

# J/psi spin alignment from polarized damping rate



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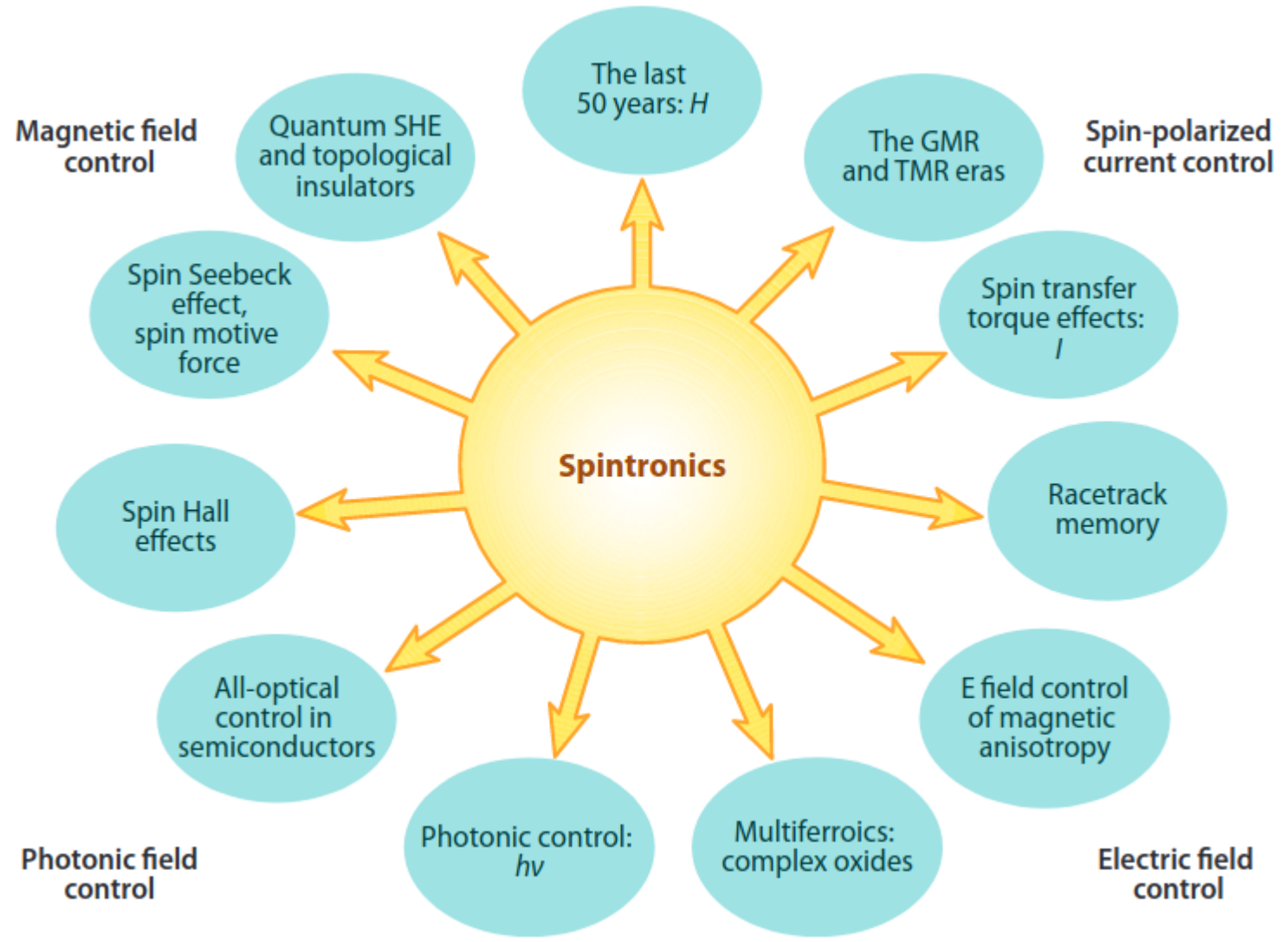
ExHIC-p workshop on polarization phenomena in nuclear collisions,  
Academia Sinica, Taipei, March 14-17, 2024

