

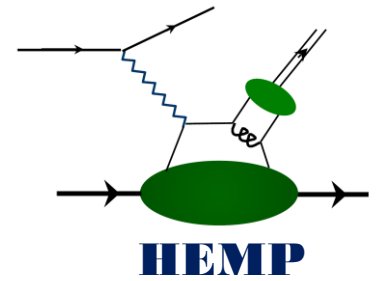
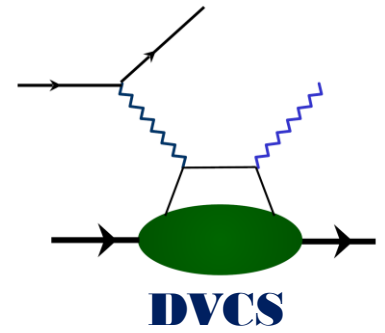
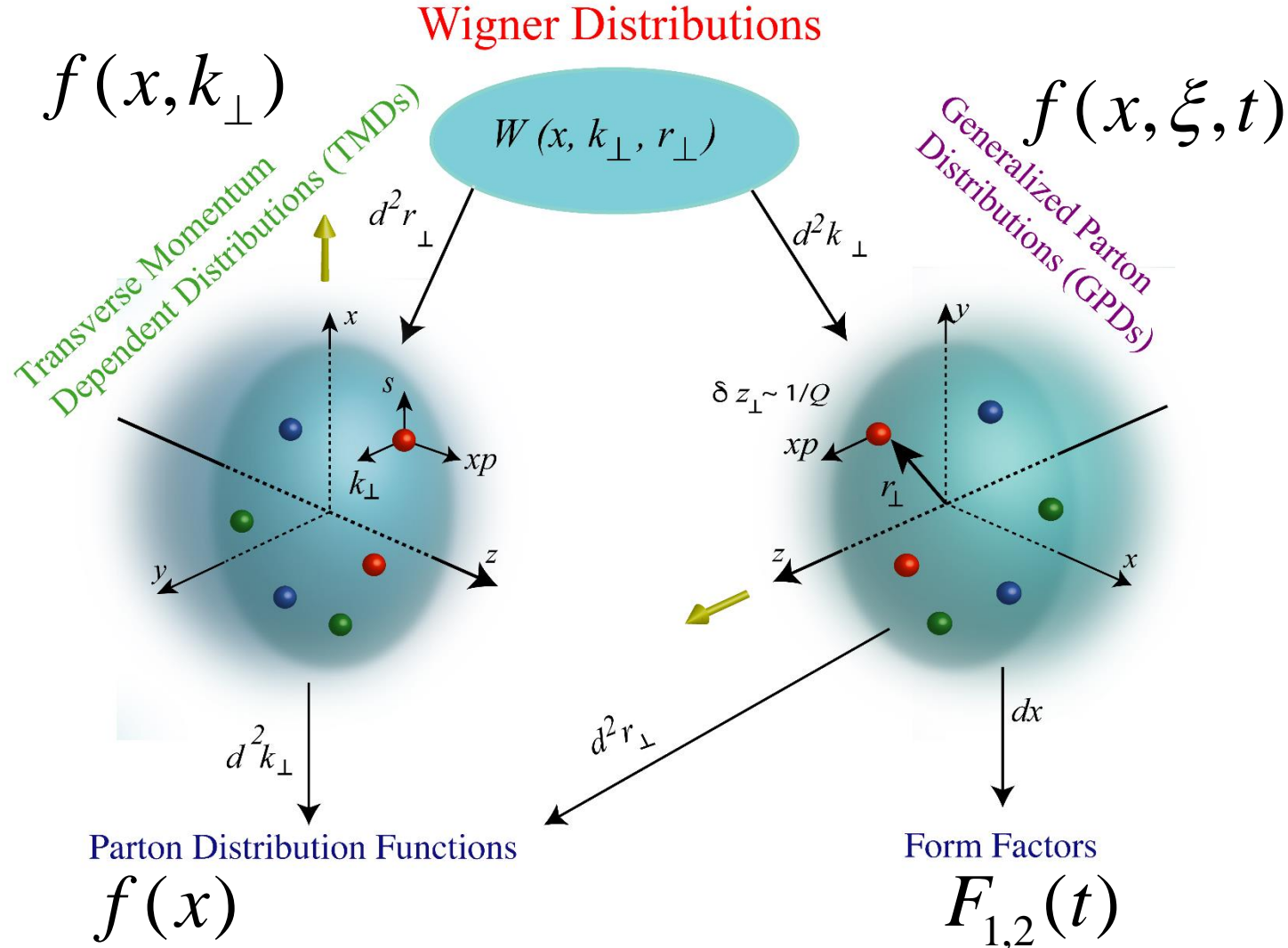
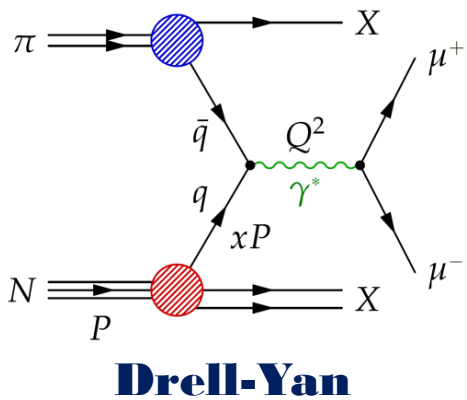
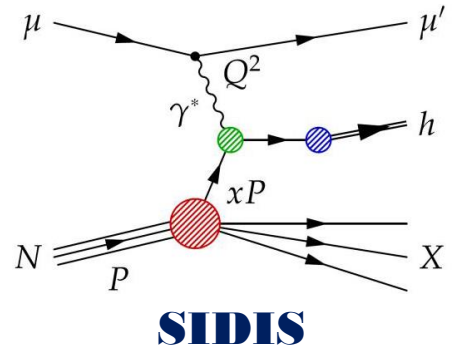


Hadron Structure Studies at the COMPASS Experiment

The 3rd EIC Asia Workshop
National Cheng Kung University
January 29, 2024

Po-Ju Lin
Department of Physics, National Central University

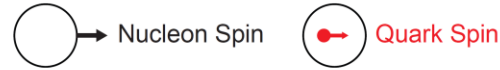
Multi-dimensional Partonic Structures



Parallelism between TMDs and GPDs



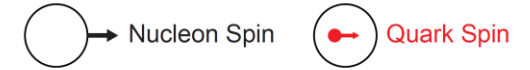
Transverse momentum k_T not shown



Eight TMDs

		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \text{Unpolarized}$		$h_1^\perp = \text{Boer-Mulders}$
	L		$g_1 = \text{Helicity}$	$h_{1L}^\perp = \text{Worm-gear}$
	T	$f_{1T}^\perp = \text{Sivers}$	$g_{1T}^\perp = \text{Worm-gear}$	$h_1 = \text{Transversity}$ $h_{1T}^\perp = \text{Pretzelosity}$

Eight GPDs



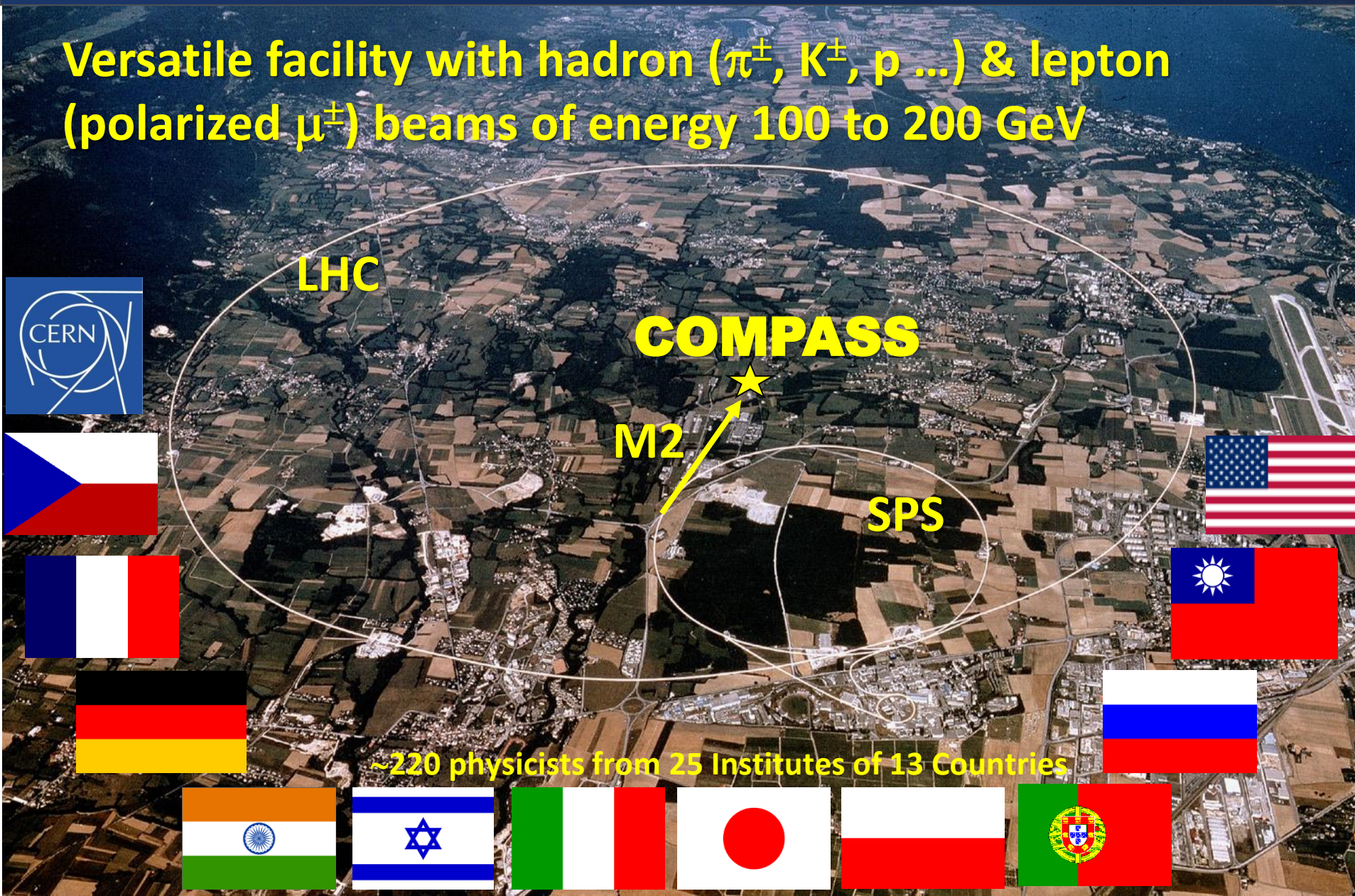
		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	H		$\bar{E}_T = 2\tilde{H}_T + E_T$
	L		\tilde{H}	E_T
	T	E	\tilde{E}	H_T, \tilde{H}_T

4 chiral-even, 4 chiral-odd, 2 T-odd

COMPASS Experiment



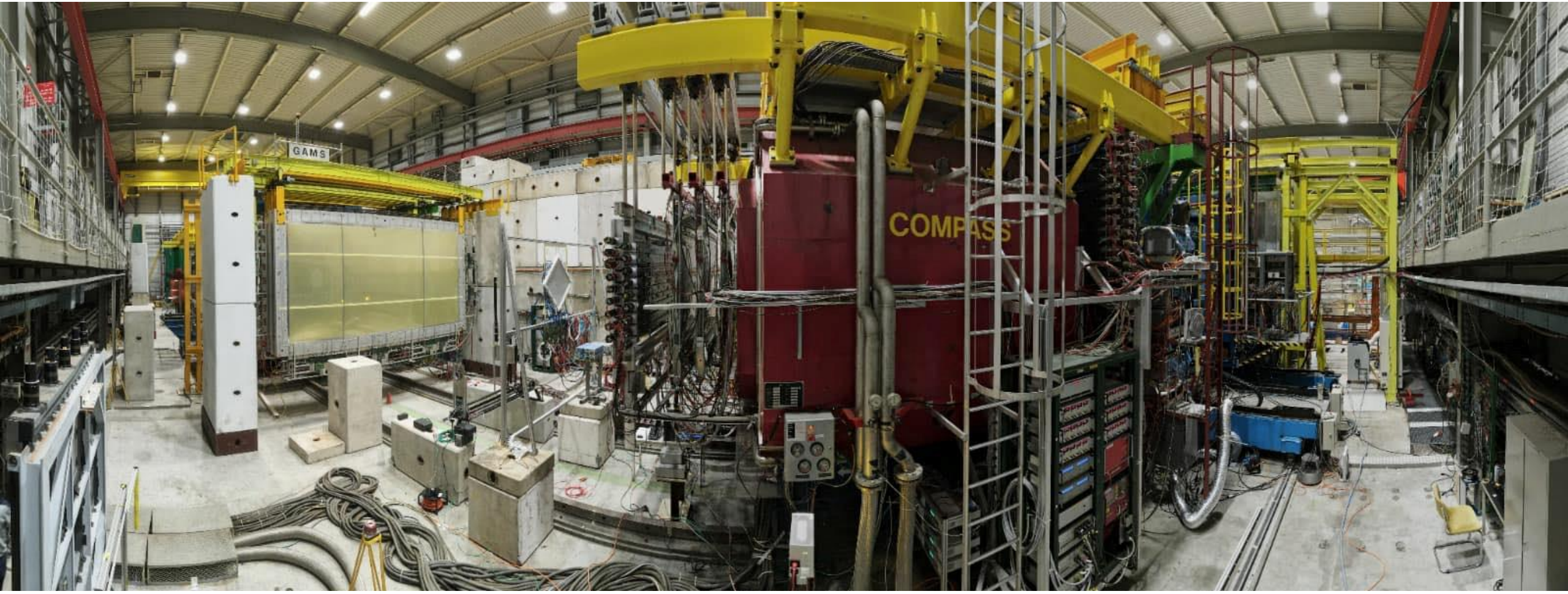
Versatile facility with hadron (π^\pm , K^\pm , p ...) & lepton (polarized μ^\pm) beams of energy 100 to 200 GeV



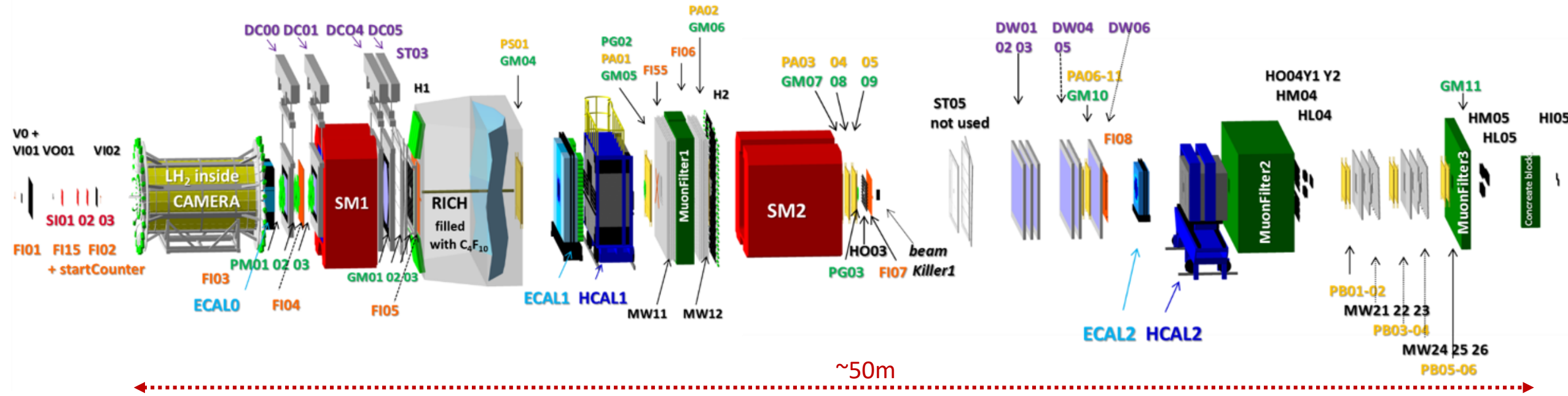
COmmun
Muon and
Proton
Apparatus for
Structure and
Spectroscopy

~220 physicists from 25 Institutes of 13 Countries

COMPASS Experimental Setup



COMPASS Experimental Setup



- Primary beam – 400 GeV p from SPS
 - Impinging on Be production target
- 190 GeV secondary hadron beams
 - h^- beam: 97% π^- , 2% K^- , 1% p
 - h^+ beam: 75% π^+ , 24% p, 1% K^+
- 160 GeV tertiary muon beams
 - μ^\pm longitudinally polarized

Large-acceptance forward spectrometer

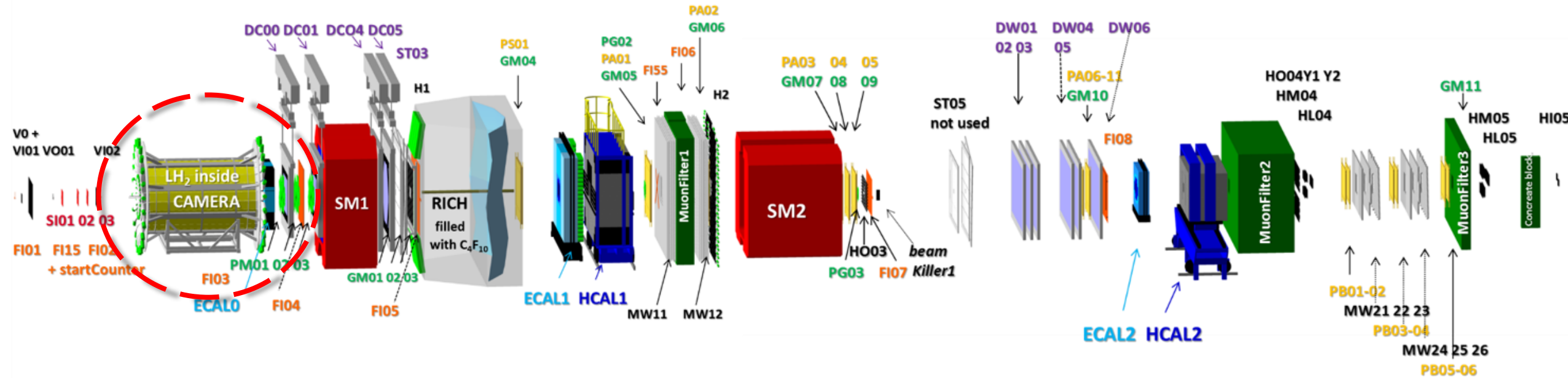
- Precise tracking (350 planes)
SciFi, Silicon, MicroMegas, GEM, MWPC, DC, straw
- PID – CEDARs, RICH, calorimeters, Muon Walls

Various targets:

- Polarized solid-state NH_3 or ^6LiD
- Liquid H_2
- Solid-state nuclear targets

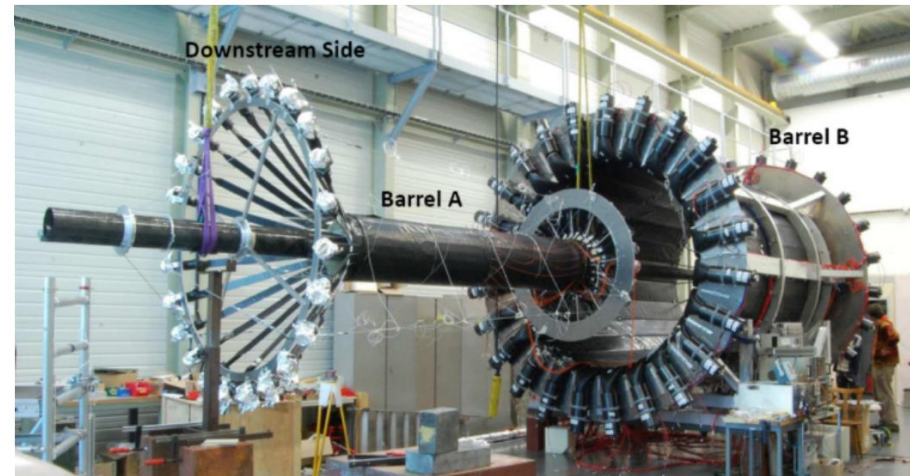
❖ NIM A 577 (2007) & NIM A 779 (2015) 69

