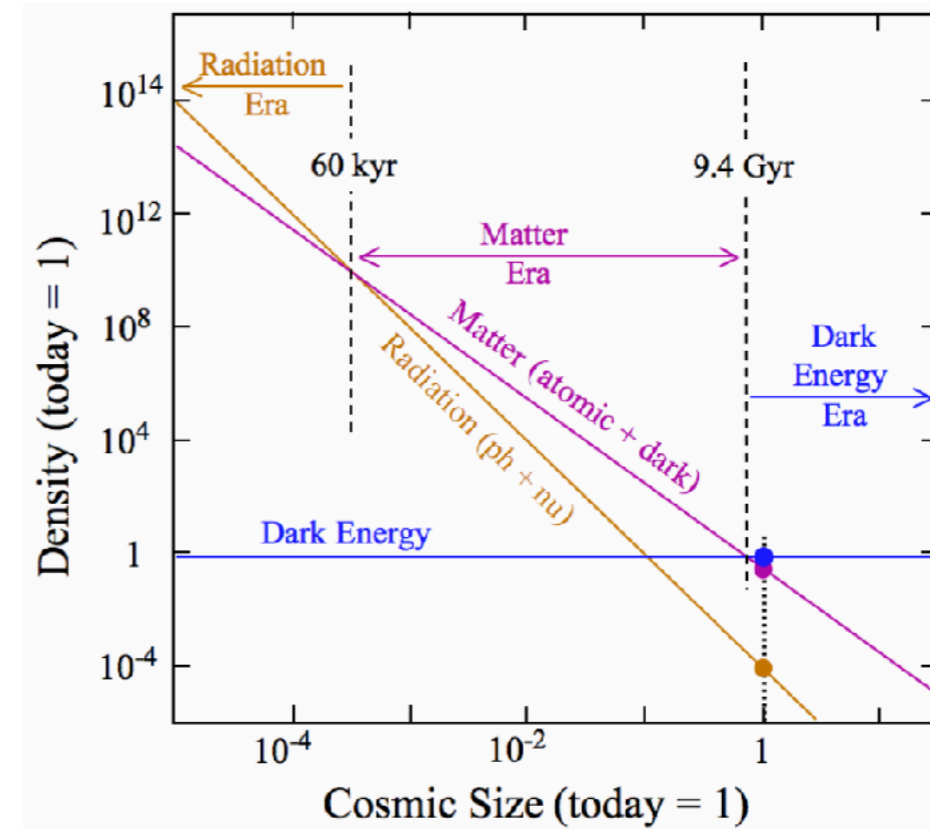
Radiation dominant



Density parameter



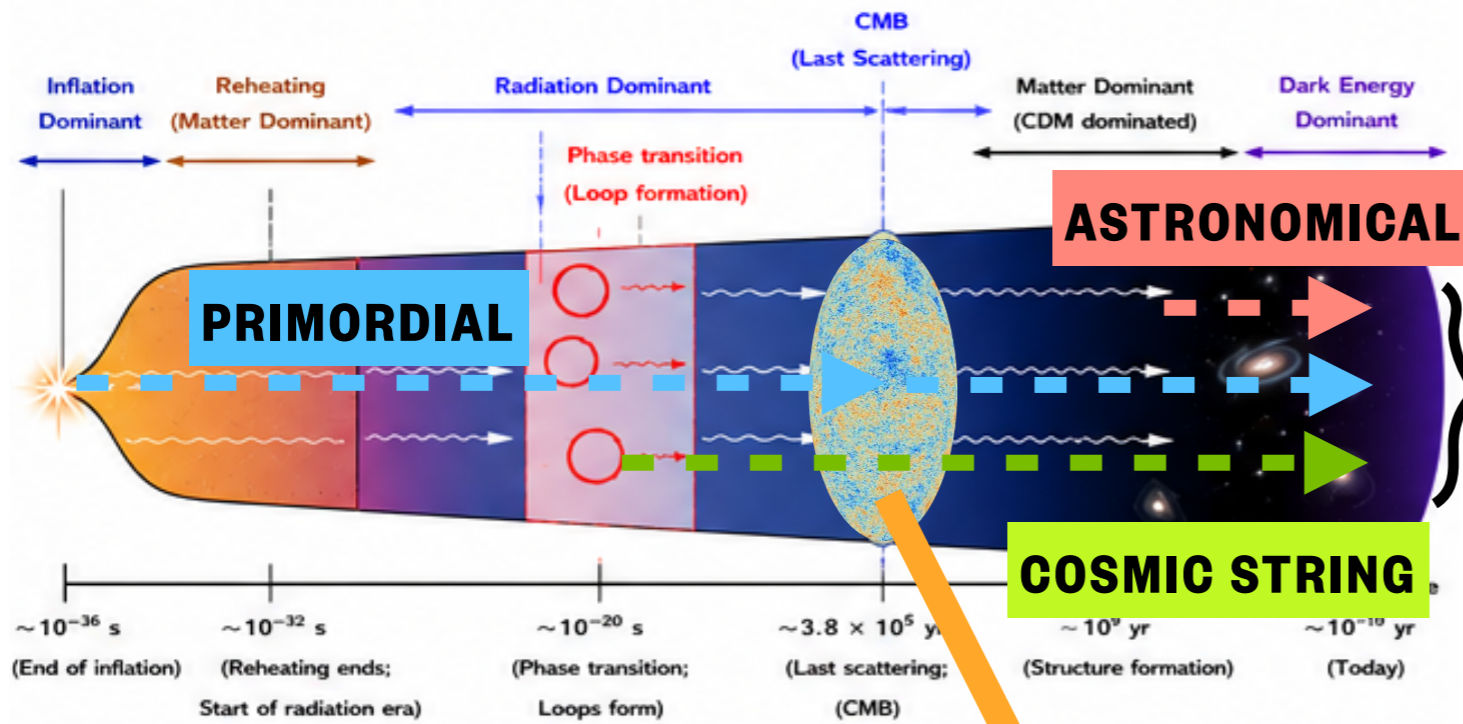
$$\Omega_i = \rho_i / \rho_{cr}$$



Friedmann equation:
$$H^2(t) = H_0^2 \left[\underbrace{\Omega_{\gamma,0} a^{-4}}_{\text{radiation}} + \underbrace{\Omega_{m,0} a^{-3}}_{\text{matter}} + \underbrace{\Omega_{\kappa} a^{-2}}_{\text{curvature}} + \underbrace{\Omega_{\Lambda}}_{\text{dark energy}} \right]$$

Fundamental questions: What's the energy density of GW, Ω_{GW} ?

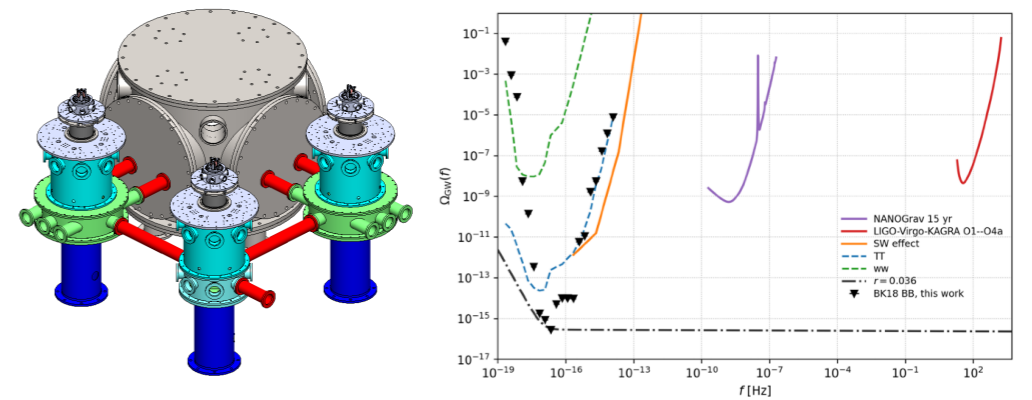
Experiment and GW source



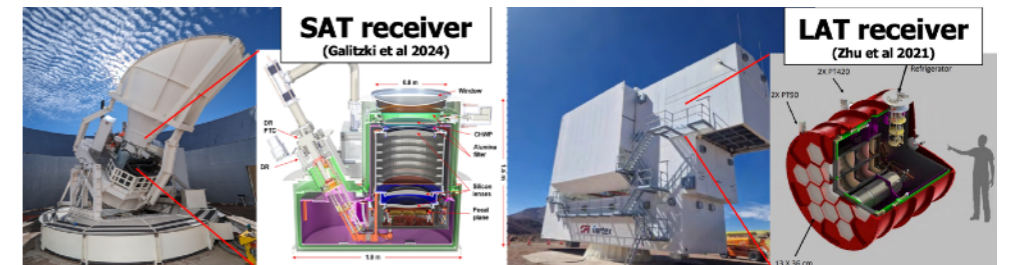
LIGO-Virgo-KAGRA



CHRONOS



Simons Observatory



LIGO



- The world largest GW detector in US.
- The most sensitive probe for SGWB.