Z. Chen, Y. Guo, M. He, SL, to appear

# Outline

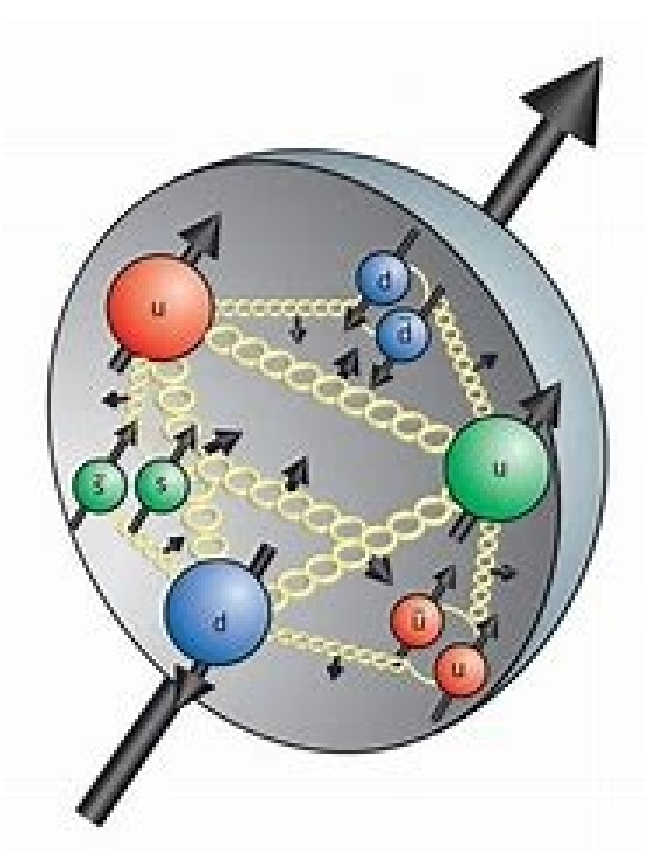
- ◆ Uniqueness of spin physics in heavy ion collisions
- ◆ Difference between spin polarization and spin alignment
- ◆ Spin alignment of  $\phi$  and  $J/\Psi$
- ◆ Effective theory of charmonium
- ◆ Spin dependent damping rate
- ◆ Heavy ion phenomenology
- ◆ Conclusion and outlook

# Spintronics in condensed matter physics



Bader+Parkin  
ARCMP 2010

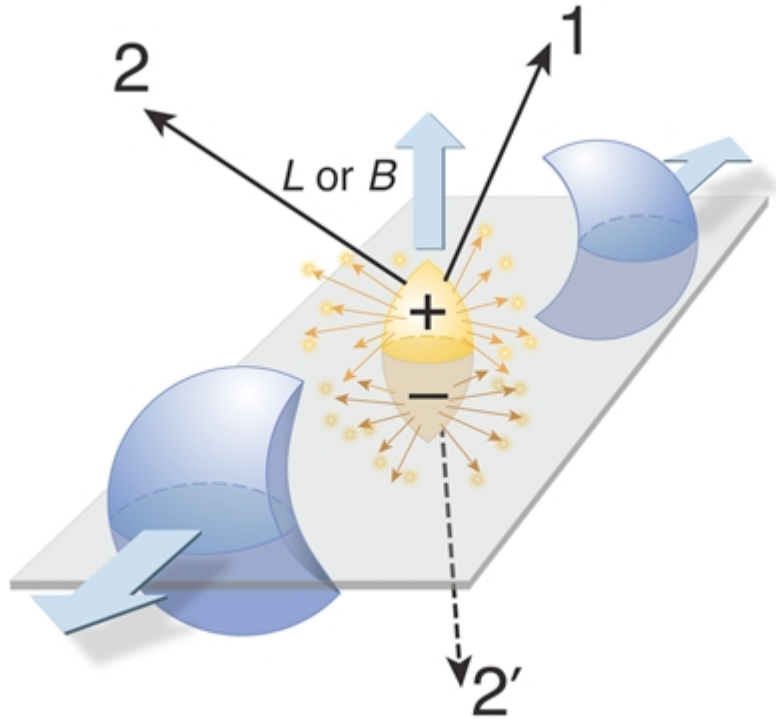
# Spin in particle physics



Proton spin composition  
(1988-now)

