

# Hadronic effects on Lambda polarization

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- Introduction
- Temperature dependence of Lambda spin polarization
- Hadronic effects on Lambda spin polarization
- Summary

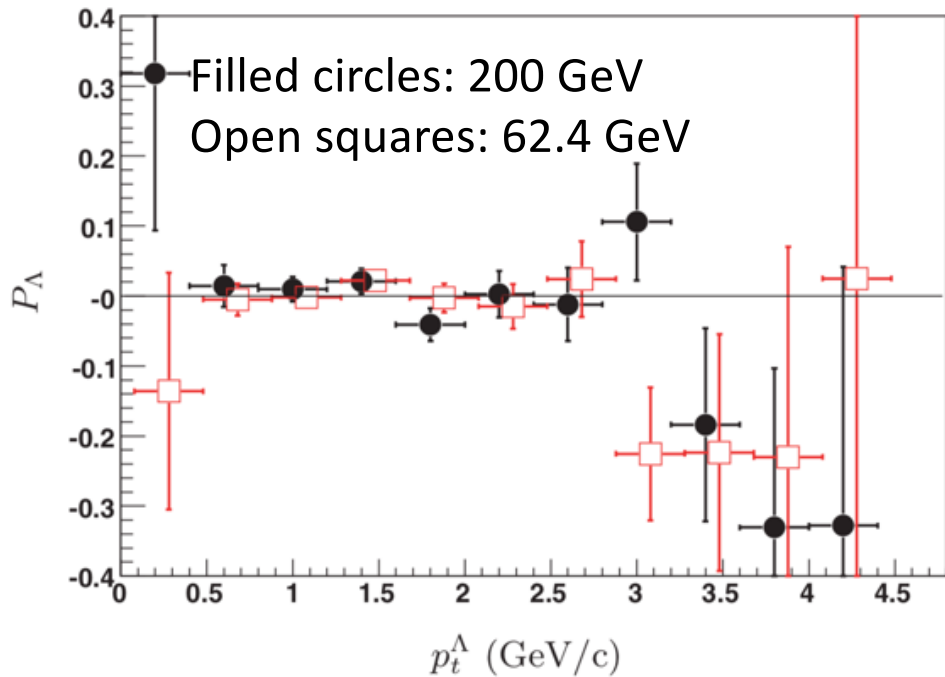
In collaboration with Haesom Sung and Su Hounng Lee



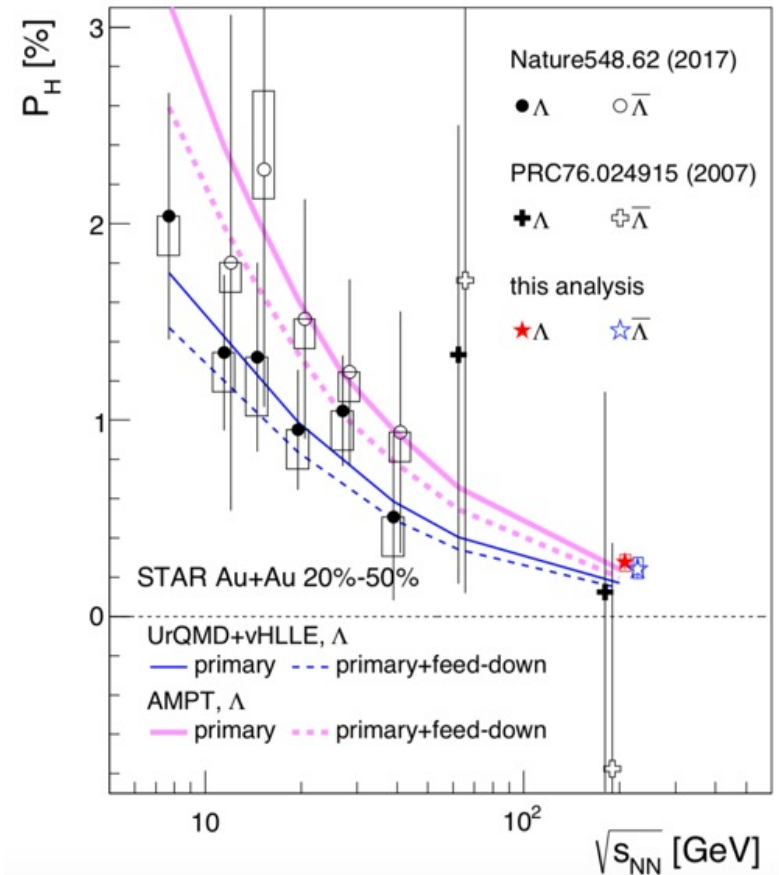
# $\Lambda$ polarization in relativistic heavy ion collisions

- First suggested by Z. T. Liang & X. N. Wang, PRL 94, 102301 (2005)

Abelev (STAR), PRC 76, 024915 (2007)



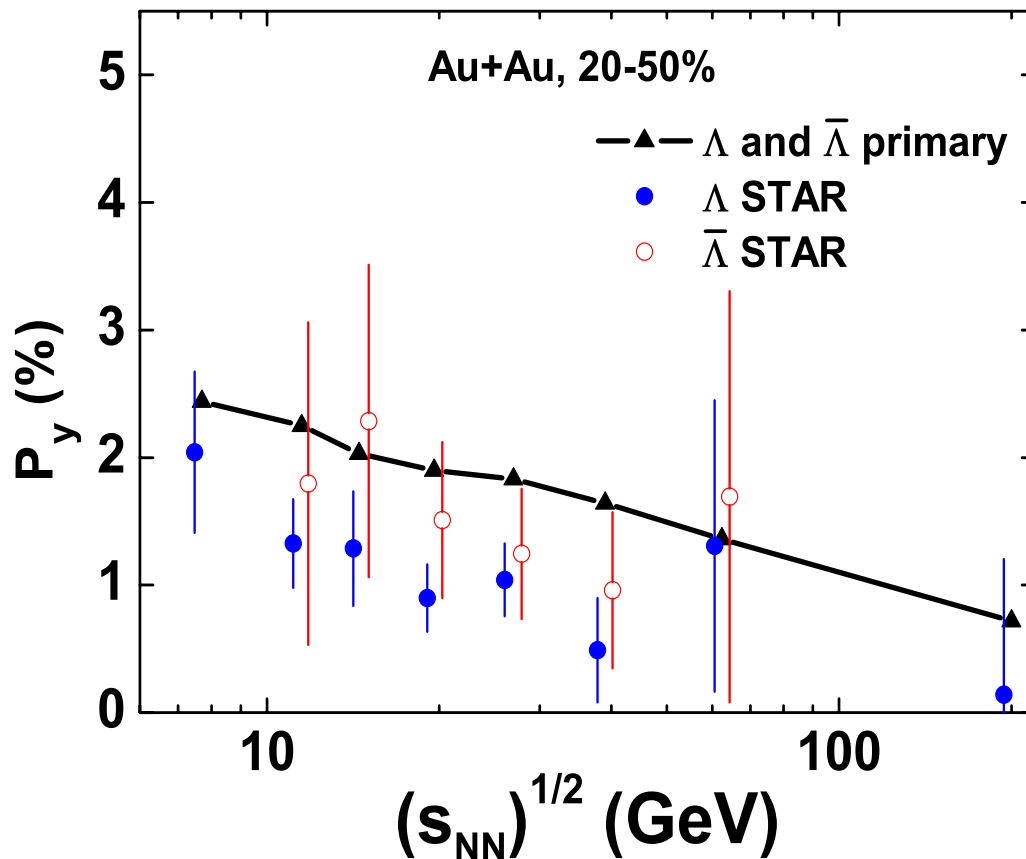
Adam (STAR), PRC 98, 14910 (2018)



- Studies based on fluid dynamics [Cernai, Becattini, Karpenko, Voloshin] and transport models [Wang et al.] assuming  $\Lambda$  in thermal equilibrium in the rotating fireball at chemical freeze out of HIC both predict  $\Lambda$  polarizations comparable to the STAR data.

