

Experimental study of in-medium  
spectral change of  
vector mesons and its polarization  
dependence at J-PARC.

**K. Aoki**

IPNS, KEK

J-PARC Hadron Section.

ExHIC-p workshop on polarization phenomena in nuclear collisions

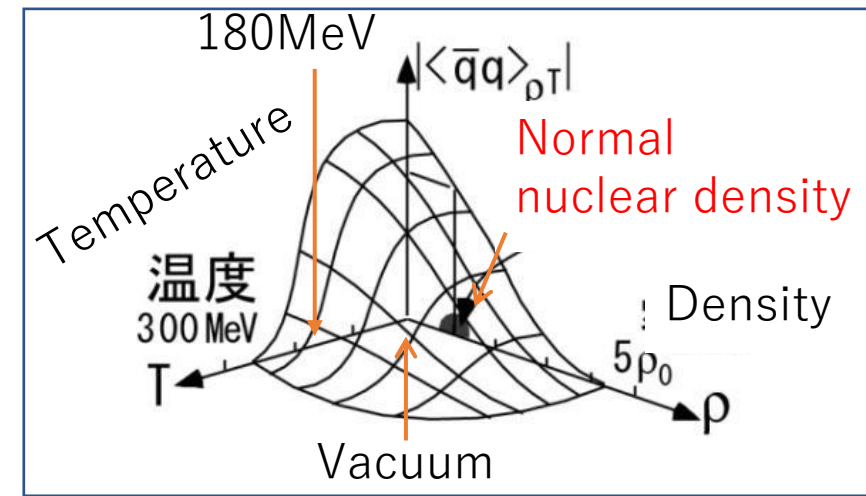
(Mar 16, 2024. Academia Sinica)

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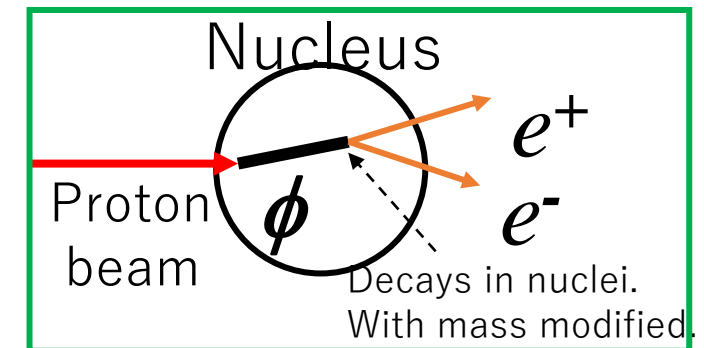
- J-PARC E16 experiment ( $p+A \rightarrow \phi \rightarrow e^+e^-$ )
  - Physics motivation (measure in-medium spectral change of VM)
  - Experimental setup
  - Staging strategy
  - Expected results.
- Measurement of polarization dependence of spectral change.
  - Motivation and principle of spin dependent measurement
  - Expected spectra
  - How to extract spin dependence
  - J-PARC E88 :  $\phi \rightarrow K^+K^-$
- Summary

# Physics

- The origin of Hadron mass.
- The study of QCD vacuum
  - **Spontaneous breaking of the chiral symmetry.**
    - An order parameter:  $\langle \bar{q}q \rangle \neq 0$
    - Depends on temperature, and density
    - **Partially restored even at normal nuclear density.**
    - Could result in a measurable change in mass.
    - $\langle \bar{q}q \rangle \sim 35\%$  reduction at  $\rho_0$  for ***u*** and ***d***. what about ***s***?
  - $\langle \bar{q}q \rangle \leftarrow$  QCD sum rule  $\rightarrow$  mass
- **J-PARC E16 experiment:**
  - Use  $\mathbf{p} + \mathbf{A} \rightarrow \rho / \omega / \phi \rightarrow \mathbf{e} + \mathbf{e}^-$ , (  $\mathbf{K}^+ \mathbf{K}^-$  E88)
  - Dielectron mass spectra are obtained.
    - mixture of decay inside and outside the nuclear target.
    - Sensitive to spectral change of vector mesons in the nuclear medium.
  - Similar to KEK-E325, but collecting more data and doing more systematic study.



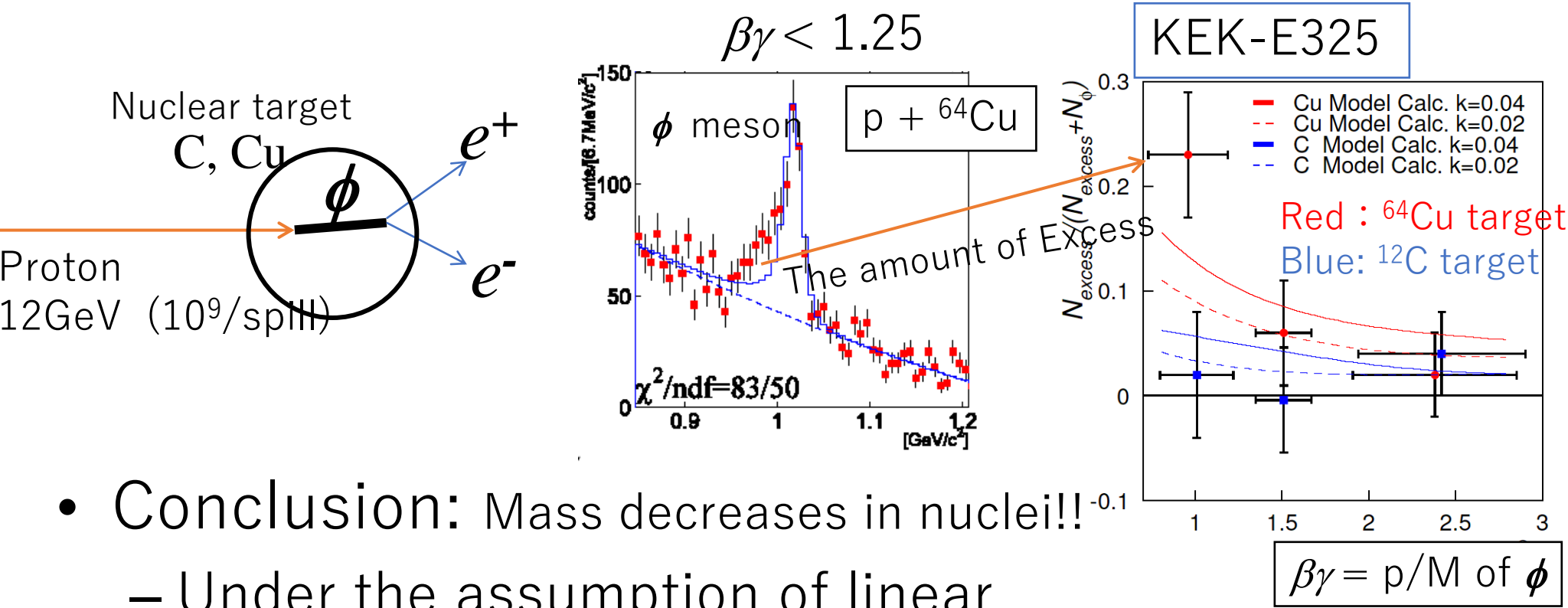
NJL model  
M. Lutz et al.  
Nucl.Phys. A542,52(1992)



J-PARC E16

# KEK-E325 results of $\phi$ meson

- The world's first results of  $\phi$  modification.



Assumption  
In analysis

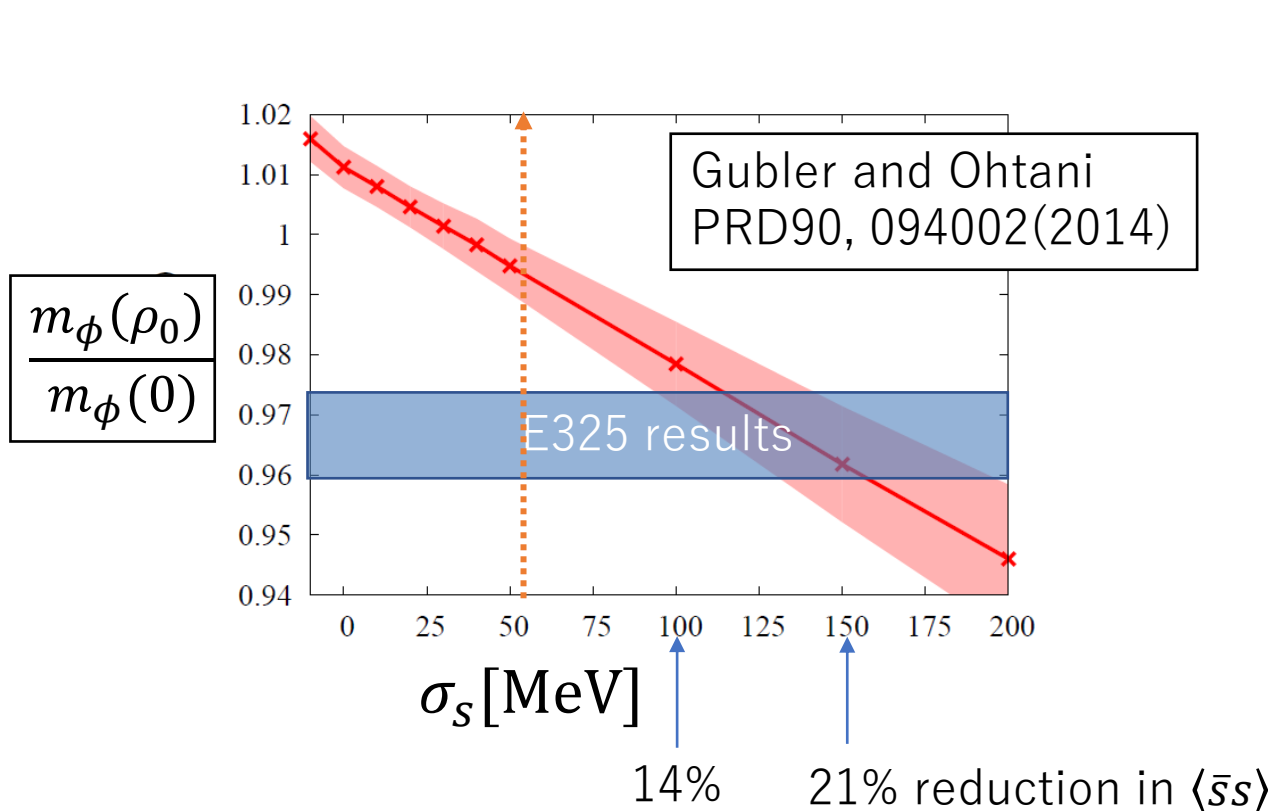
$$\frac{m(\rho)}{m(0)} = 1 - k_1 \left( \frac{\rho}{\rho_0} \right)$$

$$\frac{\Gamma(\rho)}{\Gamma(0)} = 1 + k_2 \left( \frac{\rho}{\rho_0} \right)$$

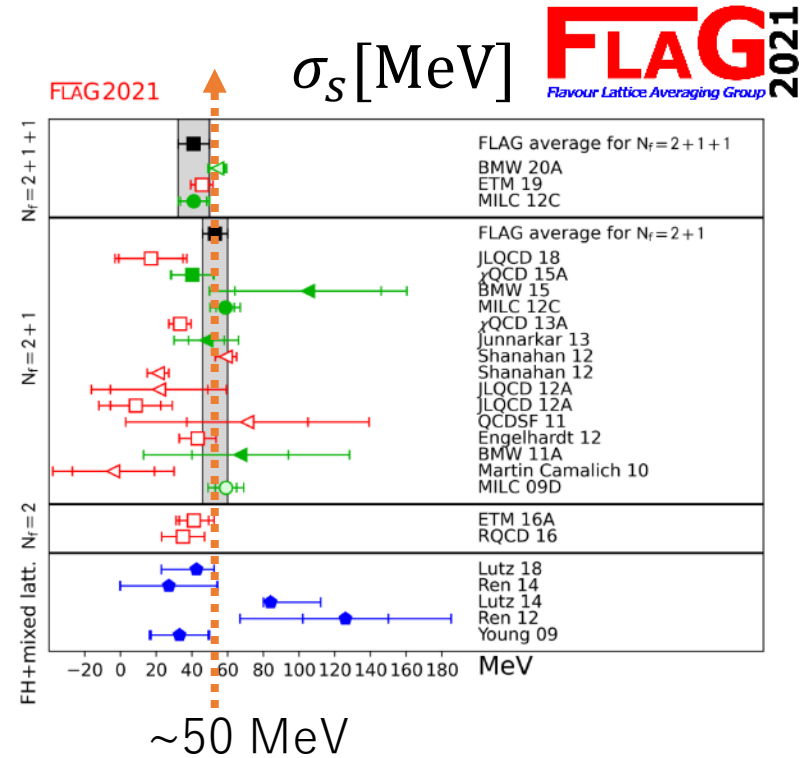
- Conclusion: Mass decreases in nuclei!!
  - Under the assumption of linear dependence of mass and width on density.
    - Mass:  $-3.4^{+0.6}_{-0.7}\%$  ↓ At normal nuclear density
    - Width:  $\times 3.6^{+1.8}_{-1.2}$

# QCD sum rule results

They provide mass of  $\phi$  meson vs  $\sigma_s$  (strangeness sigma term)  
 The  $\sigma_s$  indicates how much  $\langle \bar{s}s \rangle$  is reduced in nuclear matter.