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + L_q + \Delta G + L_g$$

# Spin polarization (alignment) in HIC



$$L_{ini} \sim 10^5 \hbar \rightarrow S_{final}$$

Liang, Wang, PRL 2005, PLB 2005

Spin polarization observed in multiple final particles ( $\Lambda$ ,  $\phi$ ,  $J/\Psi$ ) as messengers, probe different aspects of the QCD medium

Explorations of spin polarization (alignment) in HIC just begin!

Talks by A.-h. Tang,  
S. Lim

# Difference between spin polarization and alignment

Spin polarization: approx **conserved**,  
sum of parton polarization from medium,  
**insensitive to interaction**

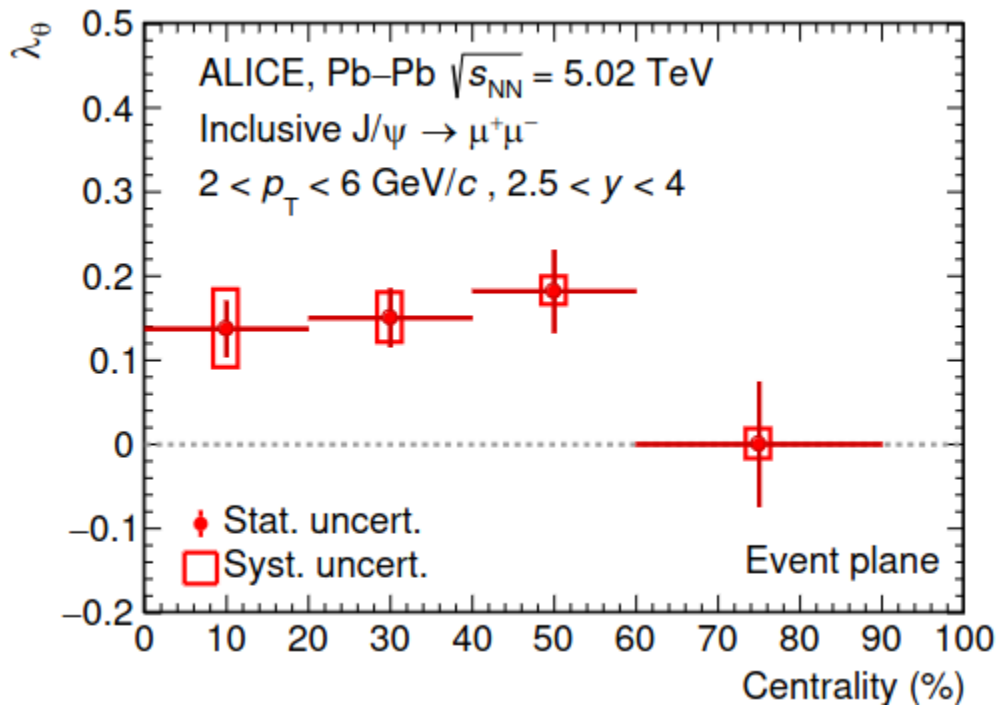
Vorticity field  
EM field  
Other hydro gradient field

Spin alignment: **not conserved**, origin  
complicated, **sensitive to interaction**

Vector meson field fluctuation  
Glasma field fluctuation  
Vorticity field  
EM field  
Fragmentation