# $\Lambda$ polarization from chiral kinetic approach

Sun & Ko, PRC 96, 024906 (2017)



$$\frac{d\mathbf{x}}{dt} = \frac{\hat{\mathbf{p}} + 2\lambda|\mathbf{p}|(\hat{\mathbf{p}} \cdot \boldsymbol{\omega})}{1 + 6\lambda|\mathbf{p}|(\mathbf{b} \cdot \boldsymbol{\omega})}$$

$\Lambda = \pm 1 = \text{helicity}$

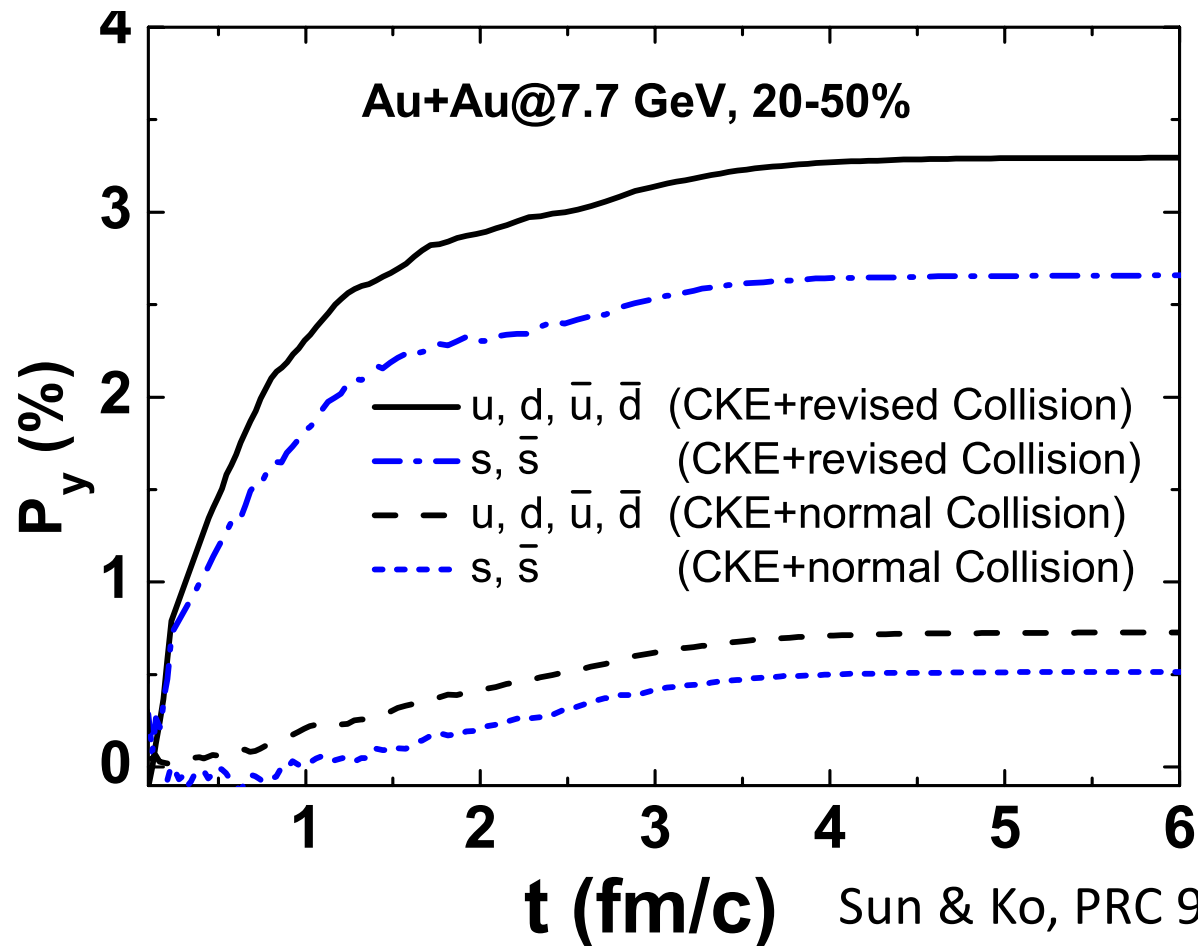
$\mathbf{b} = \frac{\hat{\mathbf{p}}}{2|\mathbf{p}|^2} = \text{Berry curvature}$

$$\frac{d\mathbf{p}}{dt} = 0$$

Including scattering that ensures the equilibrium distribution  $\sqrt{G}f$  with  $\sqrt{G} = 1 + 6\lambda|\mathbf{p}|(\mathbf{b} \cdot \boldsymbol{\omega})$ .

- Consistent with data that  $\Lambda$  polarization decreases with collision energy due to decreasing vorticity field with increasing energy.

# Global quark polarization from chiral kinetic approach



- Quark polarization of about 2.5% is generated early in time due to large vorticity field, which decreases with time.
- Modified quark scattering due to change of phase-space measure enhances global quark polarization.

# Color and spin statistical factors for polarized $\Lambda$

- Statistical factor for 3 colored quarks or antiquarks to form a colorless  $\Lambda$  or anti- $\Lambda$ :  $g_c=1/27$
- Statistic factor for 3 spin-1/2 quarks to form a polarized spin  $\frac{1}{2}$   $\Lambda$ :  $\Lambda$  spin is determined by the spin of s-quark, so u and d quarks form a spin singlet

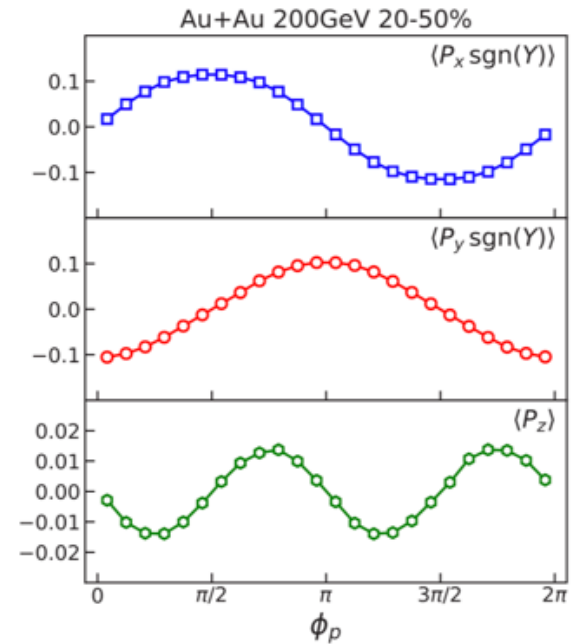
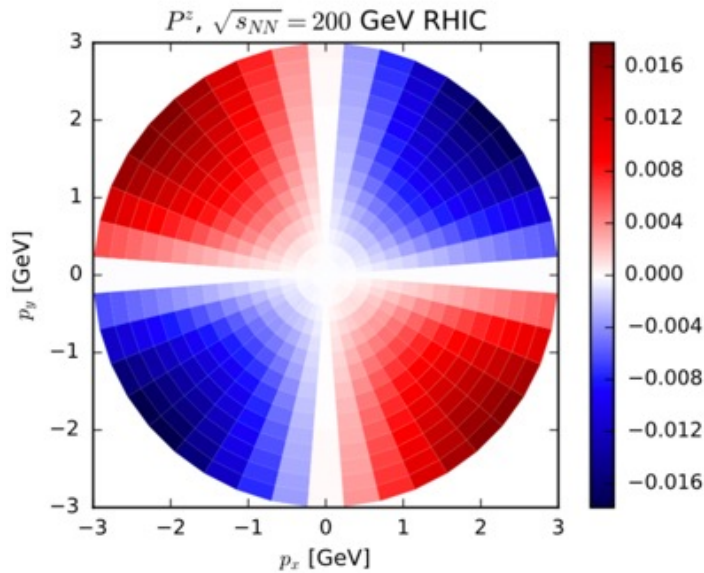
$$\begin{aligned}
 g_S &= \left| \left( \frac{1}{\sqrt{2}} \right) \left( \langle \uparrow\downarrow | - \langle \downarrow\uparrow | \right) \left[ \cos(\theta_1/2) \cos(\theta_2/2) | \uparrow\uparrow \rangle \right. \right. \\
 &\quad + \cos(\theta_1/2) \sin(\theta_2/2) e^{i\phi_2} | \uparrow\downarrow \rangle \\
 &\quad + \sin(\theta_1/2) \cos(\theta_2/2) e^{i\phi_1} | \downarrow\uparrow \rangle \\
 &\quad \left. \left. + \sin(\theta_1/2) \sin(\theta_2/2) e^{i(\phi_1+\phi_2)} | \downarrow\downarrow \rangle \right] \right|^2 \\
 &= \frac{1}{4} (1 - \cos \theta_1 \cos \theta_2 - \sin \theta_1 \sin \theta_2 \cos(\phi_1 - \phi_2)) \\
 &= \frac{1}{4} (1 - \lambda_1 \lambda_2 \hat{\mathbf{p}}_1 \cdot \hat{\mathbf{p}}_2)
 \end{aligned}$$

where  $\theta_1(\theta_2)$  and  $\phi_1(\phi_2)$  are polar angles of u(d) quark spin direction.