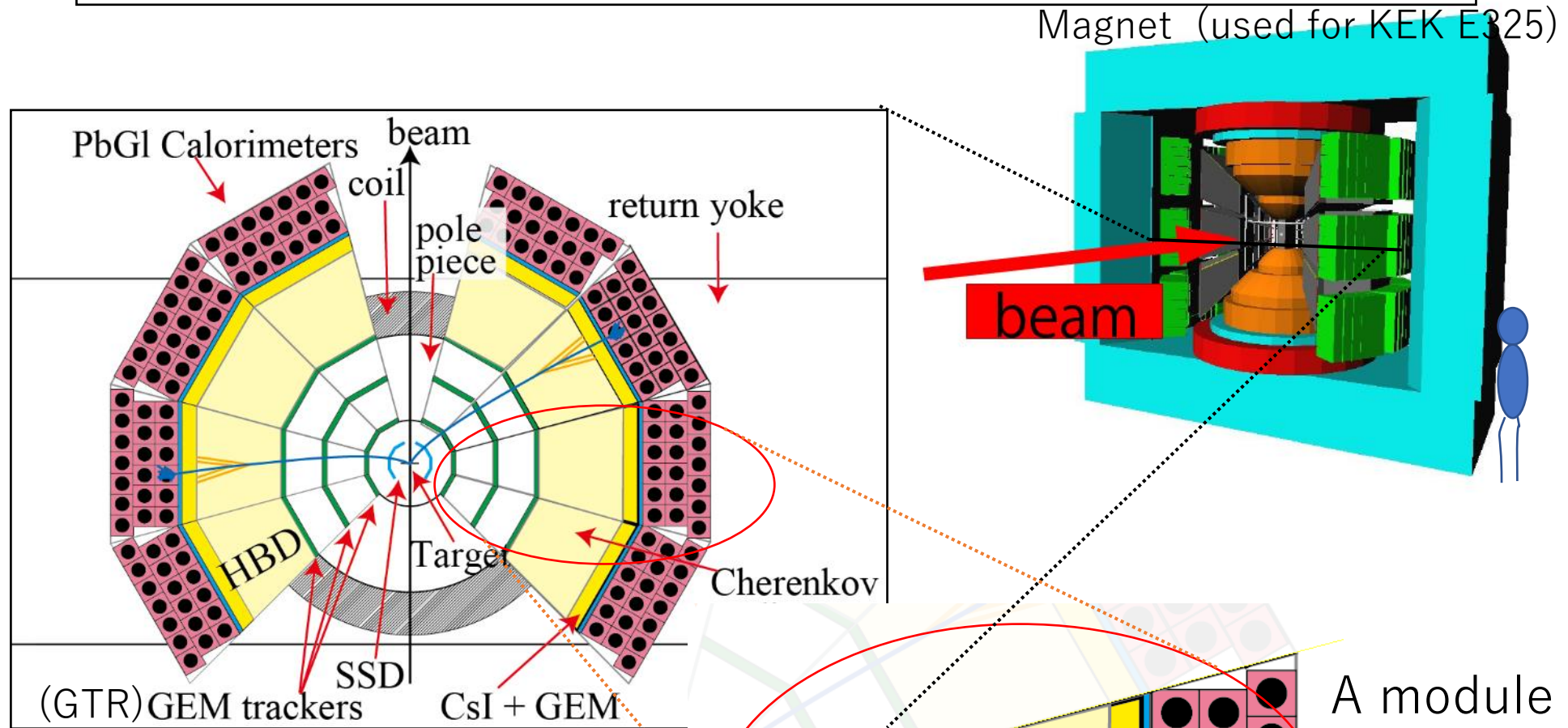
If one takes  $\sigma_s$  from Lattice and QCD sum rule,  
 Mass reduction should be much smaller. ( $dM < \sim 1\%$ )



$$\langle \bar{s}s \rangle_\rho = \langle \bar{s}s \rangle_0 + \langle N | \bar{s}s | N \rangle \rho$$

$$\sigma_s = m_s \langle N | \bar{s}s | N \rangle \quad (= m_s \frac{\partial M_N}{\partial m_s})$$

# The J-PARC E16 spectrometer



SSD : Tracking

GTR : Tracking

HBD : eID (Cherenkov)

LG : eID (Calorimeter)

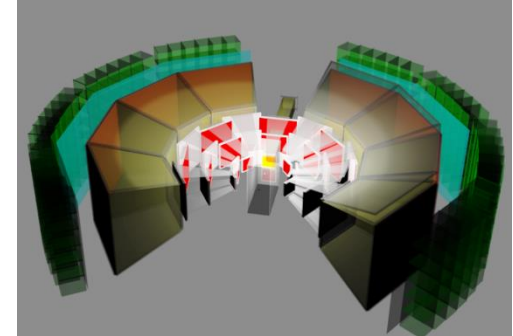
26 modules in total. 8 for the 1<sup>st</sup> physics run.

# Staging approach

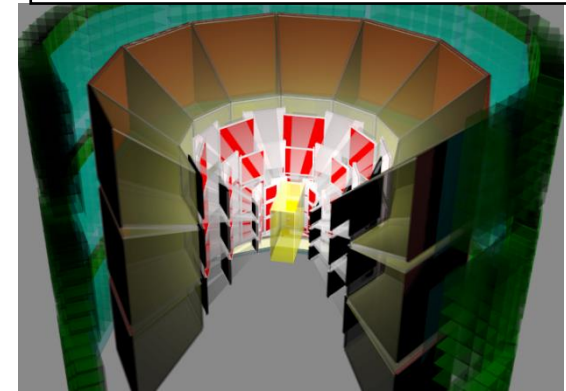
- **RUN 0a/b/c/d - 2020,2021,2023** – 413hrs.
    - **10 (SSD) + 8 (GTR) + 8 (HBD) + 8 (LG)** at last
      - Gradually increased acceptance and reached interm. Goal.
    - C+Cu targets
    - Beam / Detector commissioning
  - **RUN 0e - 2024 -- 222 hours.**
    - **8(SSD) + 10 (GTR) + 8 (HBD) + 8 (LG)**
    - Beam / Detector comm. + yield.
    - Upgraded Accelerator / DAQ. / Detectors.
- 
- **RUN 1 2024(?)** -- 1280hrs (~53days)
    - **10 (SSD) + 10 (GTR) + 8 (HBD) + 8(LG)**
    - Physics data taking.  $\phi$ : 15k for Cu.
  - **RUN 2** -- 2560 hrs (~107 days)
    - **26 (SSD) + 26 (GTR) + 26 (HBD) + 26 (LG)**
    - + Pb/CH2 target
    - Needs additional budget.

↑ PAC approved

RUN 1 (8 modules)

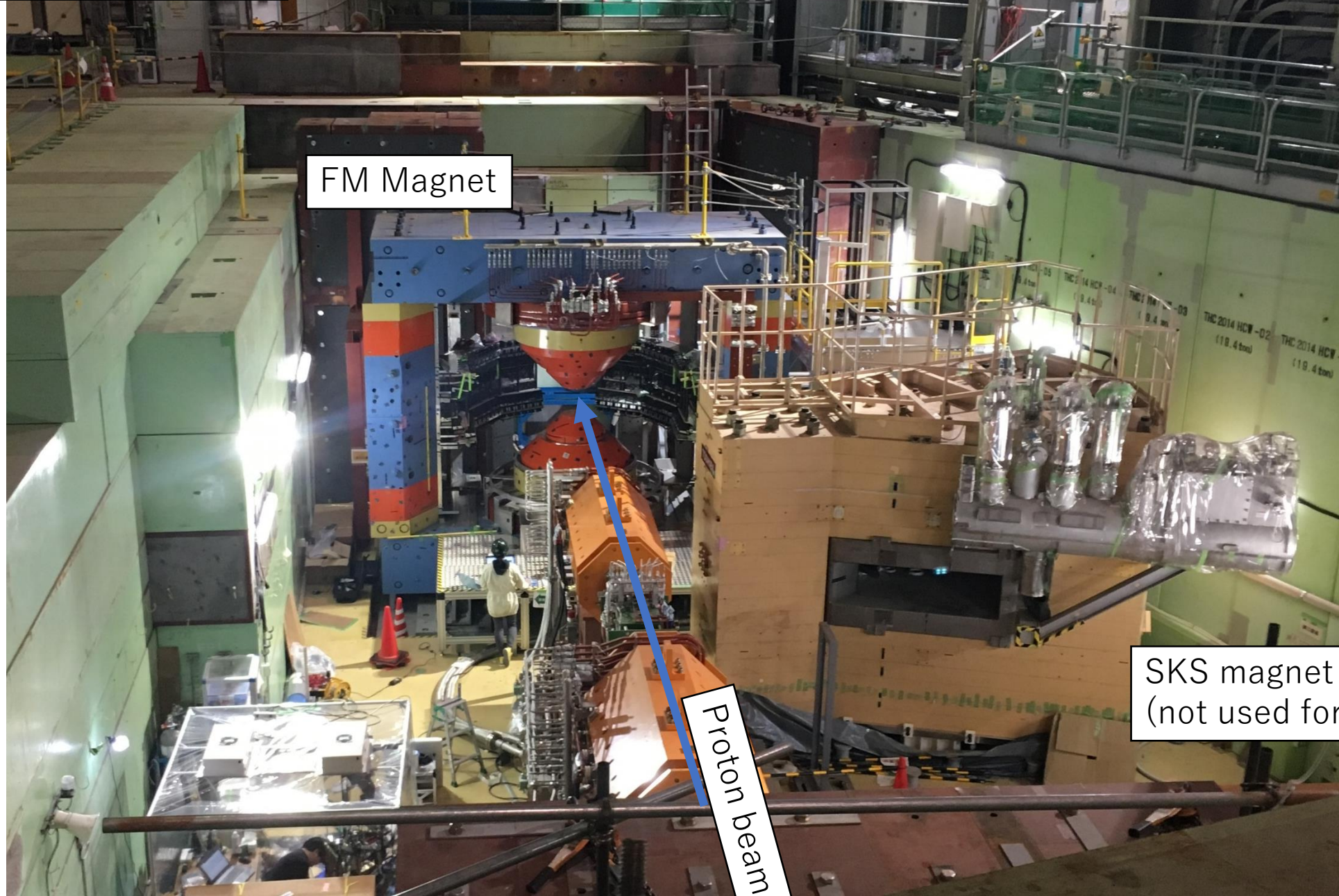


RUN 2 (26 modules)



# High-p Area

Photo taken in 2019 or so.  
Shield blocks now cover the area and hard to get this view.

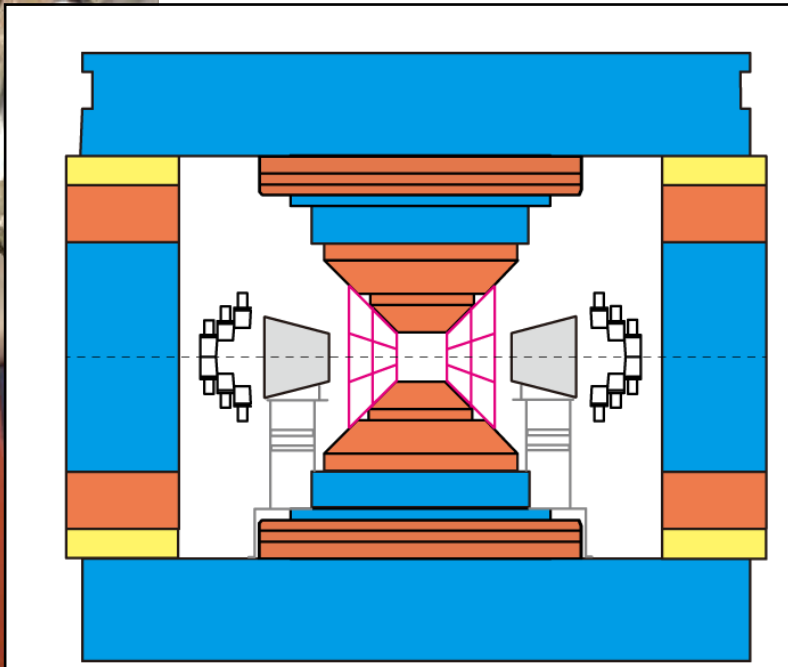
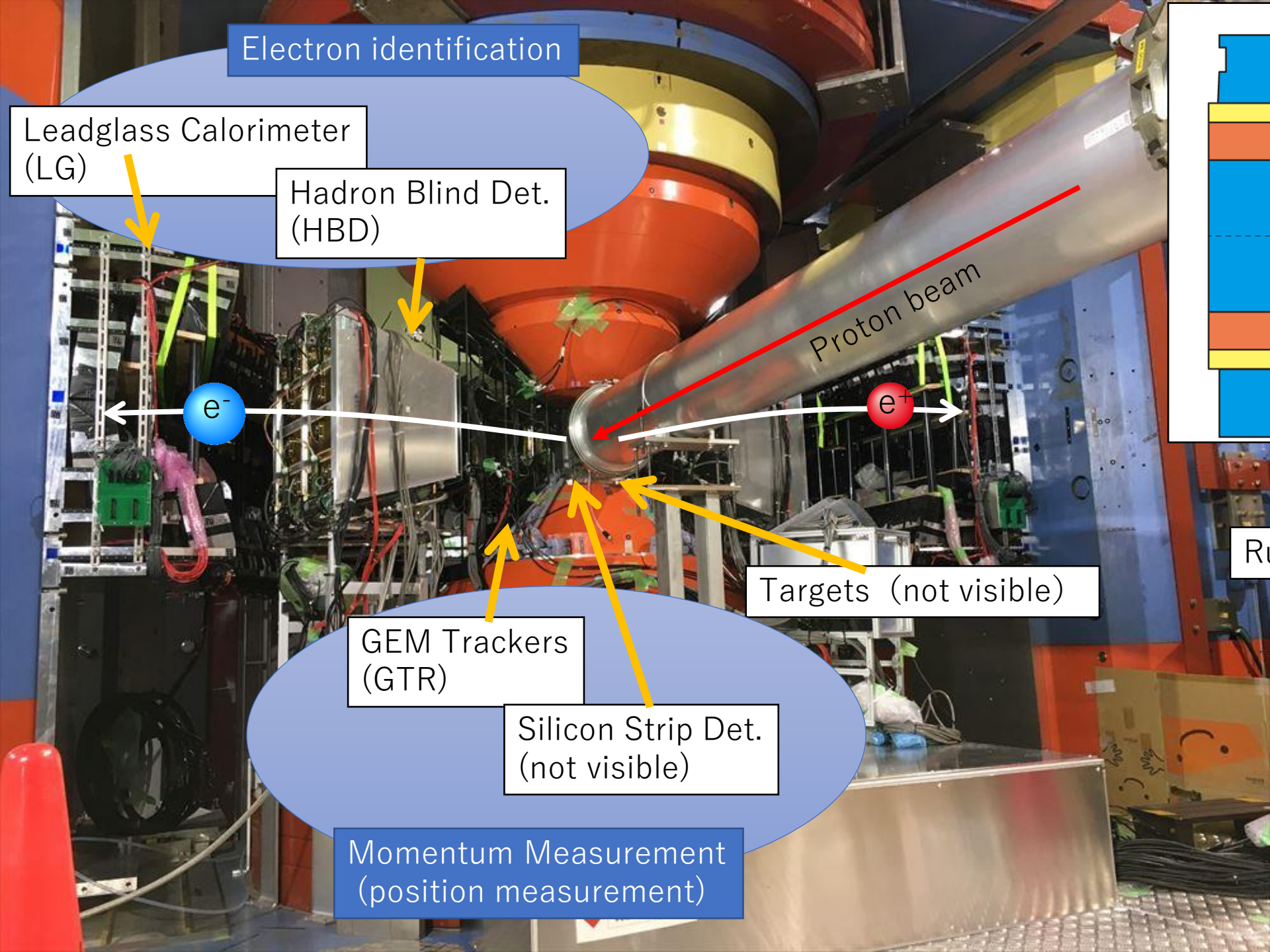