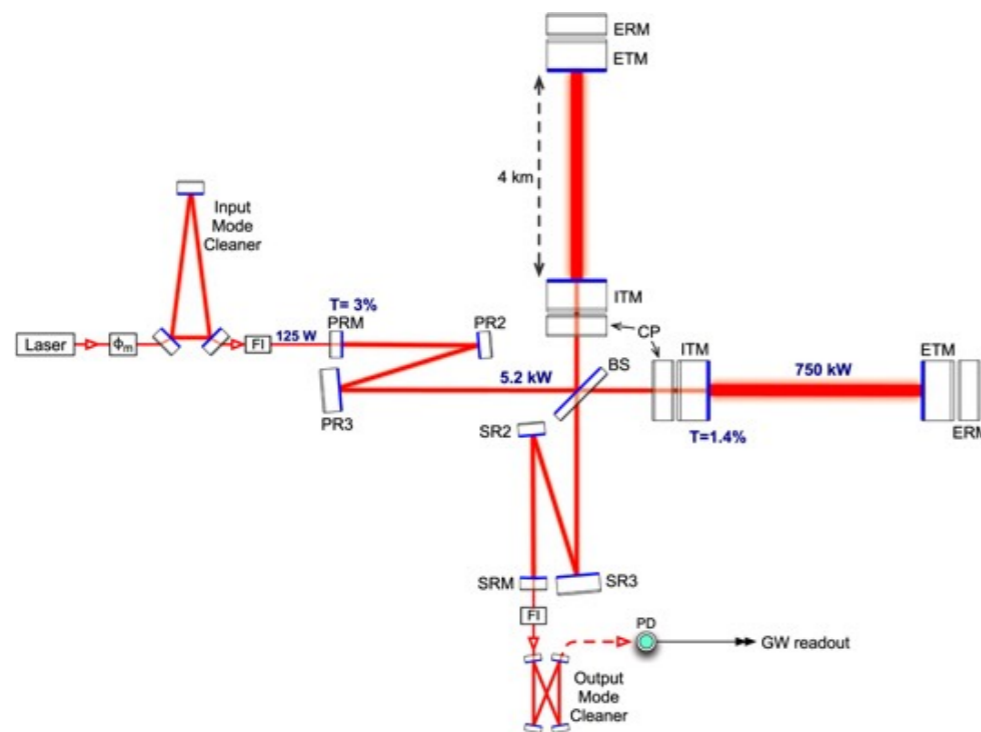
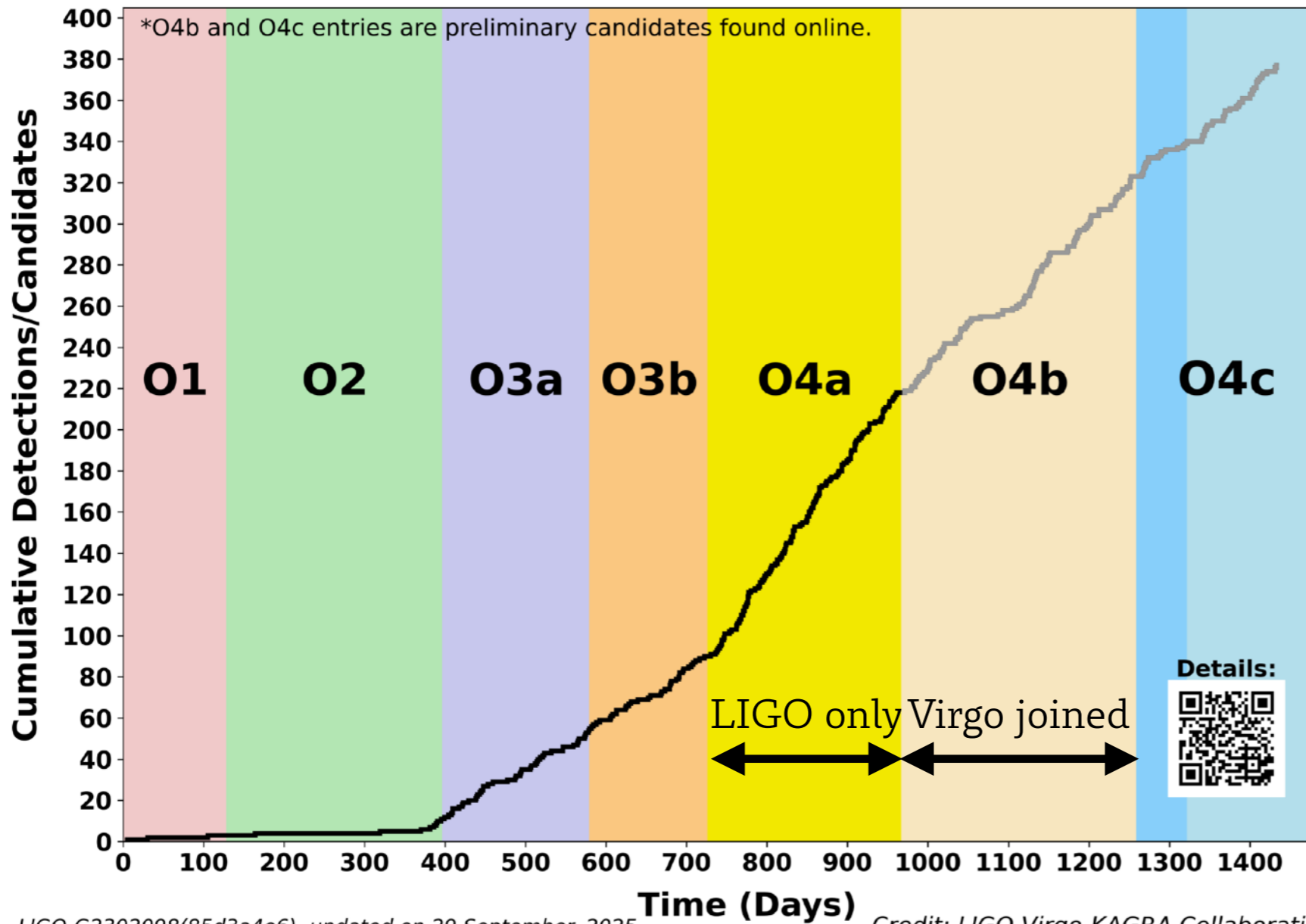


Table 1. Main parameters of the Advanced LIGO interferometers. PRC: power recycling cavity; SRC: signal recycling cavity.

Parameter	Value
Arm cavity length	3994.5 m
Arm cavity finesse	450
Laser type and wavelength	Nd:YAG, $\lambda = 1064$ nm
Input power, at PRM	up to 125 W
Beam polarization	linear, horizontal
Test mass material	Fused silica
Test mass size & mass	34cm diam. x 20cm, 40 kg
Beam radius ($1/e^2$), ITM / ETM	5.3 cm / 6.2 cm
Radius of curvature, ITM / ETM	1934 m / 2245 m
Input mode cleaner length & finesse	32.9 m (round trip), 500
Recycling cavity lengths, PRC / SRC	57.6 m / 56.0 m

Number of detections

O1+O2+O3+O4a = 218, O4b* = 105, O4c* = 54, Total = 377



LIGO-G2302098(85d3a4e6), updated on 29 September, 2025

Credit: LIGO-Virgo-KAGRA Collaboration

Data release plan

2026

O4b->GWTC-5

2027

O4c->GWTC-6

Compact binary coalescence

Binary Neutron Star

Binary Blackhole

Neutron star- Black hole binary

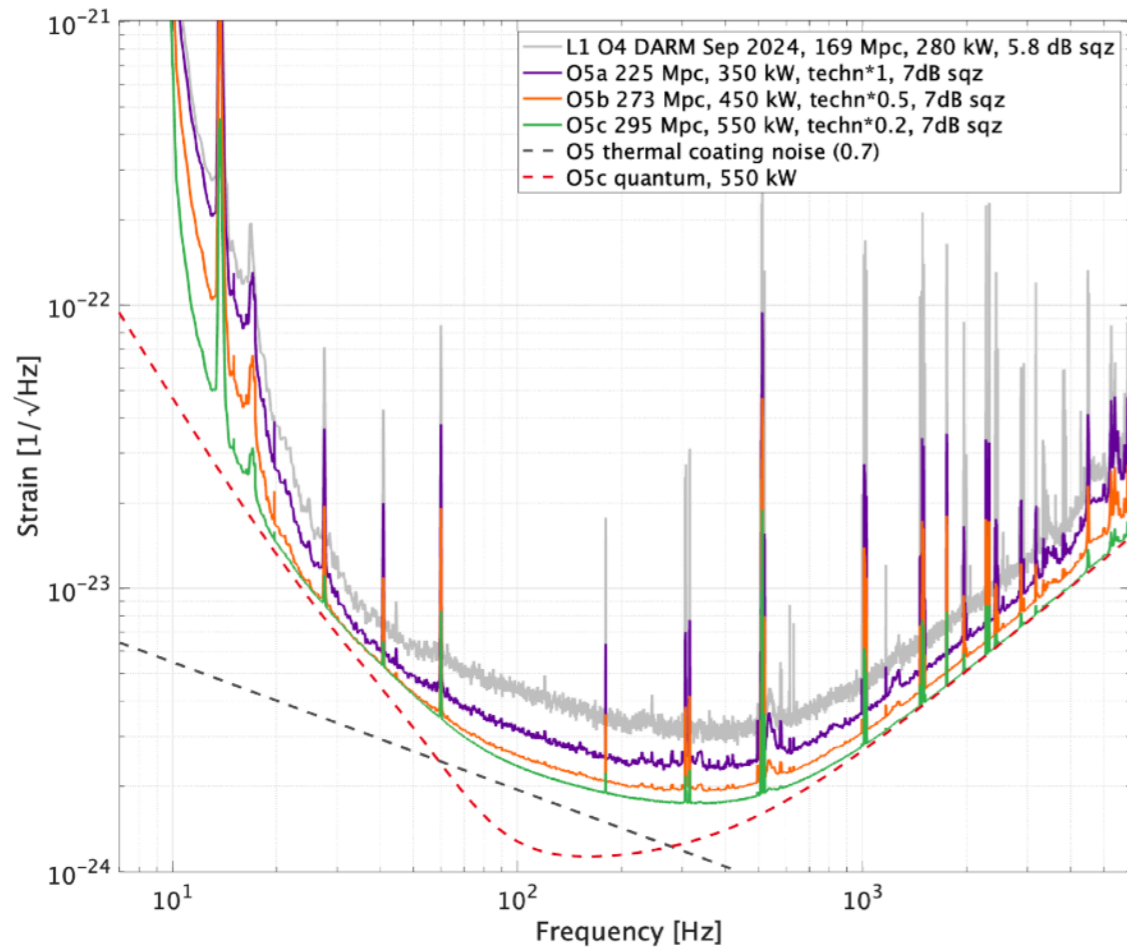
Events

Total number of events ~ 377

Every 2.8 days we detect new events

The era of O(100) events!

Sensitivity

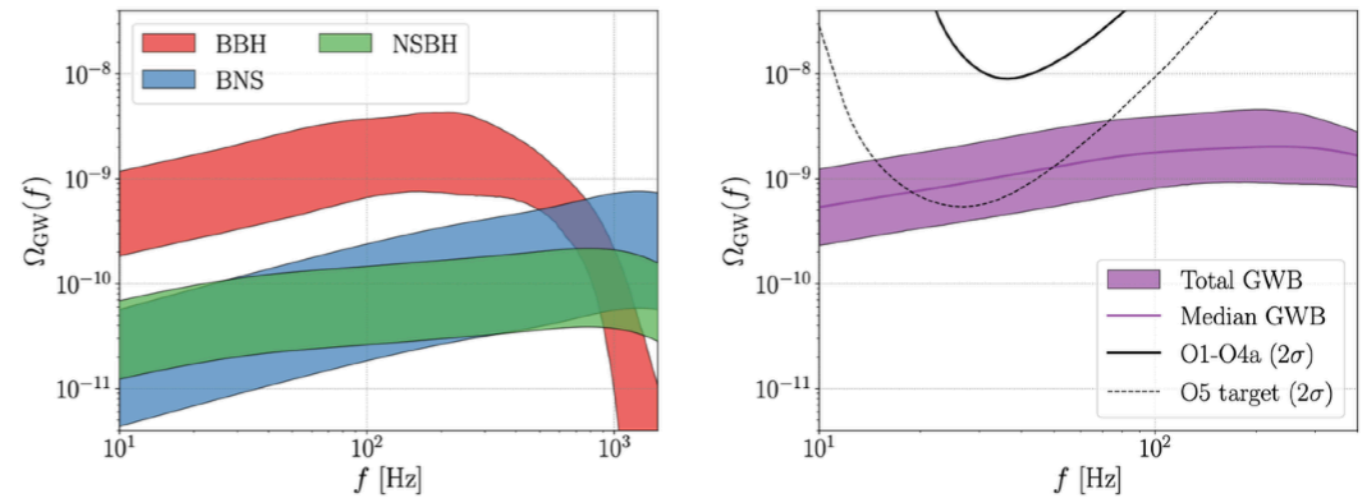


O5 epoch	BNS range	Arm Power	Tech. noise @100 Hz	Squeezing @1 kHz
O5a	225 Mpc	350 kW	$2 \times 10^{-24}/\sqrt{\text{Hz}}$	7 dB
O5b	273 Mpc	450 kW	$1 \times 10^{-24}/\sqrt{\text{Hz}}$	7 dB
O5c	295 Mpc	550 kW	$4 \times 10^{-25}/\sqrt{\text{Hz}}$	7 dB