# Longitudinal spin polarization

Becattini & Karpeno, PRL 120, 012302 (2018)

Xia, Li, Tang & Wang, PRC 98, 024905 (2018)



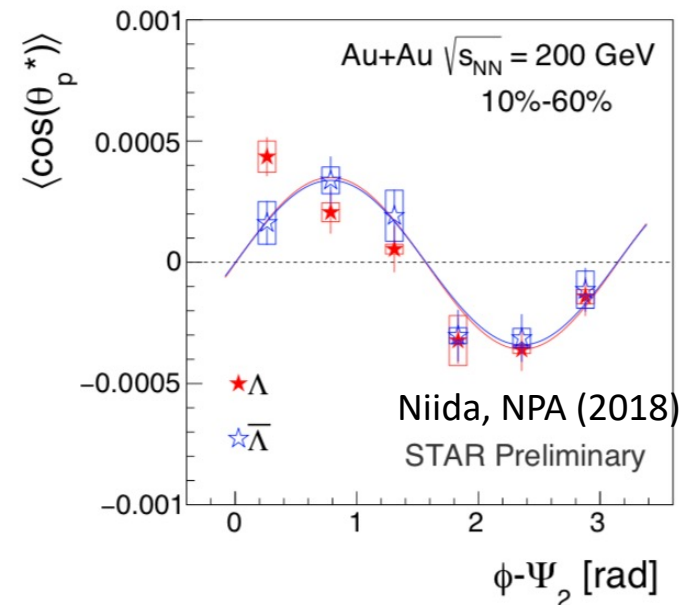
In terms of thermal vorticity

$$\bar{\omega}_{\mu\nu} = \frac{1}{2} (\partial_\nu \beta_\mu - \partial_\mu \beta_\nu), \quad \beta = \frac{u}{T}$$

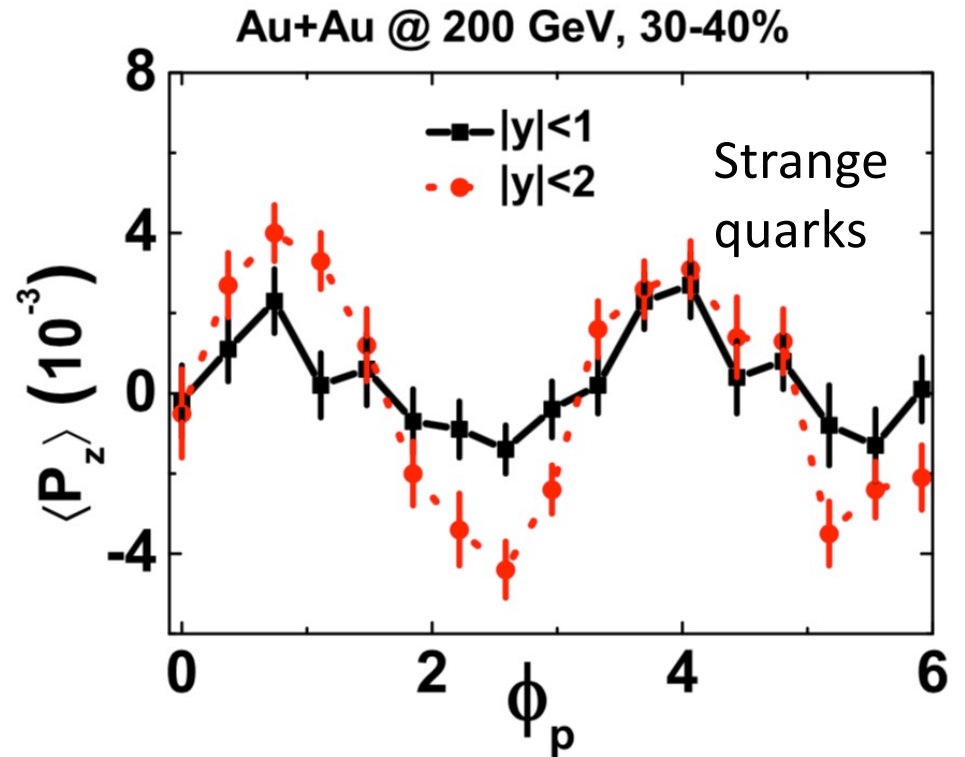
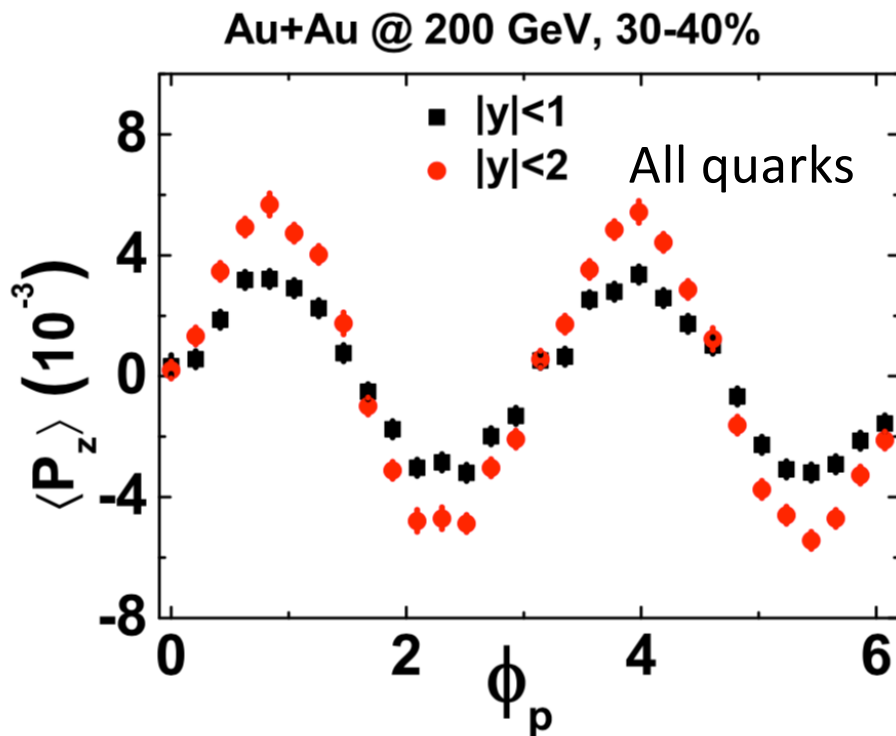
$$S^\mu(p) = -\frac{1}{8m} \epsilon^{\mu\rho\sigma\tau} p_\tau \times \frac{\int_\Sigma d\Sigma_\lambda p^\lambda \bar{\omega}_{\rho\sigma} n_F (1 - n_F)}{\int_\Sigma d\Sigma_\lambda p^\lambda n_F}$$

$$S^z(\mathbf{p}_T, y = 0) \approx \frac{dT}{d\tau} \frac{1}{mT} v_2(p_T) \sin 2\phi$$

leads to opposite sign in the azimuthal-angle dependence of  $p_z$  compared to STAR data.