COMPASS Setup for Exclusive Processes



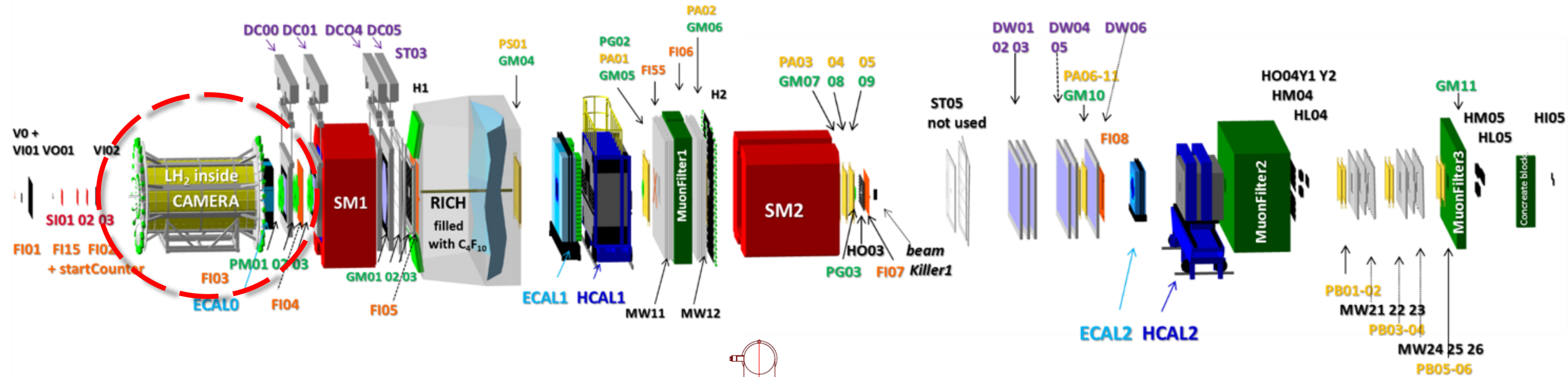
To ensure exclusivity:

- Primary beam – 400 GeV p from SPS
 - Impinging on Be production target
- 190 GeV secondary hadron beams
 - h^- beam: 97% π^- , 2% K^- , 1% p
 - h^+ beam: 75% π^+ , 24% p , 1% K^+
- 160 GeV tertiary muon beams
 - μ^\pm longitudinally polarized

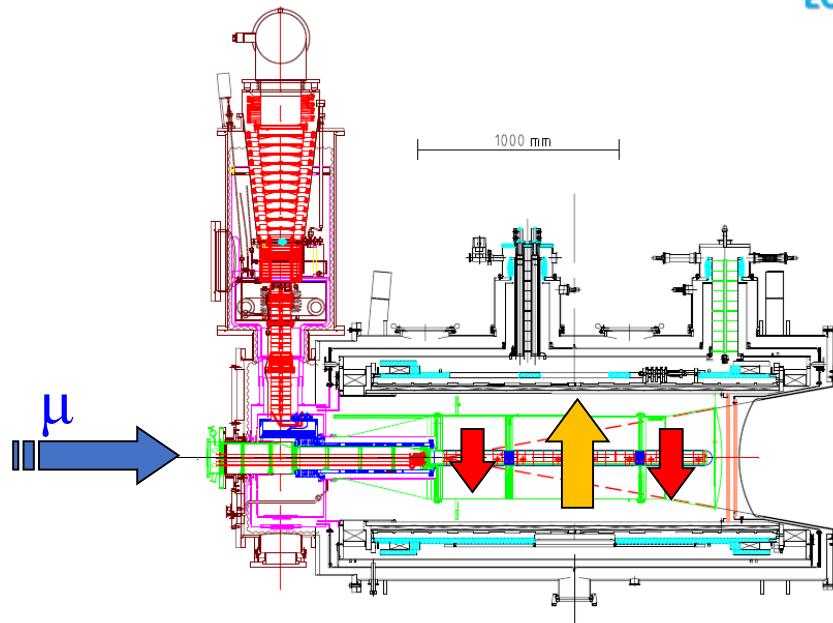


CAMERA recoil proton detector

COMPASS Setup for SIDIS

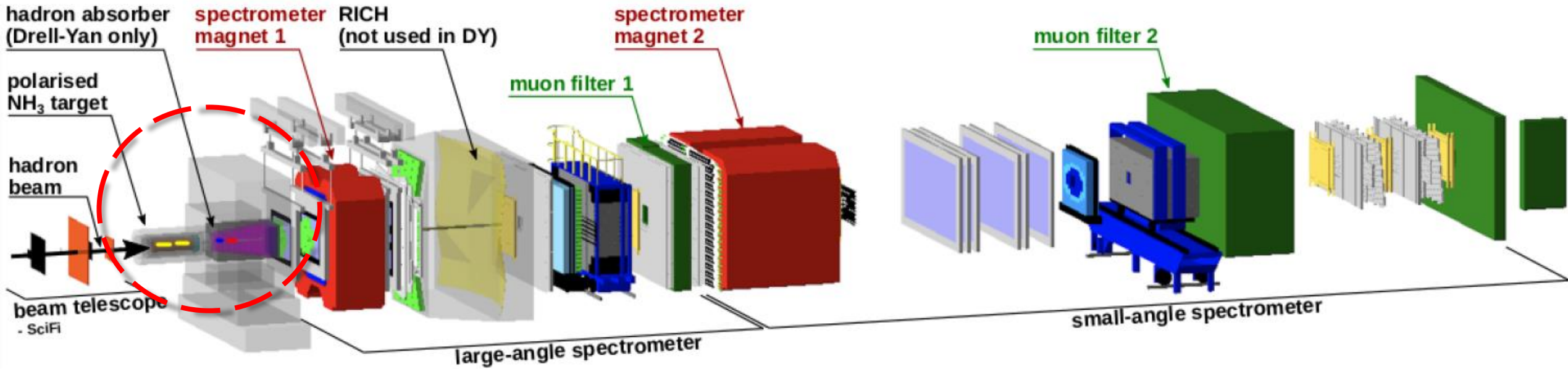


- Primary beam – 400 GeV p from SPS
 - Impinging on Be production target
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 - h^- beam: 97% π^- , 2% K^- , 1% p
 - h^+ beam: 75% π^+ , 24% p , 1% K^+
- 160 GeV tertiary muon beams
 - μ^\pm longitudinally polarized

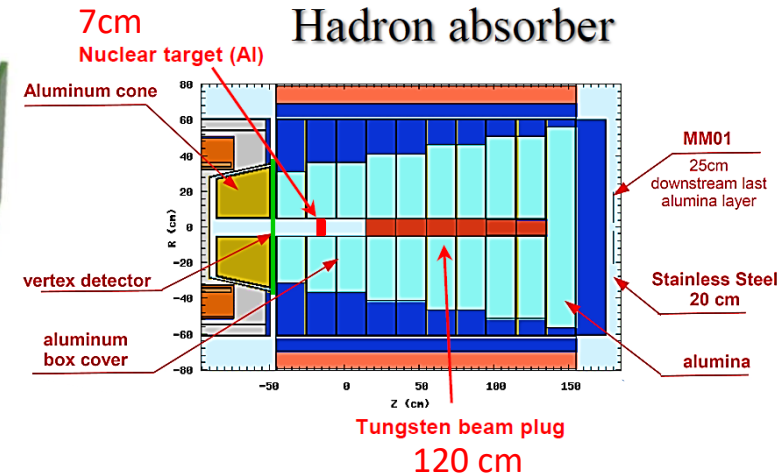
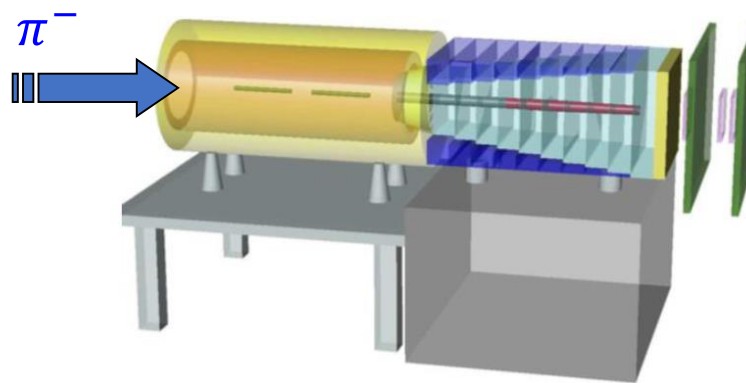


- Target polarized or unpolarized
 - ${}^6\text{LiD}$ $\sim 50\%$
 - NH_3 $\sim 85\%$
- 2 or 3 oppositely polarized cells
 - Polarization reversal by magnetic field rotation

COMPASS Setup for Drell-Yan



- Primary beam – 400 GeV p from SPS
 - Impinging on Be production target
- 190 GeV secondary hadron beams
 - h^- beam: 97% π^- , 2% K^- , 1% p
 - h^+ beam: 75% π^+ , 24% p , 1% K^+
- 160 GeV tertiary muon beams
 - μ^\pm longitudinally polarized



COMPASS Experiment



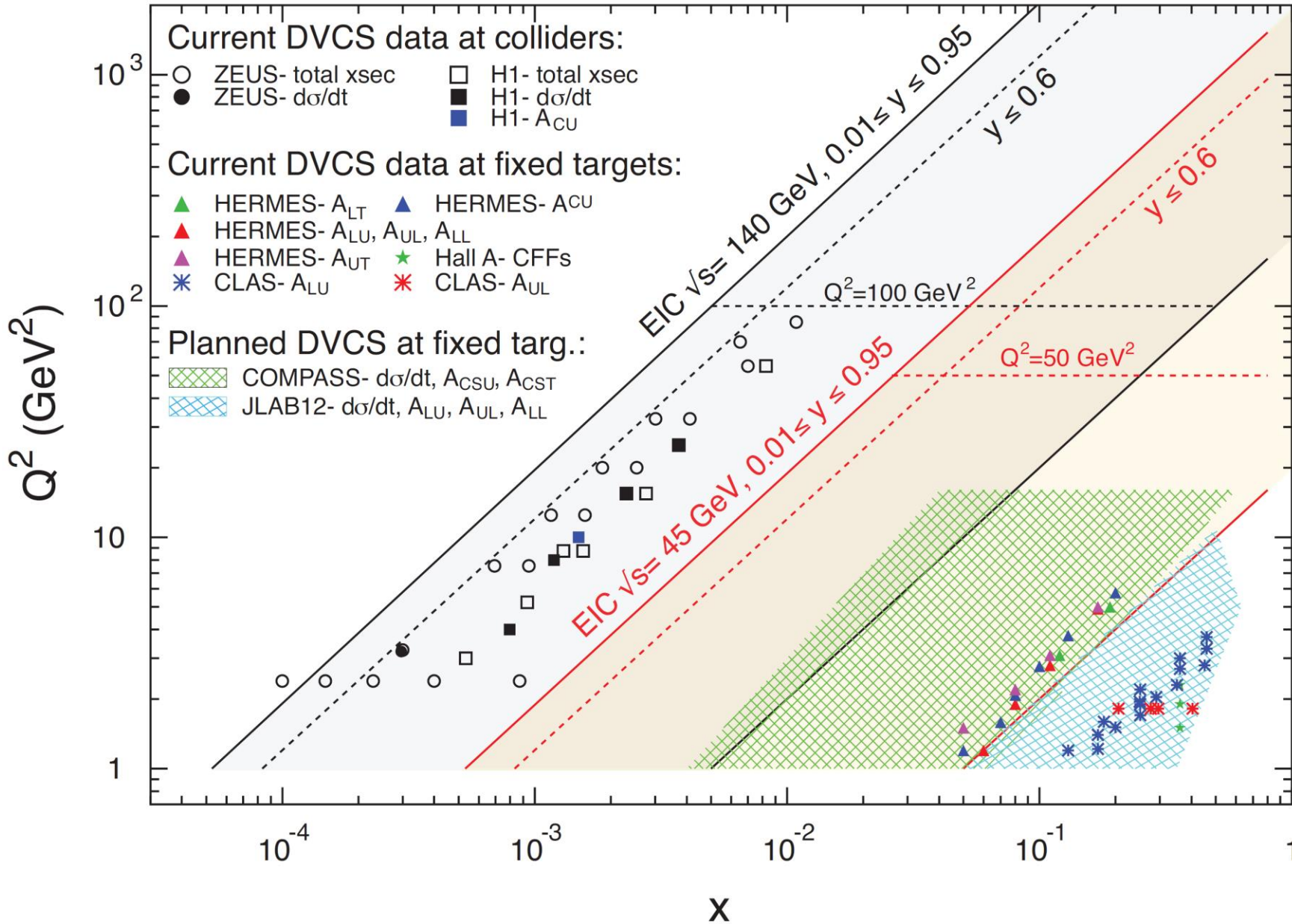
2002-2022 COMPASS data taking

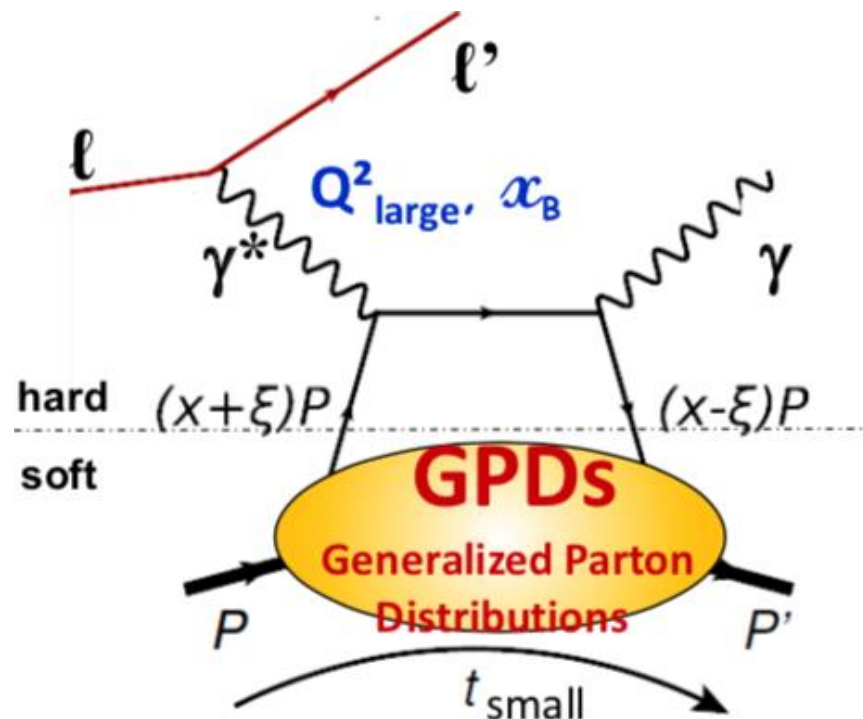
2002-2004	DIS & SIDIS, μ^+ - d , 160 GeV, L & T polarized target
2005	<i>CERN accelerator shutdown, increase of COMPASS acceptance</i>
2006	DIS & SIDIS, μ^+ - d , 160 GeV, L polarized target
2007	DIS & SIDIS, μ^+ - p , 160 GeV, L & T polarized target
2008-2009	Hadron spectroscopy & Primakoff reaction, π /K/p beam
2010	SIDIS, μ^+ - p , 160 GeV, T polarized target
2011	DIS & SIDIS, μ^+ - p , 200 GeV, L polarized target
2012	Primakoff reaction, π /K/p beam
2012 pilot run	DVCS/HEMP/SIDIS, μ^+ & μ^- - p , 160 GeV, unpolarized target
2013	<i>CERN accelerator shutdown, LS1</i>
2014-2015	Drell-Yan, π^- - p , T polarized target
2016-2017	DVCS/HEMP/SIDIS, μ^+ & μ^- - p , 160 GeV, unpolarized target
2018	Drell-Yan, π^- - p , T polarized target
2019-2020	<i>CERN accelerator shutdown, LS2</i>
2021-2022	SIDIS, μ^+ - d , 160 GeV, T polarized target

Study hadron structure with complementary tools:

- **COMPASS holds the record for the longest-running CERN experiment**
- Unpolarized or L/T polarized targets
- Polarized muon beams for DIS, SIDIS, DVCS, DVMP
- Hadron beams for hadron spectroscopy and Drell-Yan

Landscape – Global Programs of DVCS





DVCS: $l + p \rightarrow l' + p' + \gamma$

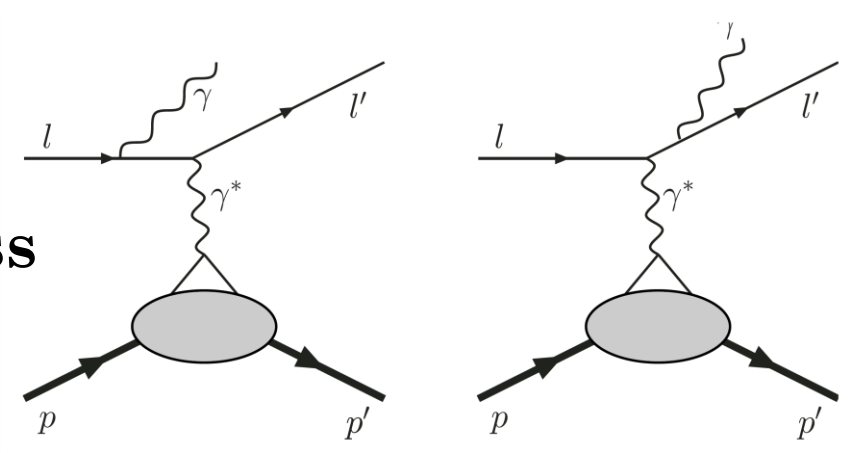
To experimentally access the information about Generalized Parton Distributions (GPDs), DVCS is regarded as the golden channel and its interference with the well-understood Bethe-Heitler process gives access to more info.