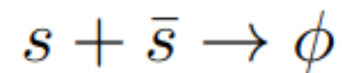
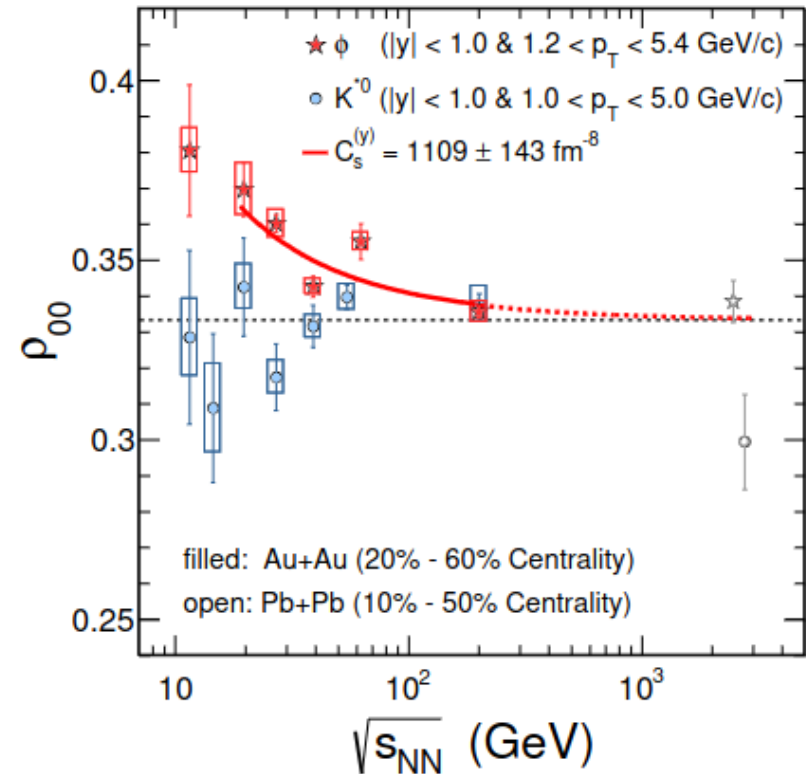
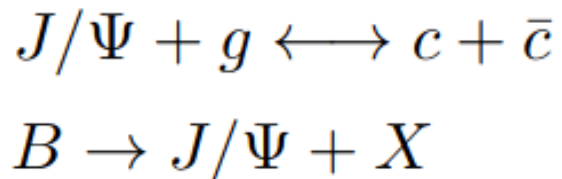
Talks by Q. Wang, X.-L. Sheng, L.  
Oliva, K. Avdhes, H. Kim