Upper Limits on the Isotropic Gravitational-Wave Background from the first part of LIGO, Virgo, and KAGRA's fourth Observing Run

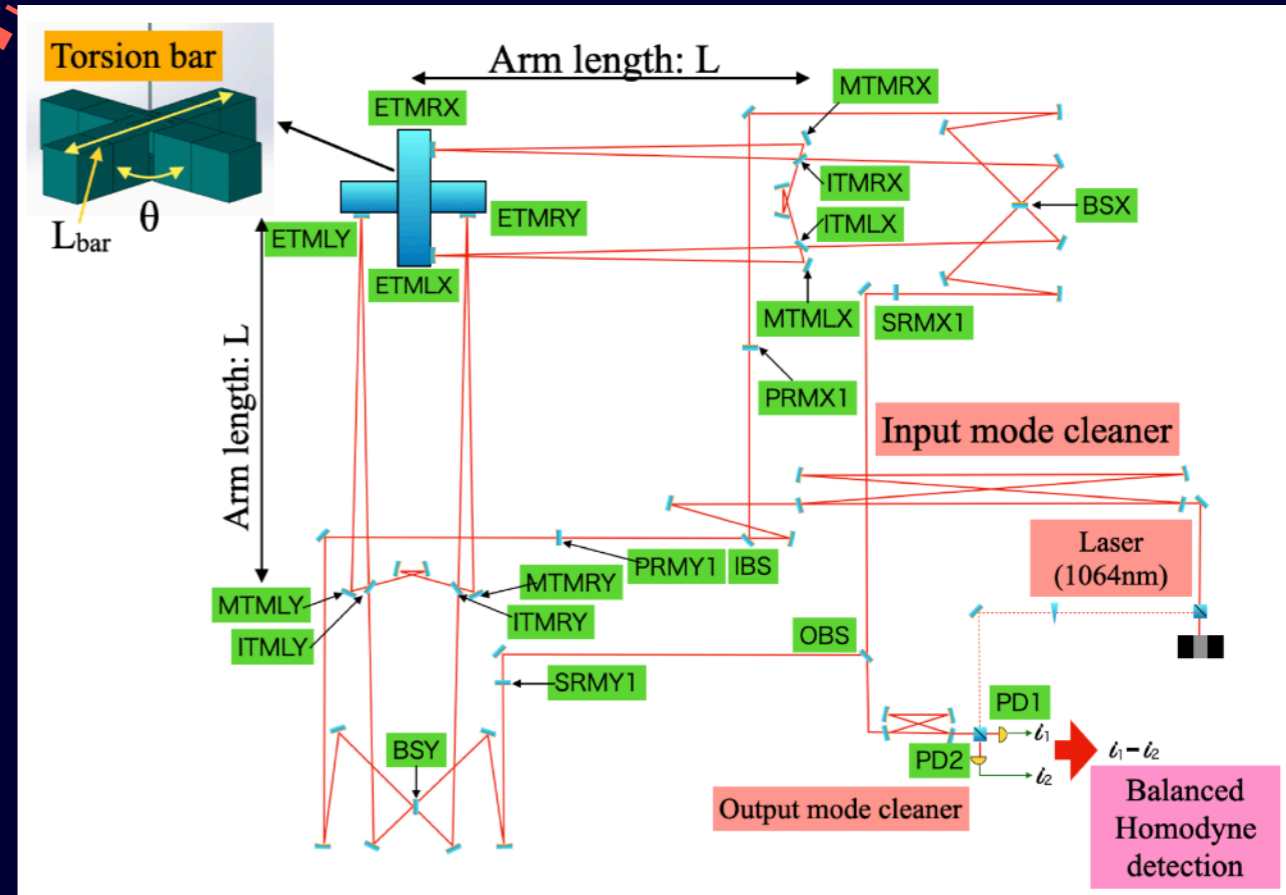
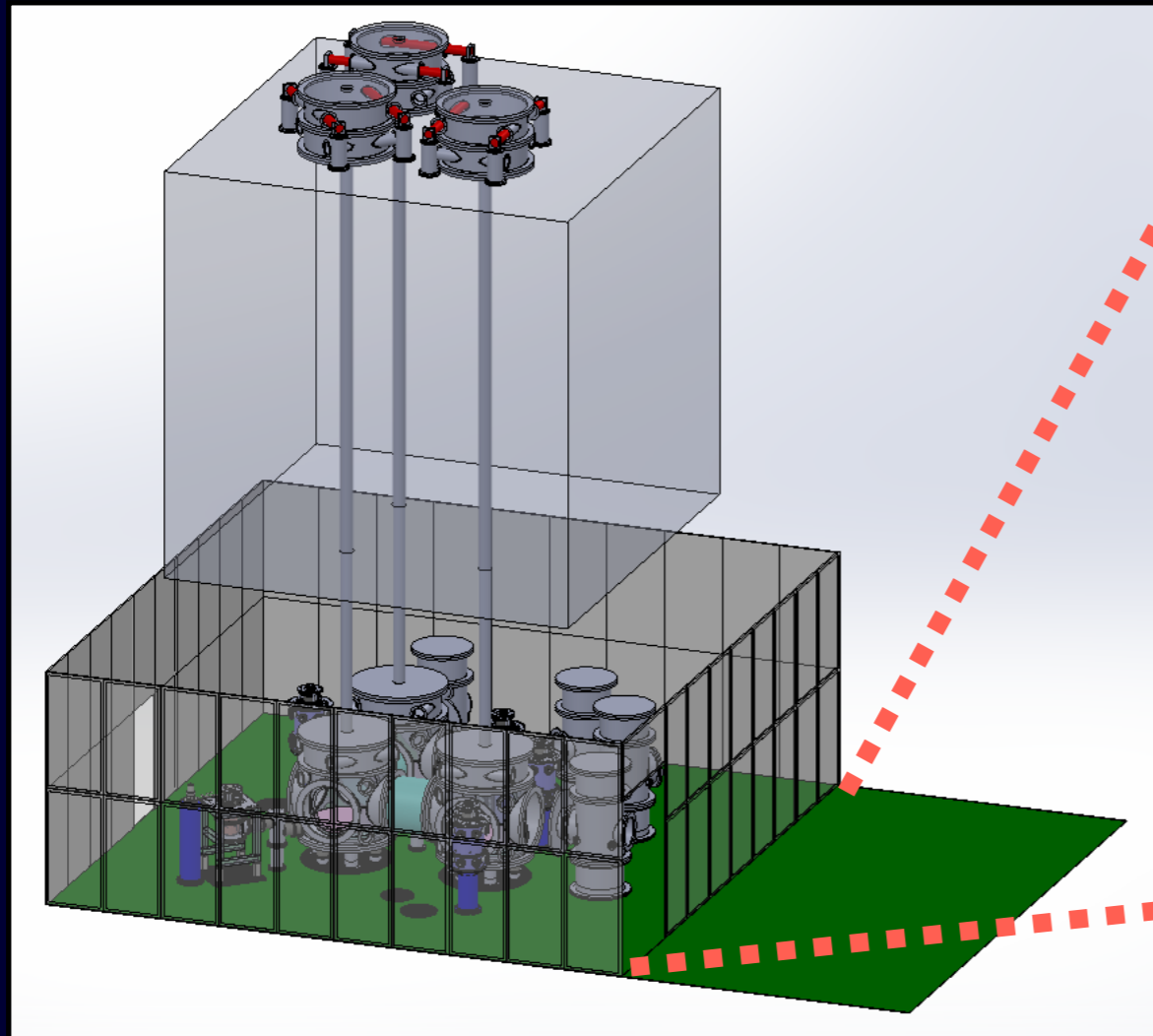
Phys. Rev. D - **Accepted** 1 December, 2025

DOI: <https://doi.org/10.1103/wq57-sjt2>



- The expected sensitivity of O5 will be reach the signal of the astronomical stochastic background.

CHRONOS Overview



Cryogenic sub-**H**z **cR**Oss torsion bar detector
with quantum **N**on-demolition **S**peed meter



CHRONOS Overview

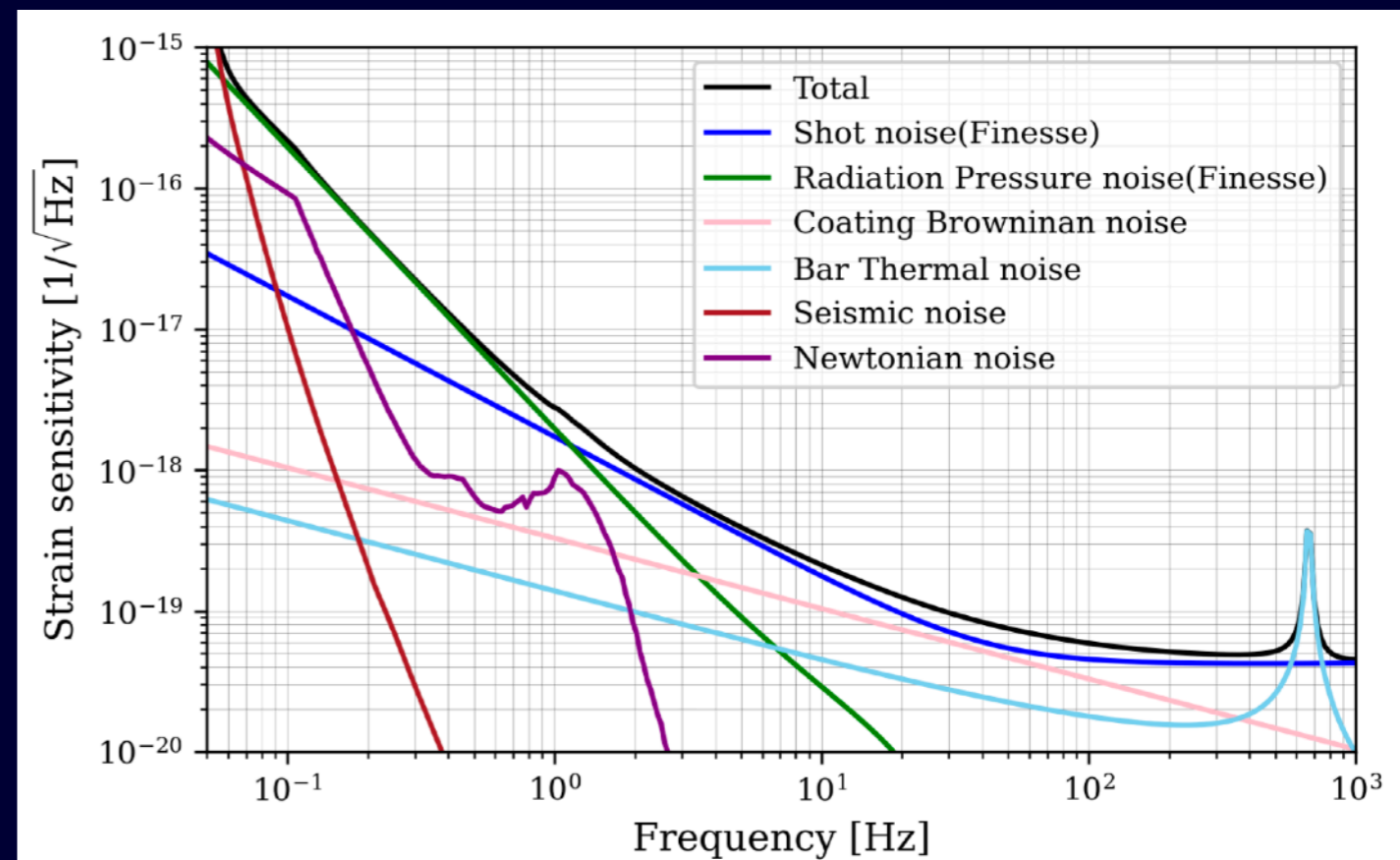
- Mission: Search for Intermediate black hole on Sub-Hz range
- Method: Interferometrical Speed meter
- Unique point: 10m x 10m Observatory
- Location: Underground site in Taiwan