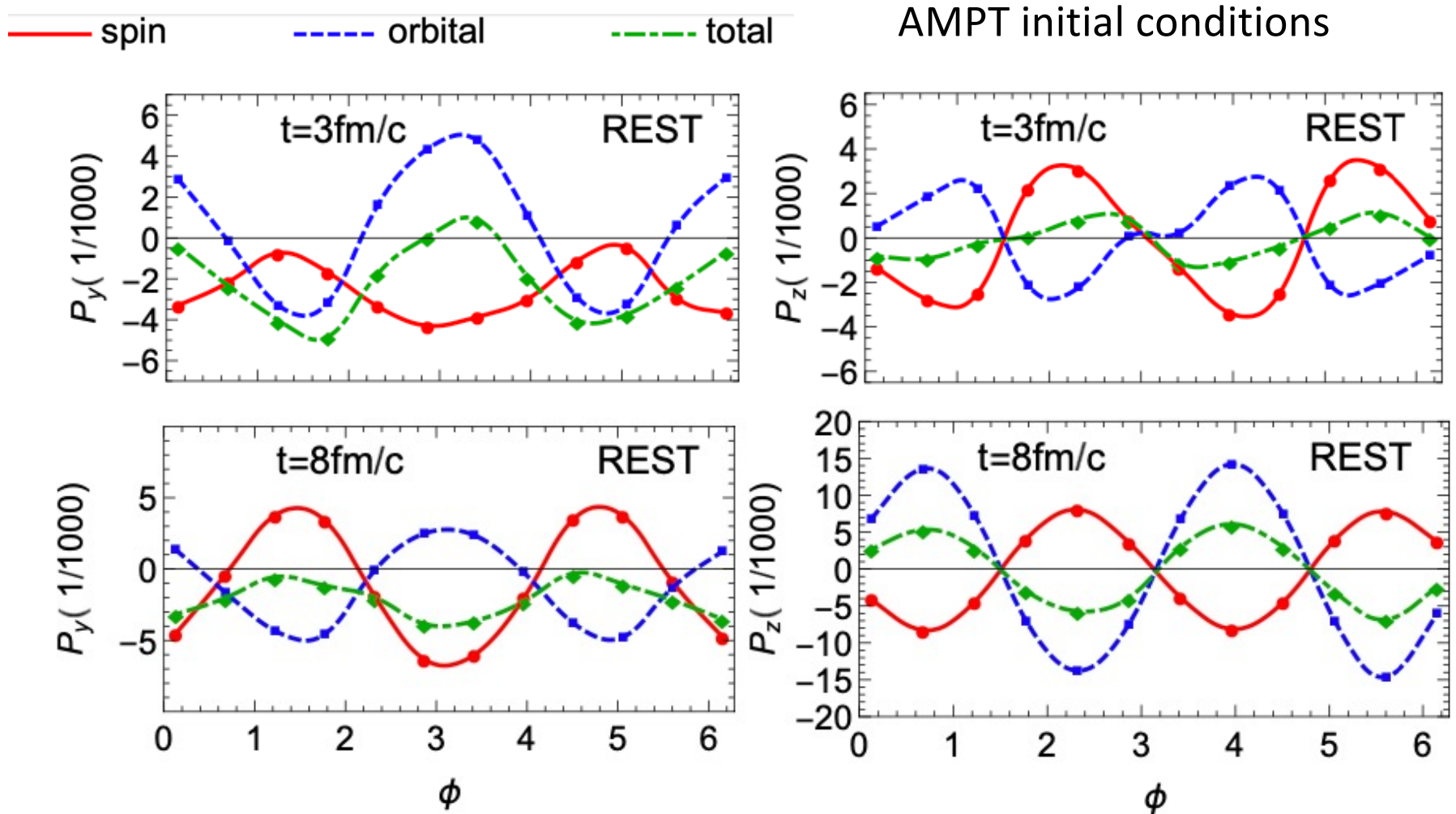
- Azimuthal angle dependence of longitudinal spin polarization in chiral kinetic approach



- Similar to that from preliminary STAR data [Niida, NPA (2018)].
- Opposite sign from those based on thermal-vorticity [Becattini & Karpenko, PRL 120, 012302 (2018); Xia et al., PRC 98, 024905 (2018)].

# Local spin polarizations in an angular momentum conserved chiral transport model

Shuai Liu, Yifeng Sun & Ko, PRL 127, 142301 (2022)



- $P_y$  is dominated initially by the orbital contribution and finally by the spin contribution, which is reversed for  $P_z$ .
- Both  $P_y$  and  $P_z$  have similar azimuthal angle dependence as in STAR data.

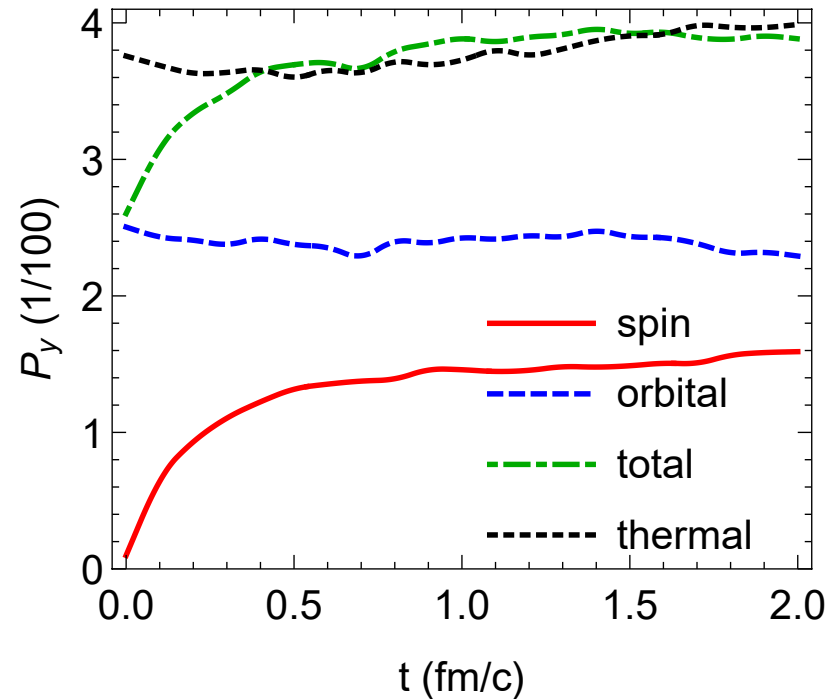
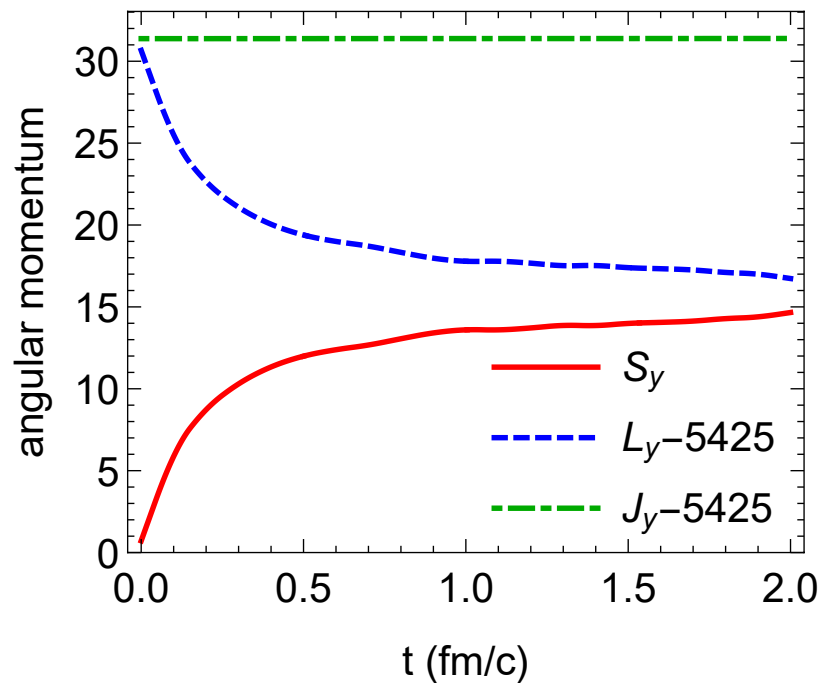


# Expanding quark matter

Shuai Liu, Yifeng Sun & CMK, PRL 127, 142301 (2021)

Conserved current 
$$j_{R/L}^\mu \approx \int \frac{d^3\mathbf{p}}{(2\pi)^3 p} \left( \underbrace{p^\mu f_{R/L}}_{\text{spin}} + \underbrace{S^{\mu\nu} \partial_\nu f_{R/L}}_{\text{orbital}} \right)$$

Spin polarization 
$$\mathcal{P}_y = \frac{\int d^3\mathbf{x} j_{5y}(\mathbf{x})}{\int d^3\mathbf{x} n(\mathbf{x})}$$



- Initial conditions: Sizes:  $5 \times 5 \times 5 \text{ fm}^3$ ;  
 Temp. : 300 MeV; Flow profile:  $\gamma \mathbf{v} = 2\boldsymbol{\omega}(x, 0, 0)$  with  $\boldsymbol{\omega} = (0, 0.12, 0) \text{ (fm/c)}^{-1}$  ;  
 $L_y = 5425 \hbar$ ,  $S_y = 0$ ; isotropic quark scattering cross section of 10 mb.