FM Magnet

SKS magnet  
(not used for E16)
















Proton beam





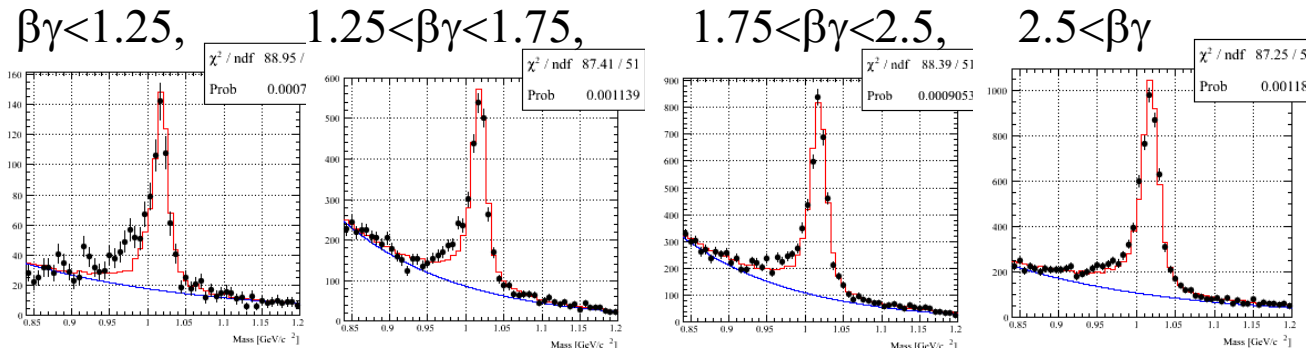
Run0b/c configuration(2021)

# J-PARC E16 Collaboration

- RIKEN 
  - S. Yokkaichi  
(spokesperson)
  - H. En'yo
  - F. Sakuma
- KEK 
  - K. Aoki
  - R. Honda
  - K. Kanno
  - Y. Morino
  - R. Muto
  - W. Nakai
  - K. Ozawa
  - S. Sawada
  - M. Sekimoto
  - H. Sugimura
- Univ. of Tokyo 
  - J. Kakunaga
  - H. Murakami
  - T.N. Murakami
- Kyoto Univ. 
  - M. Ichikawa
  - S. Nagafusa
  - S. Nakasuga
  - M. Naruki
  - S. Ochiai
- RCNP 
  - S. Ashikaga
  - H. Noumi
  - K. Shirotori
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  - H. Hamagaki
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  - R. Ejima
  - R. Yamada
  - Y.L. Yamaguchi
- JASRI 
  - A. Kiyomichi
- Univ. Tsukuba  筑波大学
  - T. Chujo
  - S. Esumi
  - T. Nonaka
- JAEA 
  - H. Sako
  - S. Sato
- BNL  Brookhaven National Laboratory
  - T. Sakaguchi
- Tohoku Univ.  東北大学
  - S. Kajikawa
- Academia Sinica 
  - W.-C. Chang
  - C.-H Lin
  - C.-S. Lin
  - P.-H. Wang
- GSI 
  - J. Heuser
  - A.R. Rodriguez
  - M. Teklishyn
- Goethe Univ.  GOETHE UNIVERSITÄT FRANKFURT AM MAIN
  - D.R. Garces
  - A. Toia

# RUN1, Cu (INPUT:E325-BW)

## Excess ratio vs $\beta\gamma$

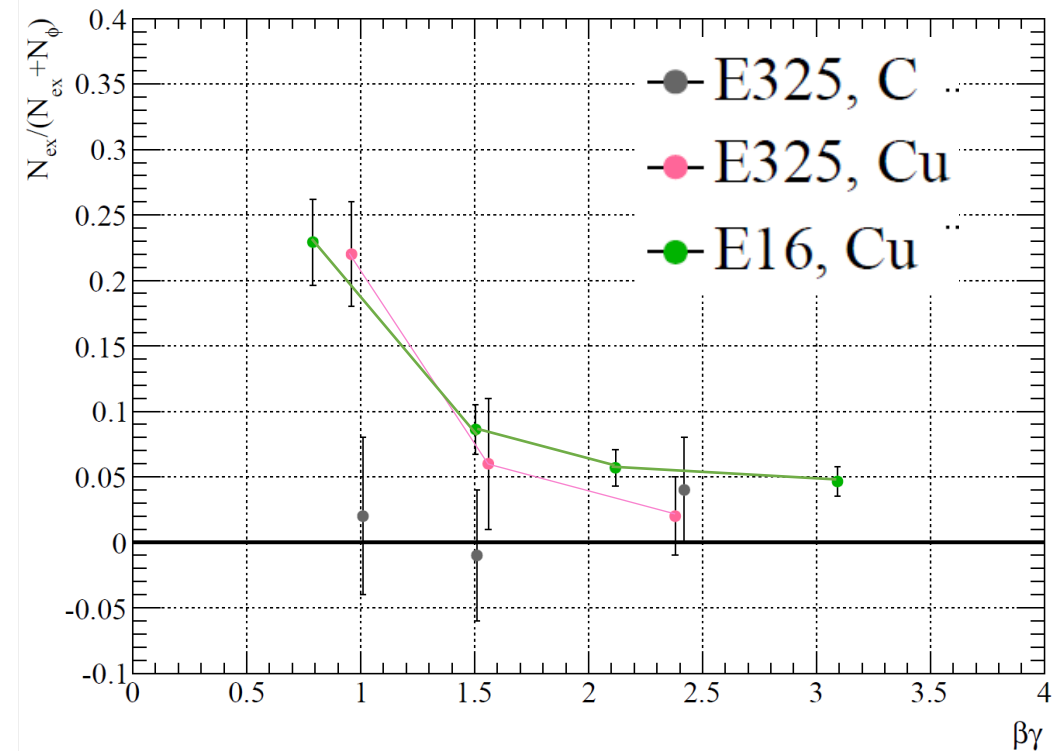
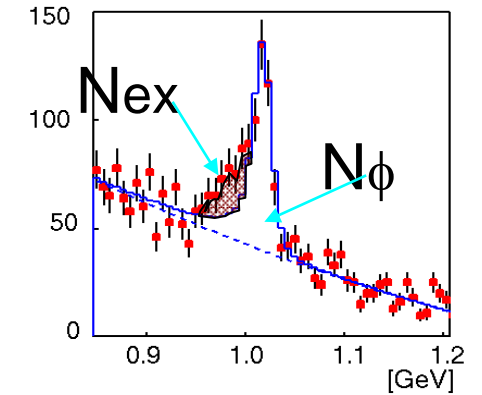


(Fit fails when vacuum shapes are used.)

- ~15k  $\phi$  for Cu target expected in RUN1
- All  $\beta\gamma$  bins for Cu are significant in E16
- (cf) E325 only fastest  $\beta\gamma$  bin is significant.

- Larger excess in lower  $\beta\gamma$  bin.
- The tendency becomes clearer and more significant compared to E325.

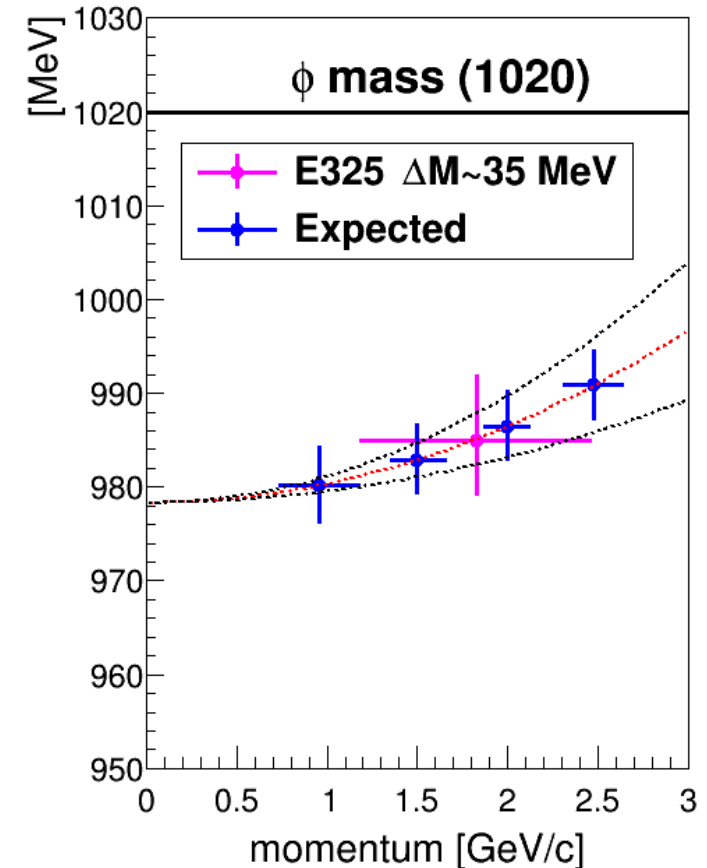
$$\frac{N_{excess}}{N_{excess} + N_{\phi}}$$



# Momentum dependence (Dispersion relation)

- Momentum dependence of mass can be obtained for the first time.
- Expectation of  $RUN1 \times 1.7$  is shown.
- Dispersion relation itself is an important property of pseudo particles.
- We can extrapolate mass into 0 momentum, where most of the QCDSR calculation results apply.
- More discussion on later slides.

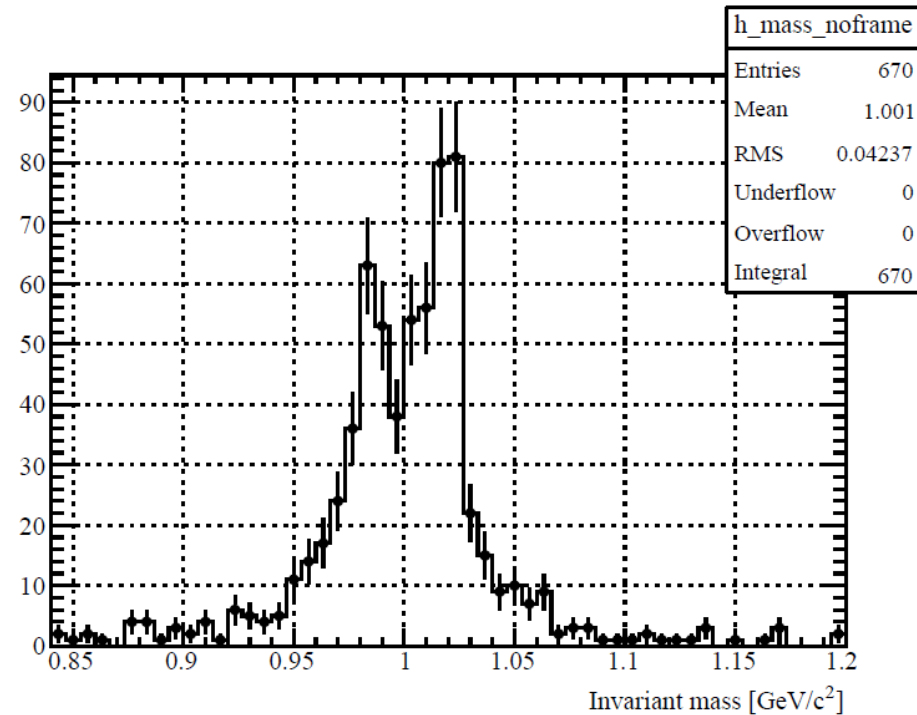
H.Kim P. Gubler PLB805, 10 (2020) extends the validity of momentum range.  
Show you on later slides.