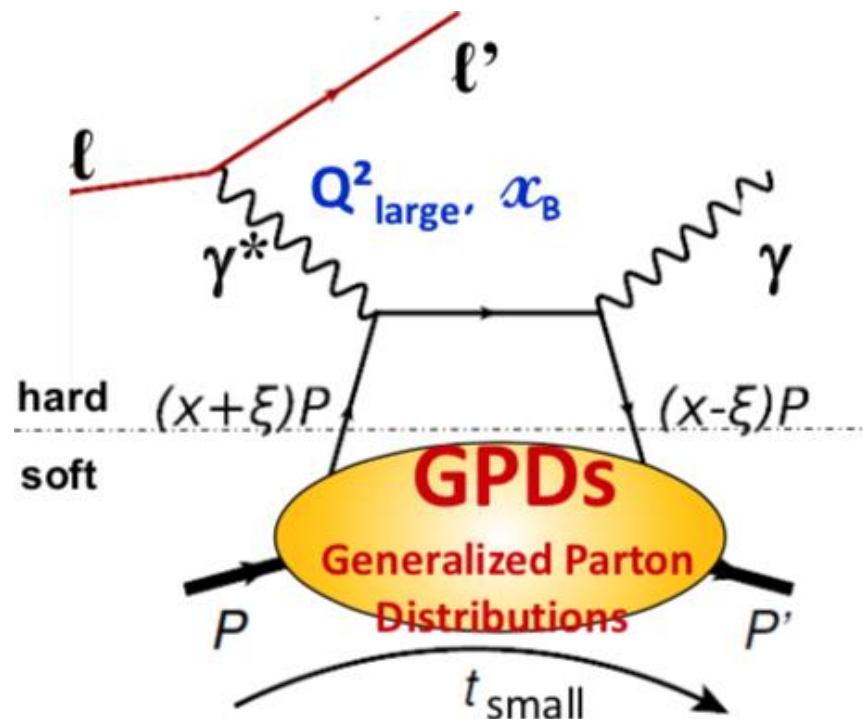
The variables measured in the experiment:

$$E_l, Q^2, x_{Bj} \sim 2\xi / (1+\xi),$$

$$t \text{ (or } \theta_{\gamma^*\gamma}) \text{ and } \phi \text{ (} \ell\ell' \text{ plane}/\gamma\gamma^* \text{ plane)}$$

BH Process





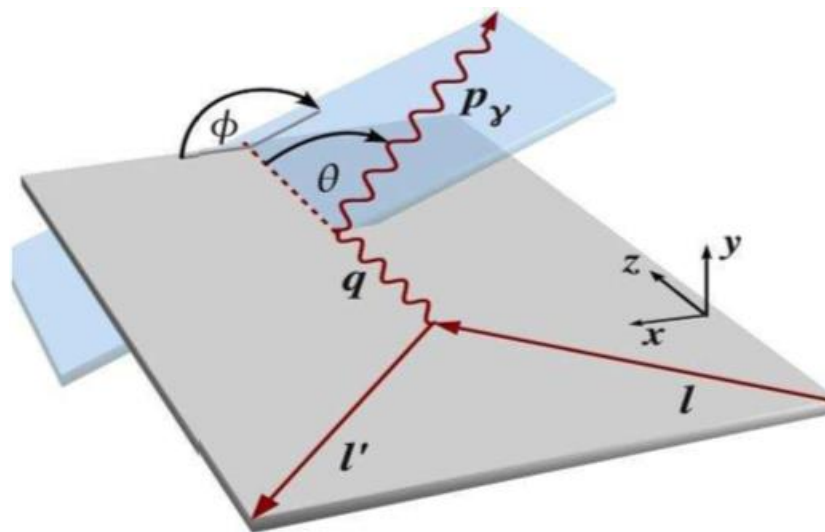
$$\text{DVCS: } l + p \rightarrow l' + p' + \gamma$$

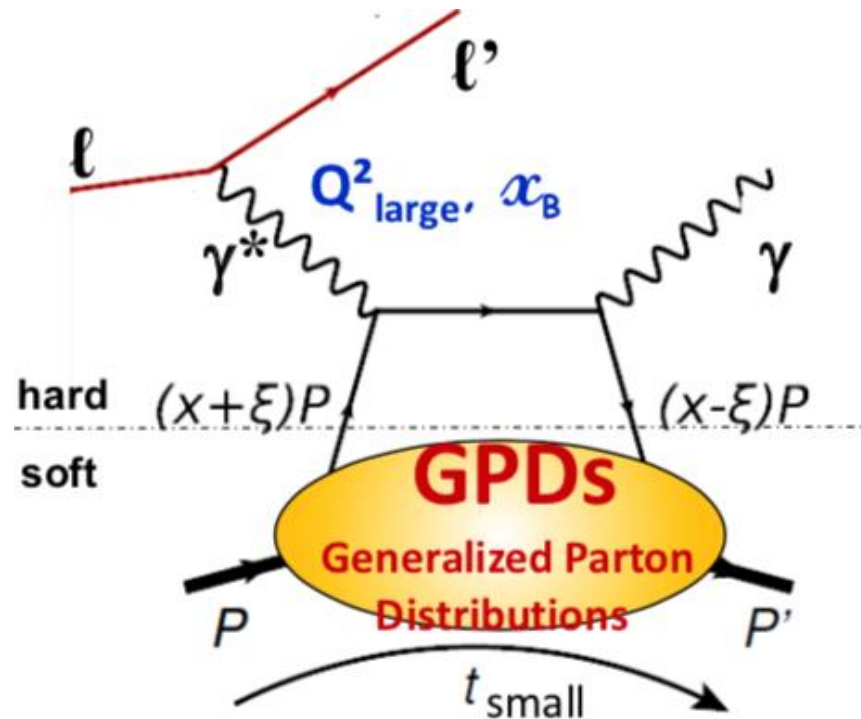
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$$E_l, Q^2, x_{Bj} \sim 2\xi / (1+\xi),$$

$$t \text{ (or } \theta_{\gamma^*\gamma}) \text{ and } \phi \text{ (} l l' \text{ plane}/\gamma\gamma^* \text{ plane)}$$





➤ The GPDs depend on the following variables:

x : average longitudinal momentum frac.

ξ : longitudinal momentum diff.

t : four momentum transfer

(correlated to b_{\perp} via Fourier transform)

Q^2 : virtuality of γ^*

Sensible to 4 GPDs, with LH_2 target and small x_B coverage

→ focuses on H at COMPASS

CFE → $\mathcal{H}(\xi, t)$
GPD → $\int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi + i\epsilon} + \dots$

$$\mathcal{H}(\xi, t) = \int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi + i\epsilon} + \dots = \mathcal{P} \int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi} - i\pi \mathbf{H}(x = \pm \xi, \xi, t) + \dots$$

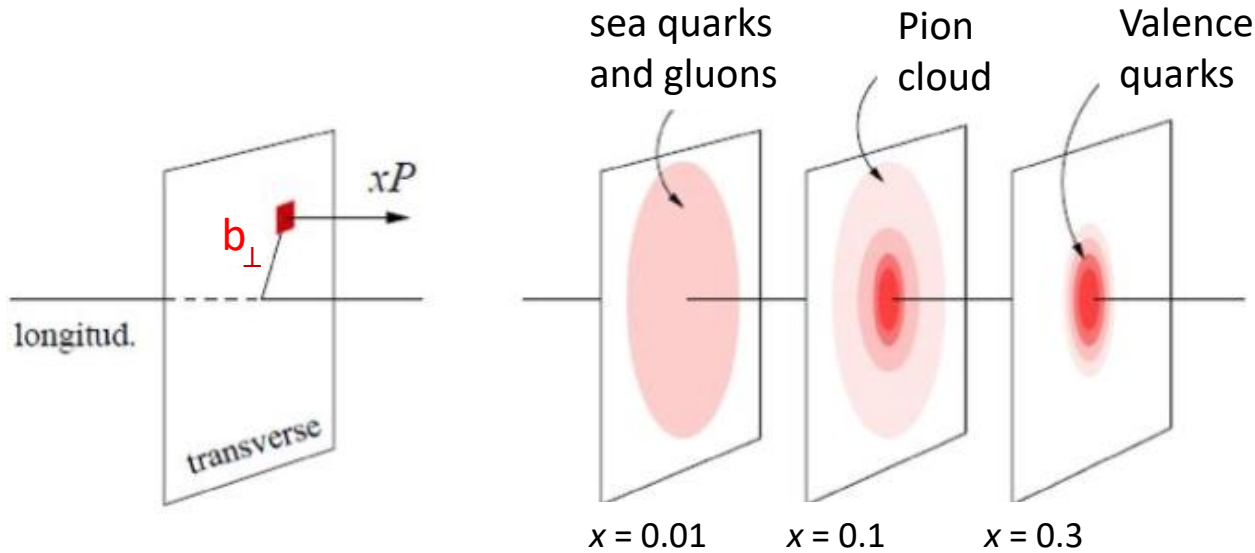
REAL part

Imaginary part

$$\text{Re } \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\text{Im } \mathcal{H}(x, t)}{x - \xi} + \Delta(t)$$

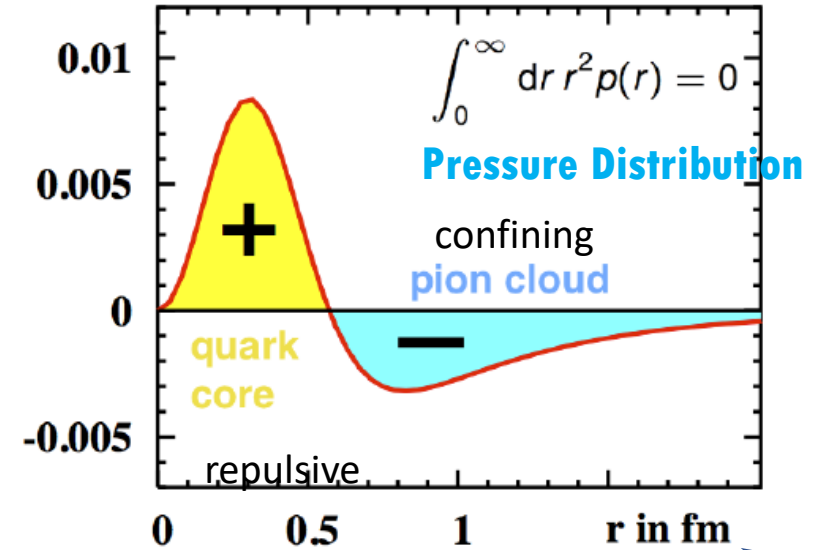
Transverse Imaging and Pressure Distribution

Mapping in the transverse plane



M. Polyakov, P. Schweitzer, *Int.J.Mod.Phys. A33* (2018)

$r^2 p(r)$ in GeV fm^{-1}



$\overset{GPD}{\mathcal{H}(\xi, t)} = \int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi + i\epsilon} + \dots = \mathcal{P} \int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi} - i\pi \mathbf{H}(x = \pm \xi, \xi, t) + \dots$

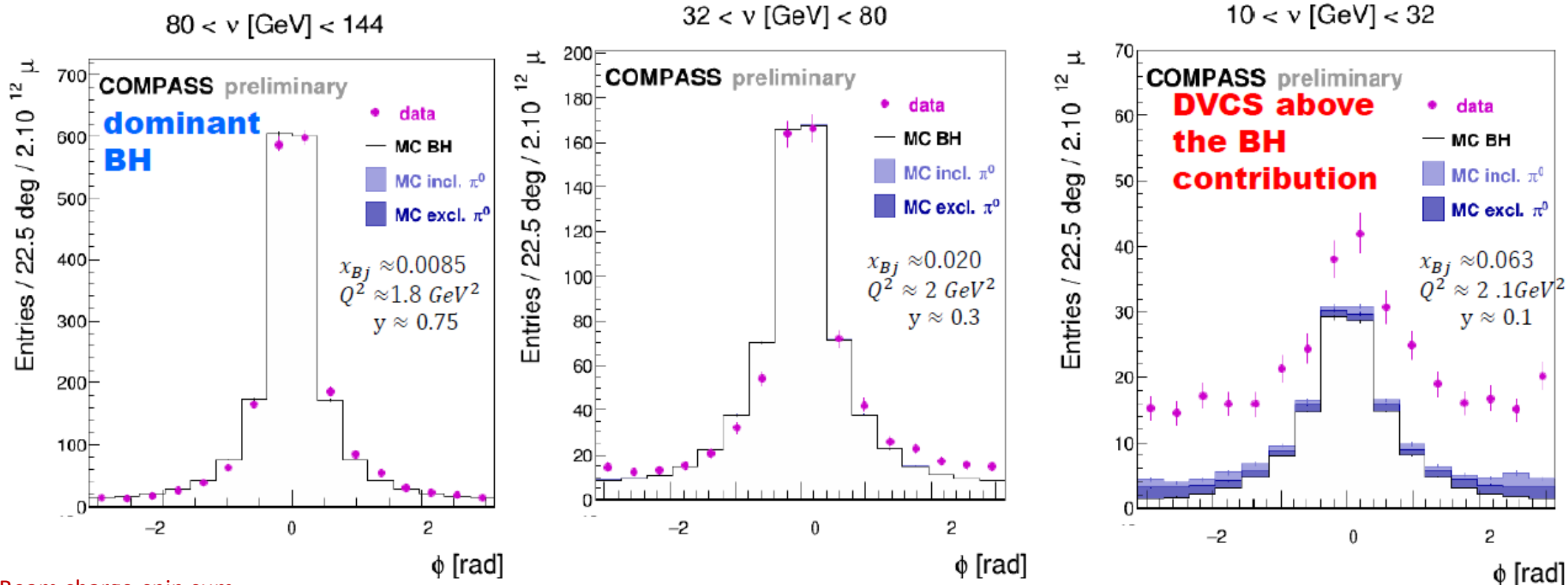
$\text{REAL part} \quad \text{Imaginary part}$

$\text{Re } \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\text{Im } \mathcal{H}(x, t)}{x - \xi} + \Delta(t)$

$\Delta(t) \equiv d_{1/2}(t)$ (D-term)

$\leftarrow \text{FT of } H(x, \xi=0, t)$

COMPASS 2016 Preliminary Results



➤ Beam charge-spin sum

$$\begin{aligned}
 S_{CS, U}(\phi) &\equiv d\sigma(\mu^{+\leftarrow}) + d\sigma(\mu^{-\rightarrow}) = 2[d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + \text{Im } I] \\
 &= 2[d\sigma^{BH} + c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi + s_1^I \sin \phi + s_2^I \sin 2\phi]
 \end{aligned}$$

$$c_0^{DVCS} \underset{\text{small } x_{Bj}}{\propto} 4(\mathcal{H}\mathcal{H}^* + \tilde{\mathcal{H}}\tilde{\mathcal{H}}^*) + \frac{t}{M^2} \mathcal{E}\mathcal{E}^* \rightarrow 4 (\text{Im } \mathcal{H})^2 \underset{\text{model dependent}}{}$$

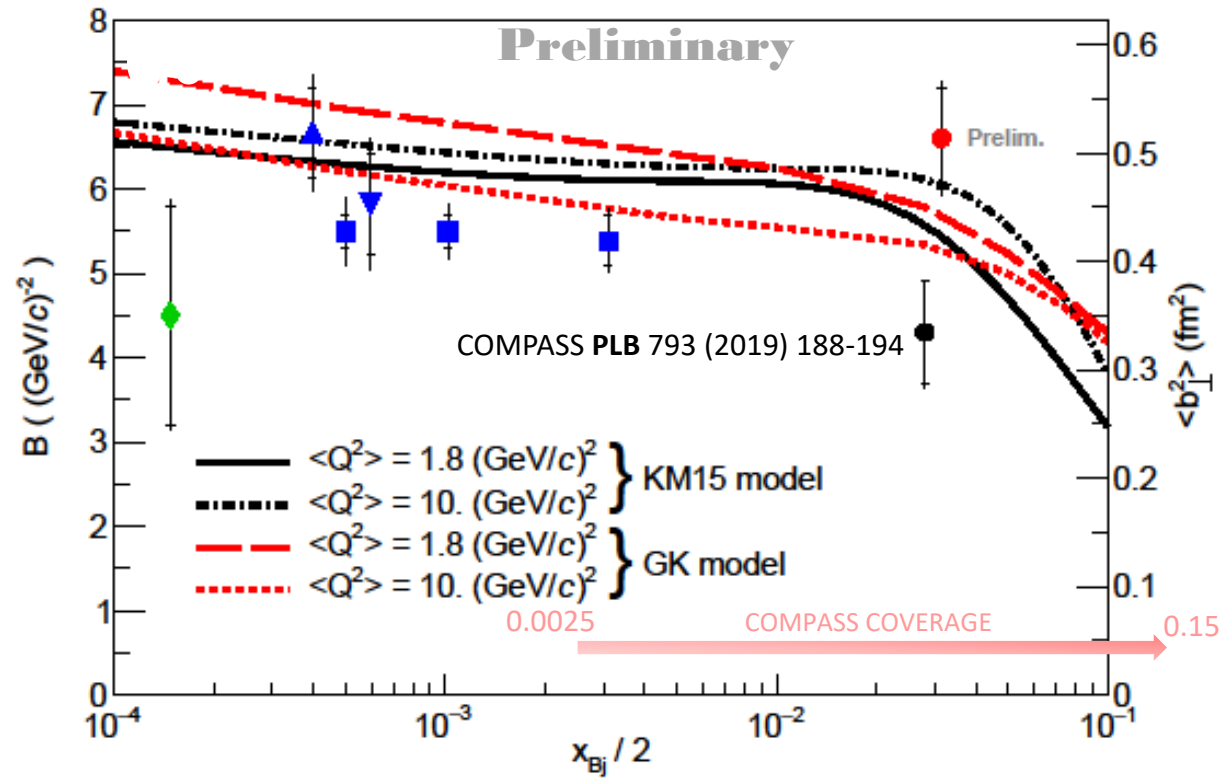
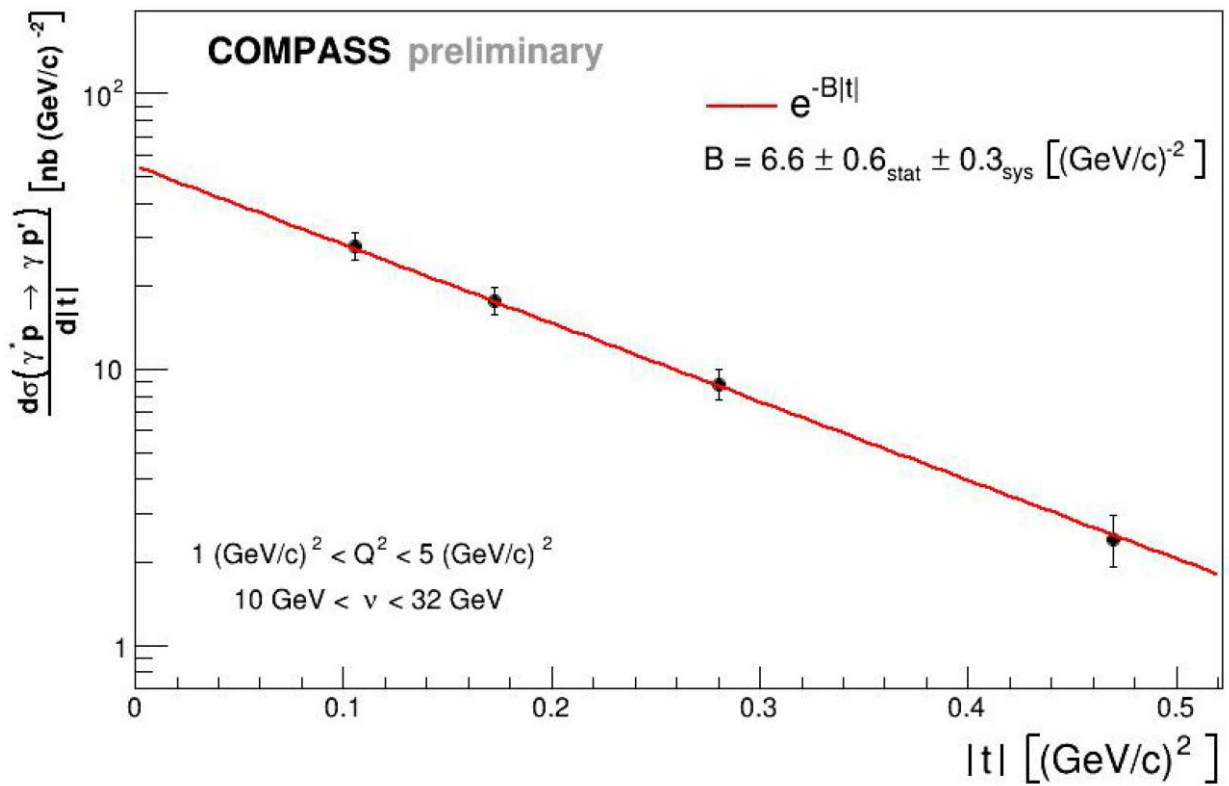
Transverse extension of partons – 2016 data



$$d\sigma^{DVCS}/d|t| \propto e^{-B|t|}$$

$$\langle r_{\perp}^2(x_B) \rangle \approx 2B(x_B) \text{ At small } x_B$$

- COMPASS: $\langle Q^2 \rangle = 1.8 \text{ (GeV/c)}^2$
- ◆ ZEUS: $\langle Q^2 \rangle = 3.2 \text{ (GeV/c)}^2$
- ▲ H1: $\langle Q^2 \rangle = 4.0 \text{ (GeV/c)}^2$
- ▼ H1: $\langle Q^2 \rangle = 8.0 \text{ (GeV/c)}^2$
- H1: $\langle Q^2 \rangle = 10. \text{ (GeV/c)}^2$

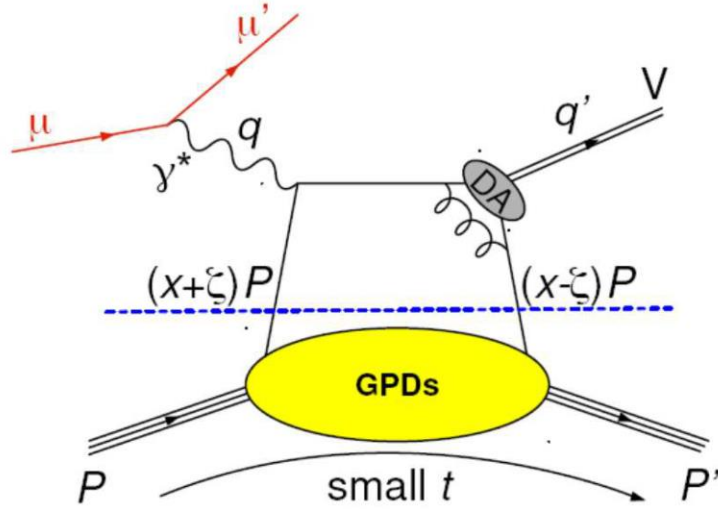


➤ The transverse-size evolution as a function of x_{Bj} → Expect at least 3 x_{Bj} bins from 2016-17 data