Key technologies

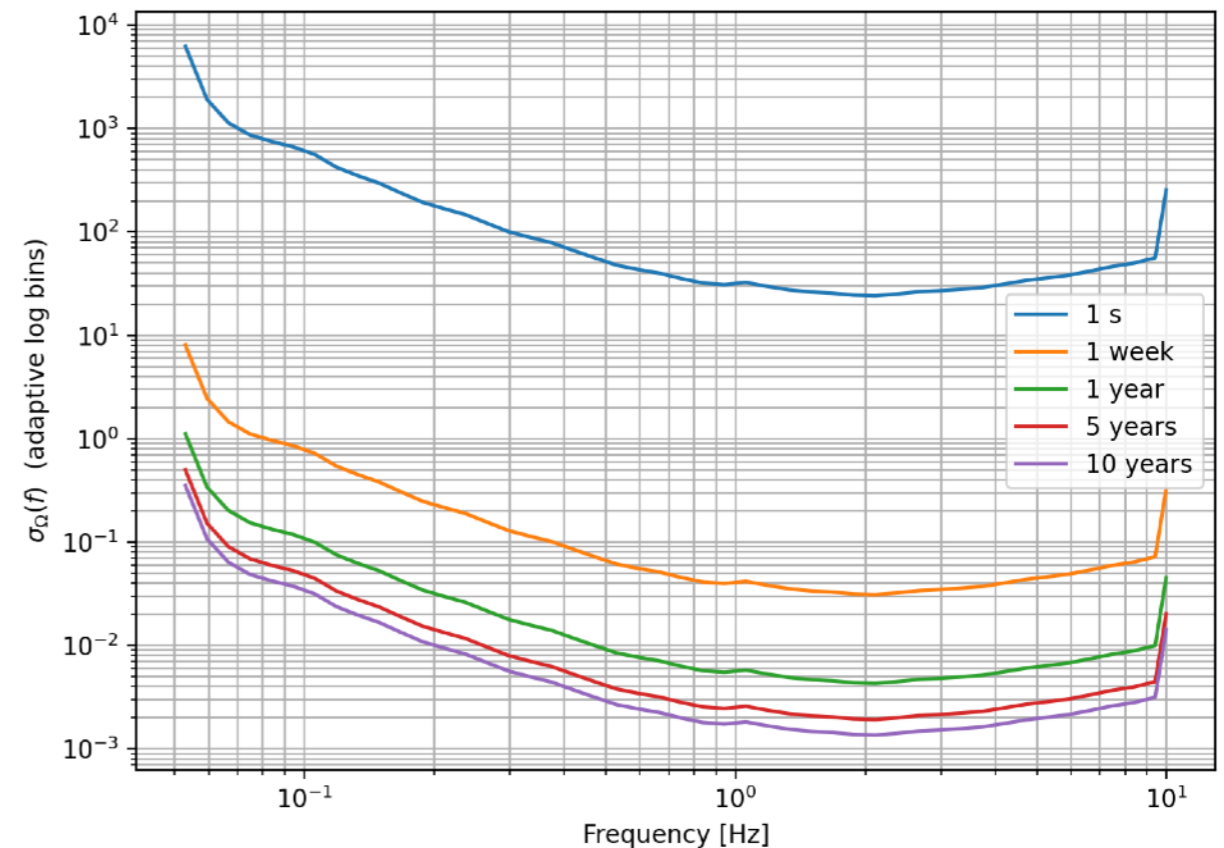
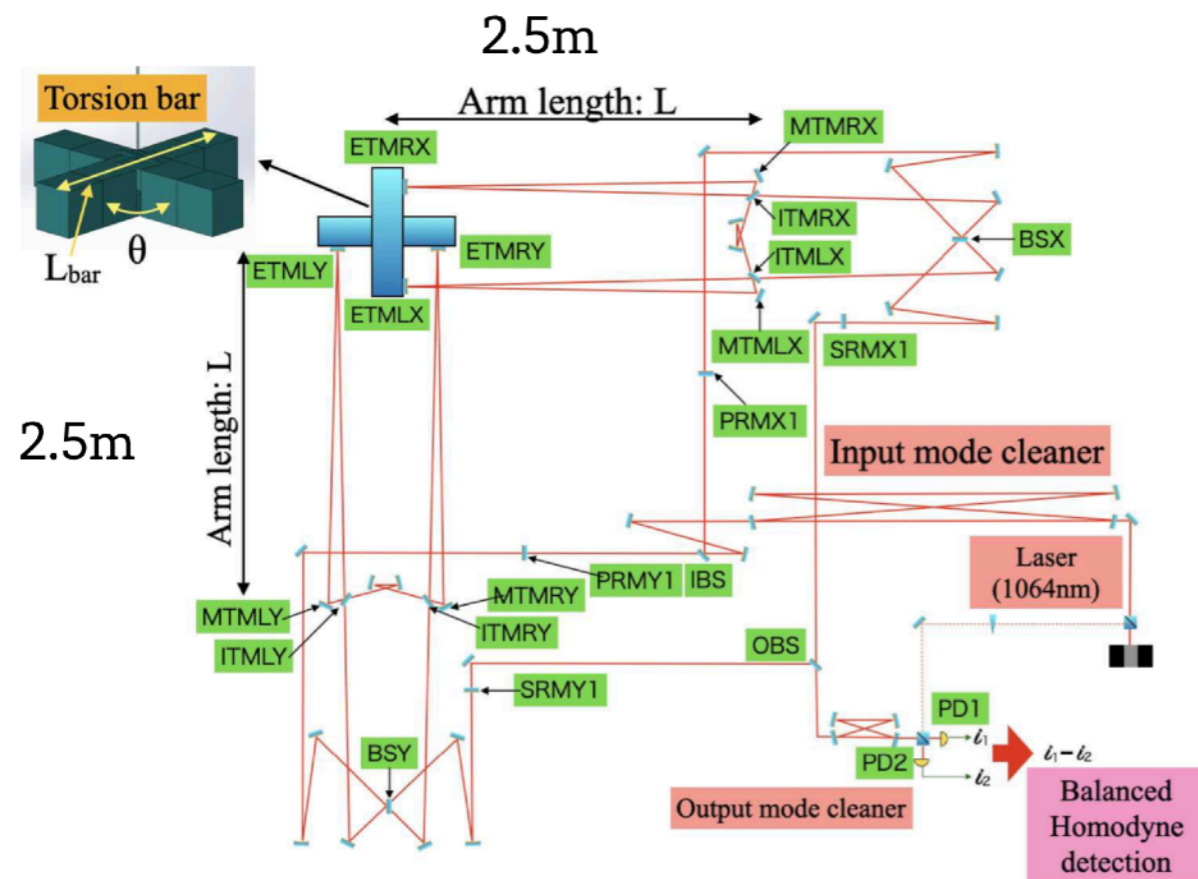
SPEED METER

TORSION BAR

CRYOGENIC



Experimental setup and sensitivity



CHRONOS detector is sensitive to the window between LISA and LIGO observation band.

Publications

Main project paper

CHRONOS: Cryogenic sub-Hz cROSS torsion bar detector with quantum NOn-demolition Speed meter

Yuki Inoue,^{1,2,3,4,*} Hsiang-Chieh Hsu,³ Hsiang-Yu Huang,^{1,2} M.Afif Ismail,^{1,2,3} Vivek Kumar,^{3,5} Miftahul Ma'arif,^{1,2} Avani Patel,^{1,2} Daiki Tanabe,^{3,2,4} Henry Tsz-King Wong,^{3,2} and Ta-Chun Yu^{1,2}

Y.Inoue et. al. arXiv: 2509.23172

Optical feasibility paper

Optical design and sensitivity optimization of Cryogenic sub-Hz cROSS torsion bar detector with quantum NOn-demolition Speed meter (CHRONOS)

Yuki Inoue,^{1,2,3,4,*} Daiki Tanabe,^{3,2,4} M.Afif Ismail,^{1,2,3} Vivek Kumar,^{3,5} Mario Juvenal S Onglao III,^{5,2} and Ta-Chun Yu^{1,2}

Y.Inoue and D.Tanabe et. al. arXiv: 2510.24780

Intensity noise paper

Torque cancellation effect of Intensity noise for Cryogenic sub-Hz cROSS torsion bar detector with quantum NOn-demolition Speed meter (CHRONOS)

Daiki Tanabe^{a,b,d†}, Yuki Inoue^{c,d,a,b‡}, Vivek Kumar^{c,a}, Miftahul Ma'arif^{c,d}, Ta-Chun Yu^{c,d}

D.Tanabe and Y.Inoue et. al. C.Q.G accepted

Calibration paper

Improving calibration accuracy with torque coupled gravity field calibrator for sub-Hz gravitational wave observation in CHRONOS

Yuki Inoue,^{1,2,3,4,*} Daiki Tanabe,^{2,3,4} and Vivek Kumar^{1,2}

¹Department of Physics, National Central University, Taoyuan, Taiwan

²Center for High Energy and High Field (CHiP), National Central University, Taoyuan, Taiwan

³Institute of Physics, Academia Sinica, Taipei, Taiwan

⁴Institute of Particle and Nuclear Studies, High Energy Acceleration Research Organization (KEK), Tsukuba, Japan

(Dated: February 24, 2026)

Y.Inoue et. al. arXiv: 2602.19436

Yukawa Gravity paper

Probing Yukawa Gravity with Modulated Newtonian Cancellation in the Torsion bar type detector