- Total angular momentum  $J_y = L_y + S_y$  is conserved.
- Total polarization increases with time and approaches the thermal value  $\omega/T$ .

# Spin polarization vector of a fermion

- Shuai Liu & Yi Yin, JHEP 07, 188 (2021)
- F. Becattini, M. Buzzegoli & A. Palermo, PLB 820, 136519 (2021)
- Cong Yi, Shi Pu & Di-Lun Yang, PRC 104, 064901 (2021)

$$S^\mu(x, p) = -\frac{1}{8m}(1 - n_F)\epsilon^{\mu\nu\rho\sigma}p_\nu\varpi_{\rho\sigma}(x) - \frac{1}{4m}(1 - n_F)\epsilon^{\mu\nu\rho\sigma}p_\nu\frac{n_\rho p^\lambda \xi_{\lambda\sigma}(x)}{n \cdot p}$$

where  $p$  is the 4-momentum of the fermion,  $n_F$  is the Fermi-Dirac distribution function,  $n$  is a unit four vector that specifies the frame of reference, and

$$\text{thermal vorticity } \varpi_{\rho\sigma} = \frac{1}{2}(\partial_\sigma\beta_\rho - \partial_\rho\beta_\sigma)$$
$$\text{thermal shear } \xi_{\rho\sigma} = \frac{1}{2}(\partial_\sigma\beta_\rho + \partial_\rho\beta_\sigma)$$

where  $\beta = u/T$  with  $u$  being the flow field.

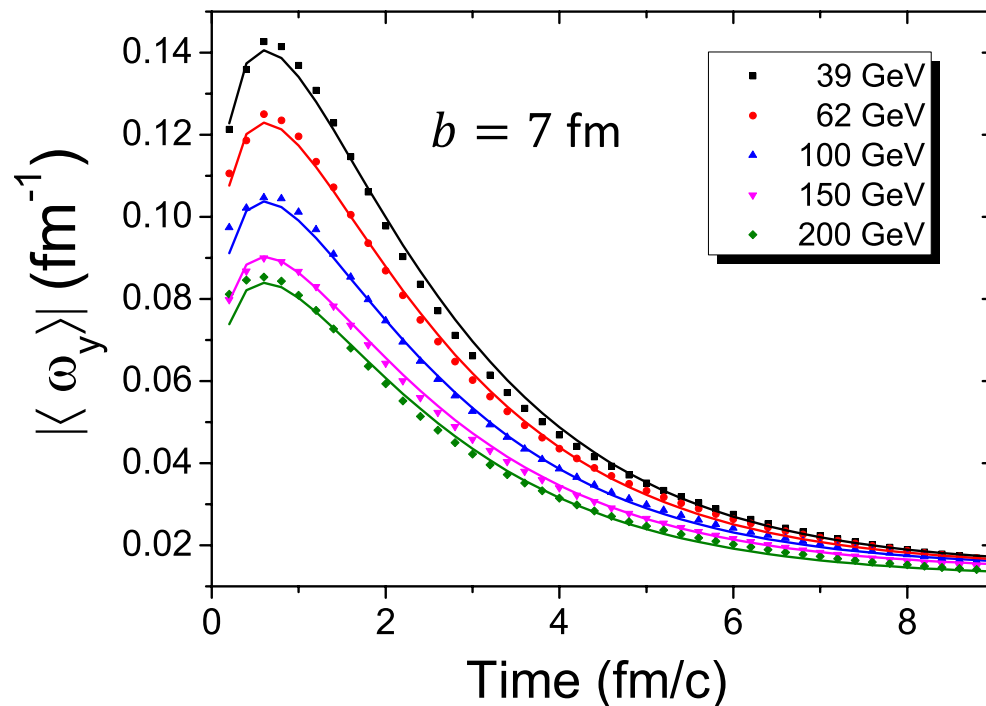
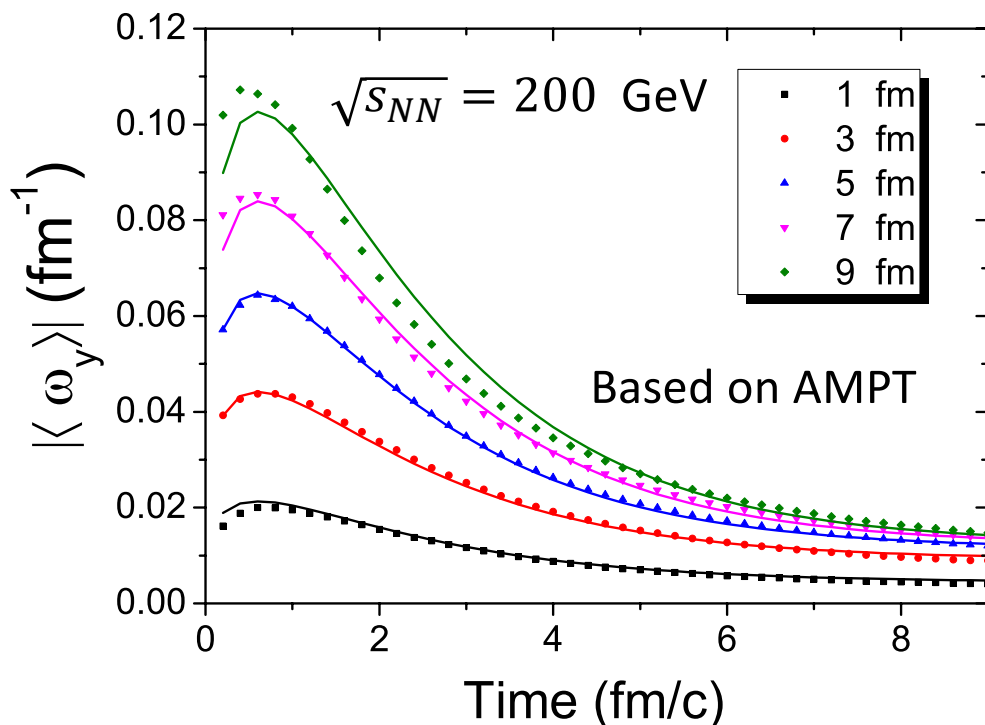
- Thermal shear is needed to describe the azimuthal angle dependence of Lambda local polarization in hydro and coarse-grained transport approaches but is naturally included in the chiral kinetic approach.

# Vorticity in relativistic heavy ion collisions

Jiang, Lin & Liao,  
PRC 94, 044910 (2016)

$$\boldsymbol{\omega} = \frac{1}{2} \nabla \times \mathbf{v}, \quad \langle \omega_y \rangle = \frac{\int d^3\mathbf{r} [\mathcal{W}(\mathbf{r})] \omega_y(\mathbf{r})}{\int d^3\mathbf{r} [\mathcal{W}(\mathbf{r})]}, \quad \mathcal{W}(\mathbf{r}) = \rho^2 \epsilon(\mathbf{r})$$