S.H. Lee PRC57, 927(1998)

# Expected in RUN2

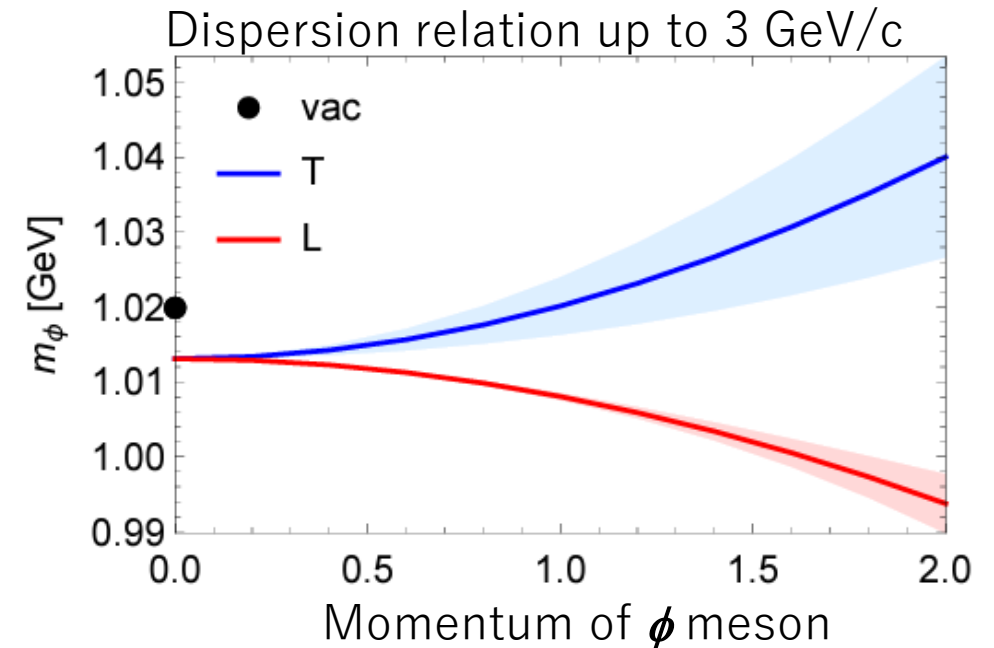
- RUN2 stat (320shifts)
- INPUT: E325-BW
  
- Pb target
- $\beta\gamma < 0.5$



Measurement of polarization  
dependence

# Pol dependence of mass distribution

- PLB805 (2020) 135412, Kim-Gubler
  - Prediction of the dispersion relation of phi meson based on the QCD sum rule.
  - Polarization dependence.
  - Interesting to see it experimentally.
- Decay angle  $\phi \rightarrow e+e / K+K^-$
- Expected spectrum
  - Based on E325-type model calc.
- How can we experimentally separate
  - Finding orthogonal functions.
- Do the methods work?



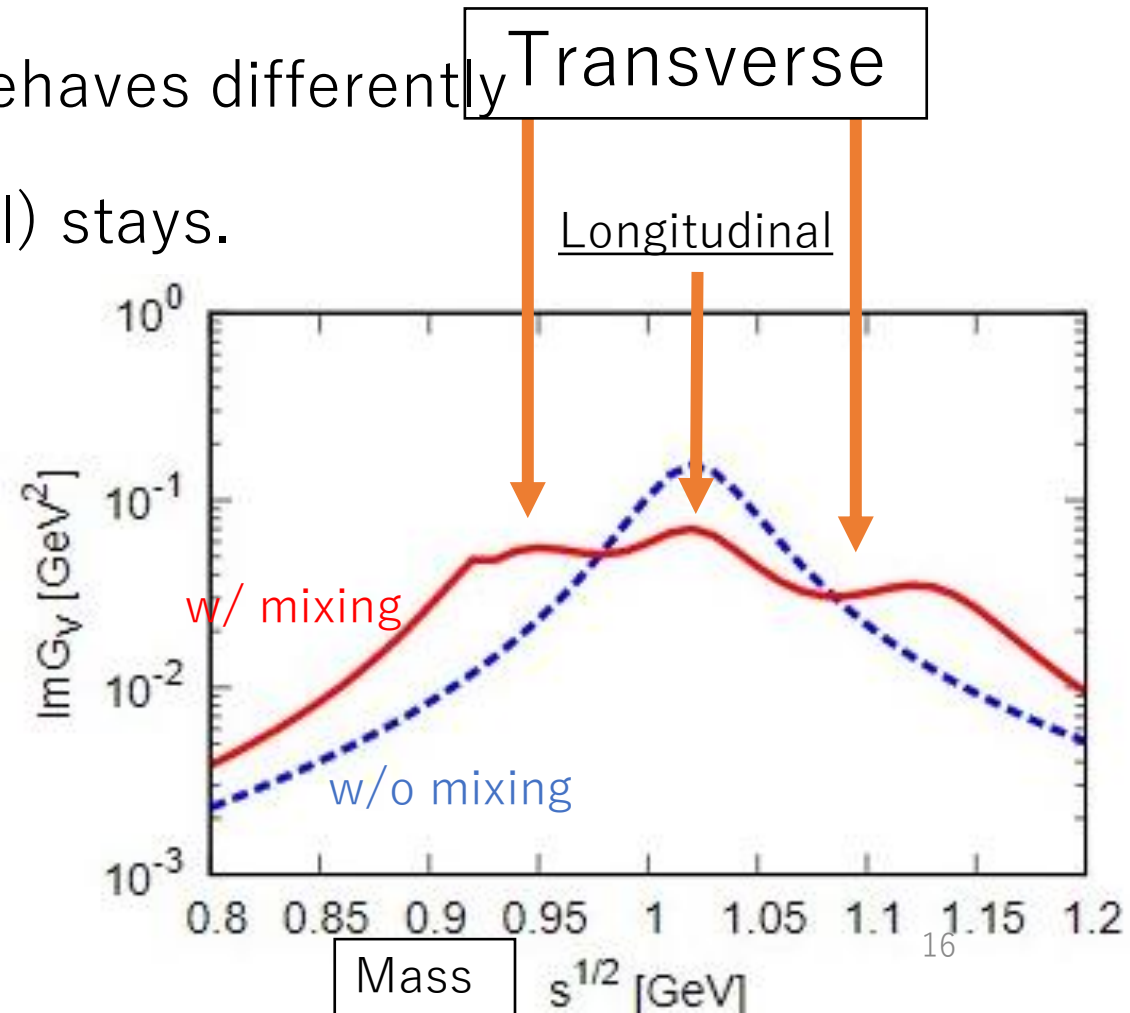
# Anomaly-induced chiral mixing of $\phi$ and $f_1(1420)$

- Genuine signal of chiral symmetry restoration:  
Degeneracy of chiral partner! by theorists.
- Phys. Rev. D106, 5 (2022) C. Sasaki
  - Chiral mixing effect in dense matter behaves differently when chiral symmetry is restored.
  - T(Transverse) affected. L(Longitudinal) stays.
- Motivation for T/L separation

$$p = 1.0 \text{ GeV}/c$$

$$T = 50 \text{ MeV}$$

$$\rho = 2.5\rho_0$$





# Polarization $\leftrightarrow$ Angular dist. in helicity rest frame

- Phys. Rev. D 107, 074033(2023)  
I.W. Park, H. Sako, K.A., P.Gubler, S.H.Lee

## • $\phi \rightarrow ee$

- Spin 1 is taken by the spin of ee.

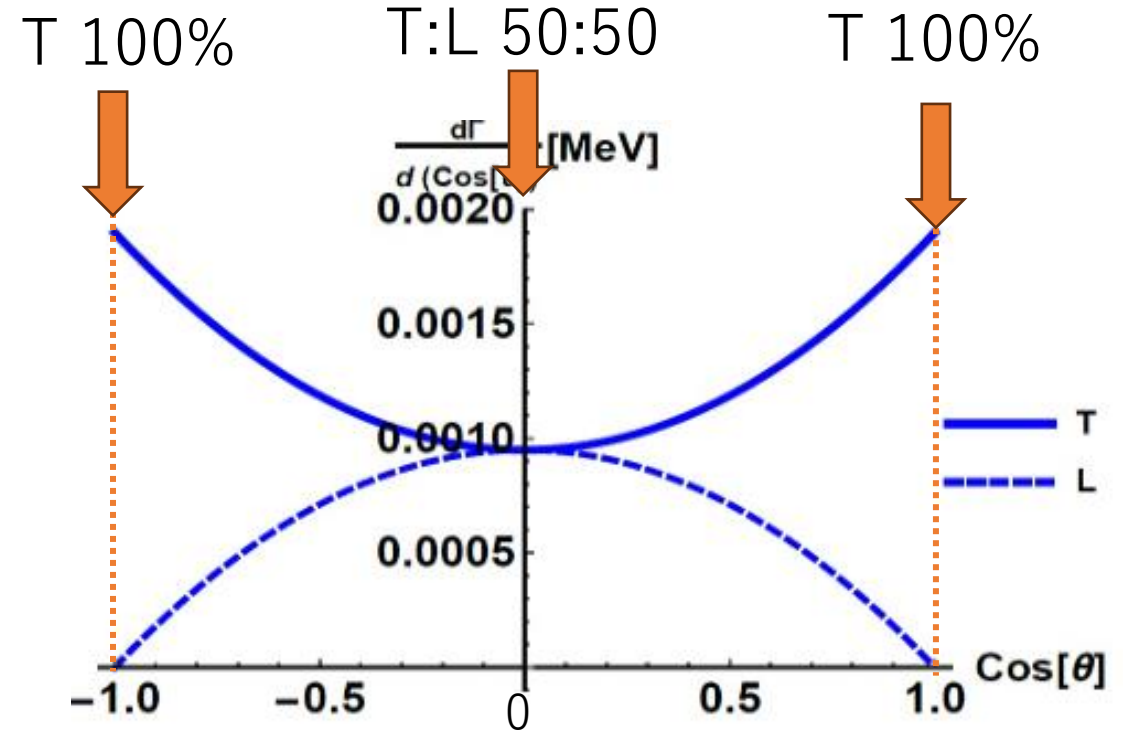
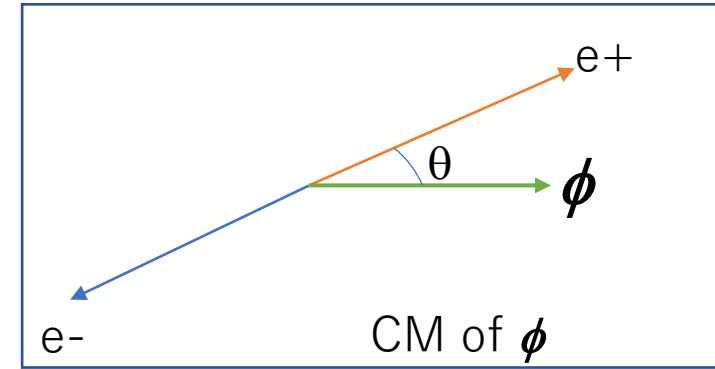
☺ •  $\cos \theta = \pm 1$  : T 100%

☹ •  $\cos \theta = 0$  : L 50%, T 50%

☺ • Small FSI

☹ • Limited acceptance at  $\cos \theta = \pm 1$

Helicity rest frame (of  $\phi$  meson)



$\phi \rightarrow e+e-$

# $\phi \rightarrow e^+e^-$ vs $\phi \rightarrow K^+K^-$

## $\phi \rightarrow e^+e^-$

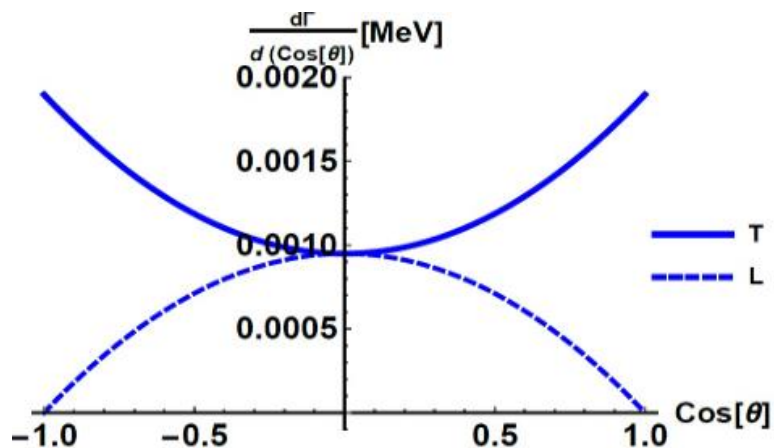
- Spin 1 is taken by ee **pol.**

😊 •  $\cos \theta = \pm 1$  : T 100%

☹️ •  $\cos \theta = 0$  : L 50%, T 50%

😊 • Small FSI

- ☹️ • Small BR ( $2.98 \times 10^{-4}$ )
  - 15k for 53 days (E16 Run1)