# Spin alignment of $J/\Psi$ vs $\phi$



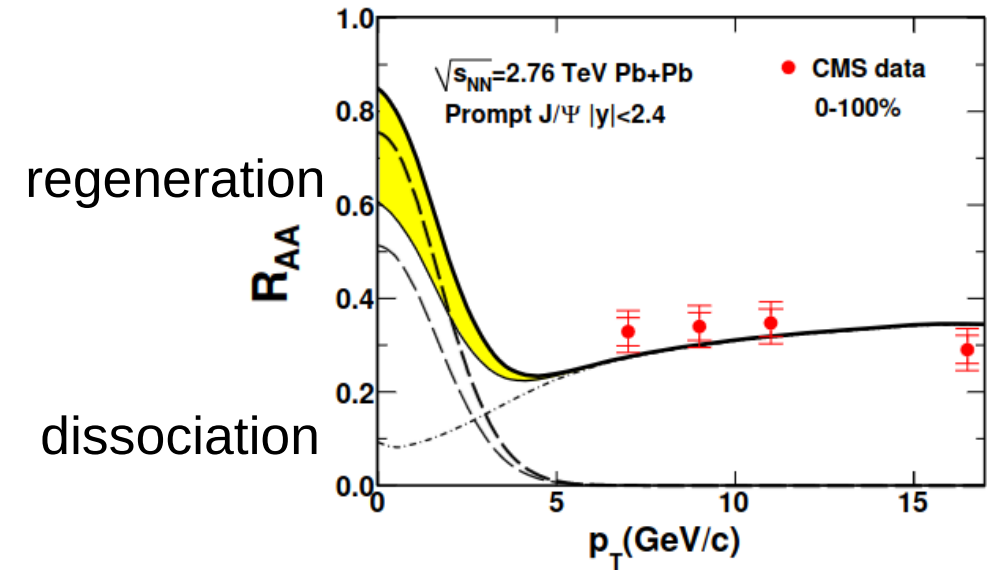
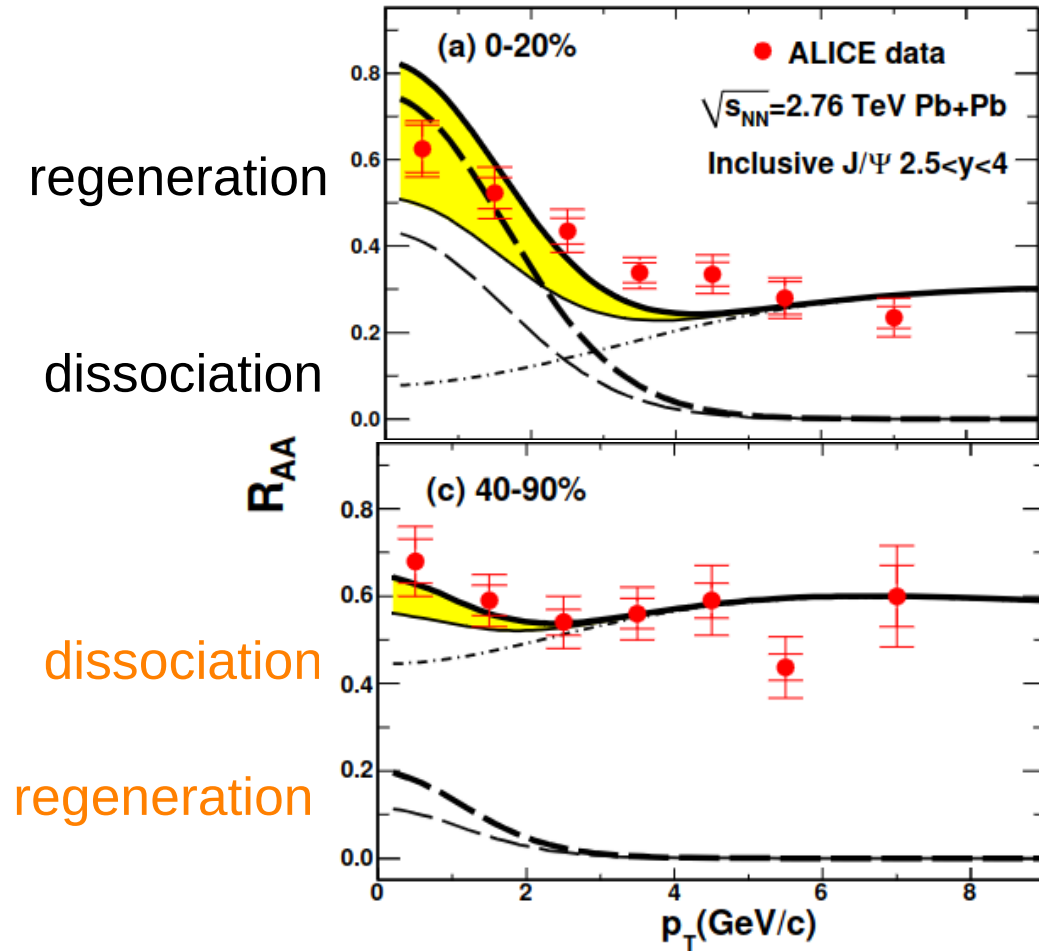
$\rho_{00} < \frac{1}{3}$   
 opposite to  $\phi$

ALICE, PRL 2023  
 STAR, Nature 2023



Talks by A.-h. Tang,  
 S. Lim

# $J/\Psi$ production mechanism at forward rapidity



At LHC energy, regeneration important at central collision, less so at peripheral collision, dissociation significant



# $J/\Psi$ spin alignment from polarized damping

Focus on dissociation of charmonium produced in hard scattering

$J/\Psi$  S-wave spin triplet  $S = 1, L = 0$

$$p^\mu \partial_\mu f_i = -C_i f_i + \cancel{D_i} \quad i: \text{spin triplet label}$$

disso    regen

Spin dependent (polarized) damping rate leads to spin alignment

$$\rho_{00} < \frac{1}{3} \text{ requires } C_0 > \frac{1}{3} (C_0 + C_+ + C_-)$$