$\rho$ : distance from y-axis  
 $\epsilon(\mathbf{r})$ : energy density

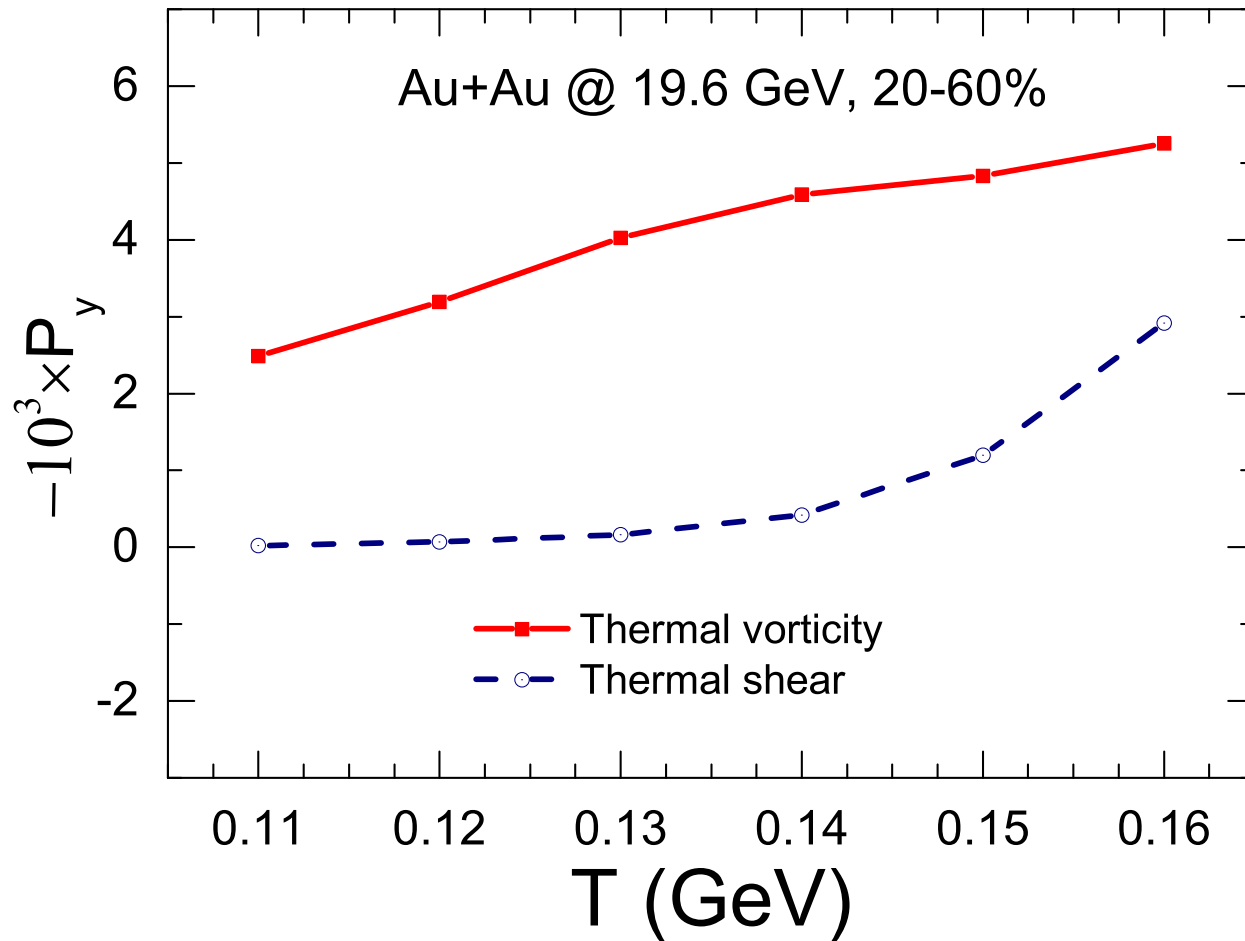


- Average vorticity decreases with time, decreasing impact parameter, and increasing collision energy. The lifetime is much longer than that of electromagnetic field.
- Can lead to chiral vortical effect and vortical separation effect

$$\mathbf{J}^V = \frac{\mu\mu_5}{\pi^2} \boldsymbol{\omega} \quad \text{and} \quad \mathbf{J}^A = \left( \frac{T^2}{6} + \frac{\mu^2 + \mu_5^2}{2\pi^2} \right) \boldsymbol{\omega}$$

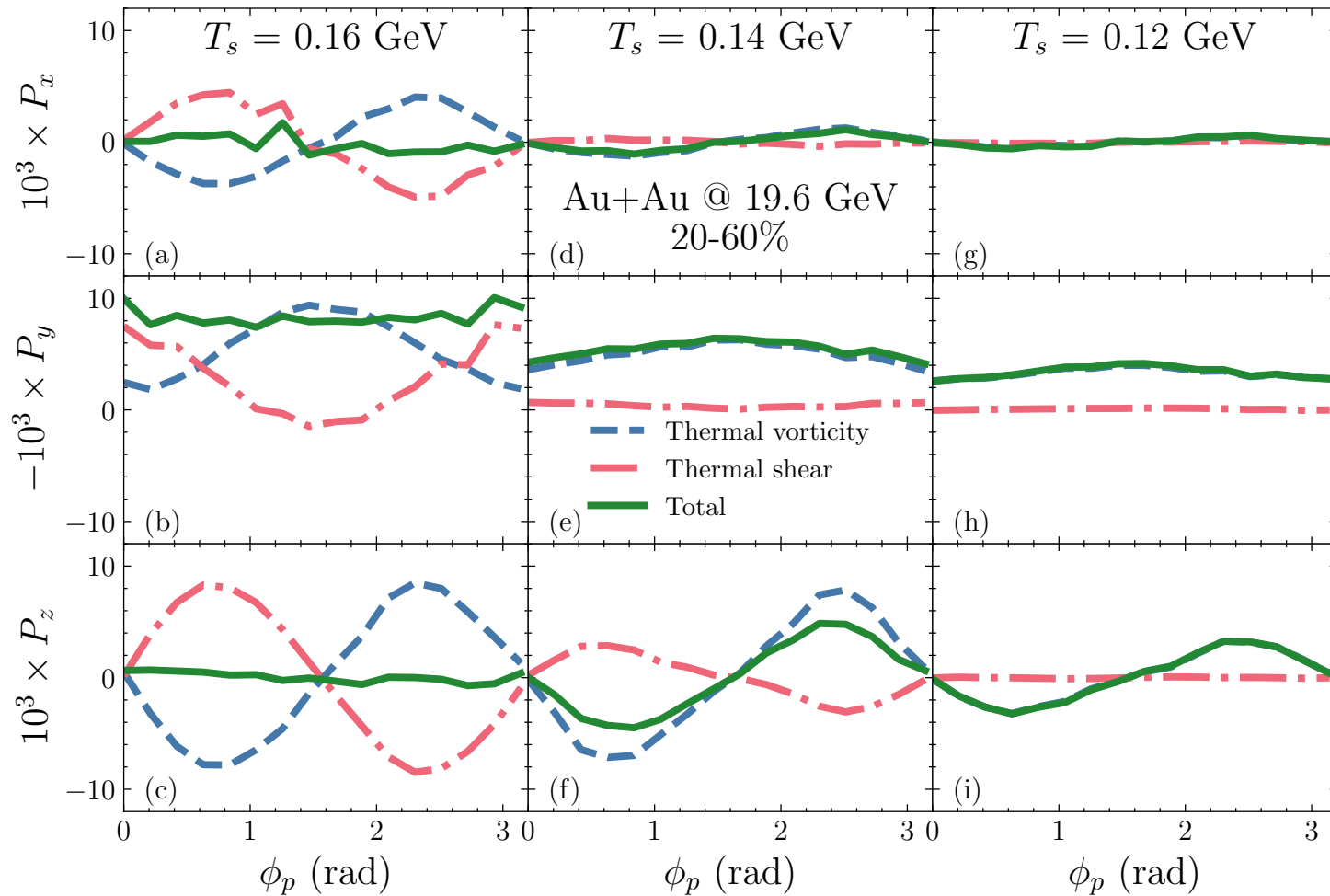
# Evolution of $\Lambda$ global polarization during hadronic expansion

Yifeng Sun, Zhen Zhang, Wenbin Zhao & Ko, PRC 105, 034911 (2022)