## $\phi \rightarrow K^+K^-$

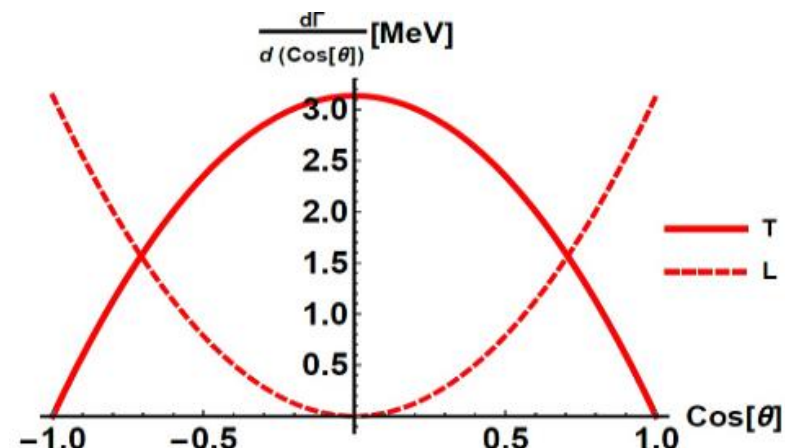
- Spin 1 is taken by KK **OAM**

😊 •  $\cos \theta = \pm 1$  : L 100%

😊 •  $\cos \theta = 0$  : T 100%

- ☹️ • Suffer from FSI
  - Treated by transport model

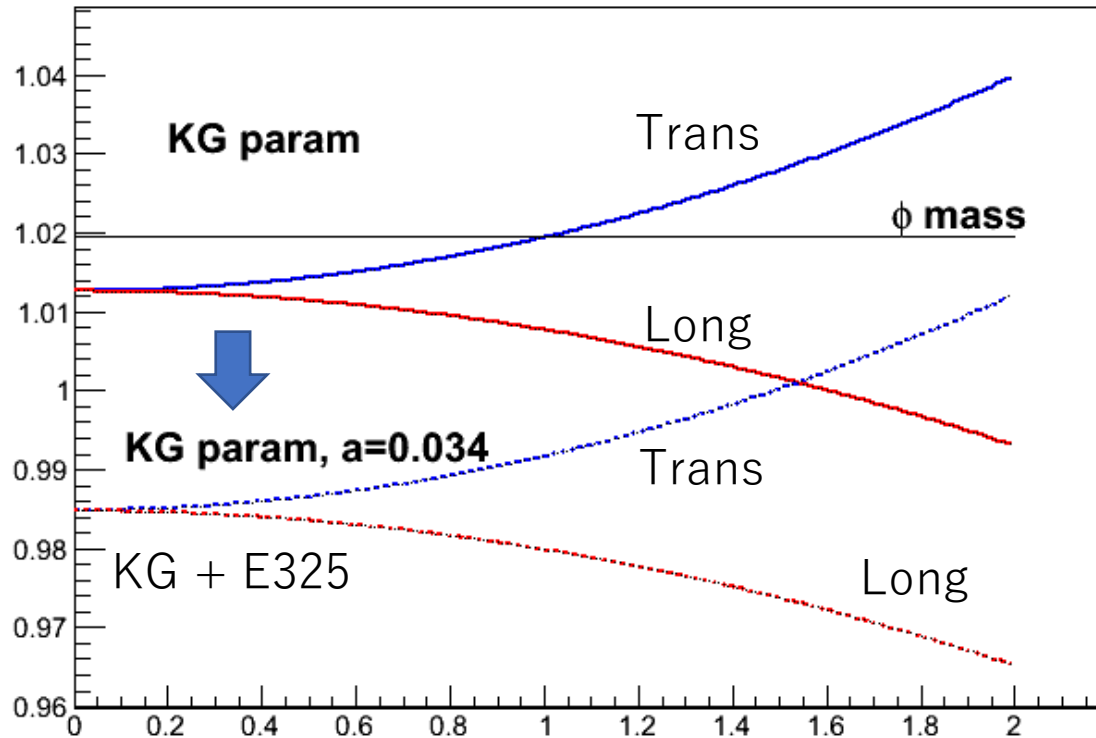
- 😊 • Large BR (49.1%)
  - 260k for 30 days (E88)



# Play with Kim-Gubler model to get expected mass spectra

- PLB 805, 10 (2020)
  - T: Transverse / L: Longitudinal
  - T : L = 2:1
- I replaced the shift with the E325 value.

$$\frac{m_{\phi}^{L/T}(\rho_N, \vec{q})}{m_{\phi}^{\text{vac}}} = 1 + \left( a + b^{L/T} |\vec{q}|^2 \right) \frac{\rho_N}{\rho_0}$$



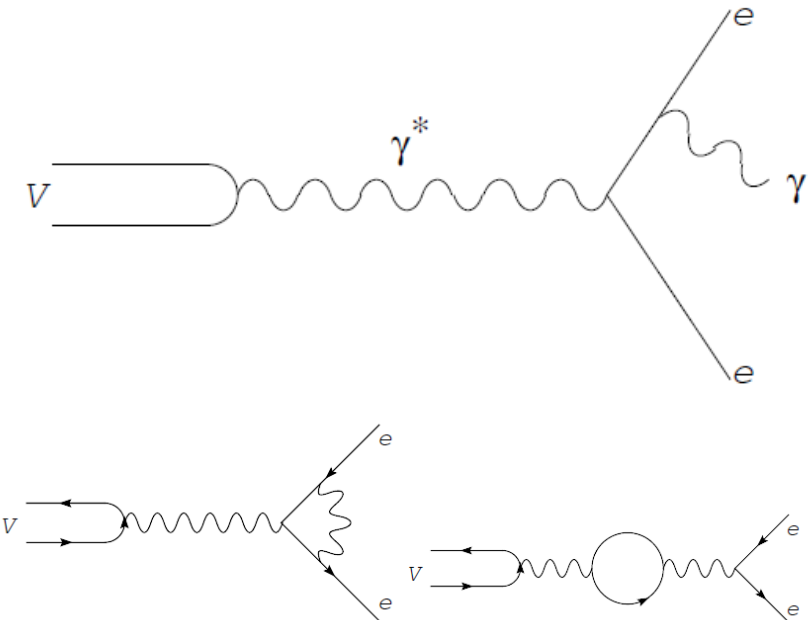
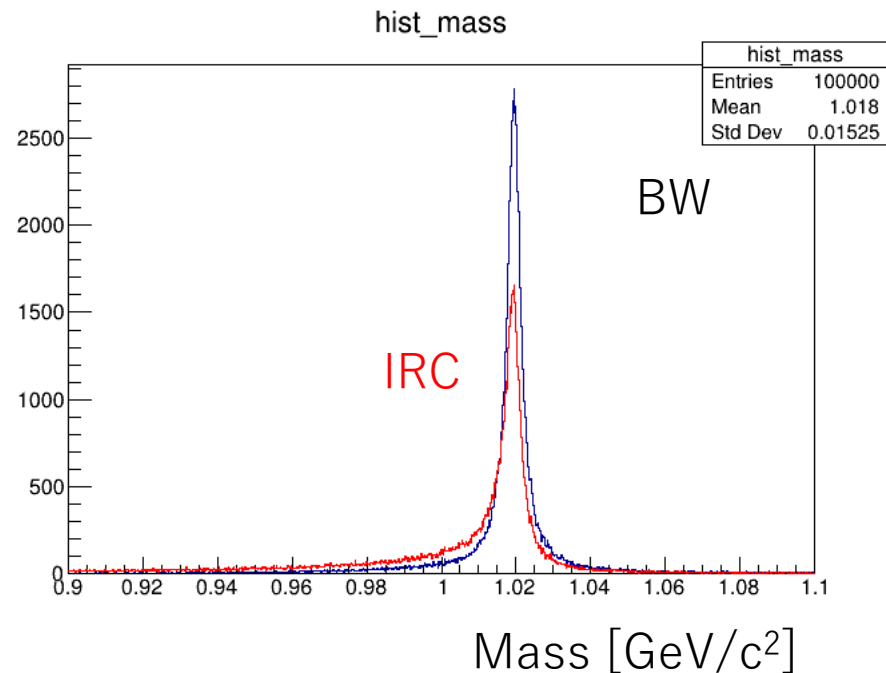
- KG param
  - $b(T) = 0.067 \text{ pm } 0.0034$
  - $b(L) = -0.0048 \text{ pm } 0.0008/\text{GeV}$
  - $a = -0.0067$



- KG + E325 param
  - $a=0.034$
  - $b$  : same as KG param.

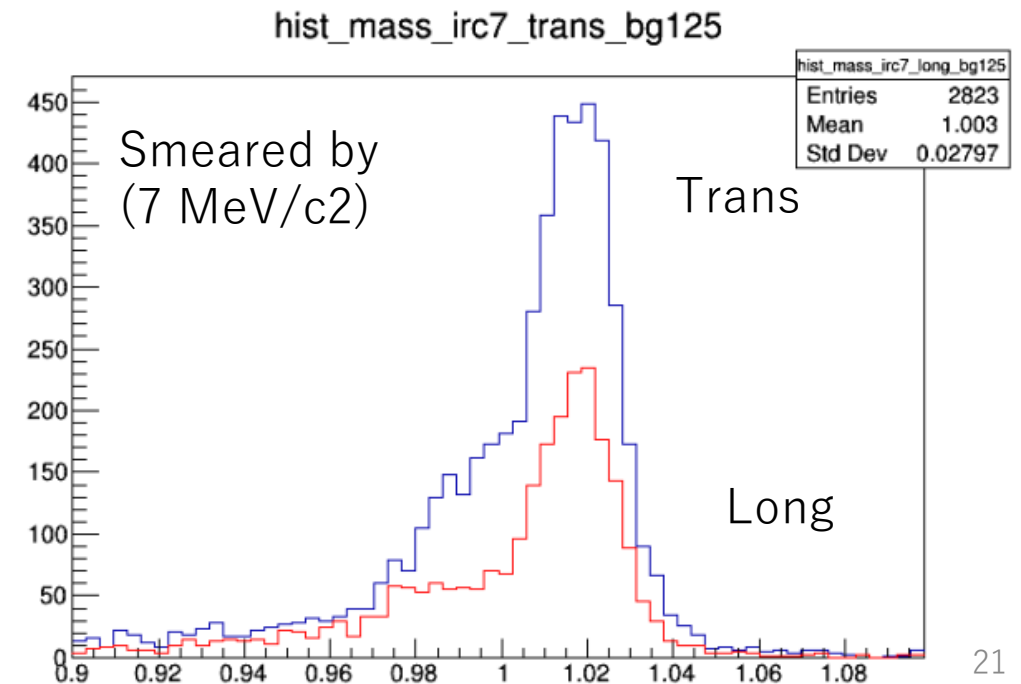
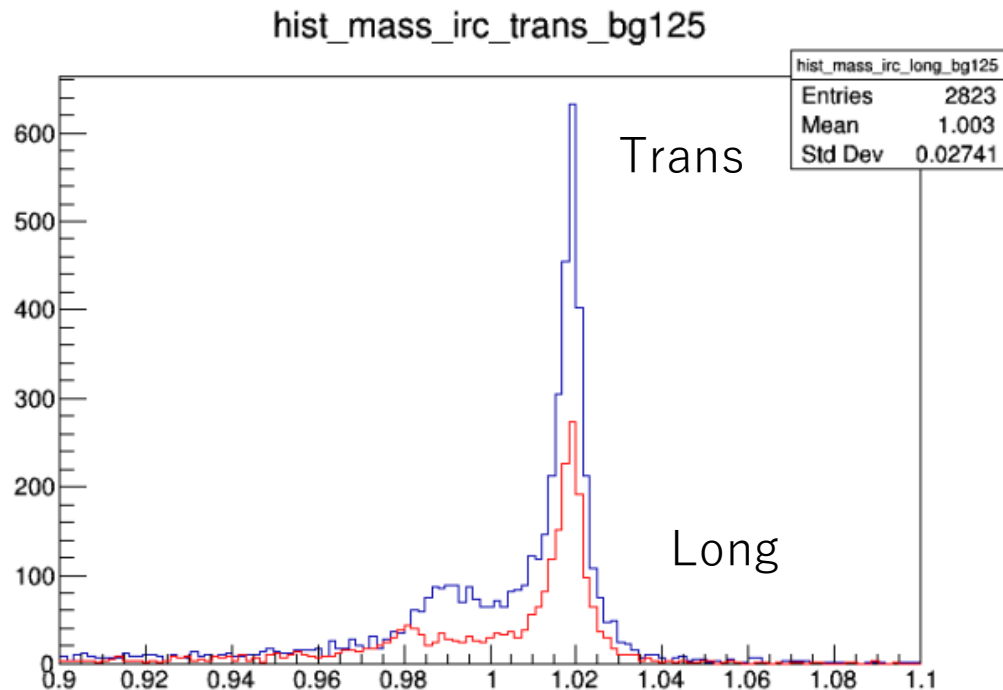
# Monte Carlo simulation input

- Momentum distribution is taken from JAM.
- Mass: Breit-Wigner distribution.
- Internal Radiative Correction (IRC)
  - Calculated by PHOTOS
  - IRC makes a tail on the lower side.



# E325-type calculation using KG param.

- E325 model assumption
  - Density assumed to be WS potential shape.
  - $\phi$  production probability proportional to density.
    - According to mass-number dependence of  $\sigma$  ( $\sigma_{pA} \sim A$ )
  - # of entries is arbitrary.
    - (cf) Run1 exp:  $\sim 1.7k$  ( $\beta\gamma < 1.25$ ), Run2 exp: 12k for ( $\beta\gamma < 1.25$ )
- Smearing (mimic experimental effect)
  - Mass by 7 MeV/c<sup>2</sup>,  $\cos(\theta)$  by 0.01



Basic idea: find orthogonal func. (to extract T. mass)

- $G(m, x)$ : Measured mass ( $m$ ) and angle ( $x = \cos \theta$ ) distribution:

$$G(m, x) = g_T(m) f_T(x) + g_L(m) f_L(x)$$

Measured

Want to know

Known

Want to know

Known

- $g_{T,L}(m)$ : Mass distribution for T and L.
- $f_{T,L}(x)$ : Daughter particle's angular distribution for T and L.

$$f_T(x) \propto (1 + x^2)$$

$$f_L(x) \propto (1 - x^2).$$

- If we can find a function  $h_T(x)$  that is orthogonal to  $f_L(x)$

- $h_T(x)$ : eliminates L and what's left is T.

$$\int_a^b h_T(x) G(m, x) dx = h_T(x) g_T(m) f_T(x) + h_T(x) g_L(m) f_L(x)$$

Measured

Want to know

Known

Want to know

Known

$$\begin{aligned} \int_a^b G(m, x) h_T(x) dx &= \int_a^b [g_T(m) f_T(x) h_T(x) + g_L(m) f_L(x) h_T(x)] dx \\ &= g_T(m) \int_a^b f_T(x) h_T(x) dx \\ &= g_T(m) \times \text{Const.} \end{aligned}$$

# Finding orthogonal functions

- The Gram-Schmidt's method:
  - Assume we have  $\alpha_1(x), \alpha_2(x)$  and build two functions:

$$\begin{array}{l} \alpha_1 \\ \alpha_2 - \frac{\langle \alpha_1 \cdot \alpha_2 \rangle}{\langle \alpha_1 \cdot \alpha_1 \rangle} \alpha_1 \end{array} \begin{array}{l} \curvearrowright \\ \curvearrowleft \end{array} \text{Orthogonal to each other.} \quad \langle \alpha_1 \cdot \alpha_2 \rangle = \int_a^b \alpha_1(x) \alpha_2(x) dx$$

- $h_L(x)$  : (orthogonal to  $f_T$  = eliminates T) extracts L.
- $h_T(x)$  : (orthogonal to  $f_L$  = eliminates L) extracts T.