Yuki Inoue,^{1,2,3,4,*} Hsiang-Yu Huang,^{1,2} Vivek Kumar,^{1,2} and Daiki Tanabe^{2,3}

Y.Inoue et. al. arXiv: 2604.11167

Science paper

Science of Cryogenic sub-Hz cROSS torsion bar detector with quantum NOn-demolition Speed meter (CHRONOS)

Yuki Inoue,^{1,2,3,4,*} Hsiang-Yu Huang,^{1,2} Vivek Kumar,^{1,2} Mario Juvenal S. Onglao II,^{5,2} Daiki Tanabe,^{3,2,4} and Ta-Chun Yu^{1,2}

Y.Inoue et. al. arXiv: 2604.0626

Sensitivity paper

Noise budget of Cryogenic sub-Hz cROSS torsion-bar detector with quantum NOn-demolition Speed meter (CHRONOS)

Mario Juvenal S. Onglao III,^{1,2,*} Hsiang-Yu Huang,^{3,2} Yuki Inoue,^{3,2,4,5} Vivek Kumar,^{3,2} and Daiki Tanabe^{4,2,5}

M.Onglao et. al. arXiv: 2604.05840

Instruments paper

Instrumental development for Cryogenic sub-Hz cROSS torsion bar detector with quantum NOn-demolition Speed meter (CHRONOS)

Daiki Tanabe,^{1,2,3,4,*} Hsiang-Yu Huang,^{3,2} Yuki Inoue,^{3,2,1,4} Mario Juvenal S. Onglao III,^{5,3,2} and Ta-Chun Yu^{3,2}

D.Tanabe et. al. arXiv: 2604.05801

In preparation (Release on May)

Elastic deformation paper (Tanabe et al.)

Stochastic background paper (Inoue et al.)

Photon pressure actuator paper (Tanabe et al.)

Gravity gradient paper (Onglao et al.)

White paper

WHITE PAPER
VER.1.0
LAST UPDATE: 2026 MAR.11

CHRONOS Science Program

Author:
Yuki INOUE, Mario Juvenal S Onglao III, Daiki Tanabe,
Vivek Kumar
on the behalf of CHRONOS collaboration

CHRONOS
MANAGEMENT



arXiv: 2603.10070

Collaboration is very welcome!!

CHRONOS Science stage

- Phase 1: R&D stage(2020-2025)
- Phase 2: Integration test (2026-2033)
- Phase 3: CHRONOS in Underground lab (2030-2035)

SCIENCE STAGE IN PHASE2-3

CHRONOS's target observation year = 2035

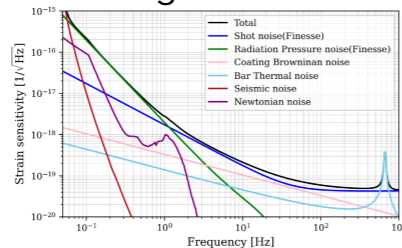
Quantum science

Quantum science for uncertainty principle

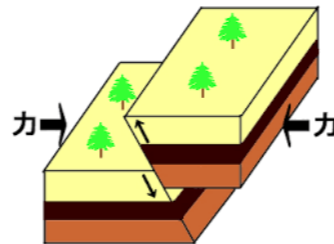
$$\epsilon(A)\eta(B) + \sigma(A_{in})\eta(B) + \epsilon(A)\sigma(B_{in}) \geq \frac{1}{2} |\langle \psi | [\hat{A}_{in}, \hat{B}_{in}] | \psi \rangle|$$