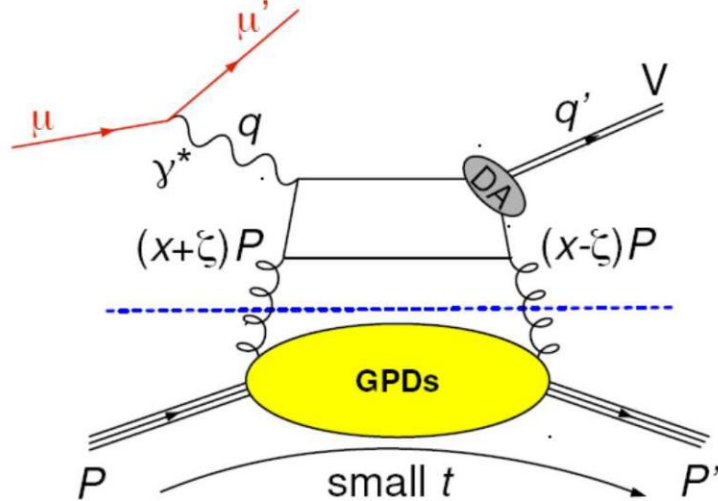
GPDs in Hard Exclusive Meson Production



quark contribution



gluon contribution



4 chiral-even GPDs: helicity of parton unchanged

$$\mathbf{H}^q(x, \xi, t) \quad \mathbf{E}^q(x, \xi, t) \quad \rightarrow \text{Vector Meson}$$

$$\tilde{\mathbf{H}}^q(x, \xi, t) \quad \tilde{\mathbf{E}}^q(x, \xi, t) \quad \rightarrow \text{Pseudo-Scalar Meson}$$

+ 4 chiral-odd or transversity GPDs: helicity of parton changed
(not possible in DVCS)

$$\mathbf{H}_T^q(x, \xi, t)$$

$$\mathbf{E}_T^q(x, \xi, t)$$

$$\tilde{\mathbf{H}}_T^q(x, \xi, t)$$

$$\tilde{\mathbf{E}}_T^q(x, \xi, t)$$

$$\bar{\mathbf{E}}_T^q = 2 \tilde{\mathbf{H}}_T^q + \mathbf{E}_T^q$$

- Universality of GPDs, quark flavor filter
- Ability to probe the chiral-odd GPDs.
- Additional non-perturbative term from meson wave function
- In addition to nuclear structure, provide insights into reaction mechanism

Exclusive π^0 Production on Unpolarized Proton



$\mu p \rightarrow \mu \pi^0 p$

$$\frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[\left(\frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

ϵ : degree of longitudinal polarization

$$\frac{d\sigma_L}{dt} = \frac{4\pi\alpha}{k'} \frac{1}{Q^6} \left\{ (1-\xi^2) |\langle \tilde{H} \rangle|^2 - 2\xi^2 \text{Re} [\langle \tilde{H} \rangle^* \langle \tilde{E} \rangle] - \frac{t'}{4m^2} \xi^2 |\langle \tilde{E} \rangle|^2 \right\}$$

Leading twist expected to be dominant
But measured as \approx only a few % of $\frac{d\sigma_T}{dt}$

The other contributions arise from the coupling between chiral-odd (quark helicity flip) GPDs to the **twist-3** pion amplitude

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k'} \frac{\mu_\pi^2}{Q^8} \left[(1-\xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \right]$$

$$\frac{d\sigma_{LT}}{dt} = \frac{4\pi\alpha}{\sqrt{2}k'} \frac{\mu_\pi}{Q^7} \xi \sqrt{1-\xi^2} \frac{\sqrt{-t'}}{2m} \text{Re} [\langle H_T \rangle^* \langle \tilde{E} \rangle]$$

$$\frac{d\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k'} \frac{\mu_\pi^2}{Q^8} \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$$

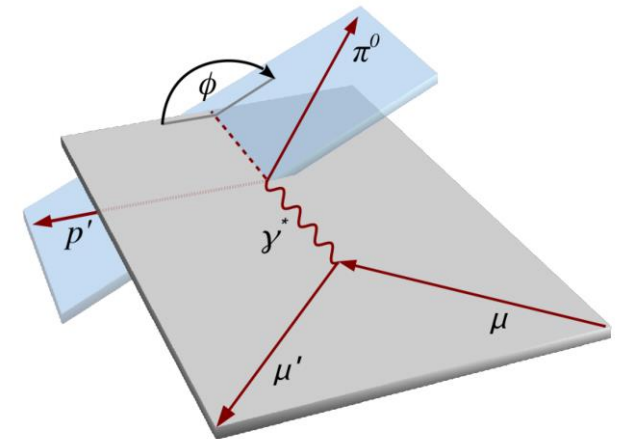
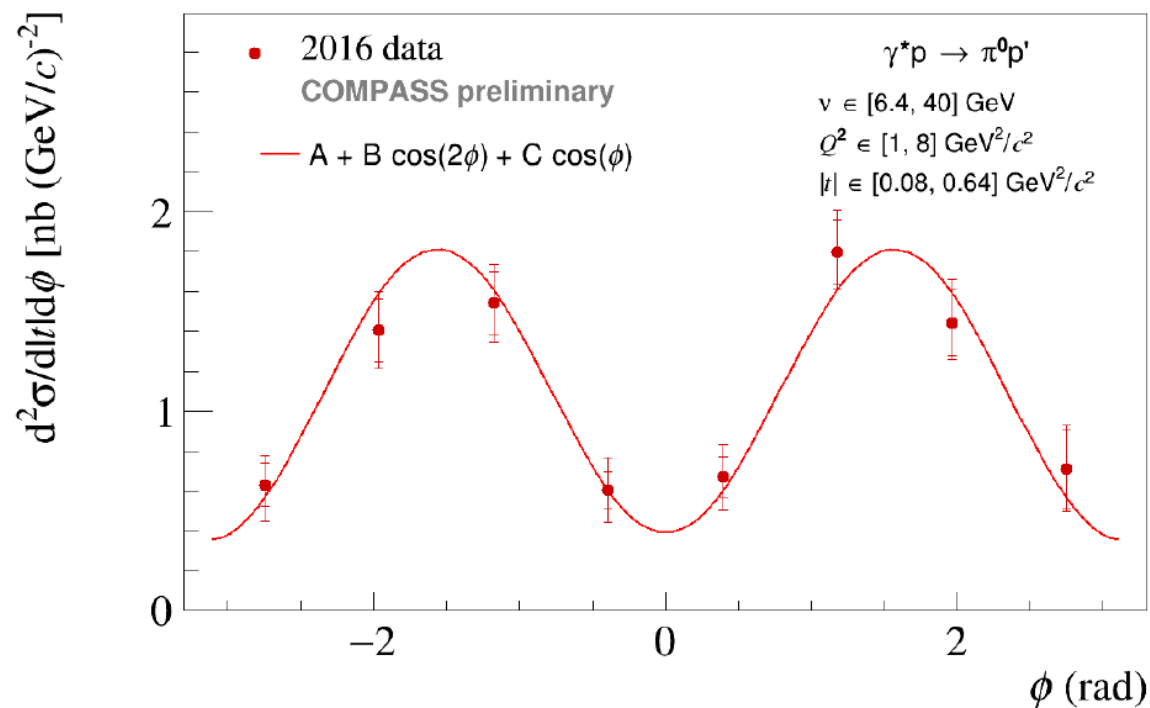


Fig: M.G. Alexeev et al. *Phys.Lett.B* 805 (2020)

2016 Exclusive π^0 Prod. on Unpolarized Proton



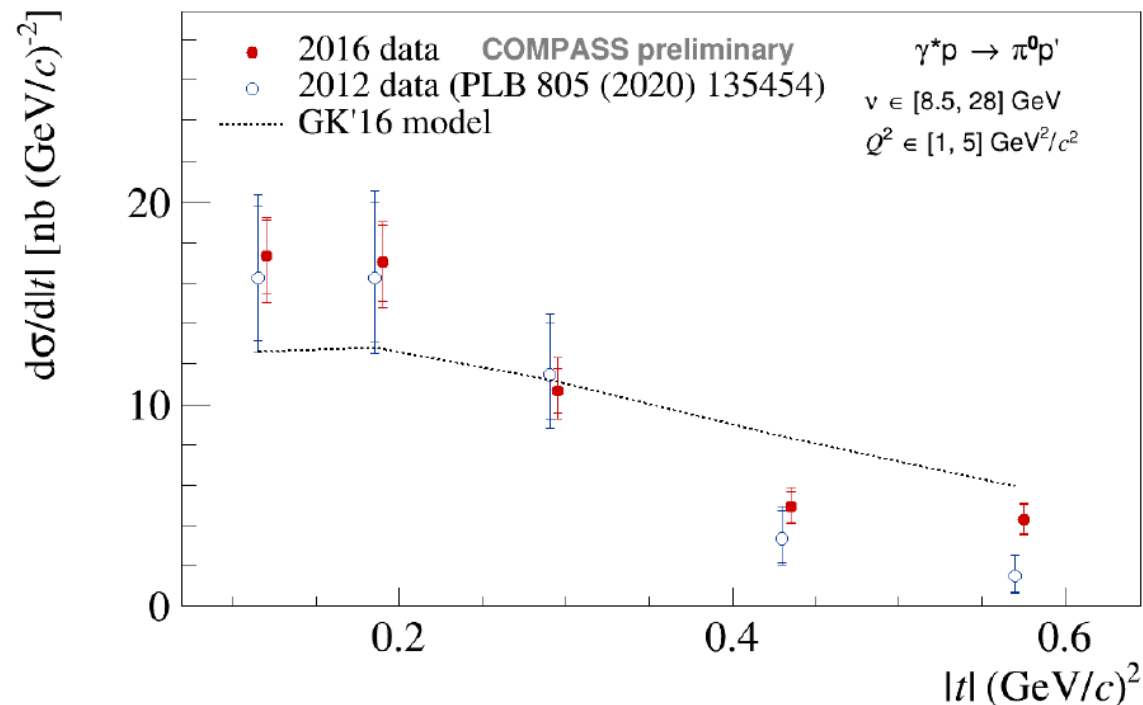
➤ **New 2016 data release:** statistics about 2.3 times larger than the published 2012 pilot run.



$$\left\langle \frac{\sigma_T}{|t|} + \epsilon \frac{\sigma_L}{|t|} \right\rangle = (6.9 \pm 0.3_{\text{stat}} \pm 0.8_{\text{syst}}) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{\sigma_{TT}}{|t|} \right\rangle = (-4.5 \pm 0.5_{\text{stat}} \pm 0.2_{\text{syst}}) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{\sigma_{LT}}{|t|} \right\rangle = (0.06 \pm 0.2_{\text{stat}} \pm 0.1_{\text{syst}}) \frac{\text{nb}}{(\text{GeV}/c)^2}$$



- Inputs for constraining phenomenological models
- **The whole collected 2016/2017 statistics ~ 9 times larger than the 2012 data**

SIDIS Cross Section and TMDs at Leading Twist



$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} = \left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L})$$

Unpol target

$$1 + \left[\sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \right] \leftarrow \text{Cahn \& Boer-Mulders}$$

$$+ \lambda \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\phi_h} \sin\phi_h$$

Long pol target

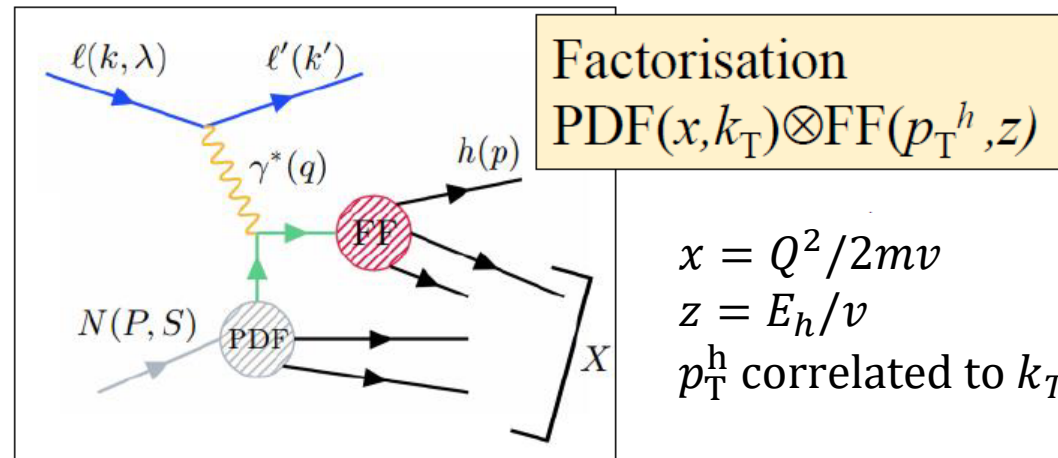
$$+ S_L \left[\sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h \right] \leftarrow \text{Worm-gear L}$$

$$+ S_L \lambda \left[\sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \cos\phi_h \right]$$

Trans pol target

$$\times \left\{ \begin{array}{l} A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) \leftarrow \text{Sivers effect} \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} \sin(\phi_h + \phi_S) \leftarrow \text{Collins effect} \\ + S_T \left[\begin{array}{l} + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)} \sin(3\phi_h - \phi_S) \leftarrow \text{Pretzelosity} \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_S} \sin\phi_S \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_S)} \sin(2\phi_h - \phi_S) \end{array} \right] \\ \hline + S_T \lambda \left[\begin{array}{l} \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_S)} \cos(\phi_h - \phi_S) \leftarrow \text{Worm-gear T} \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_S} \cos\phi_S \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h - \phi_S)} \cos(2\phi_h - \phi_S) \end{array} \right] \end{array} \right.$$

λ Beam polarization



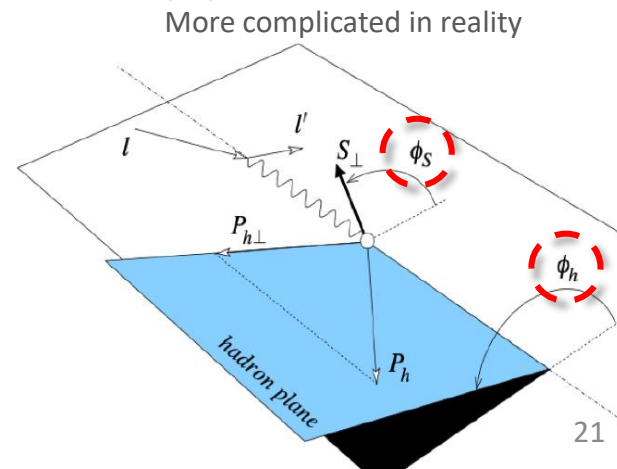
➤ Measure the azimuthal modulations in experiment

$$A_{UT}(\phi) = \frac{1}{f S_T} \frac{N^\uparrow(\phi) - N^\downarrow(\phi)}{N^\uparrow(\phi) + N^\downarrow(\phi)}$$



1st: beam, 2nd: target

U: Unpolarized
T: Transversely
L: Logitudinally



COMPASS 2010 – Trans. Pol. Target



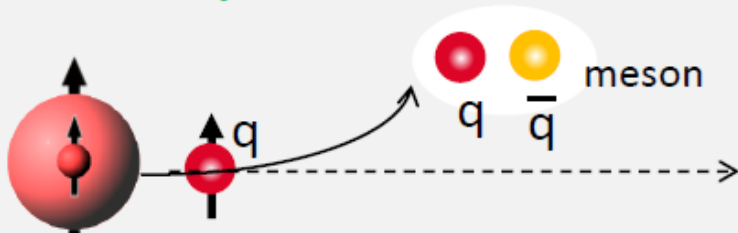
$$h_1 = \text{Diagram 1} - \text{Diagram 2}$$

Transversity

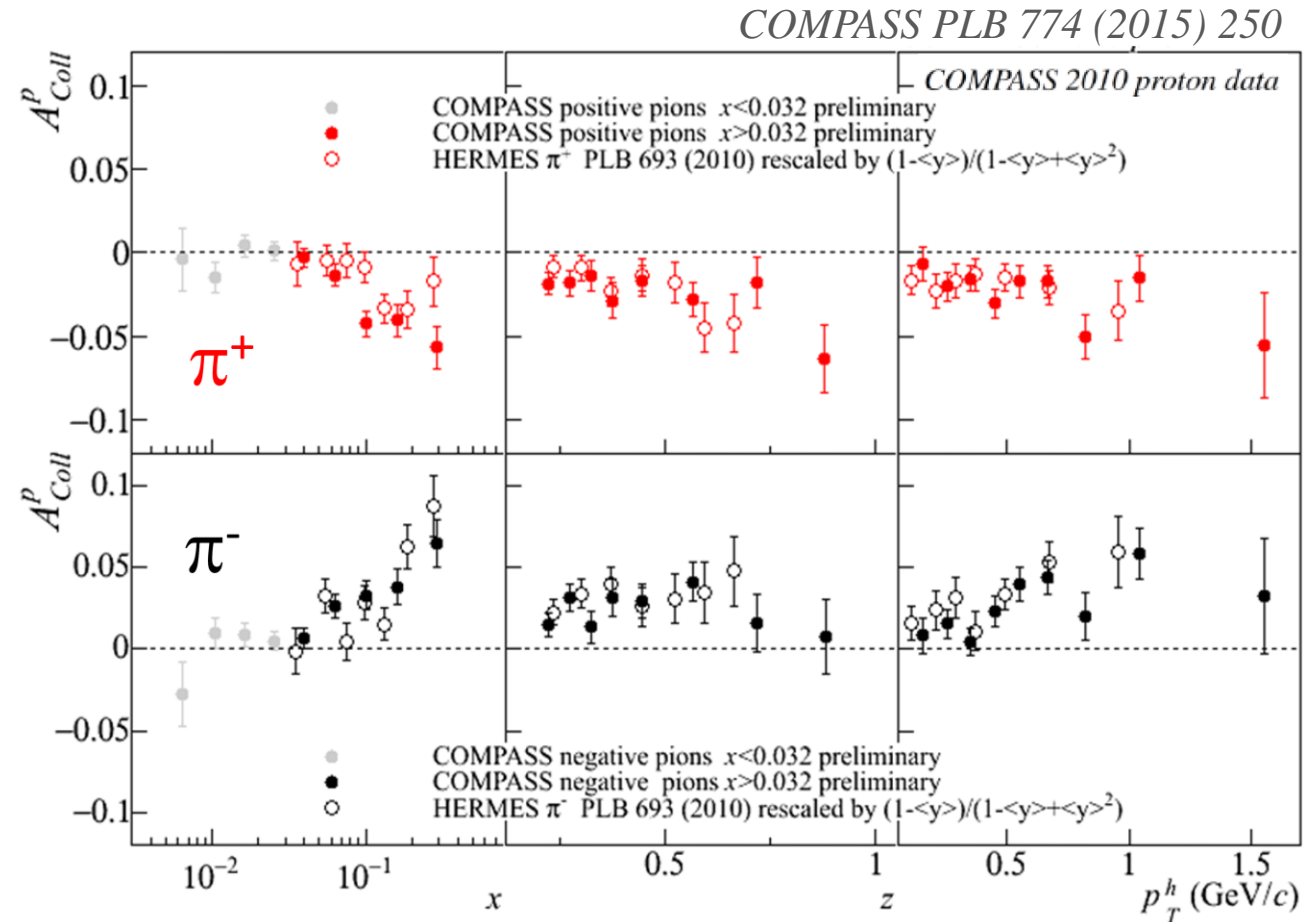
- Difference of quarks with spin parallel or anti-parallel to the transverse spin of the nucleon
- Describes the spin-spin correlation of a transversely polarized parton in a transversely polarized hadron.

Collins Asymmetry

Transversity chiral-odd PDF \times Collins odd FF



$$A_{\text{Coll}} \approx \frac{\sum_q e_q^2 h_1^q(x) \otimes H_{1q}^{\perp h}(z, p_T^h)}{\sum_q e_q^2 f_1^q(x) \otimes D_{1q}^h(z, p_T^h)}$$



Significant asymmetry of opposite sign for π^+ & π^-

- Agreement between COMPASS & HERMES for $x > 0.032$
- COMPASS Q^2 domain larger by a factor of 2 to 3
 \rightarrow Absence of Q^2 evolution?