$$x = \cos \theta = [-1, 1]$$

$$f_T = 1 + x^2$$

$$f_L = 1 - x^2$$

$$h_T = 5x^2 - 1$$

$$h_L = 2 - 5x^2$$

$$x = \cos \theta = [-0.8, 0.8]$$

$$f_T = 1 + x^2$$

$$f_L = 1 - x^2$$

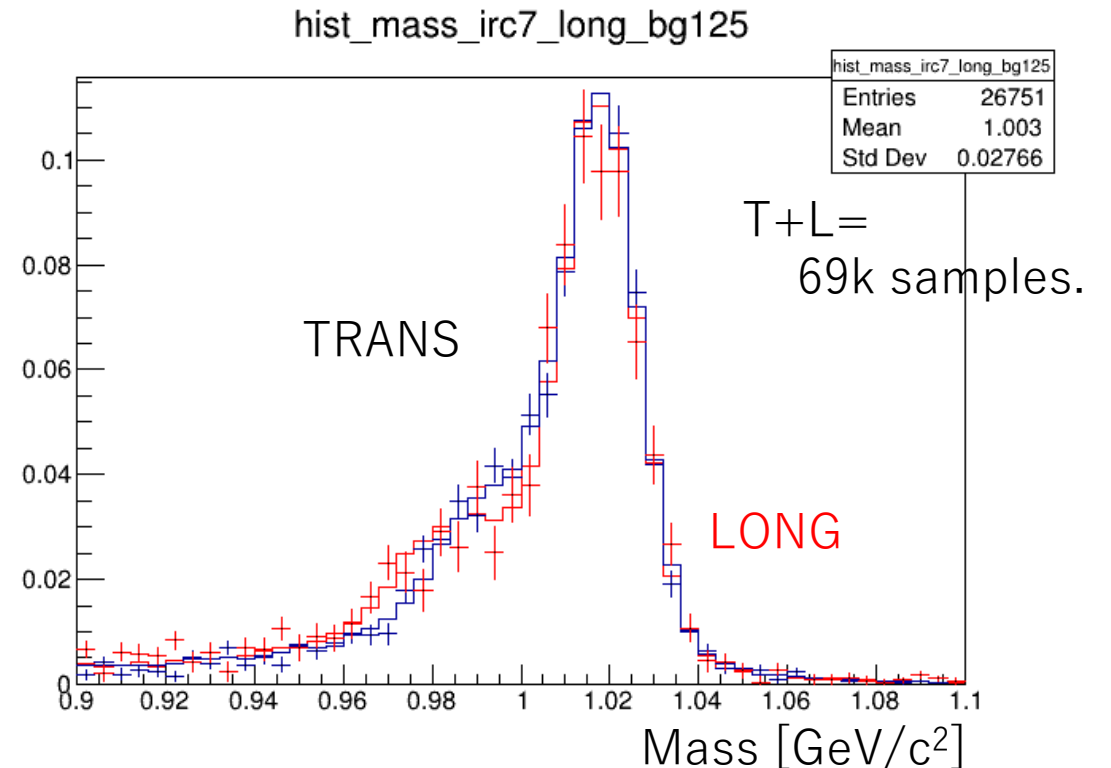
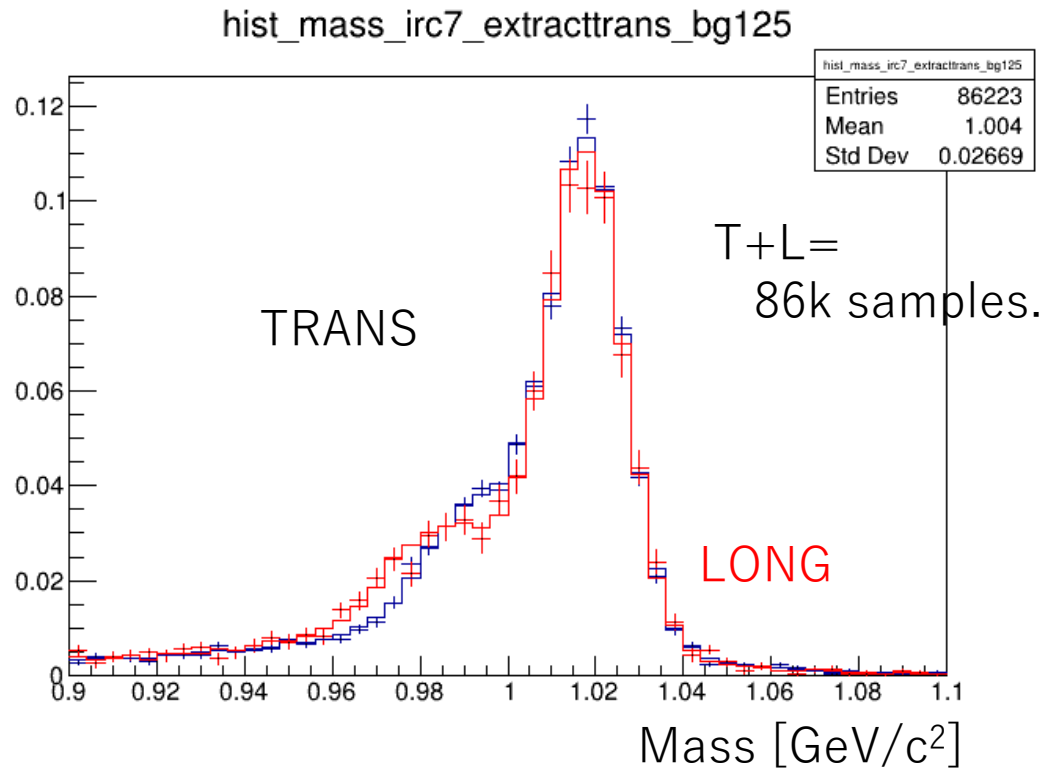
$$h_L = 3.1897 - 13.108x^2$$

$$h_T = 13.1077x^2 - 2.18963$$

# The method applied. for $\beta\gamma < 1.25$ sample.

- $\cos \theta = [-1,1]$

- $\cos \theta = [-0.8,0.8]$



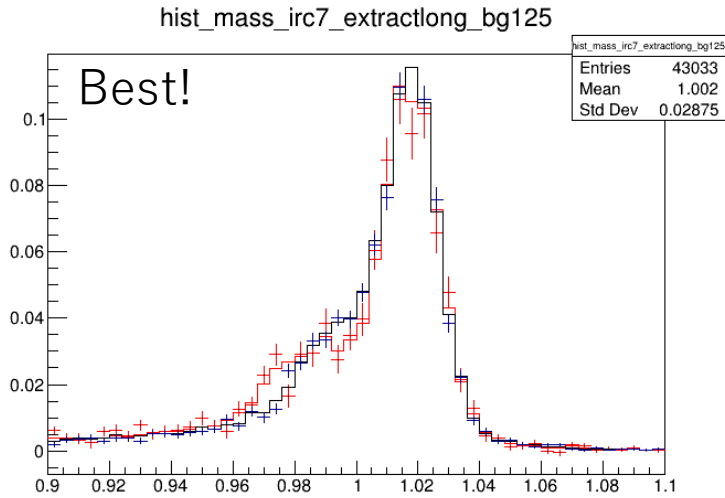
LINE : According to polarization information which God only knows

+ : Extracted using the orthogonal functions  $h_T(x), h_L(x)$

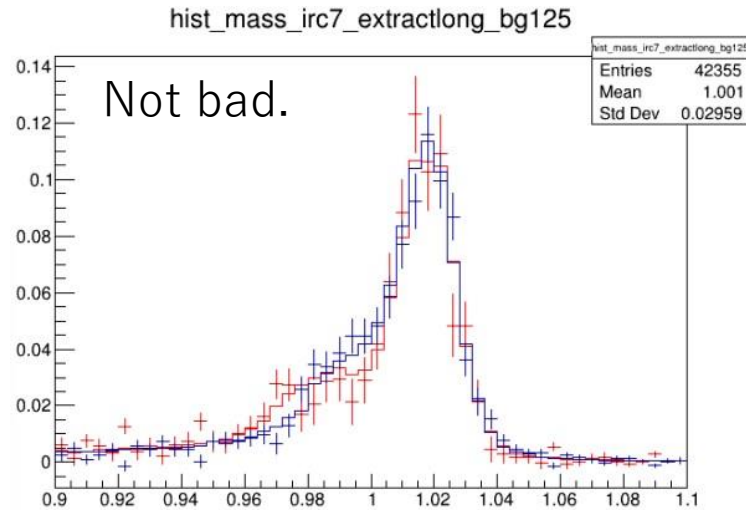


# Same statistics but different angular acceptance in the rest frame of $\phi$ .

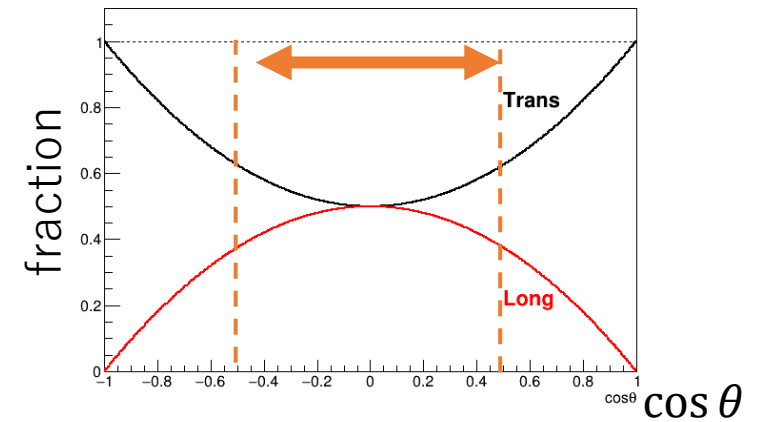
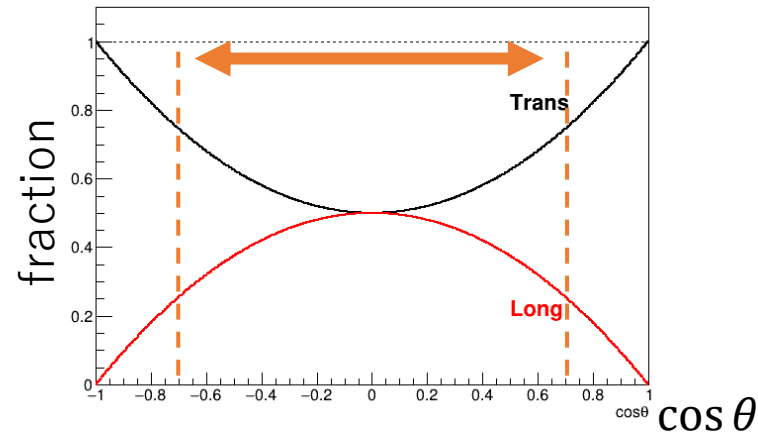
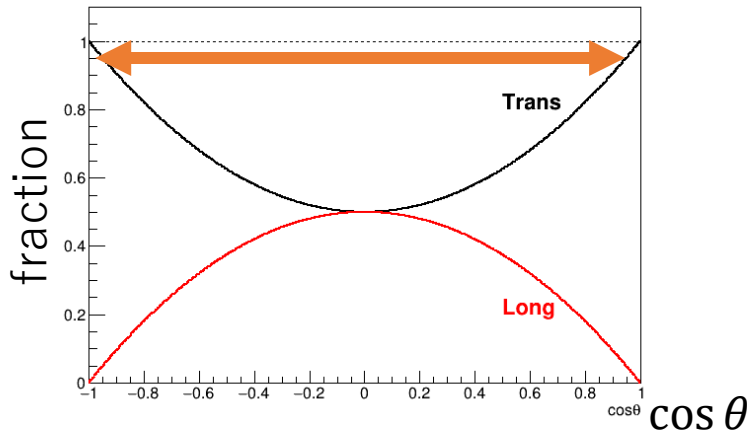
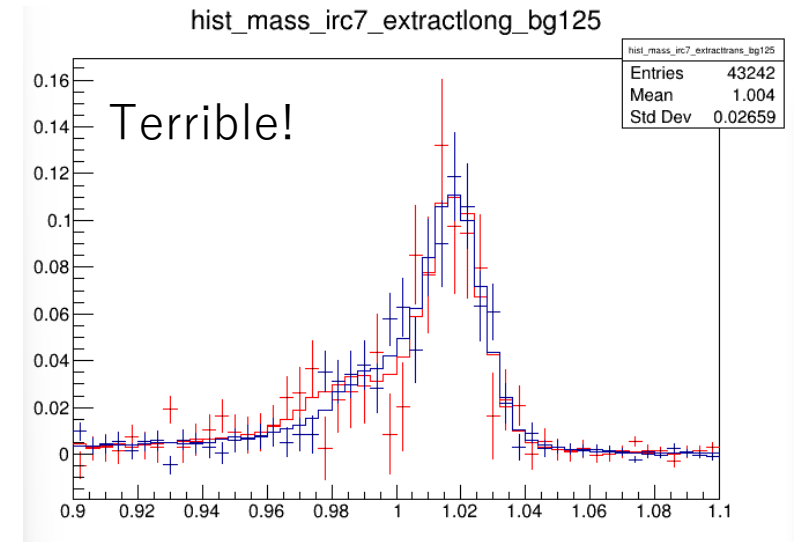
- $\cos \theta = [-1, 1]$