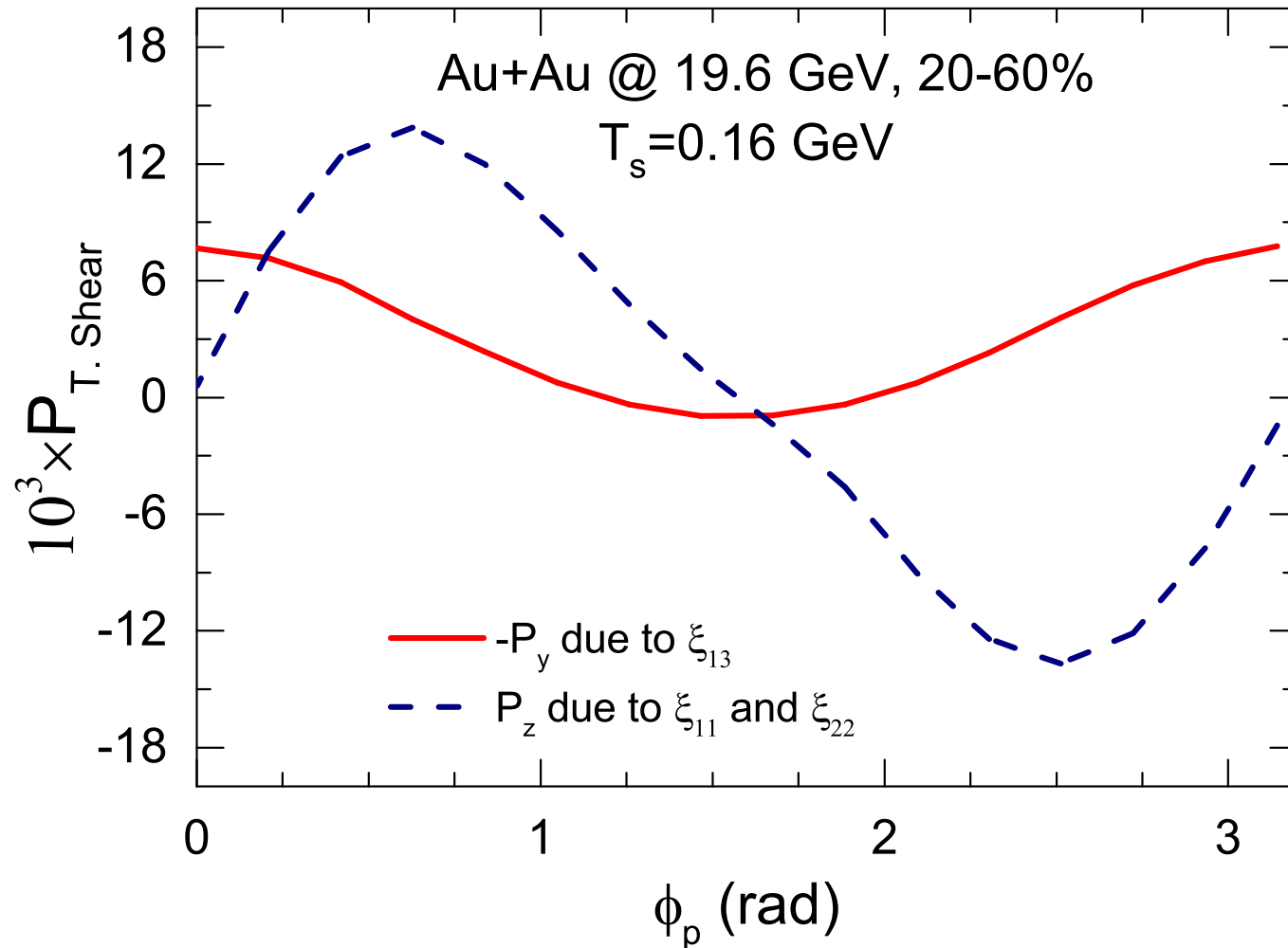
MUSIC+UrQMD: Thermal vorticity contributes to  $\Lambda$  global polarization more than that from thermal shear, and both contributions decrease with decreasing temperature.

# Temperature dependence of thermal vorticity and thermal shear to $\Lambda$ local spin polarization



Thermal vorticity and thermal shear give opposite azimuthal angle dependence of  $\Lambda$  local polarization, and both contributions decrease with temperature.

# Contribution of thermal shear components to $\Lambda$ polarization



Transverse components of thermal shear give  $\Lambda$  polarization a similar azimuthal angle dependence as seen in experiments.

# Hadron production from heavy ion collisions

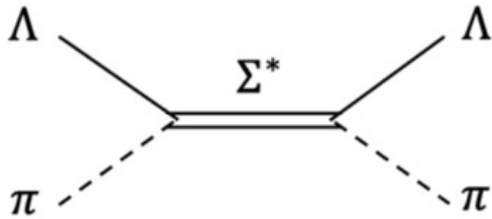
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**Abstract.** A brief review of some topics in hadron production from heavy ion collisions is given. They include charged pion ratio as a probe of nuclear symmetry energy, in-medium effects on pion production, enhanced  $\Lambda_c/D^0$  ratio,  $\Lambda$  local polarization, and  $X(3872)$  production.

of 150 MeV [48]. Both  $\Lambda$  global and local spin polarizations decrease, however, with temperature as the hadronic matter cools [49]. The fact that the experimental data is consistent with  $\Lambda$  spin polarizations at the hadronization temperature indicates that they freeze out or decouple early from the hadronic matter. This would be the case if the  $\Lambda - \pi$  scattering is through the spin 3/2, parity positive  $\Sigma^*(1358)$  resonance since the ratio of  $\Lambda$  spin non-flip to flip probabilities in this scattering is 3.5.

## S-channel $\Lambda - \pi$ scattering



$$\bar{\sigma}(s) = \frac{8\pi}{k^2} \frac{s\Gamma^2(s)}{(s - m_{\Sigma^*}^2)^2 + s\Gamma^2(s)}$$

$$M_{\Sigma^*} = 1358 \text{ MeV}, \quad \Gamma(M_{\Sigma^*}) = 39.4 \text{ MeV}$$

$$k = \sqrt{\frac{[s - (m_{\Lambda} + m_{\pi})^2][s - (m_{\Lambda} - m_{\pi})^2]}{4s}}$$

$$\sigma_{++} = \frac{1}{3} \bar{\sigma} \sum_{m, M} \left| \left\langle \frac{1}{2} \frac{1}{2} 1m \left| \frac{3}{2} M \right\rangle \right|^4 = \frac{14}{27} \bar{\sigma}$$

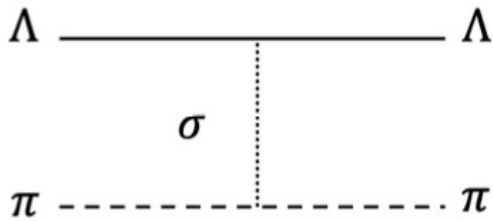
$$\sigma_{+-} = \sigma \frac{1}{3} \sum_{m, M} \left| \left\langle \frac{1}{2} - \frac{1}{2} 1m \left| \frac{3}{2} M \right\rangle \left\langle \frac{3}{2} M \left| \frac{1}{2} \frac{1}{2} 1m \right\rangle \right|^2 = \frac{4}{27} \bar{\sigma}$$

Ratio of spin flip to Non-flip cross sections:

$$R = \frac{\sigma_{+-}}{\sigma_{++}} \approx 0.3$$



## t-channel $\Lambda - \pi$ scattering



$$\mathcal{L} = g_{\sigma\Lambda\Lambda}\bar{\Lambda}\Lambda\sigma, \quad \mathcal{L} = g_{\sigma\pi\pi}\sigma\pi\pi$$

$$m_{\sigma} = 400 - 550 \text{ MeV}, \quad \Gamma_{\sigma}(m_{\sigma}) = 200 - 350 \text{ MeV}$$