Extraction of Transversity PDF



$$A_{Coll}^{p,\pi^+} \sim e_u^2 h_1^u H_1^{\perp,fav} + e_d^2 h_1^d H_1^{\perp,unf}$$

$$A_{Coll}^{p,\pi^-} \sim e_u^2 h_1^u H_1^{\perp,unf} + e_d^2 h_1^d H_1^{\perp,fav}$$

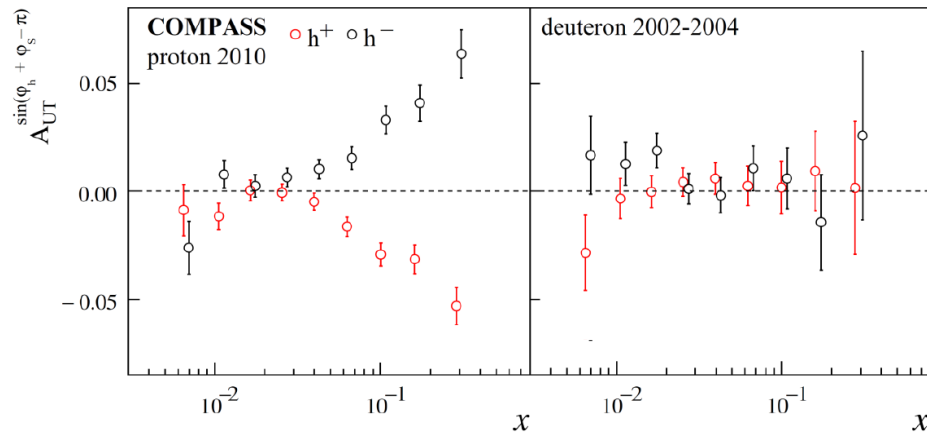
Favored: $u \rightarrow \pi^+, d \rightarrow \pi^-$
 Unfavored: $u \rightarrow \pi^-, d \rightarrow \pi^+$

$$H_1^{\perp,fav} \approx -H_1^{\perp,unf}$$

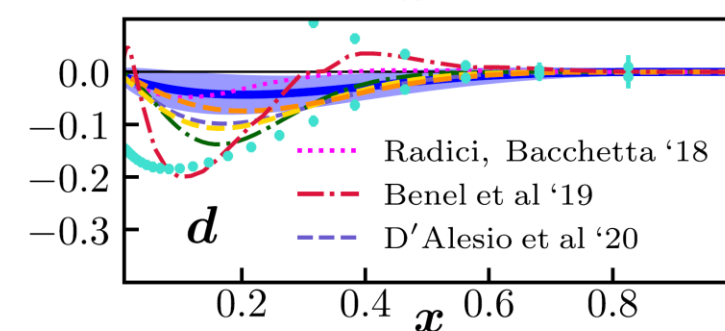
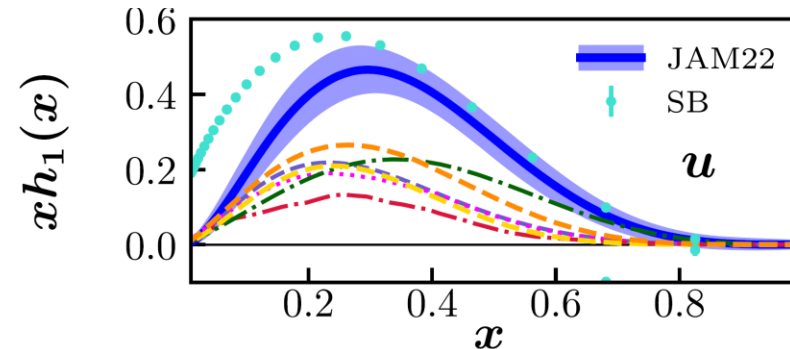
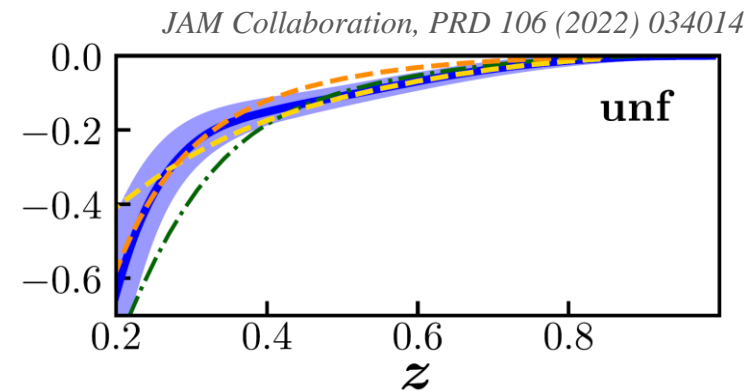
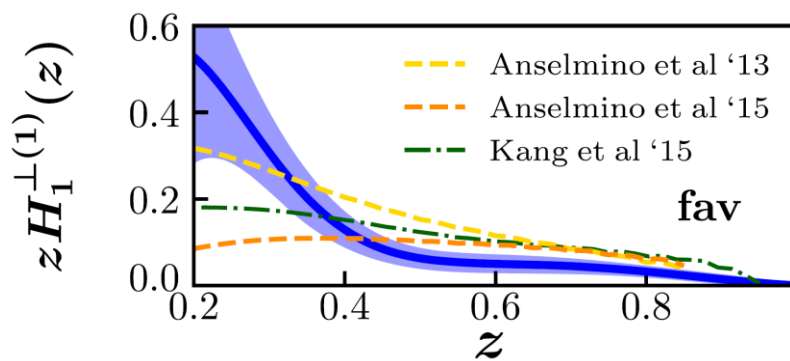
$$\langle \sin(\varphi + \varphi_s) \rangle_{UT}^{\pi^+} \sim 4(h_1^u - h_1^d) H_1^{\perp,fav}$$

$$\langle \sin(\varphi + \varphi_s) \rangle_{UT}^{\pi^-} \sim -4(h_1^u - h_1^d) H_1^{\perp,fav}$$

- COMPASS Collins asymmetries on the deuteron compatible with zero
 - Cancellation between u & d quark
 - u- and d-quark transversity PDFs have opposite sign.
- d-quark transversity PDF relatively poor determined due to the lack of neutron (deuteron) data



Extensive analyses and global fits: using data from HERMES (p), COMASS (p & d), Belle (e^+e^-)

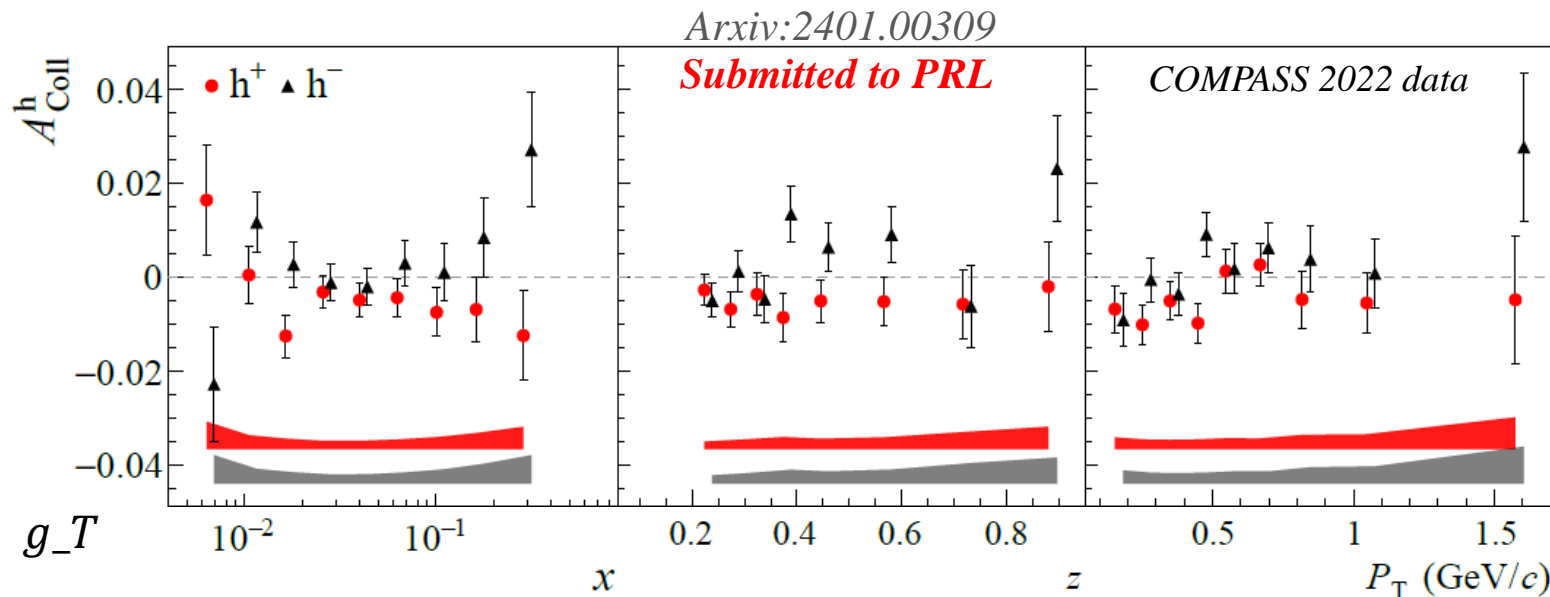
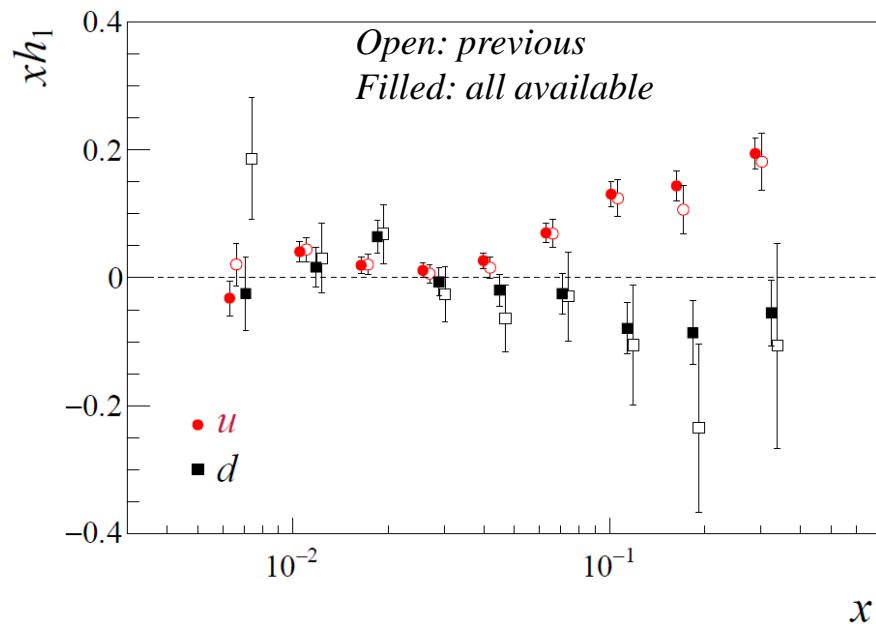


COMPASS 2022 – Trans. Pol. Deuteron



$$h_1 = \text{Transversity}$$

- Important input for Transversity PDF
- Uncertainty reduced in all p and 2022 d data, especially for the d-quark h_1



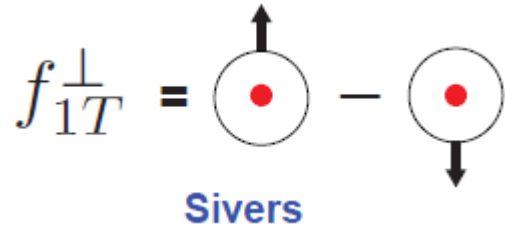
Tensor charge: $\delta q(Q^2) = \int_0^1 dx [h_1^q(x, Q^2) - h_1^{\bar{q}}(x, Q^2)]$ & $q_T = \delta u - \delta d$
 Isovector combination

- Interesting quantity not only related to QCD phenomenology, but also for ab initio studies and BSM physics.

data	$\delta u = \int_{0.008}^{0.210} dx h_1^{u\nu}(x)$	$\delta d = \int_{0.008}^{0.210} dx h_1^{d\nu}(x)$	$g_T = \delta u - \delta d$
previous [25, 28, 29]	0.187 ± 0.030	-0.178 ± 0.097	0.365 ± 0.078
previous [25, 28, 29] and present	0.214 ± 0.020	-0.070 ± 0.043	0.284 ± 0.045

- Complementary measurements at JLab and future EIC

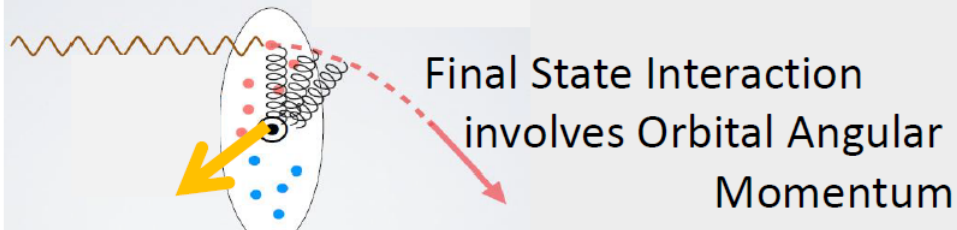
COMPASS 2010 – Trans. Pol. Target



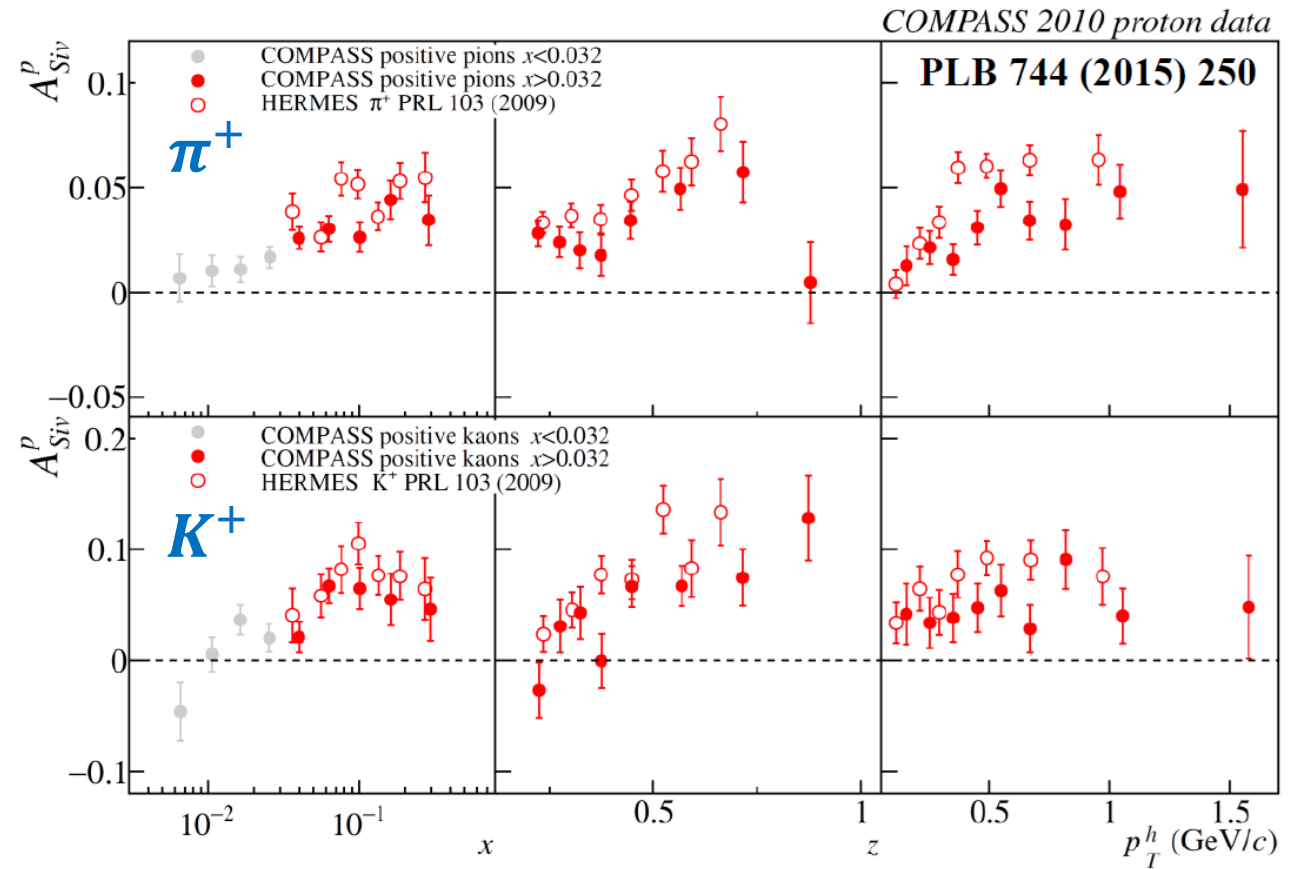
- Correlates the quark transverse momentum k_T and the transverse spin of the nucleon
- Describes the strength of the distortion in transverse momentum space relative to the symmetric unpolarized distribution f_1

Sivers Asymmetry

Sivers Chiral-even but T-odd

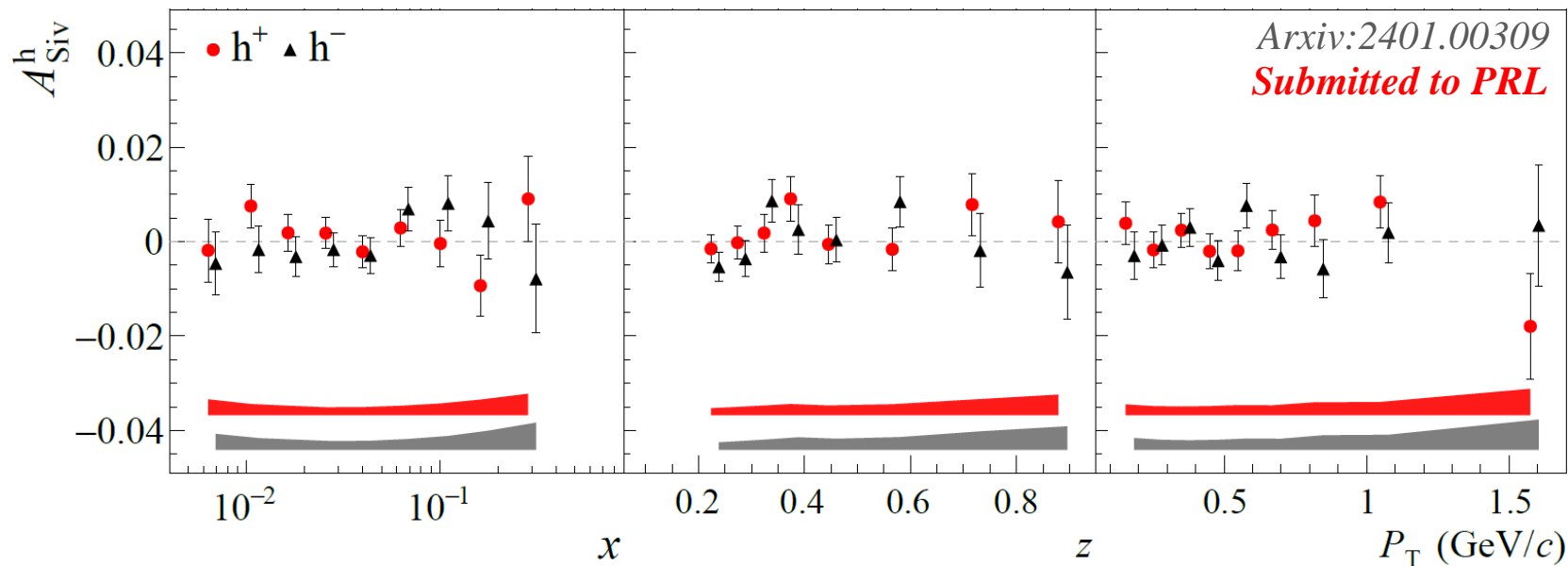
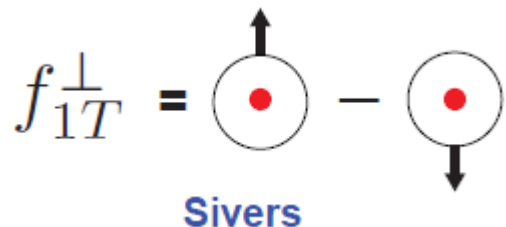


$$A_{Siv} \approx \frac{\sum_q e_q^2 f_{1T}^{\perp q}(x) \otimes D_{1q}^h(z, p_T^h)}{\sum_q e_q^2 f_1^q(x) \otimes D_{1q}^h(z, p_T^h)}$$