- $\cos \theta = [-0.7, 0.7]$



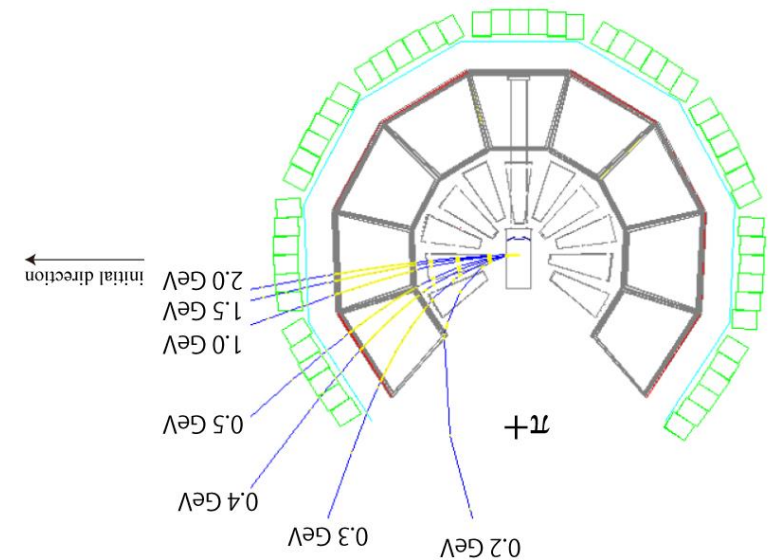
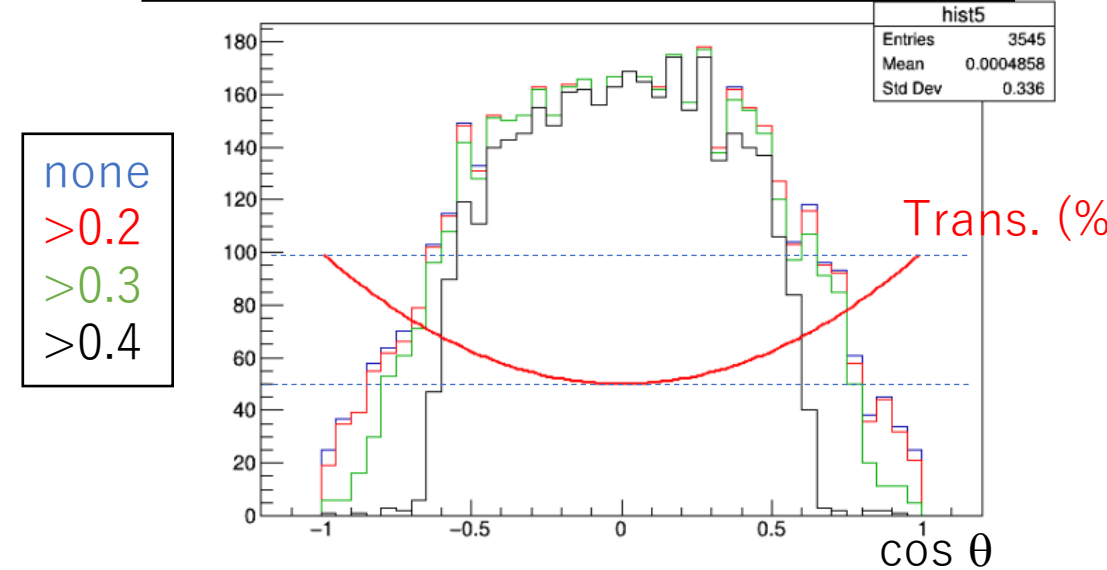
- $\cos \theta = [-0.5, 0.5]$



# Angular acceptance in the rest frame of $\phi$ .

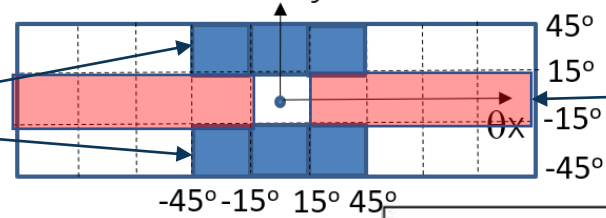
- GEANT4 as an acceptance filter.
  - Notes on the plot
    - # of entry is arbitrary.
    - Transverse pol fraction is overlaid.
  - Results
    - Smaller acceptance for  $\cos \theta = \pm 1$
    - LG trig eff  $\sim 90\%$  0.4GeV,  $\sim 75\%$  0.3GeV
    - Reality is between Green and black.
- Needs acceptance correction for analysis.
- $\cos \theta = [-0.7, 0.7]$  maybe used w/ correction but rather marginal.

In the acceptance & phi mom < 1.25 & e+ - momentum cut

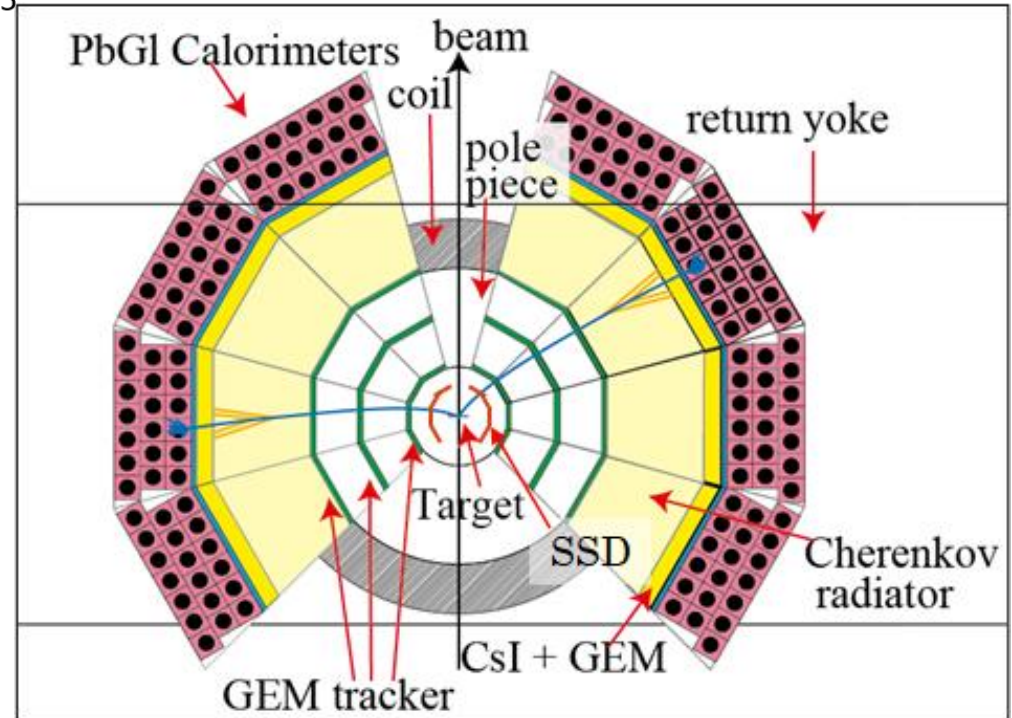
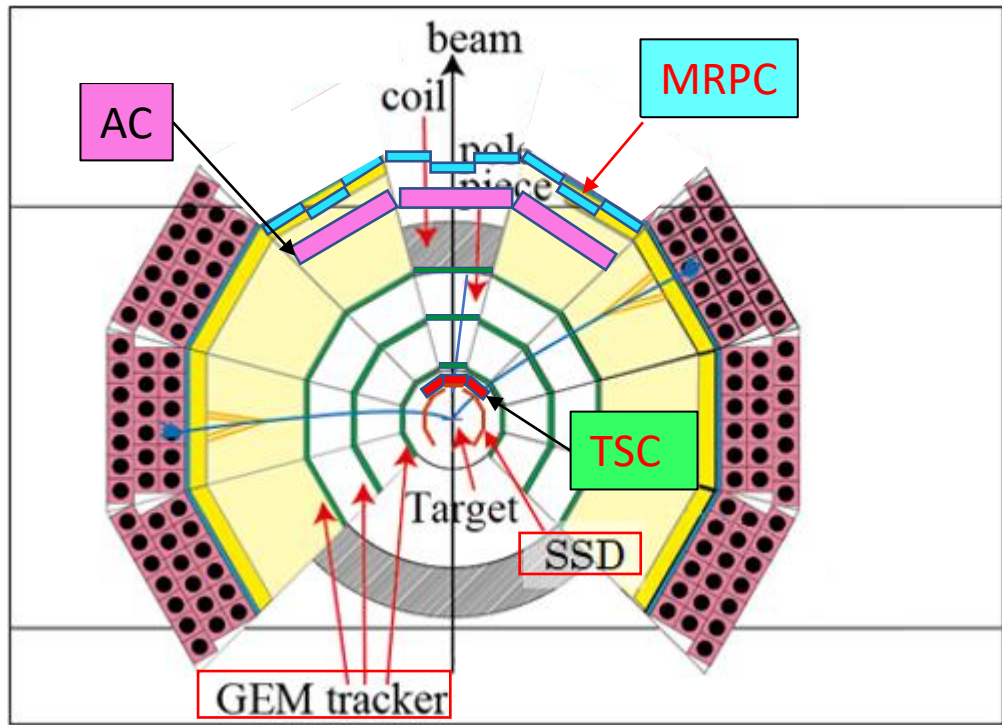


# J-PARC E88 : $pA \rightarrow \phi \rightarrow K^+K^-$

Top and bottom layers  
Kaon-ID detectors

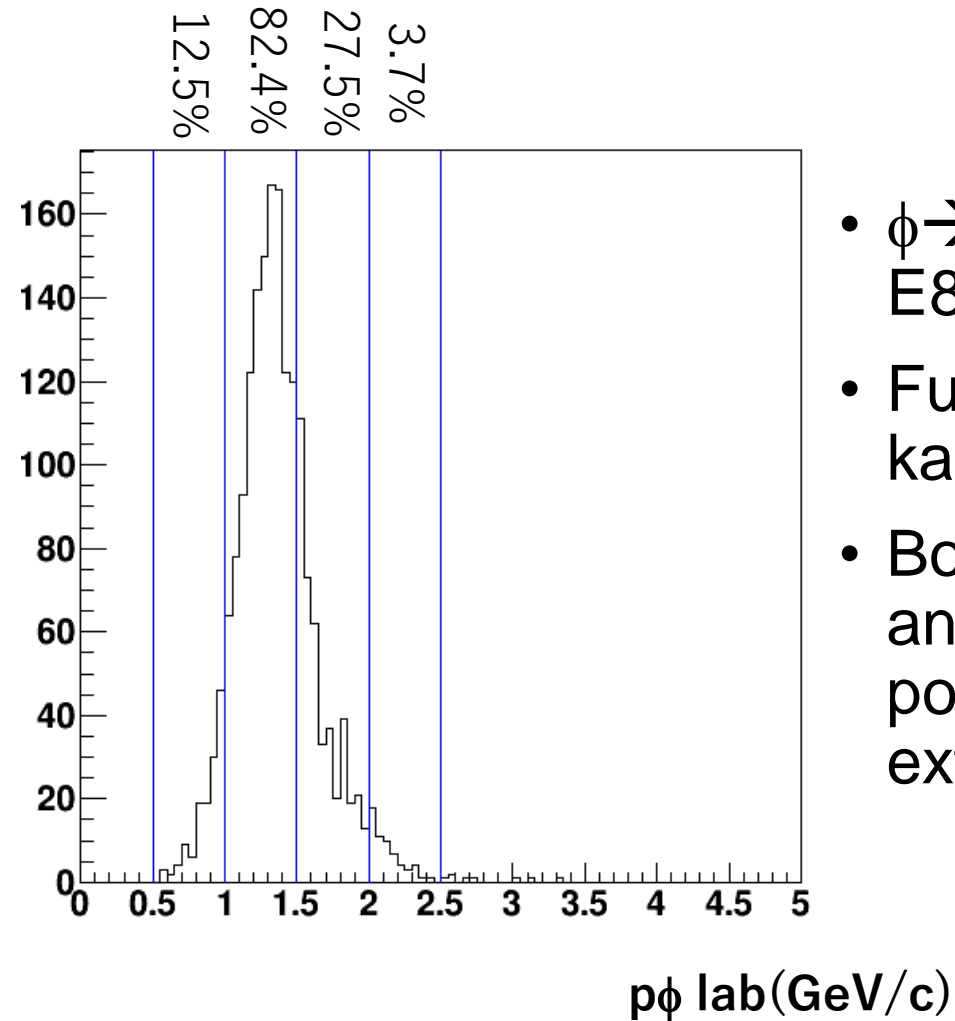
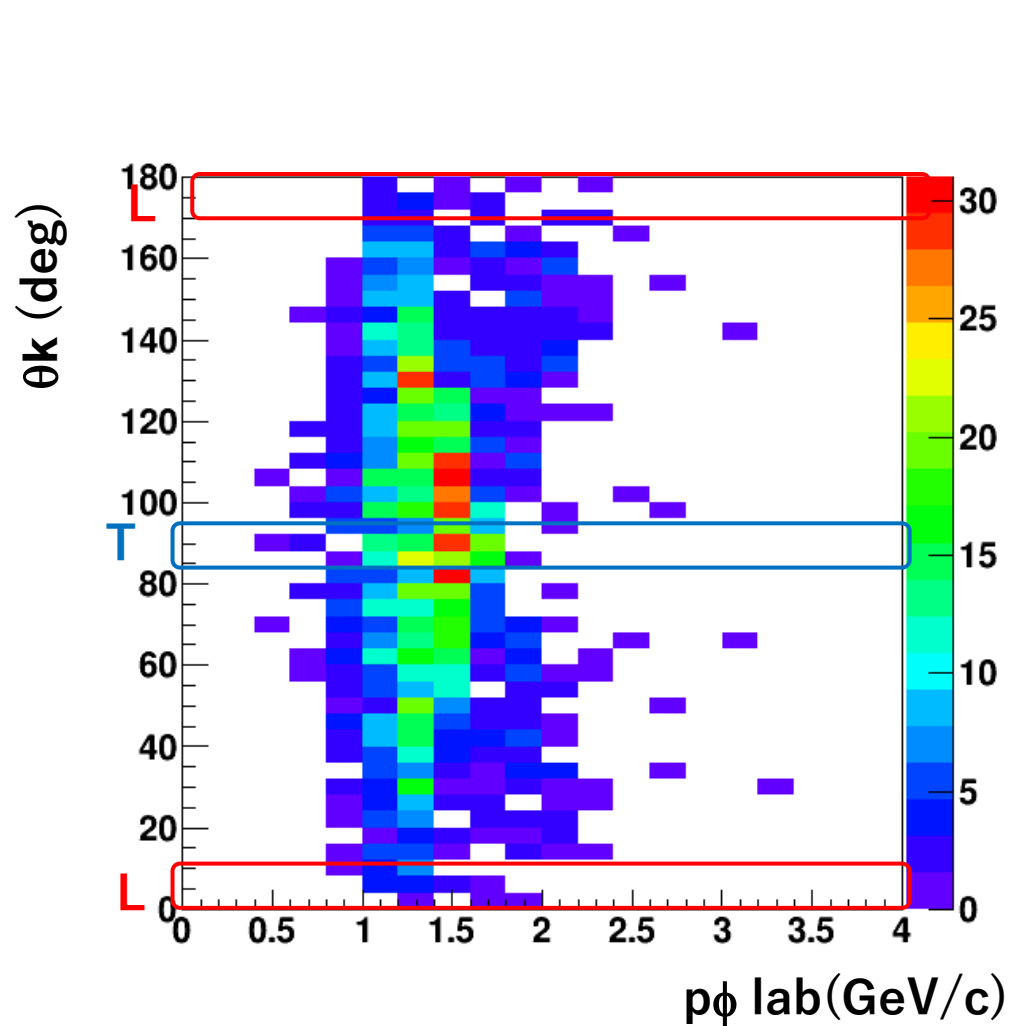