Gravity gradient science

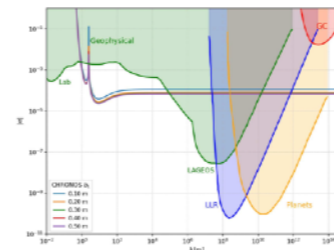
Newtonian gravity background



Earthquake

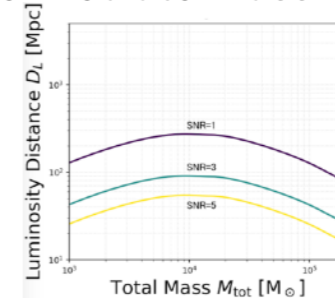


Yukawa Gravity

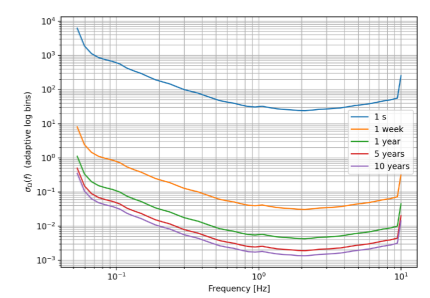


Gravitational wave science

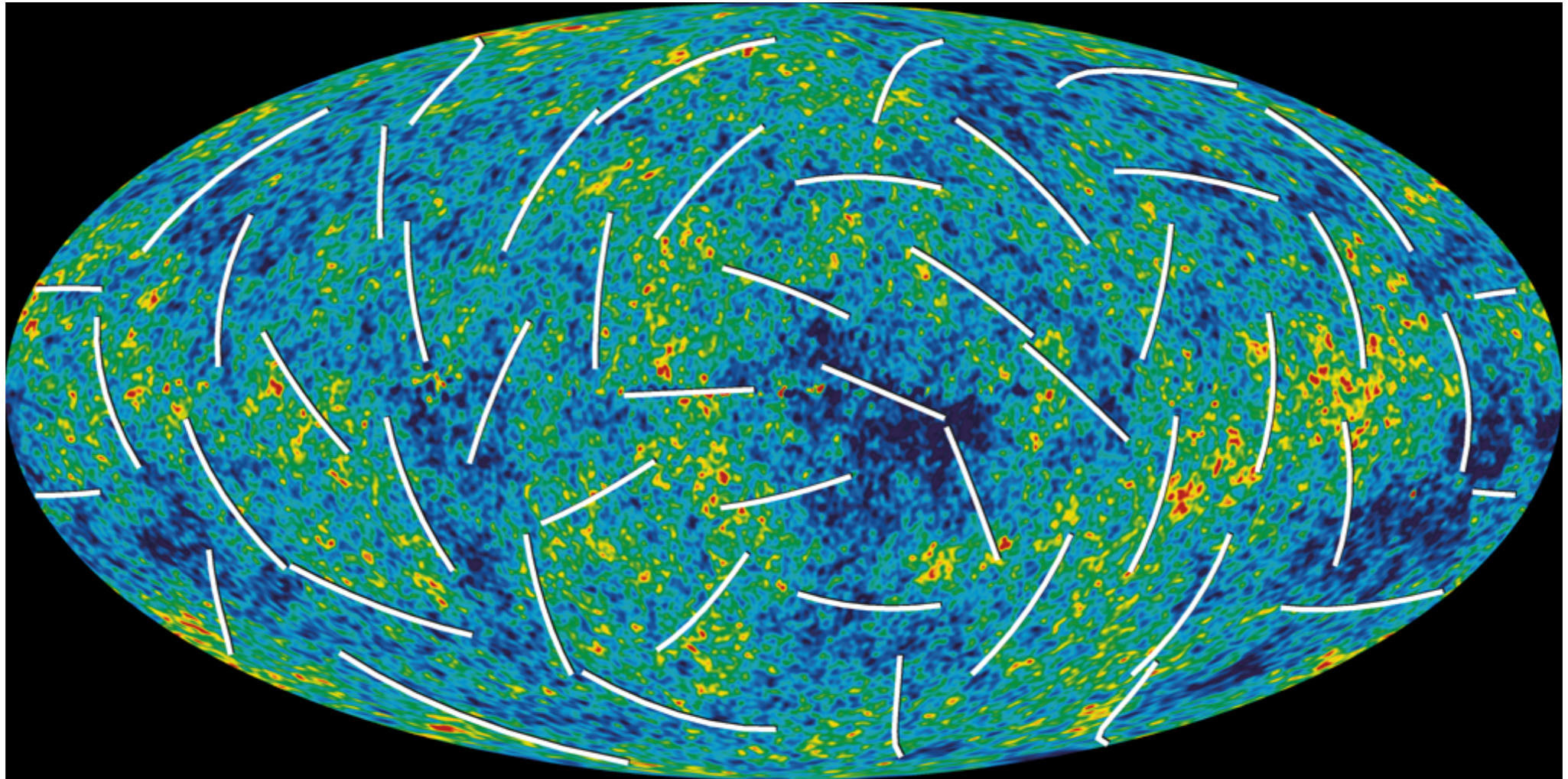
Intermediate mass GW



SGWB

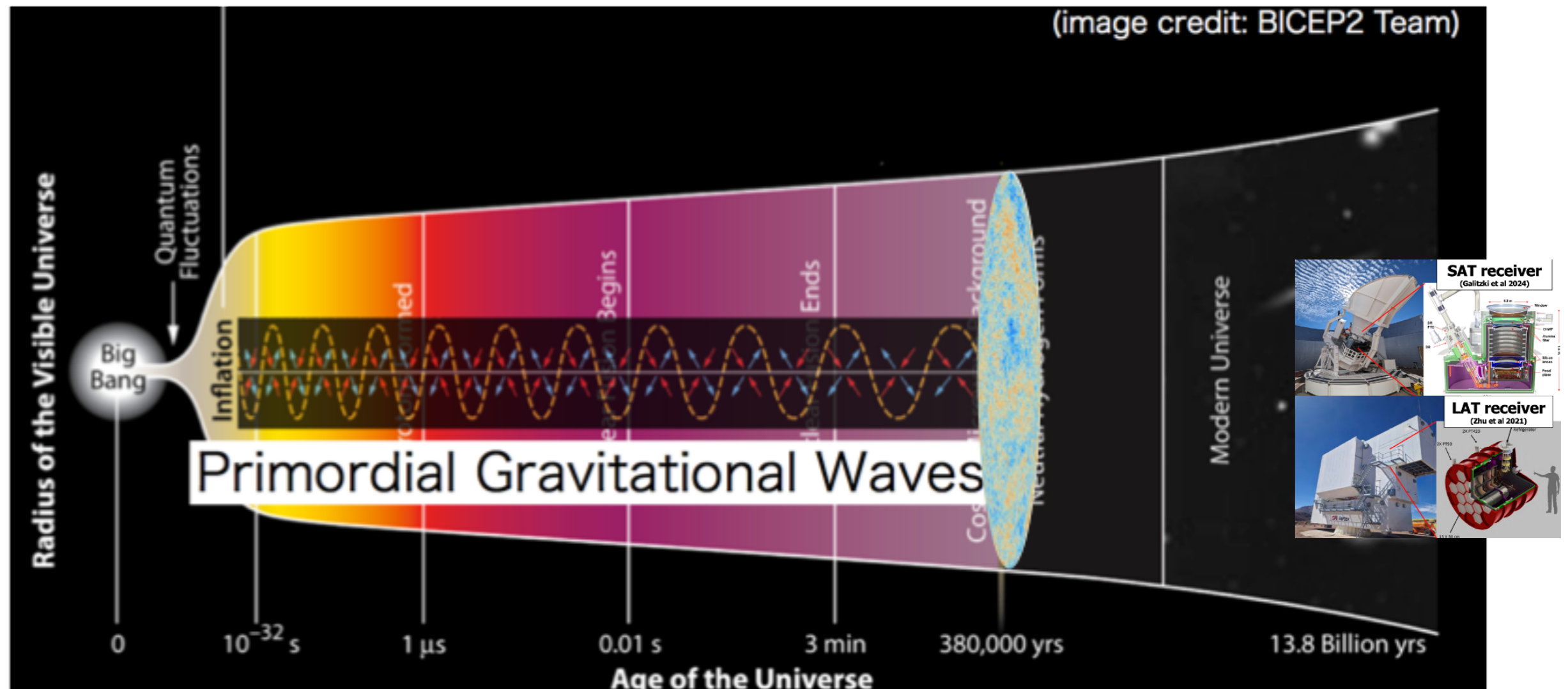


Cosmic microwave background



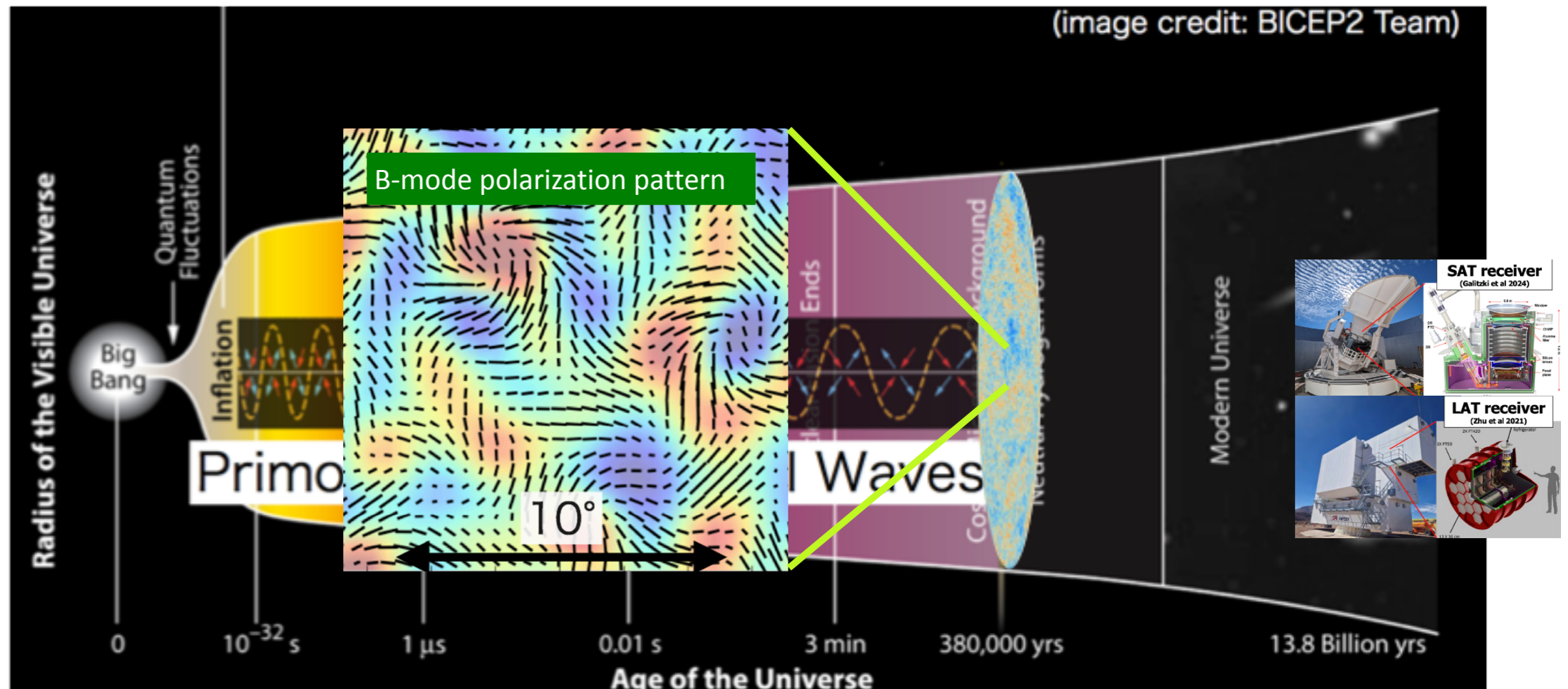
- Oldest observable photons from the early universe at the age of 380,000 years.
 - Polarization pattern
-

CMB inflationary B-mode polarization



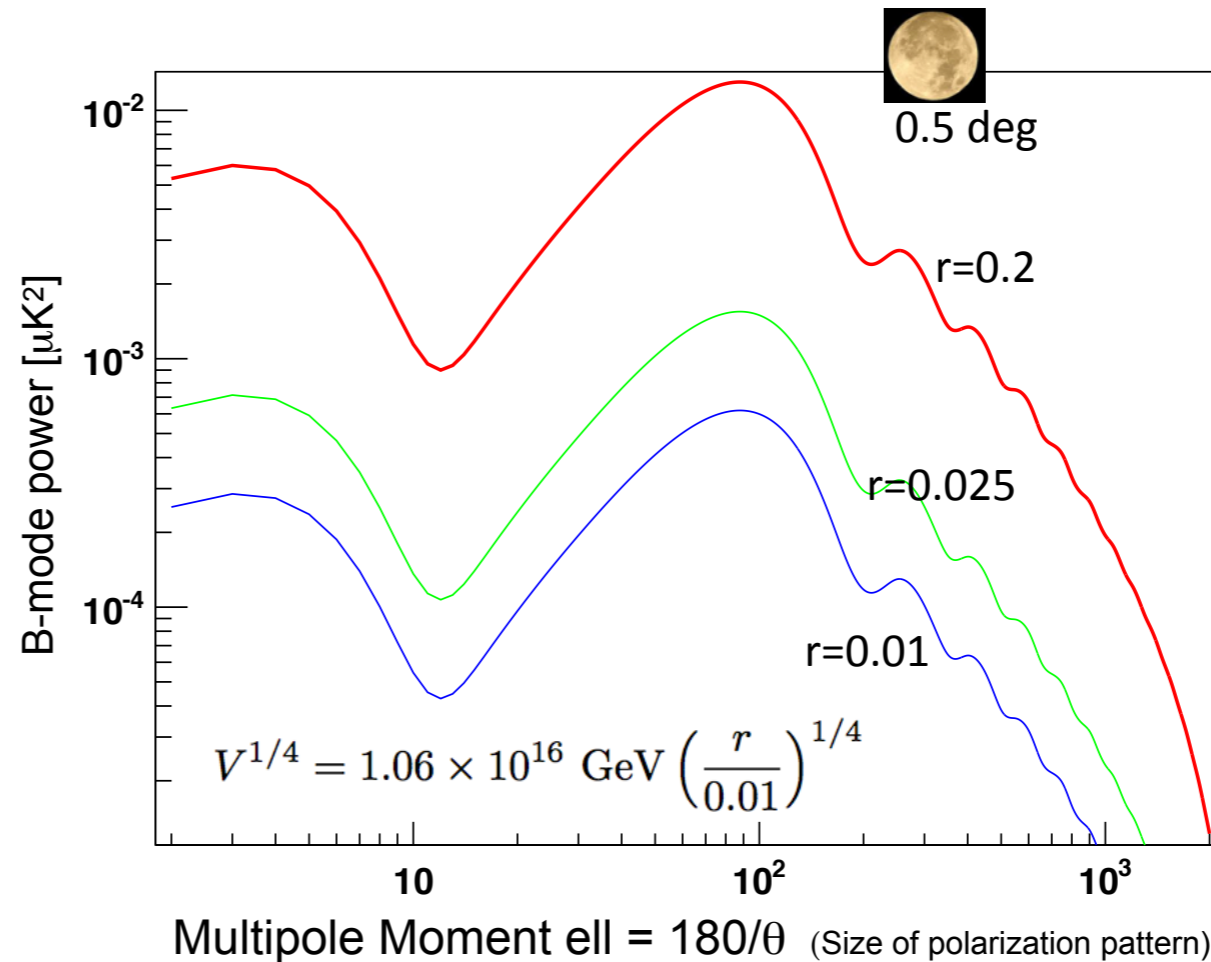
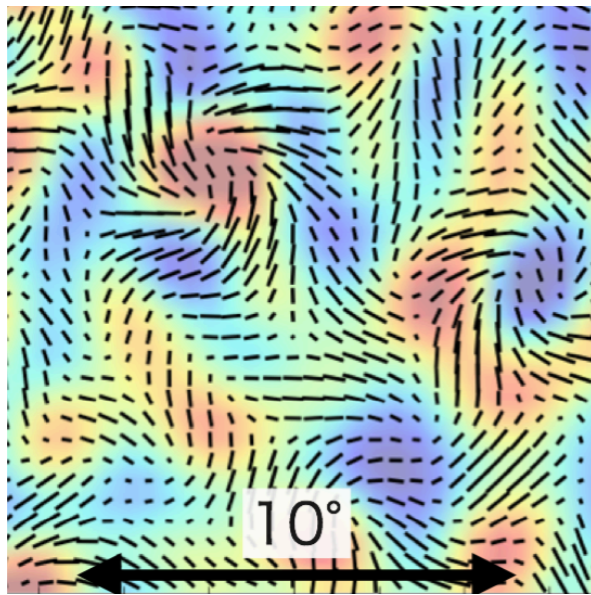
predicted to be imprinted as degree-scale
rot-like polarization pattern (B-mode)