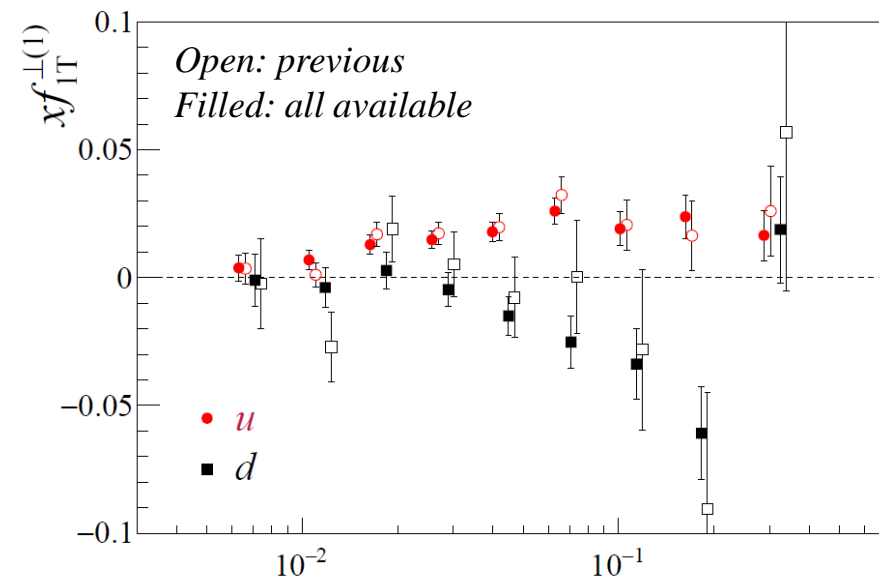


- Sivers effect smaller at COMPASS than at HERMES. **TMD evolution?**
- Kaon amplitudes larger than pion, unexpected if u-quark scattering dominates. **Role of sea quarks?**

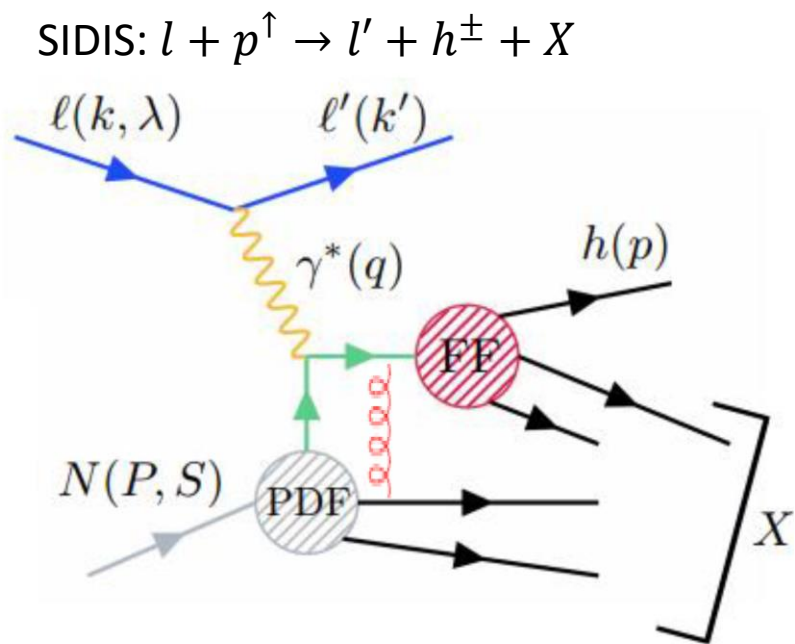
COMPASS 2022 – Trans. Pol. Deuteron



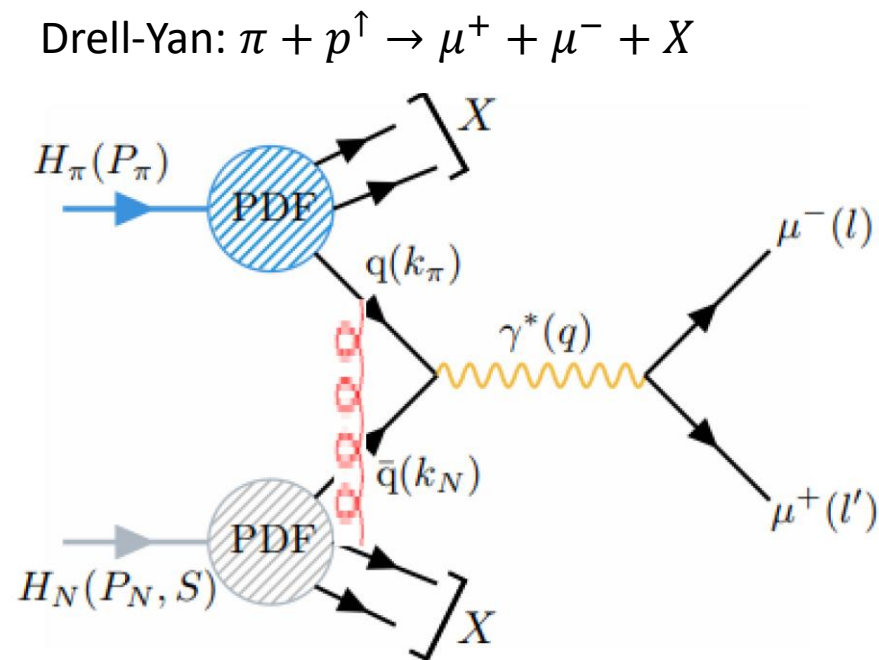
- **Sivers** asymmetries, weighted with the hadron transverse momentum P_T , provide direct measurement of TMD k_T^2 moments without assumptions on K_T shape.
- Different signs in u- and d-quark Sivers functions, uncertainty significantly reduced in d-quark case
- Crucial input for **Sivers** PDF for the d-quark



SIDIS & Drell-Yan



SIDIS: $\text{TMD} \otimes \text{FF}^h$
 TMDs involve **final state** interaction



DY: $\text{TMD}^{\text{Beam}} \otimes \text{TMD}^{\text{Target}}$
 TMDs involve **initial state** interaction

TMD universality, expect **same magnitude but different signs** for naïve T-odd TMD PDFs in SIDIS and DY

$$h_{1,p}^{\perp q} \Big|_{\text{SIDIS}} = -h_{1,p}^{\perp q} \Big|_{\text{DY}}$$

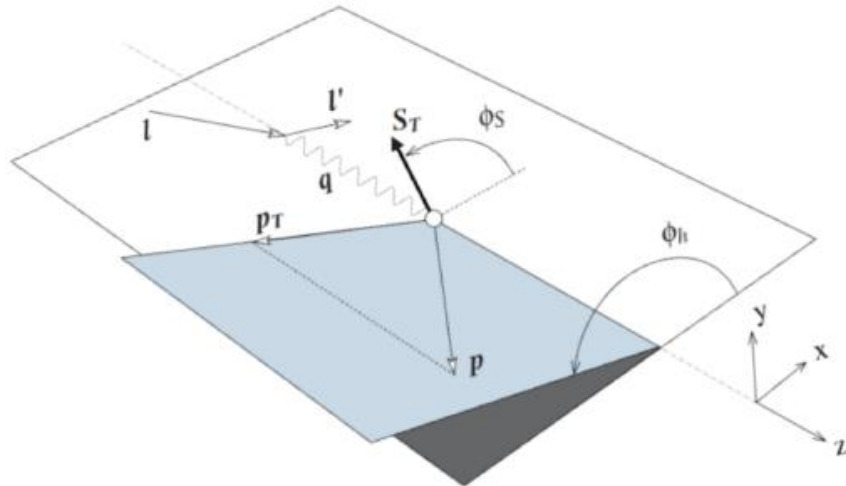
$$f_{1T,p}^{\perp q} \Big|_{\text{SIDIS}} = -f_{1T,p}^{\perp q} \Big|_{\text{DY}}$$

SIDIS and Single-polarised Drell-Yan

$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L})$$

SIDIS

$$\times \left\{ \begin{aligned} & 1 + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ & + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} \\ & + S_T \begin{bmatrix} A_{UT}^{\sin(\phi_h-\phi_S)} \sin(\phi_h-\phi_S) \\ + \varepsilon A_{UT}^{\sin(\phi_h+\phi_S)} \sin(\phi_h+\phi_S) \\ + \varepsilon A_{UT}^{\sin(3\phi_h-\phi_S)} \sin(3\phi_h-\phi_S) \end{bmatrix} \\ & + S_T \lambda \left[\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h-\phi_S)} \cos(\phi_h-\phi_S) \right] \end{aligned} \right\}$$

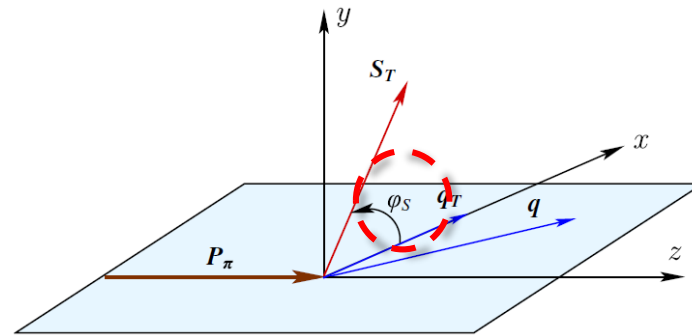


$$\frac{d\sigma^{LO}}{dq^4 d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS})$$

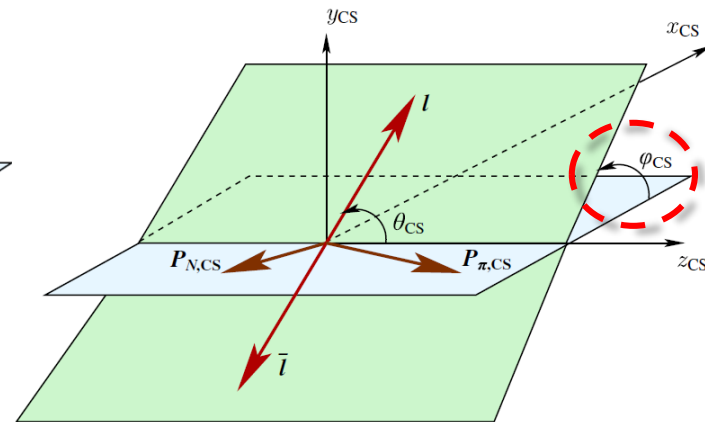
Drell-Yan

$$\times \left\{ \begin{aligned} & 1 + D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS} \\ & + S_L \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \\ & + S_T \begin{bmatrix} A_T^{\sin \varphi_S} \sin \varphi_S \\ + D_{[\sin^2 \theta_{CS}]} \begin{bmatrix} A_T^{\sin(2\varphi_{CS}-\varphi_S)} \sin(2\varphi_{CS}-\varphi_S) \\ + A_T^{\sin(2\varphi_{CS}+\varphi_S)} \sin(2\varphi_{CS}+\varphi_S) \end{bmatrix} \end{bmatrix} \end{aligned} \right\}$$

where $D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$



Target rest frame



Collins-Soper frame

SIDIS and Single-polarised Drell-Yan



$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_s} \propto (F_{UU,T} + \varepsilon F_{UU,L})$$

SIDIS

$$\frac{d\sigma^{LO}}{dq^4 d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS})$$

Drell-Yan

$$\times \left\{ \begin{aligned} & 1 + \boxed{\varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h} \\ & + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} \\ & + S_T \begin{bmatrix} A_{UT}^{\sin(\phi_h-\phi_s)} \sin(\phi_h-\phi_s) \\ + \varepsilon A_{UT}^{\sin(\phi_h+\phi_s)} \sin(\phi_h+\phi_s) \\ + \varepsilon A_{UT}^{\sin(3\phi_h-\phi_s)} \sin(3\phi_h-\phi_s) \end{bmatrix} \\ & + S_T \lambda \left[\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h-\phi_s)} \cos(\phi_h-\phi_s) \right] \end{aligned} \right\}$$

$$\times \left\{ \begin{aligned} & 1 + \boxed{D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS}} \\ & + S_L \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \\ & + S_T \begin{bmatrix} A_T^{\sin \varphi_S} \sin \varphi_S \\ + D_{[\sin^2 \theta_{CS}]} \begin{pmatrix} A_T^{\sin(2\varphi_{CS}-\varphi_S)} \sin(2\varphi_{CS}-\varphi_S) \\ + A_T^{\sin(2\varphi_{CS}+\varphi_S)} \sin(2\varphi_{CS}+\varphi_S) \end{pmatrix} \end{bmatrix} \end{aligned} \right\}$$

where $D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$

$$A_{UU}^{\cos 2\phi_h} \propto \underline{h_1^{\perp q}} \otimes \underline{H_{1q}^{\perp h}} + \dots$$

Boer-Mulders

$$A_U^{\cos 2\varphi_{CS}} \propto \underline{h_{1,\pi}^{\perp q}} \otimes \underline{h_{1,p}^{\perp q}}$$

$$A_{UT}^{\sin(\phi_h-\phi_s)} \propto \underline{f_{1T}^{\perp q}} \otimes \underline{D_{1q}^h}$$

Sivers

$$A_T^{\sin \varphi_S} \propto \underline{f_{1,\pi}^q} \otimes \underline{f_{1T,p}^{\perp q}}$$

$$A_{UT}^{\sin(\phi_h+\phi_s)} \propto \underline{h_1^q} \otimes \underline{H_{1q}^{\perp h}}$$

Transversity

$$A_T^{\sin(2\varphi_{CS}-\varphi_S)} \propto \underline{h_{1,\pi}^{\perp q}} \otimes \underline{h_{1,p}^q}$$

$$A_{UT}^{\sin(3\phi_h-\phi_s)} \propto \underline{h_{1T}^{\perp q}} \otimes \underline{H_{1q}^{\perp h}}$$

Pretzelosity

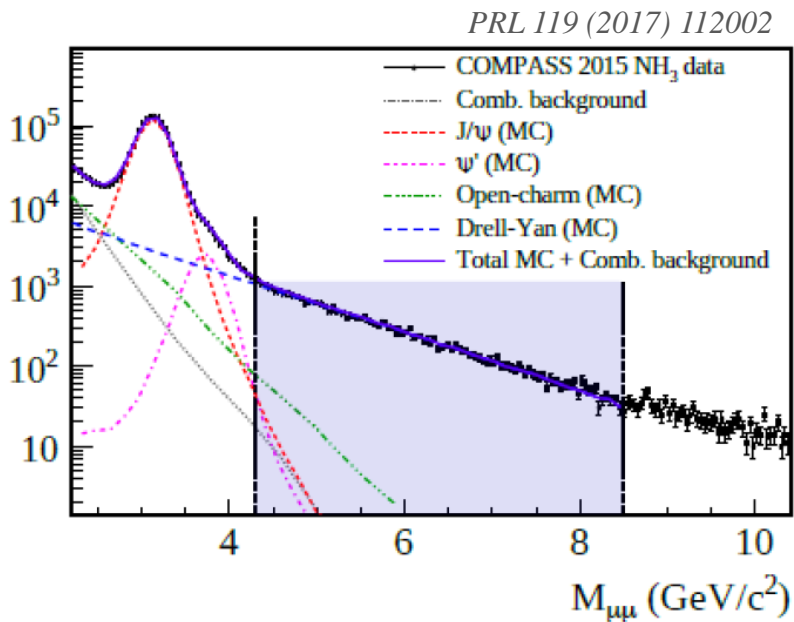
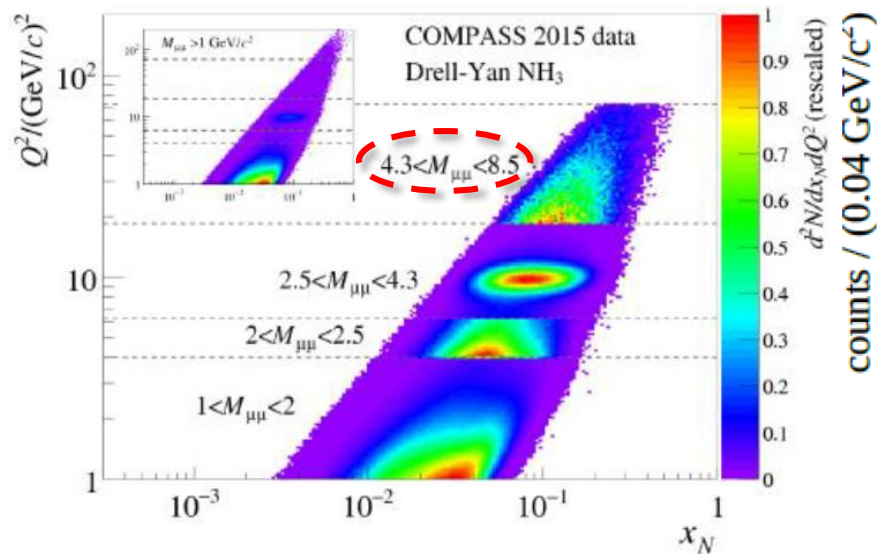
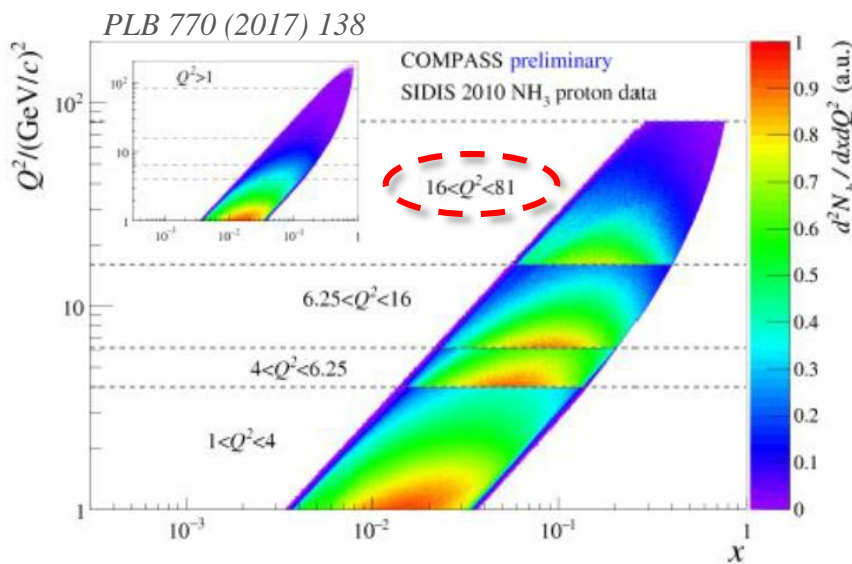
$$A_T^{\sin(2\varphi_{CS}+\varphi_S)} \propto \underline{h_{1,\pi}^{\perp q}} \otimes \underline{h_{1T,p}^{\perp q}}$$

Uniqueness in Testing TMD Universality



- SIDIS with transversely polarized proton
→ COMPASS 2007, 2010

- Pion-induced transversely polarized Drell-Yan
→ COMPASS 2015, 2018



SIDIS: $16 < Q^2 / (\text{GeV}/c)^2 < 81$

Drell-Yan: $4.3 < M_{\mu\mu} / (\text{GeV}/c^2) < 8.5$

- Q^2 -evolution effect minimized with similar (x, Q^2) coverage in comparing the TMDs extracted from DIDIS and Drell-Yan