$$g_{\sigma\Lambda\Lambda} = 7.07, \quad g_{\sigma\pi\pi} = 2.37 \text{ GeV}$$

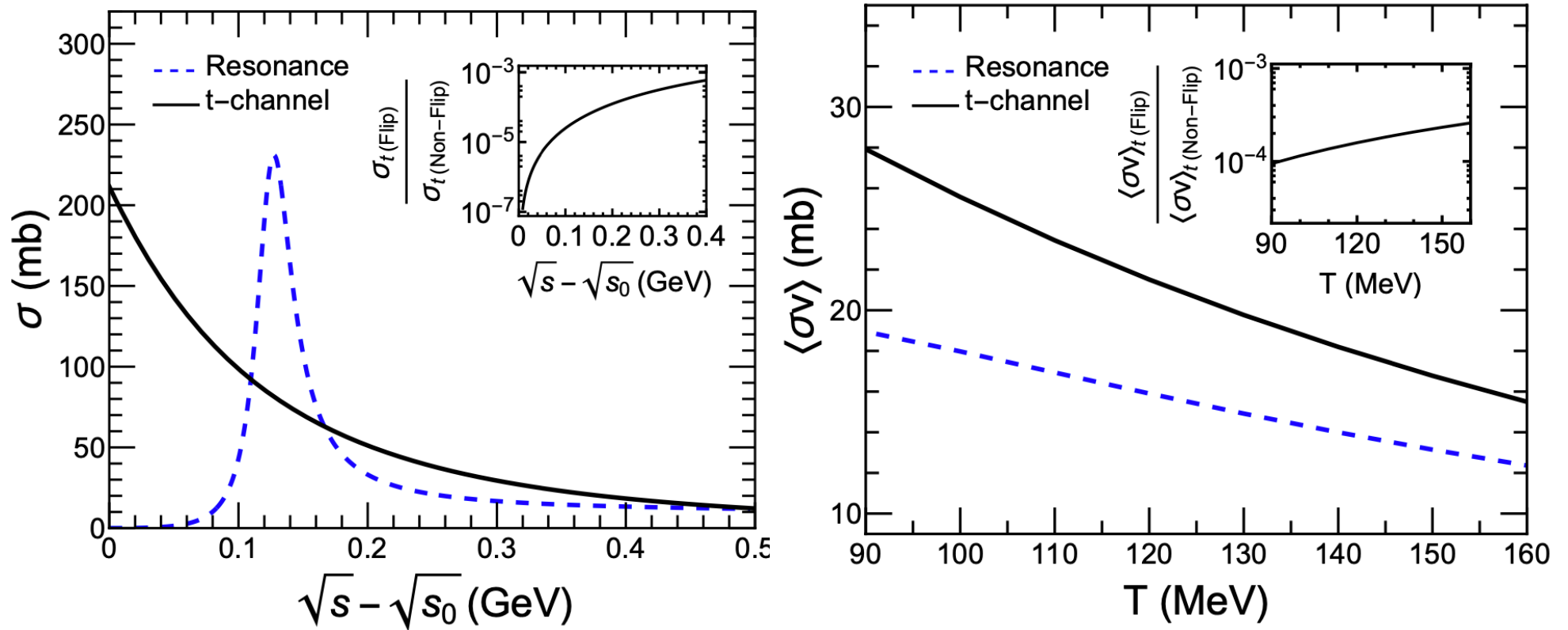
$$|\mathcal{M}_{t++}|^2 = \frac{g_{\Lambda\Lambda\sigma}^2 g_{\sigma\pi\pi}^2 F^2(t)}{(t - m_{\sigma}^2)^2 + m_{\sigma}^2 \Gamma_{\sigma}(s)^2} \times (E_{\Lambda} + m_{\Lambda})^2 \left[ 1 - \frac{p^2 \cos \theta}{(E_{\Lambda} + m_{\Lambda})^2} \right]^2$$

$$|\mathcal{M}_{t+-}|^2 = \frac{g_{\Lambda\Lambda\sigma}^2 g_{\sigma\pi\pi}^2 F^2(t)}{(t - m_{\sigma}^2)^2 + m_{\sigma}^2 \Gamma_{\sigma}(s)^2} \frac{p^4 \sin^2 \theta}{(E_{\Lambda} + m_{\Lambda})^2}$$

$$F(t) = \frac{\Lambda^2 + m_{\sigma}^2}{\Lambda^2 + t}, \quad \Lambda = 1.8 \text{ GeV}$$

Spin flip is a relativistic effect.

# $\Lambda - \pi$ scattering cross sections and their thermal average



- t-channel cross section at  $\sqrt{s} < m_{\Sigma^*}$  is larger than s-channel one.
- t-channel has a larger thermal averaged cross section than s-channel one at all temperature.
- Lambda spin flip cross section is 1/3.5 in s-channel and negligible in t-channel.

# Kinetic equations for Lambda spin evolution

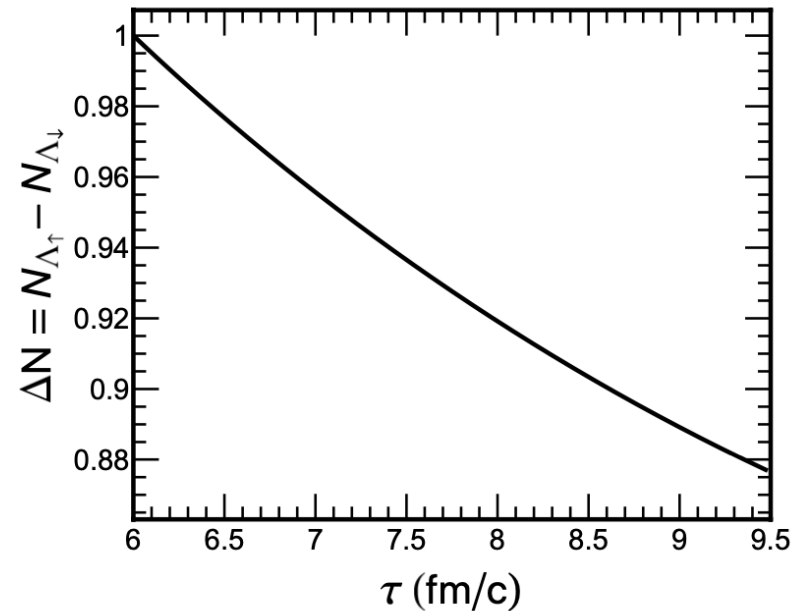
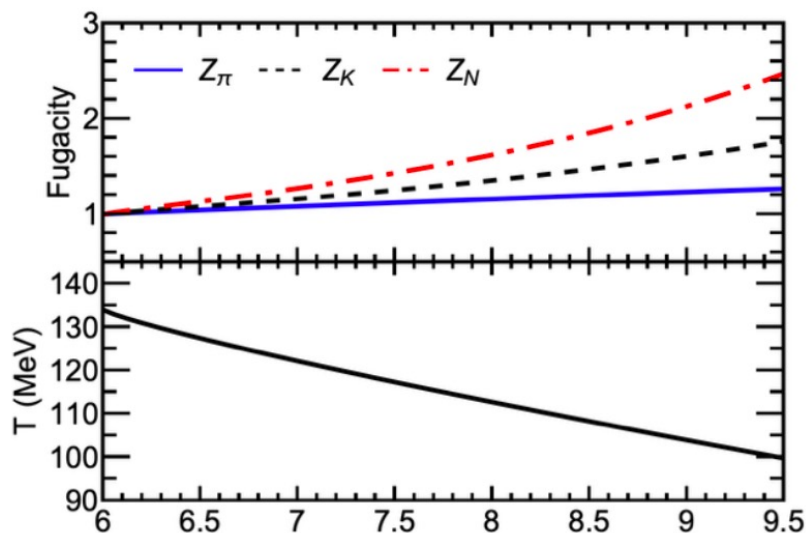
$$\frac{dN_{\Lambda_+}}{d\tau} = -\langle\sigma_{\Lambda_+\pi\rightarrow\Lambda_-\pi}v\rangle z_\pi n_\pi N_{\Lambda_+} + \langle\sigma_{\Lambda_-\pi\rightarrow\Lambda_+\pi}v\rangle z_\pi n_\pi N_{\Lambda_-}$$

$$\frac{dN_{\Lambda_-}}{d\tau} = \langle\sigma_{\Lambda_+\pi\rightarrow\Lambda_-\pi}v\rangle z_\pi n_\pi N_{\Lambda_+} - \langle\sigma_{\Lambda_-\pi\rightarrow\Lambda_+\pi}v\rangle z_\pi n_\pi N_{\Lambda_-}$$

$$\langle\sigma_{\Lambda_+\pi\rightarrow\Lambda_-\pi}v\rangle = \langle\sigma_{\Lambda_-\pi\rightarrow\Lambda_+\pi}v\rangle \equiv \langle\sigma v\rangle \longrightarrow \frac{d\Delta N}{d\tau} = -2\langle\sigma v\rangle z_\pi n_\pi \Delta N$$

$$T(\tau) = T_{\text{ch}} - (T_{\text{ch}} - T_{\text{k}}) \left( \frac{\tau - \tau_{\text{ch}}}{\tau_{\text{k}} - \tau_{\text{ch}}} \right)^{0.85}$$

$\sqrt{s_{NN}}$ (GeV)	$T_{\text{ch}}$ (MeV)	$T_{\text{k}}$ (MeV)	$\tau_{\text{ch}}$ (fm/c)	$\tau_{\text{k}}$ (fm/c)
7.7	144	110	5.96	9.47



- Lambda polarization is reduced by only 11% from chemical to kinetic freeze out.

# Summary

- Small Lambda spin flip than non-flip cross sections justifies the neglect of hadronic scattering effect on Lambda spin polarization.
- Need however to include effects due to Lambda-pion scattering via the omega meson exchange and also effects due to Lambda-nucleon scattering.