CMB inflationary B-mode polarization



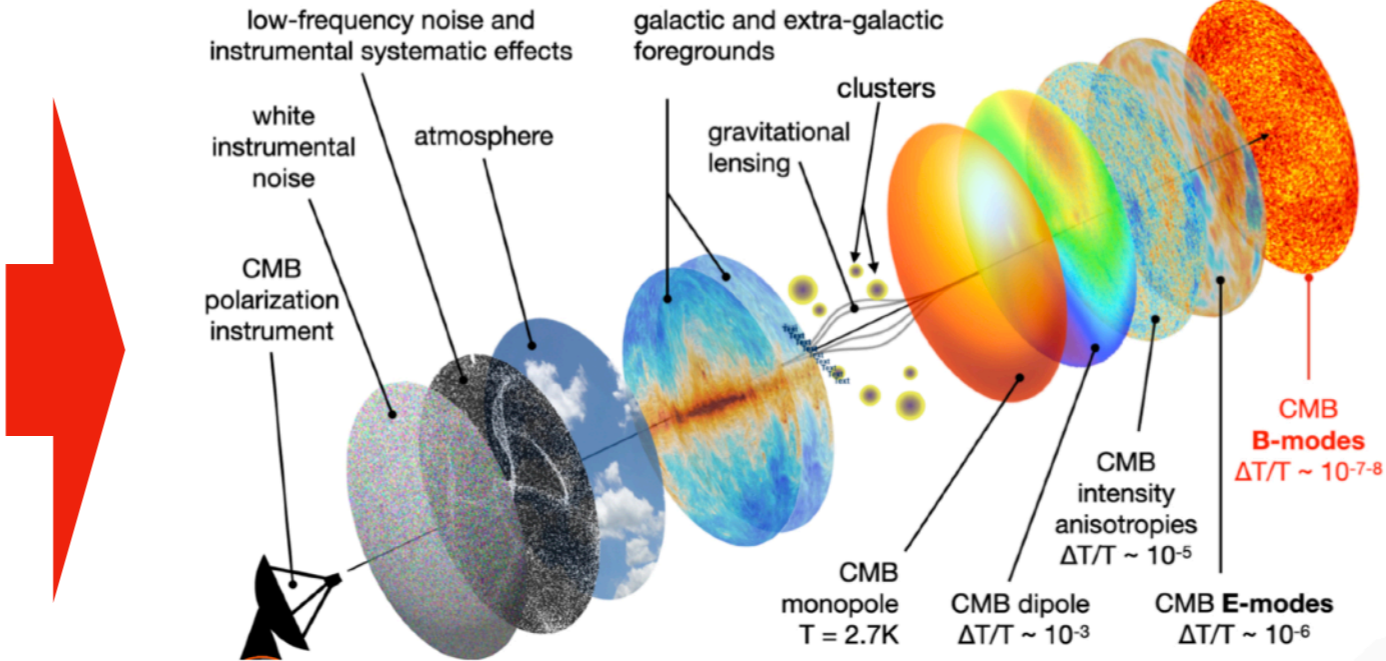
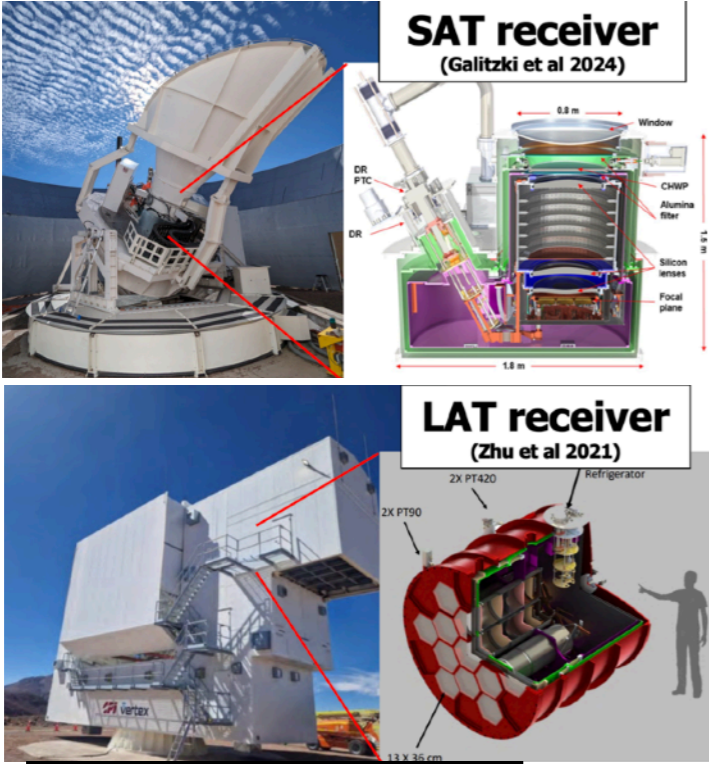
predicted to be imprinted as degree-scale
rot-like polarization pattern (B-mode)

CMB inflationary B-mode



CMB B-mode can be a probe of physics of ultra high energy scale (\sim GUT scale)!

Science of Simons Observatory

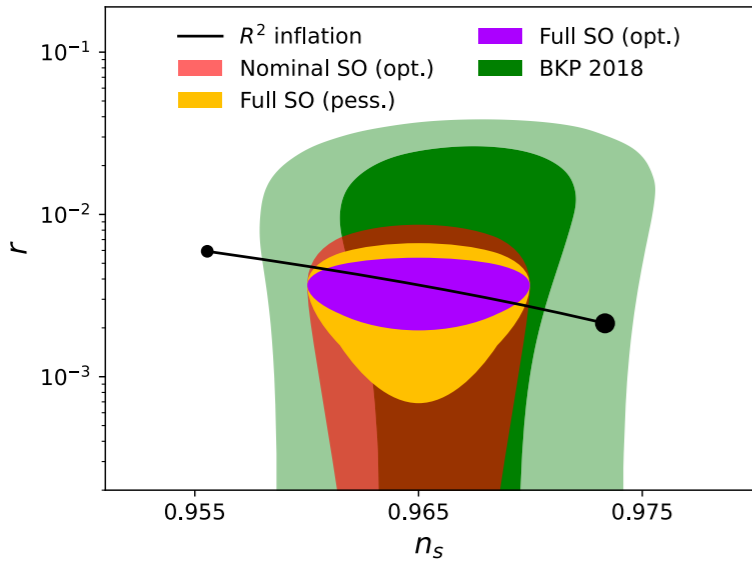


Credit: J. Errard

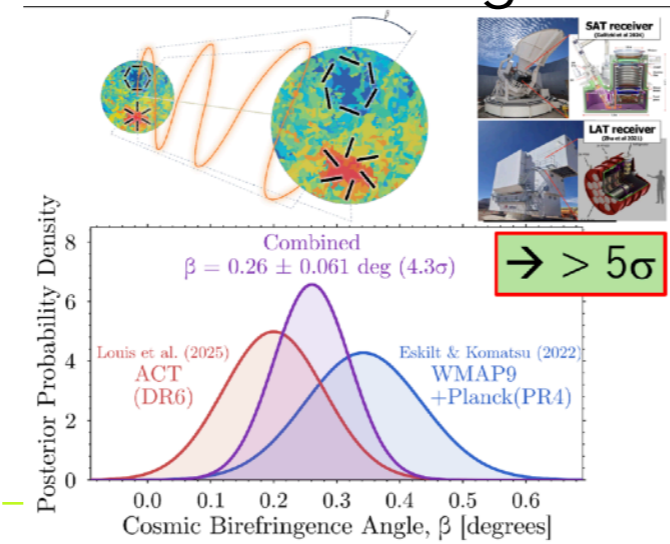
B-mode analysis

Test of standard model with CMB, GW, LSS data

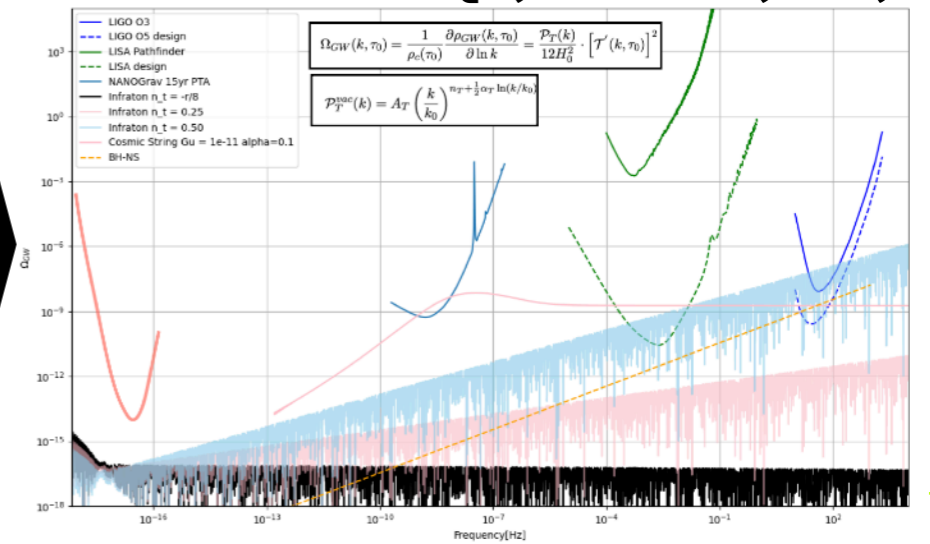
Inflation model



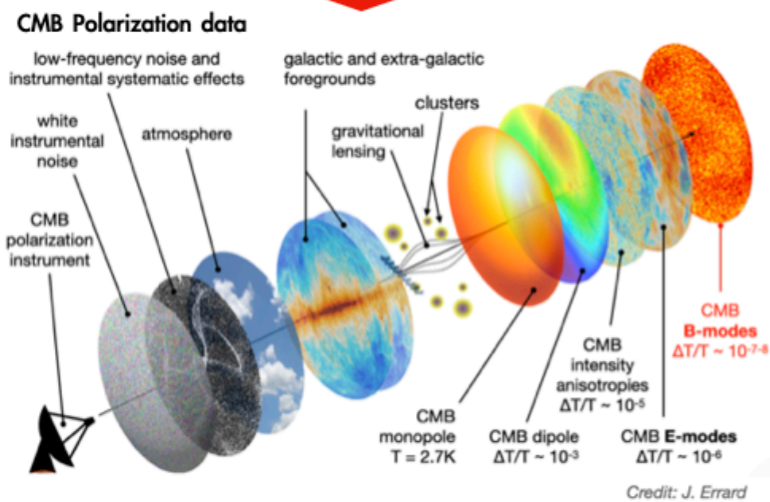
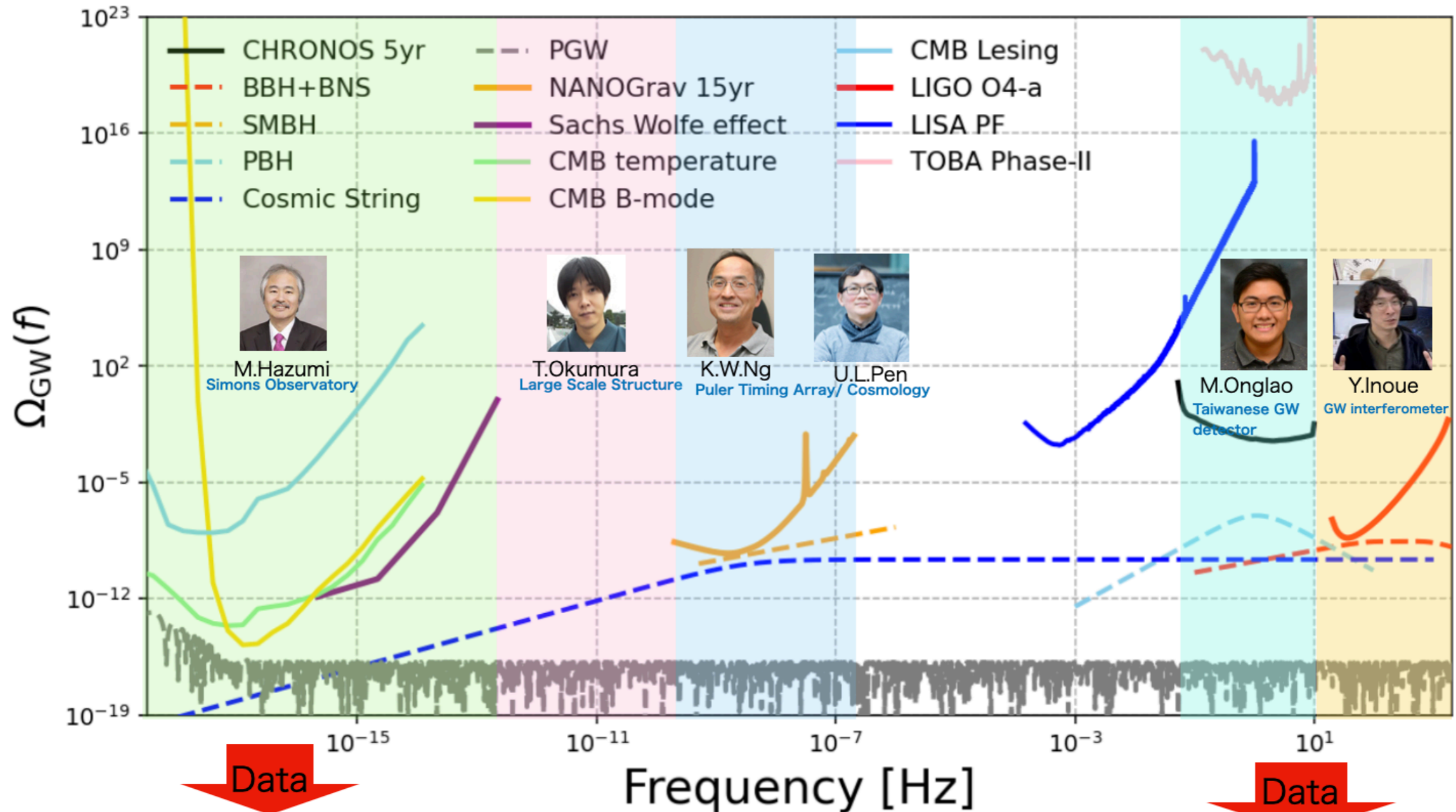
Cosmic Birefringence