Sivers in Drell-Yan and SIDIS

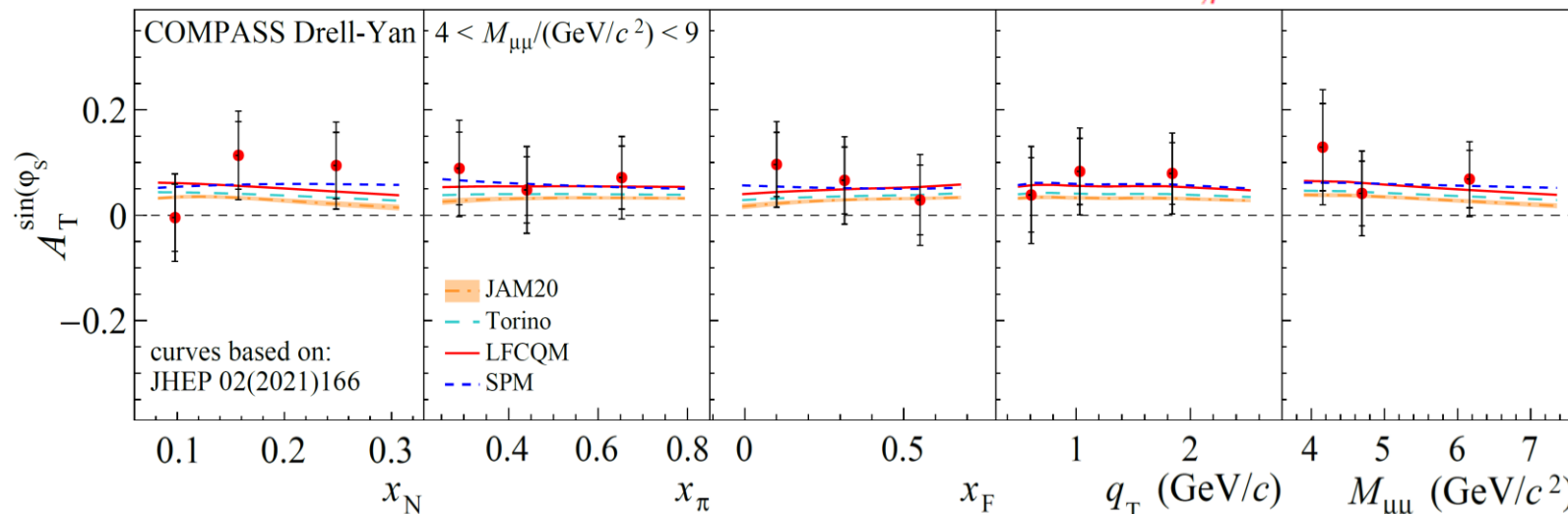


Arxiv:2312.17379

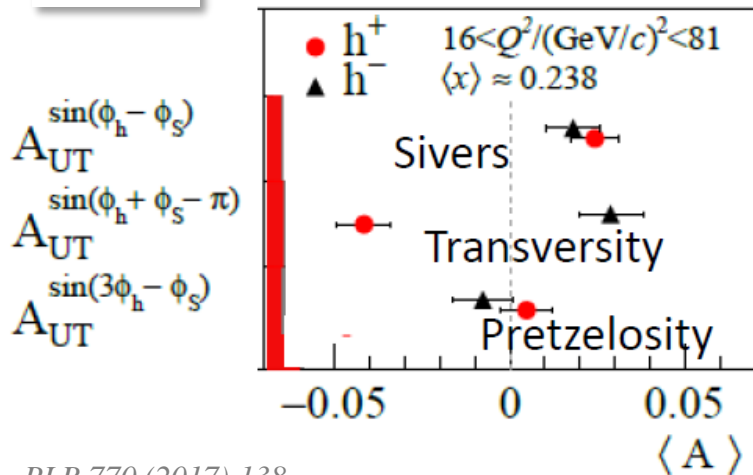
Drell-Yan

- First ever polarized DY in 2015
- Final result: 2015 & 2018 data combined

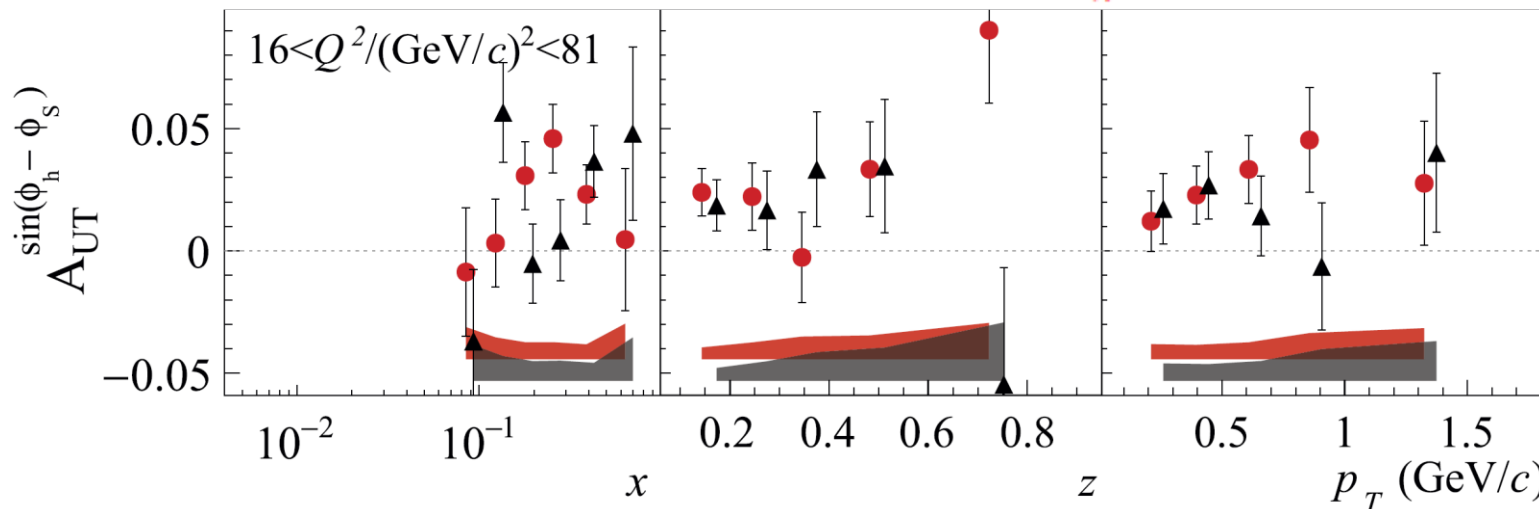
Sivers in Drell-Yan: $A^{\sin(\phi_S)} \propto f_{1,\pi} \otimes f_{1T,p}^\perp$



SIDIS



Sivers in SIDIS: $A^{\sin(\phi_h - \phi_S)} \propto f_{1T,p}^\perp \otimes D_1^h$

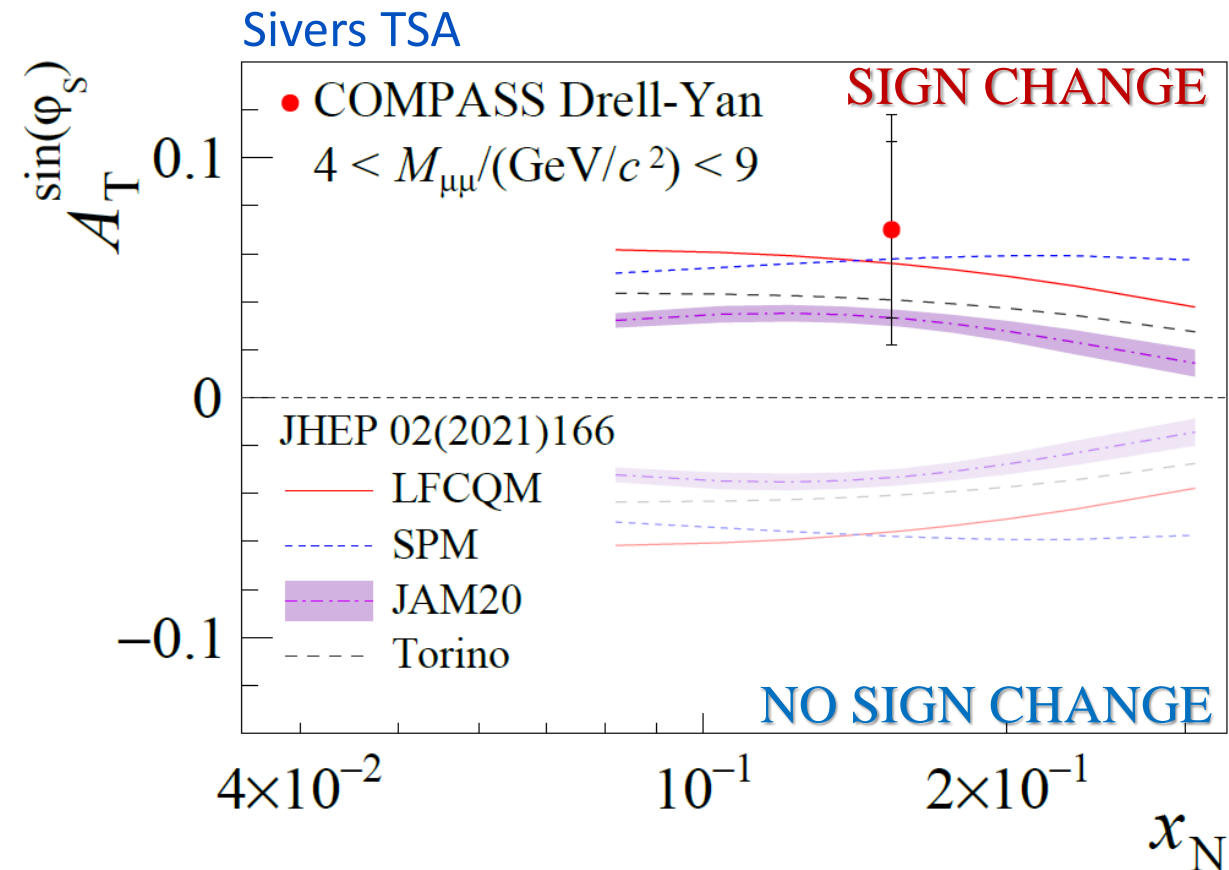


Final Result on TSA in Drell-Yan



Arxiv:2312.17379
Submitted to PRL

COMPASS pion induced DY 2015 + 2018



$$\langle A_T^{\sin \varphi_s} \rangle = 0.070 \pm 0.037(\text{stat.}) \pm 0.031(\text{sys.})$$

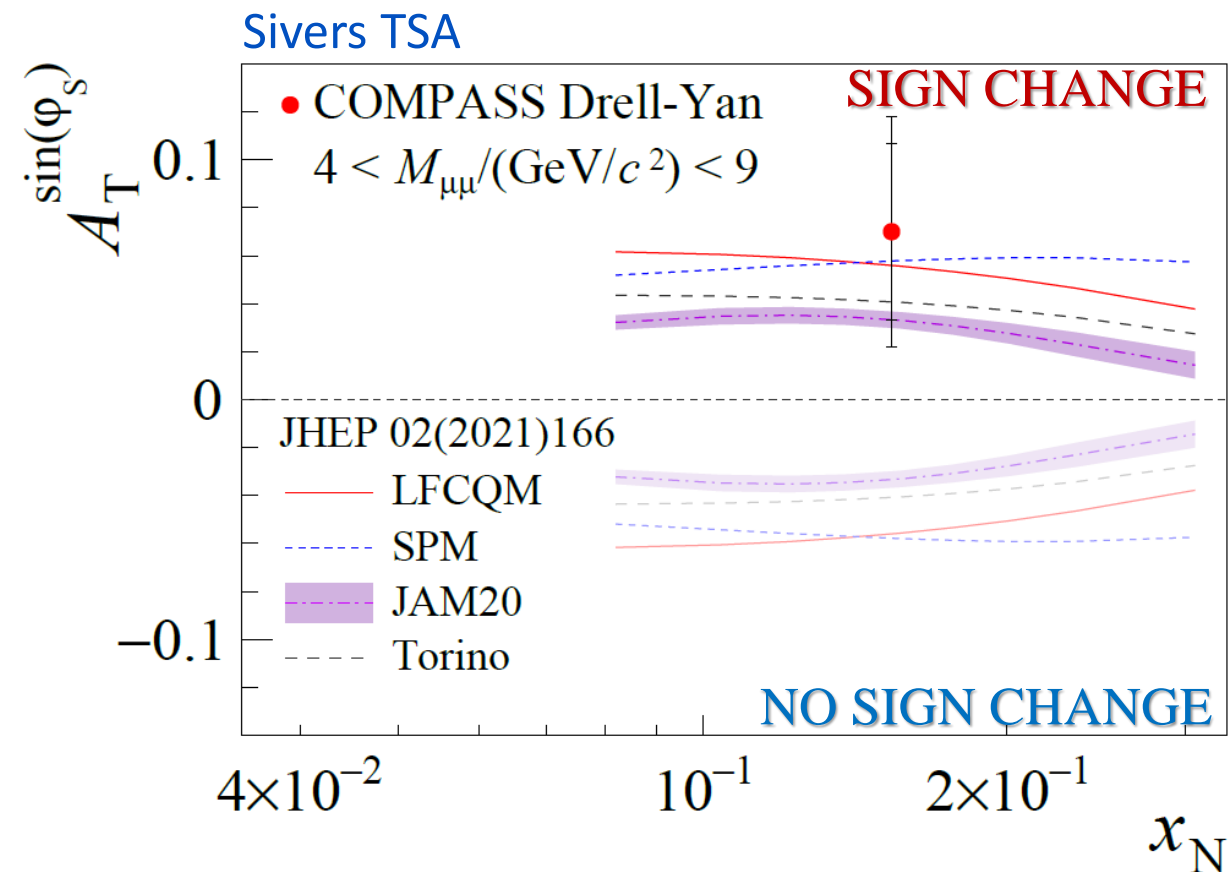
- Average Sivers asymmetry integrated over the entire kinematic range found to be **above zero at about 1.5σ of the total uncertainty.**
- Confirm the fundamental QCD prediction of a sign change of naïve time-reversal-odd TMD PDFs when comparing Drell-Yan and SIDIS.

Final Result on TSA in Drell-Yan

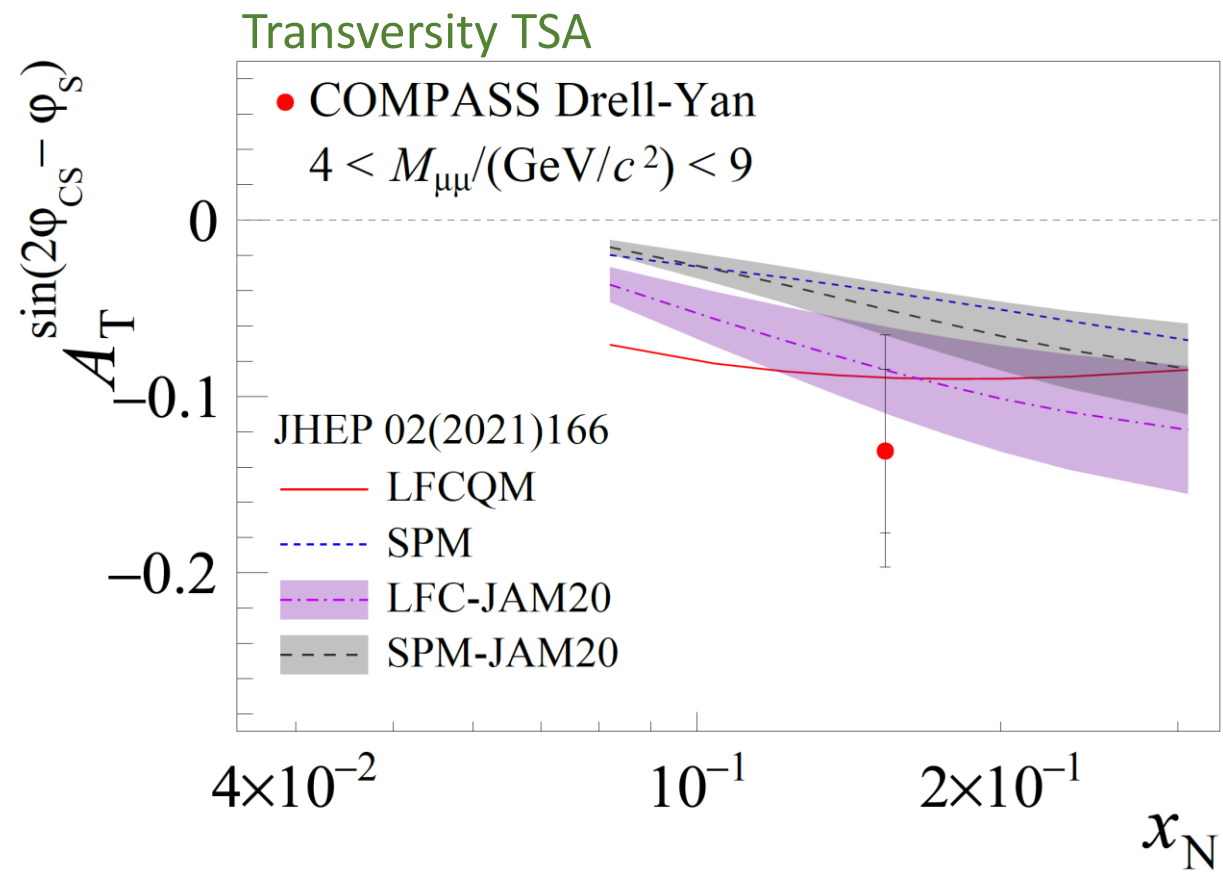


Arxiv:2312.17379
Submitted to PRL

COMPASS pion induced DY 2015 + 2018



$$\langle A_T^{\sin \varphi_s} \rangle = 0.070 \pm 0.037(\text{stat.}) \pm 0.031(\text{sys.})$$



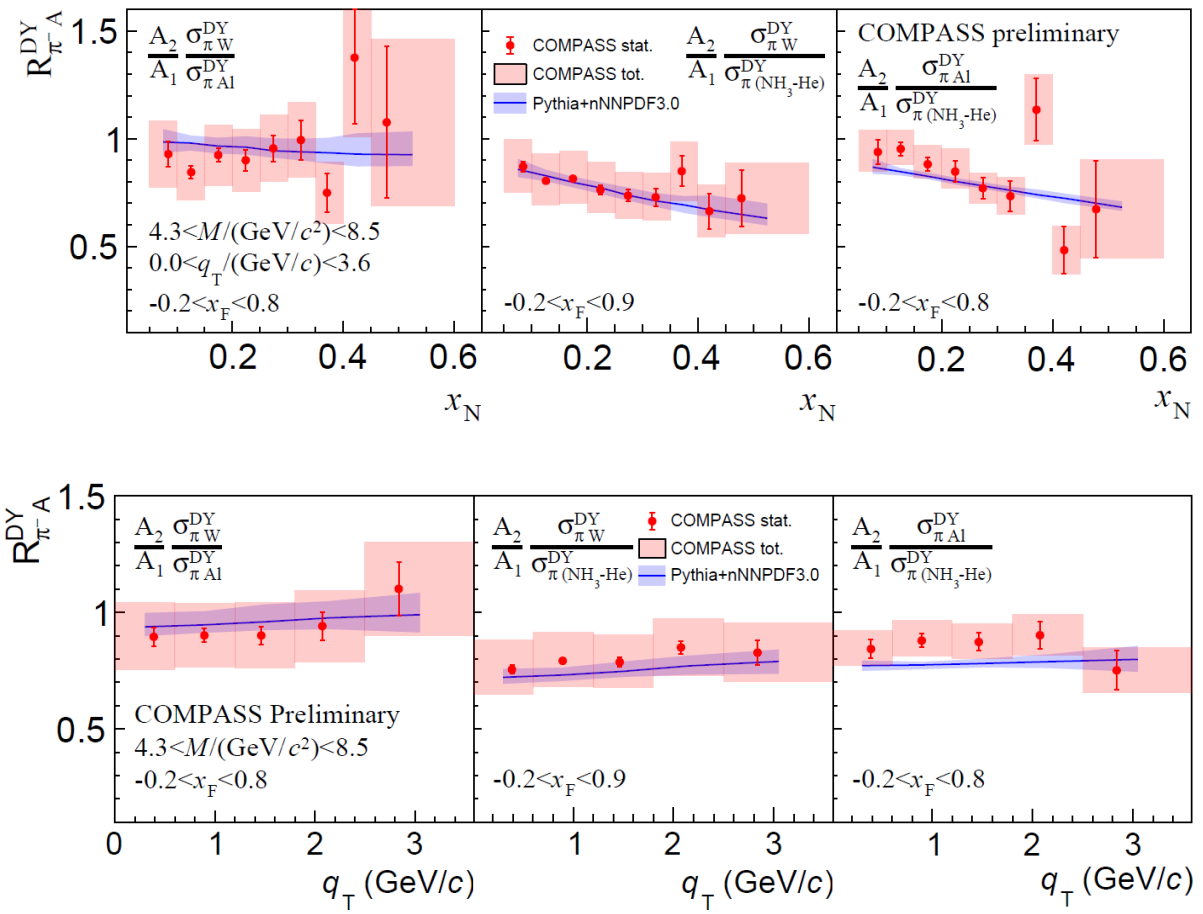
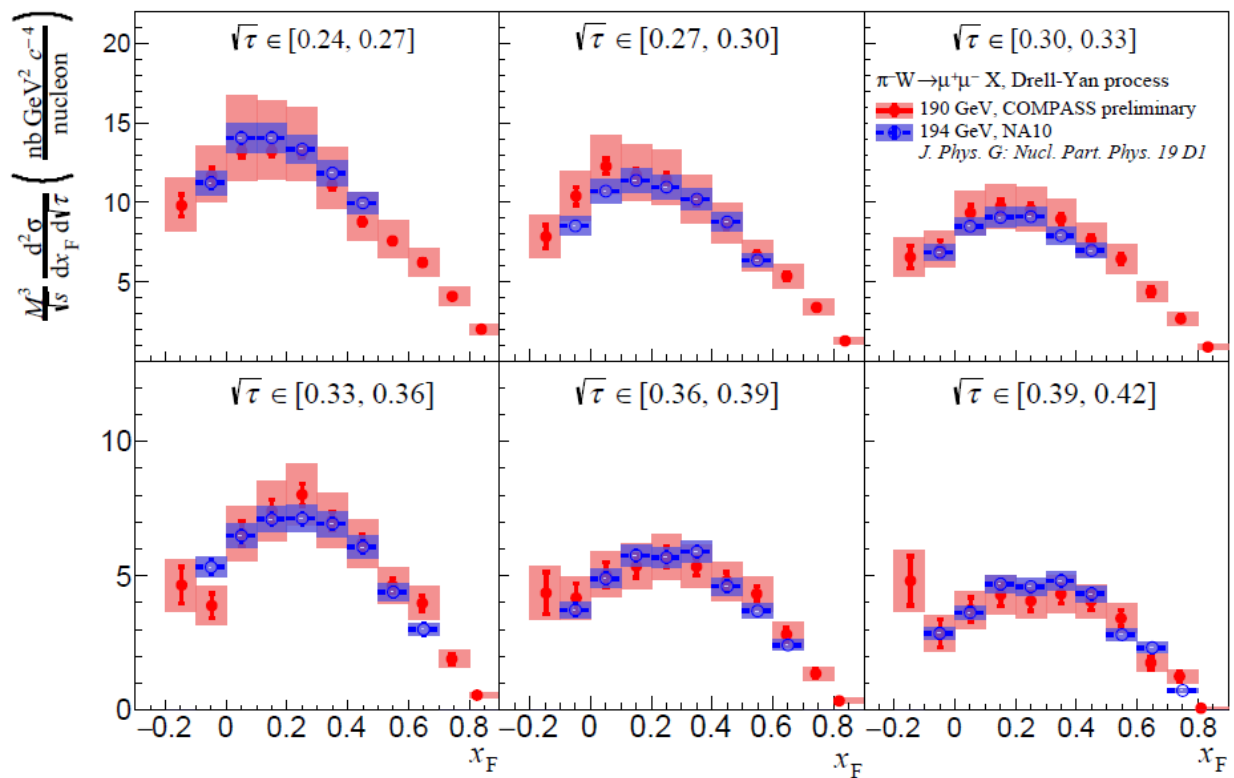
$$\langle A_T^{\sin(2\varphi_{cs}-\varphi_s)} \rangle = -0.131 \pm 0.046(\text{stat.}) \pm 0.047(\text{sys.})$$