Middle layer  
e-ID detectors (same as E16)



- 6 forward modules (detector unit) in top and bottom layers
- MRPC (Multi-gap Resistive Plate Chamber) and TSC (Track start counter) for Time-of-Flight measurement
- AC (Aerogel Cherenkov Counter) for pion rejection
- SSDs (Silicon Strip Detectors) and GTRs (GEM Trackers) for tracking

# Distinguishing $\phi$ polarization at E88



- $\phi \rightarrow K^+K^-$  within E88 acceptance
- Full acceptance in kaon decay angle
- Both transverse and longitudinal polarized  $\phi$  can be extracted

# Orthogonal functions for K+K-

- We can also find orthogonal functions for KK
- Thanks to the high statistics and lucky distribution, we may simply select sweet spots (near  $\cos=1$  or  $0$ ) to see the spectrum.

- KK

$$x = \cos \theta = [-1, 1]$$

$$f_T(x) = (1 - x^2)$$

$$f_L(x) = x^2$$

$$h_T(x) = \frac{1}{2}[3 - 5x^2]$$

$$h_L(x) = \frac{1}{2}[5x^2 - 1]$$

- ee

$$x = \cos \theta = [-1, 1]$$

$$f_T = 1 + x^2$$

$$f_L = 1 - x^2$$

$$h_T = 5x^2 - 1$$

$$h_L = 2 - 5x^2$$

# Polarization-dependent mass measurement

- Model independent T/L separation is pursued here for ee.
  - Note: Model comparison is possible w/o separating T/L experimentally.
- Need further consideration
  - Angular dependence of acceptance/efficiency.
  - Background effects
  - Increase statistics / acceptance if necessary
    - Widen acceptance for low momentum particles.
    - Covering wider acceptance, closer to the targets.
- KK performs better in terms of polarization dependence measurement although FSI need to be taken care of.

# Summary

- J-PARC E16 will measure  $ee$  in pA collisions at 30GeV to study the origin of hadron mass through the spectral change of vector mesons in the nuclear medium.
- We gradually increased our acceptance and reached an intermediate goal (RUN1), which is 1/3 of the design configuration (RUN2).
- We are preparing for Run0e planned in 2024.
  - Get PAC approval for RUN1 (1<sup>st</sup> physics runs).
- The possibility of measuring polarization-dependent mass modification.
  - Extraction method.
  - Its results. (further realistic consideration needed.)
  - E88 (KK) performs better in terms of pol measurement. Commentary each other.





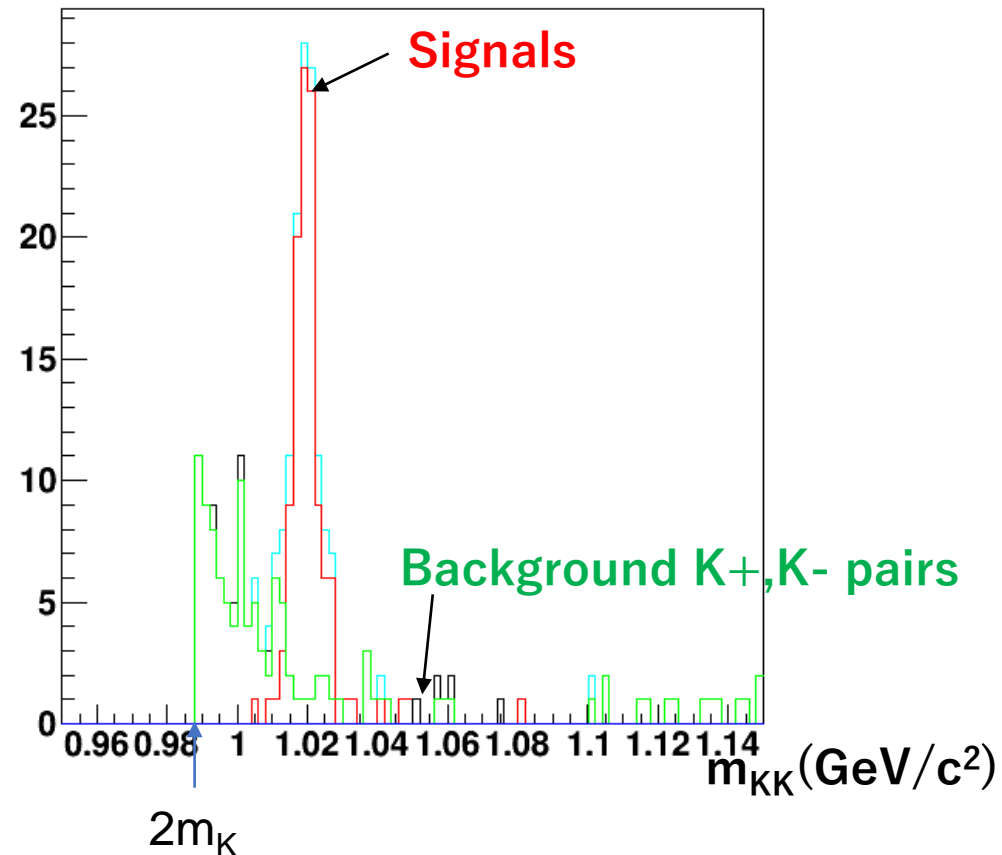
# Expected S/B

p+Cu, JAM event generator + GEANT4

- S/B ~ 7.1 (integral in 1.013-1.028 GeV/c<sup>2</sup>)

~ 27 (at the  $\phi$  peak)

w/KK trigger, w/ PID cuts



# Simple method (maybe easier to subt. BG)

- Divide sample into two : Say,  $A = \{x; |x| > 0.5\}$ ,  $B = \{x; |x| < 0.5\}$ 
  - (Subtract BG at this point.)

$$\begin{aligned}G_A(m) &= \int_A G(m, x) \\ &= \int_A g_T(m) f_T(x) + g_L(m) f_L(x) dx \\ &= g_T(m) \int_A f_T(x) dx + g_L(m) \int_A f_L(x) dx \\ &\equiv C \cdot g_T(m) + D \cdot g_L(m)\end{aligned}$$

$$\begin{aligned}G_B(m) &= \int_B G(m, x) \\ &= \int_B g_T(m) f_T(x) + g_L(m) f_L(x) dx \\ &\equiv E \cdot g_T(m) + F \cdot g_L(m)\end{aligned}$$

角度サンプルA = C x Trans + D x Long

角度サンプルB = E x Trans + F x Long

- Then solve them. (連立一次方程式)

$$g_T(m) = \frac{F \cdot G_A(m) - D \cdot G_B(m)}{CF - DE}$$

$$g_L(m) = \frac{E \cdot G_A(m) - C \cdot G_B(m)}{DE - FC}$$

# Expected statistics

Beam time: 30 days with 30 GeV proton beam at  $10^9$  / spill

- C (0.1% int.) + Cu (0.1% int.) + new Pb (0.1% int.) target

$\phi \rightarrow K^+K^-$ signals				E325	
	C	Cu	Pb	C	Cu
Total $\phi$	159k	262k	662k	419	833
$\phi$ ( $\beta\gamma < 1.25$ )	72k	113k	314k		
$\phi$ ( $1.25 < \beta\gamma < 1.75$ )	84k	146k	340k		

$\phi \rightarrow K^+K^-$ rate			
	C	Cu	Pb
$\phi$ signal rate (/spill)	2.95	5.41	12.8
Trigger rate (/spill)	78	161	365

F. Sakuma, et al,  
PRL 98, 152302 (2007)

Information from  $p$ - $\phi$  interaction  
 Attractive interaction  $\rightarrow$  mass reduction

$p$ - $\phi$  interaction info in terms of  
scattering length and  
effective range.

- Mass reduction
  - HAL :  $5.3\% \pm 0.4\%$
  - ALICE :  $5.8\% \pm 1.8\%$
  - ALICE-HAL: 1.3~9.0%
  - E325 :  $3.4\%^{+0.6}_{-0.7}$

nucl-ex/0306011(2003) and E. Chizzali, R. Del Grande, L. Fabbietti

$f_0, d_0 \rightarrow$  First order optical potential

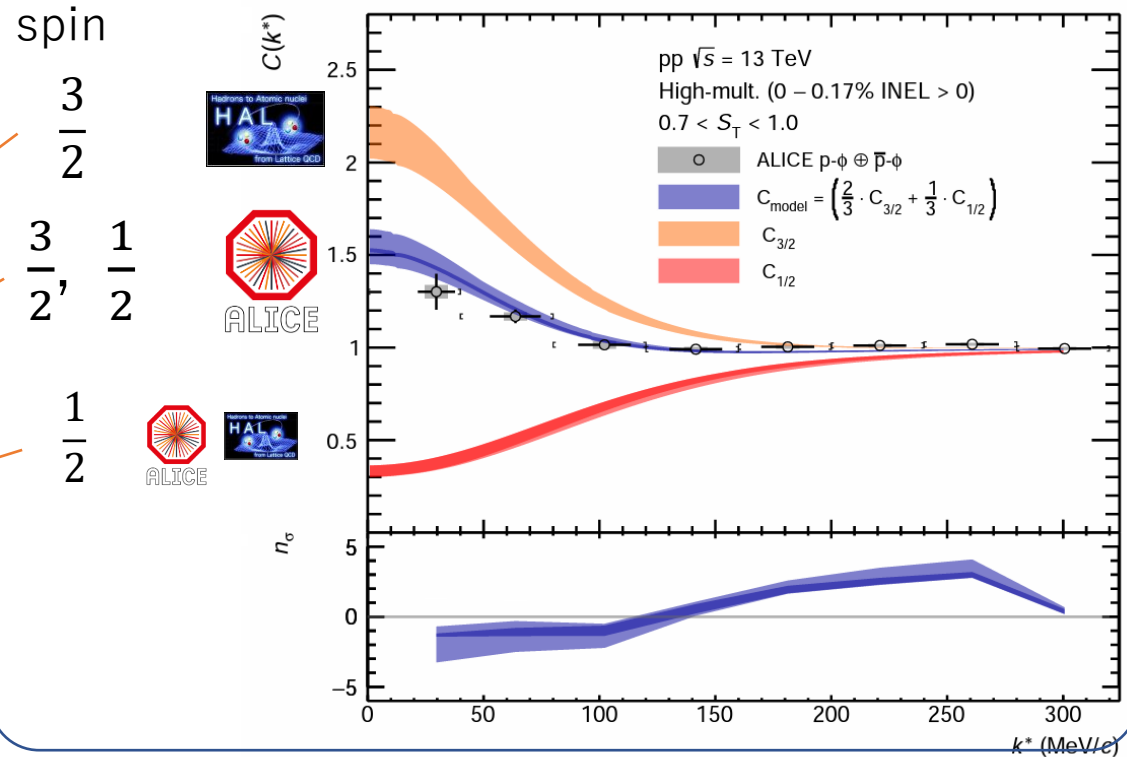
$$V(r) \sim \frac{1}{2m_\phi} 4\pi\rho(r) \frac{b}{1 + \frac{b}{d_0}}, \quad b = f_0 \left(1 + \frac{m_\phi}{m_{proton}}\right)$$

arXiv: 2212.12690

$$E_B \simeq \frac{1}{2\mu d_0^2} \left(1 - \sqrt{1 + 2\frac{d_0}{f_0}}\right)^2, \quad E_B \simeq 13.6-92.0 \text{ MeV},$$

arXiv: 2212.12690

## Two-particle correlation



HAL QCD method, arXiv:2205.10544 (2022)

$$a_0^{(3/2)} = -1.43(23) \text{ fm}$$

$$r_0^{(3/2)} = 2.36(10) \text{ fm}$$

ALICE: Phys. Rev. Lett. 127, 172301(2021)

$$d_0 = 7.85 \pm 1.54 \text{ (stat.)} \pm 0.26 \text{ (syst.) fm}$$

$$\Re(f_0) = 0.85 \pm 0.34 \text{ (stat.)} \pm 0.14 \text{ (syst.) fm}$$

$$\Im(f_0) = 0.16 \pm 0.10 \text{ (stat.)} \pm 0.09 \text{ (syst.) fm}$$

ALICE-HAL: arXiv: 2212.12690

$$\text{Re } f_0^{(1/2)} = -1.47^{+0.44}_{-0.37} \text{ (stat.)}^{+0.14}_{-0.17} \text{ (syst.) fm,}$$

$$\text{Re } d_0^{(1/2)} = +0.37^{+0.07}_{-0.08} \text{ (stat.)}^{+0.03}_{-0.03} \text{ (syst.) fm,}$$