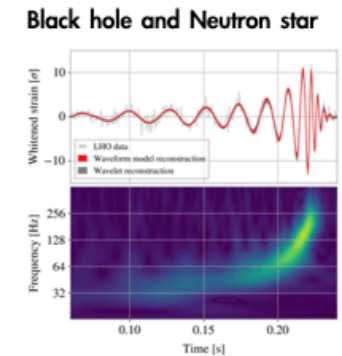
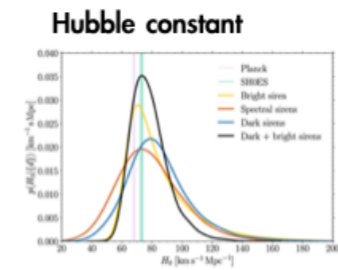
Λ -DCM + {r, $\Sigma m_\nu, n_t, \dots$ }



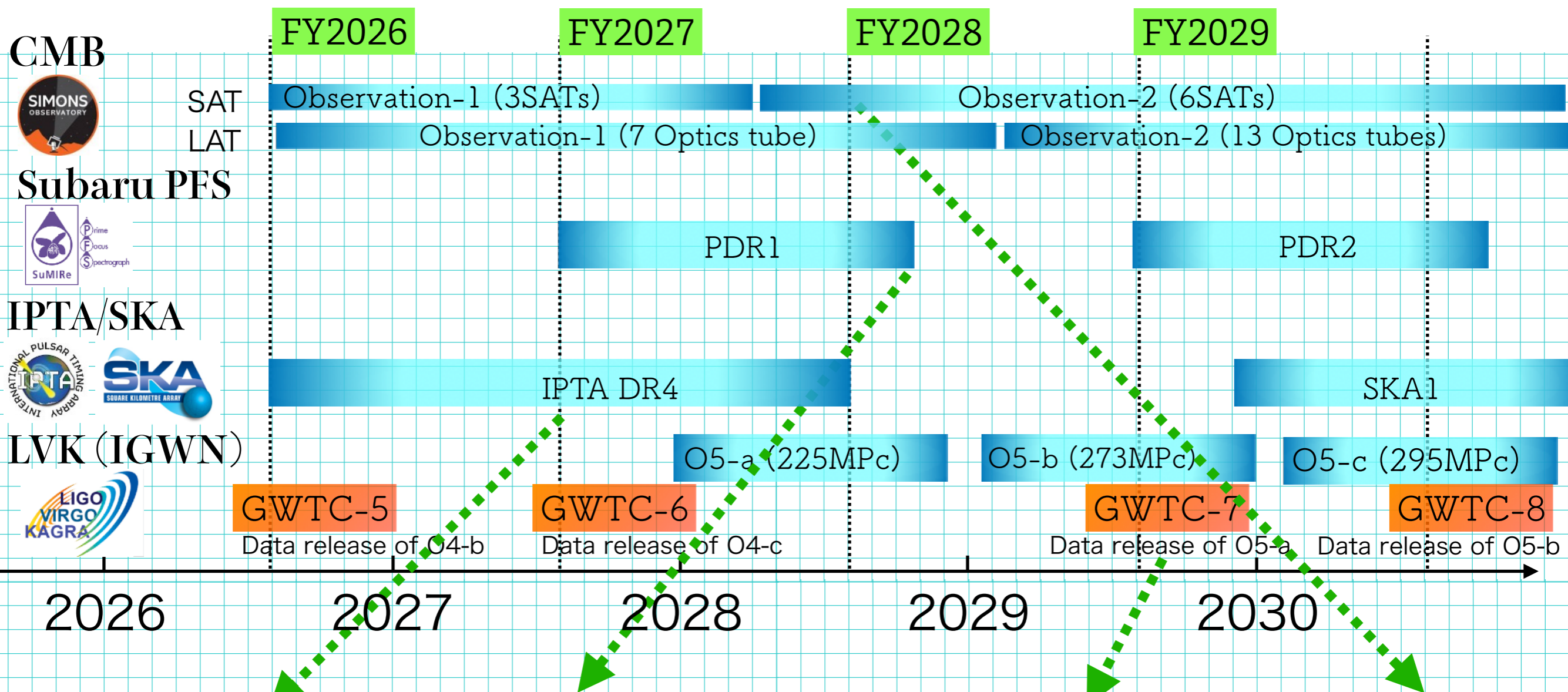
Team Taiwan



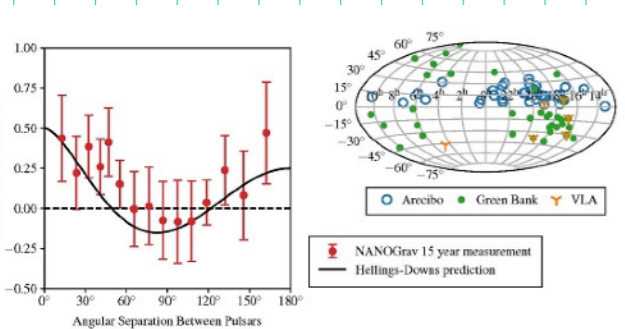
Frequency [Hz]



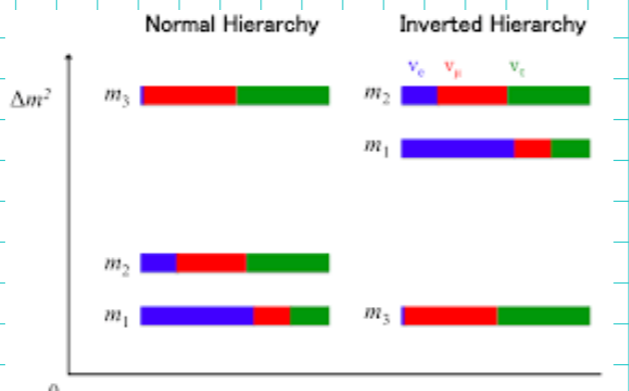
The golden age of Observational Cosmology - Expected high impact sciences-



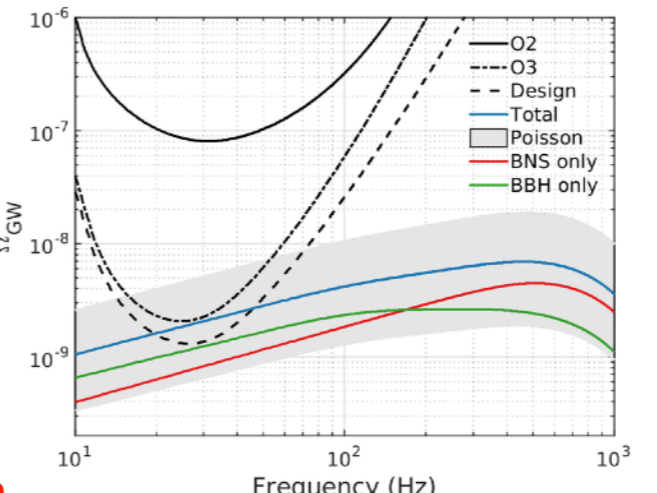
IPTA(nano-Hz) Subaru PFS(pico-Hz) LIGO (20-5000Hz) CMB B-mode



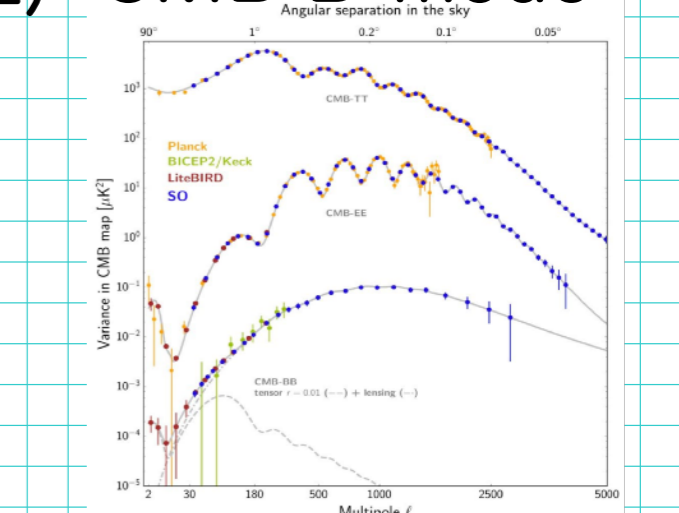
5-sigma detection of SGWB(nHz)



Expected to solve Neutrino Hierarchy problem



First detection of ASGWB b/w 20-5000Hz



First detection of B-mode

Summary

- National Central University promotes multi-band SGWB observations using CMB experiments, CHRONOS, and LIGO Gravitational wave detector.
 - These experiments probe different GW frequency bands and different epochs of the Universe.
 - CHRONOS fills the frequency gap between space observations and ground-based interferometers.
 - Combined observations enable broadband studies of $\Omega_{\text{GW}}(f)$ from primordial to astrophysical origins.
 - Multi-band GW cosmology provides a new probe of inflation, cosmic history, and fundamental physics.
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