- Universality of transversity TMD PDFs
- Constraint on pion Boer-Mulders

Pion Structure and More



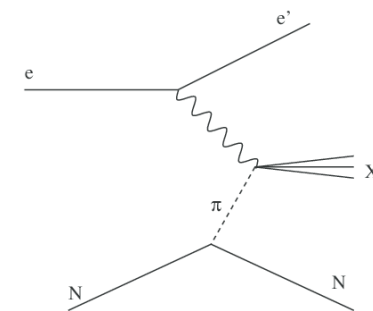
Figure: Vincent Andrieux, 25th Spin Symposium



- Inputs for pion PDF study
- Cold nuclear matter effect

- **3-D partonic structure provides further insights into nucleon properties**
- **A limited selection of COMPASS results has been presented**
 - GPDs through DVCS & HEMP → working on 2016-2017
 - TMDs through SIDIS & Drell-Yan → new 2022 data release
- **COMPASS has entered its analysis phase, expect more results soon!**

- **EIC will further extend the measurements covered by COMPASS**
 - **Wide phase space coverage**
 - **GPD & TMD study with various processes**
 - **Meson structure via Sullivan process**
 - **Cold nuclear matter effect**



Backup Slides

COMPASS 2016 – Unpol. Target



➤ Cahn effect & Boer-Mulders \otimes Collins FF

➤ **Boer-Mulders**: contributing to $\cos \varphi_h$ and $\cos 2\varphi_h$

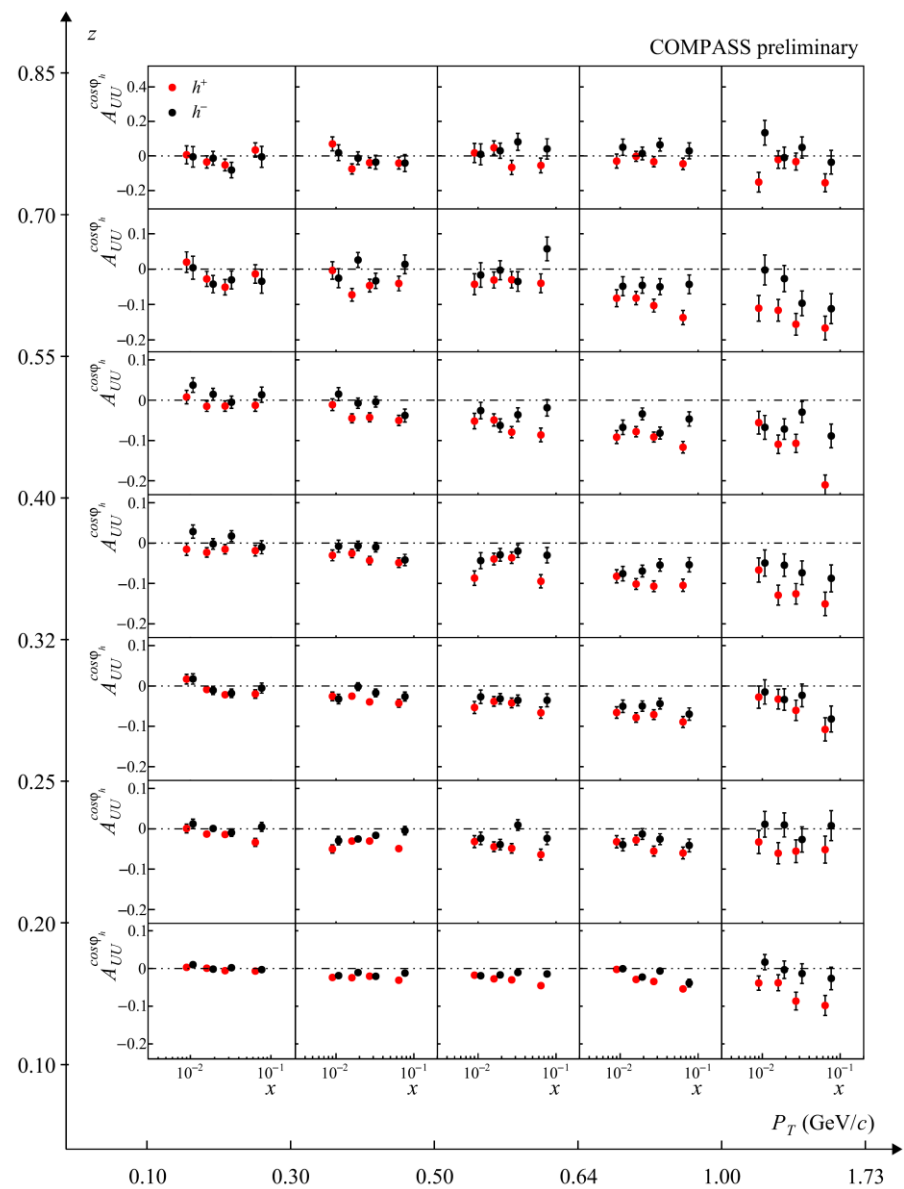
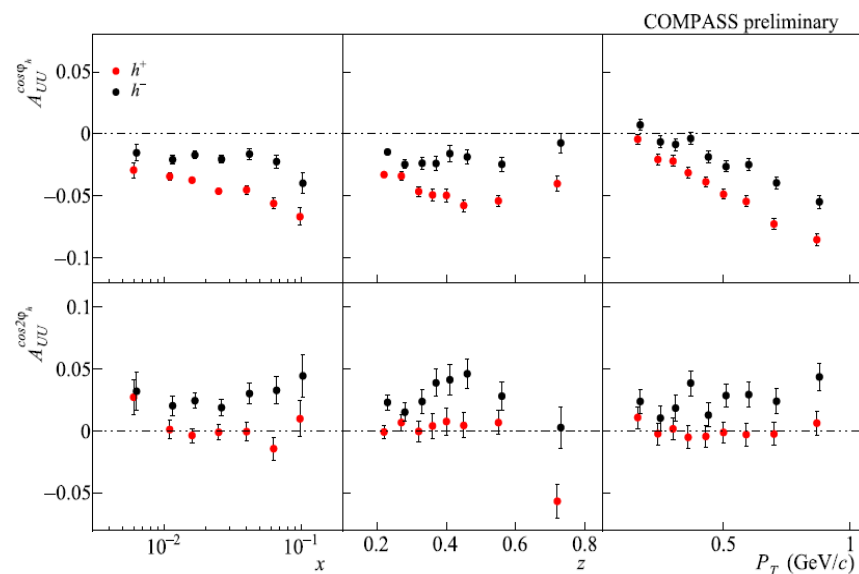
Describes the strength of the spin-orbit correlation between the quark spin s_T and the intrinsic transverse momentum k_T

- Still Unknown
- Complex kinematic dependences & interesting differences between positive and negative hadrons from previous observations

➤ **Cahn effect**: contributing to $\cos \varphi_h$

Azimuthal modulation induced due to the presence of non-zero intrinsic transverse momentum k_T of unpolarized quarks in the unpolarized nucleon.

- Strong P_T dependence
- Complementary access to k_T
- On-going analysis with proton data
- **More to come with 2022 deuteron data**



2012 Exclusive ω Prod. on Unpolarized Proton

SCHC ($\lambda_\gamma = \lambda_V$)

(S-Channel Helicity Conservation)

SCHC implies:

• $r_{1-1}^1 + \text{Im} r_{1-1}^2 = 0$

= $-0.010 \pm 0.032 \pm 0.047$ OK

• $\text{Re} r_{10}^5 + \text{Im} r_{10}^6 = 0$

= $0.014 \pm 0.011 \pm 0.013$ OK

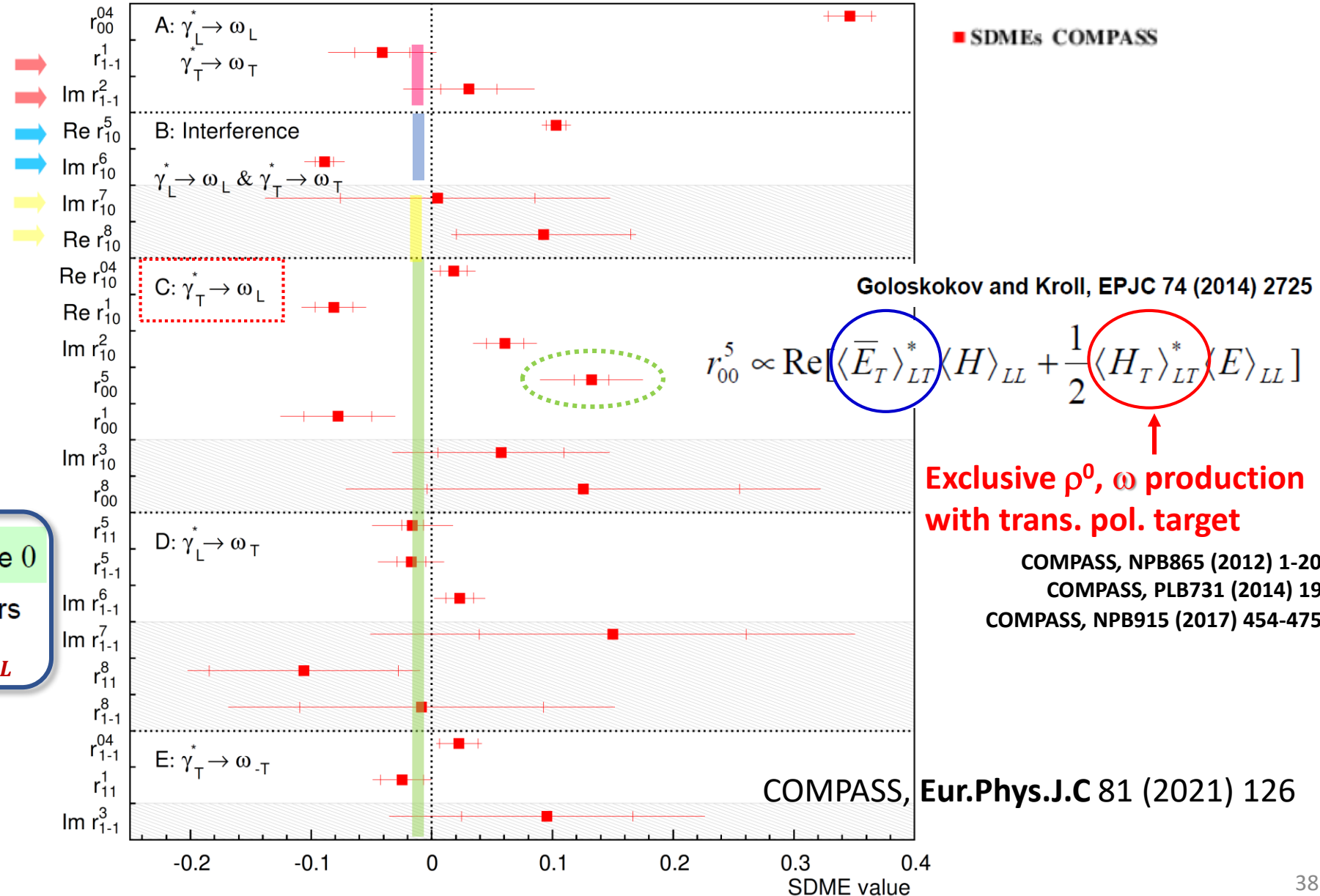
• $\text{Im} r_{10}^7 - \text{Re} r_{10}^8 = 0$

= $-0.088 \pm 0.110 \pm 0.196$ OK

• all elements of classes C, D, E should be 0

for $\gamma_L^* \rightarrow \omega_T$ and $\gamma_T^* \rightarrow \omega_T$ OK within errors

NOT OBSERVED for transitions $\gamma_T^* \rightarrow \omega_L$



COMPASS⁺⁺ / AMBER



A new QCD facility
at the M2 beam line of the CERN SPS



- Unique beam line with polarised μ^\pm and high-intensity **Pion** beam
- Possible high-intensity **antiproton** and **Kaon** beams, provided by RF-separation technique
- With upgraded apparatus

Proposed physics goals

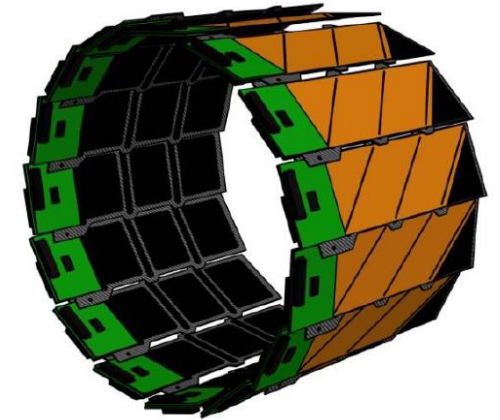
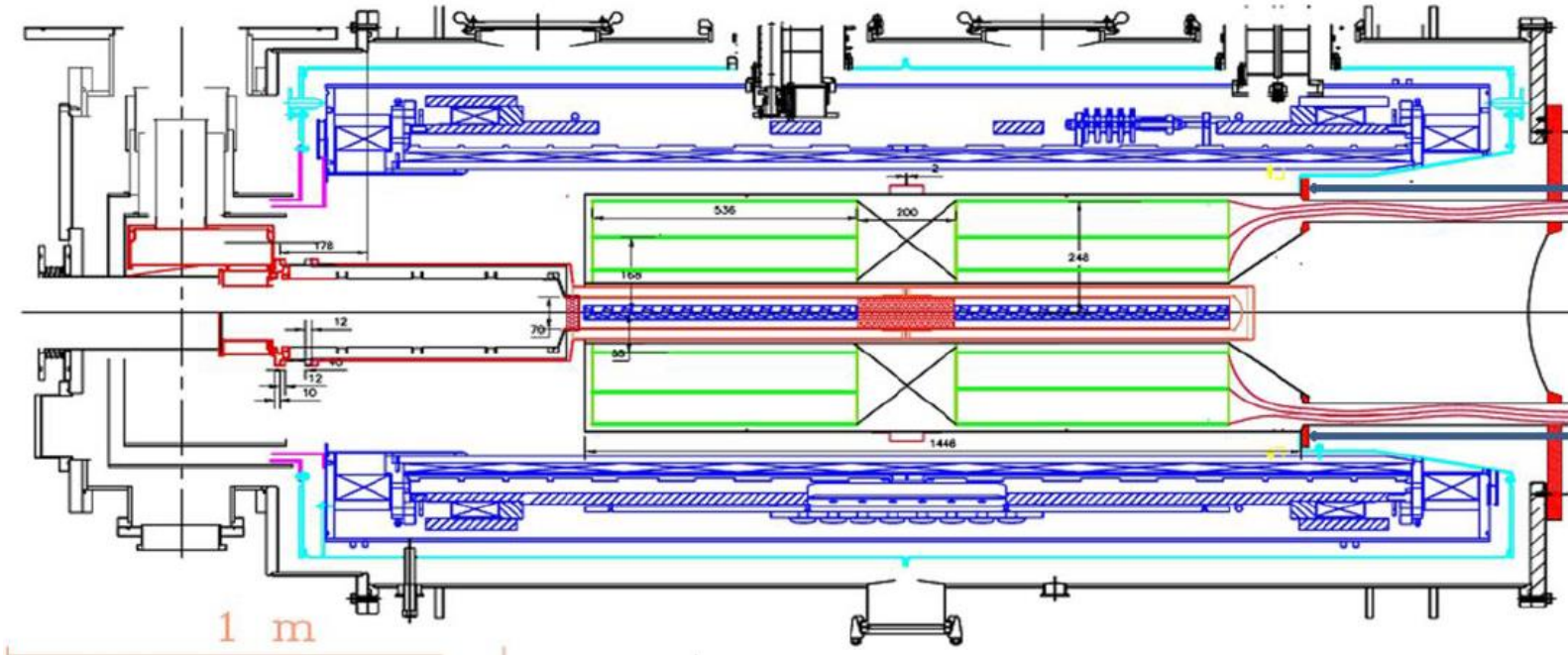
Proton Radius
Meson PDF – gluon PDF
Proton spin structure
3D imaging (TMDs and GPDs)
Hadron spectroscopy
Anti-matter cross section

Program	Physics Goals	Beam Energy [GeV]	Beam Intensity [s^{-1}]	Trigger Rate [kHz]	Beam Type	Target	Earliest start time, duration	Hardware Additions
μp elastic scattering	Precision proton-radius measurement	100	$4 \cdot 10^6$	100	μ^\pm	high-pressure H2	2022 1 year	active TPC, SciFi trigger, silicon veto,
Hard exclusive reactions	GPD E	160	$2 \cdot 10^7$	10	μ^\pm	NH_3^\dagger	2022 2 years	recoil silicon, modified PT magnet
Input for Dark Matter Search	\bar{p} production cross section	20-280	$5 \cdot 10^5$	25	p	LH2, LHe	2022 1 month	LHe target
\bar{p} -induced Spectroscopy	Heavy quark exotics	12, 20	$5 \cdot 10^7$	25	\bar{p}	LH2	2022 2 years	target spectr.: tracking, calorimetry
Drell-Yan	Pion PDFs	190	$7 \cdot 10^7$	25	π^\pm	C/W	2022 1-2 years	
Drell-Yan (RF)	Kaon PDFs & Nucleon TMDs	~ 100	10^8	25-50	K^\pm, \bar{p}	NH_3^\dagger , C/W	2026 2-3 years	"active absorber", vertex det.
Primakoff (RF)	Kaon polarisability & pion life time	~ 100	$5 \cdot 10^6$	> 10	K^-	Ni	non-exclusive 2026 1 year	
Prompt Photons (RF)	Meson gluon PDFs	≥ 100	$5 \cdot 10^6$	10-100	K^\pm π^\pm	LH2, Ni	non-exclusive 2026 1-2 years	hodoscope
K -induced Spectroscopy (RF)	High-precision strange-meson spectrum	50-100	$5 \cdot 10^6$	25	K^-	LH2	2026 1 year	recoil TOF, forward PID
Vector mesons (RF)	Spin Density Matrix Elements	50-100	$5 \cdot 10^6$	10-100	K^\pm, π^\pm	from H to Pb	2026 1 year	

Possible RPD for COMPASS⁺⁺ / AMBER



A recoil proton detector (RPD) is mandatory to ensure the exclusivity. A Silicon detector is included *between* the target surrounded by the modified MW cavity *and* the polarizing magnet



A technology developed at JINR for NICA for the BM@N experiment

No possibility for ToF → PID of p/π with dE/dx
Momentum and trajectory measurements
 $|t|_{\min} \sim 0.1 \text{ GeV}$