# Quantum mechanical description of charmonium

$$H_{\text{eff}} = H_0 + H_I,$$

Yan, PRD 1980, Kuang-Yan,  
PRD 1981

$$H_0 = \frac{\vec{p}^2}{m_Q} + V_1(|\vec{r}|) + \sum_a \frac{\lambda^a}{2} \frac{\bar{\lambda}^a}{2} V_2(|\vec{r}|),$$

rest frame of  $J/\Psi$

color singlet      color octet

$$H_I = Q^a A_0^a(t, \vec{0}) - \vec{d}^a \cdot \vec{E}^a(t, \vec{0}) - \vec{m}^a \cdot \vec{B}^a(t, \vec{0}) + \dots$$

Spin dependent interaction

$$\vec{d}^a = \frac{1}{2} g_s \vec{r} \left( \frac{\lambda^a}{2} - \frac{\bar{\lambda}^a}{2} \right),$$

chromo-electric dipole moment

$$\vec{m}^a = \frac{g_s}{2m_Q} \left( \frac{\lambda^a}{2} - \frac{\bar{\lambda}^a}{2} \right) \left( \frac{\vec{\sigma}}{2} - \frac{\vec{\sigma}'}{2} \right)$$

chromo-magnetic dipole moment

# Cross sections from chromo-electric interaction

$$\sigma_{E_1, \text{Coulomb}}^{g+J/\psi \rightarrow c+\bar{c}}(E_g) = \frac{2^7}{9} g_s^2 \frac{\epsilon_B^{5/2} (E_g - \epsilon_B)^{3/2}}{m_Q E_g^5}, \quad c\bar{c} \quad S=1, L=1$$

$$\propto |\langle (c\bar{c})_8, \vec{p} | \vec{r} | J/\psi \rangle|^2,$$

Peskin, NPB 1979, Bhanot-  
Peskin, NPB 1979  
Chen-He, PRC 2017

Spin independent interaction

# Cross sections from chromo-magnetic interaction

$$\sigma_{M_1, \text{Coulomb}}^{g+J/\psi \rightarrow c+\bar{c}}(E_g) = \frac{2^3}{3} g_s^2 \frac{\epsilon_B^{5/2}}{m_Q^2} \frac{(E_g - \epsilon_B)^{1/2}}{E_g^3}. \quad c\bar{c} \quad S=0, L=0$$

$$\propto |\langle (c\bar{c})_8 | \left( \frac{\vec{\sigma}}{2} - \frac{\vec{\sigma}'}{2} \right) \cdot (\vec{k} \times \vec{\epsilon}_{k\lambda}) | J/\psi \rangle|^2$$

Peskin, NPB 1979, Bhanot-  
Peskin, NPB 1979  
Chen-He, PRC 2017

Spin dependent interaction

$$\left| \left\langle \frac{\uparrow\downarrow - \downarrow\uparrow}{\sqrt{2}} \left| \left( \frac{\vec{\sigma}}{2} - \frac{\vec{\sigma}'}{2} \right) \cdot \vec{B} \right| \uparrow\uparrow \right\rangle \right|^2 = \left| \left\langle \frac{\uparrow\downarrow - \downarrow\uparrow}{\sqrt{2}} \left| \left( \frac{\vec{\sigma}}{2} - \frac{\vec{\sigma}'}{2} \right) \cdot \vec{B} \right| \downarrow\downarrow \right\rangle \right|^2 = \frac{B_\perp^2}{2}$$

$$\left| \left\langle \frac{\uparrow\downarrow - \downarrow\uparrow}{\sqrt{2}} \left| \left( \frac{\vec{\sigma}}{2} - \frac{\vec{\sigma}'}{2} \right) \cdot \vec{B} \right| \frac{\uparrow\downarrow - \downarrow\uparrow}{\sqrt{2}} \right\rangle \right|^2 = B_\parallel^2 \quad \parallel, \perp \text{ defined w.r.t quantization axis } n$$

$$B_n^2 \sim \sum_\lambda \left| (\vec{k}' \times \vec{\epsilon}_{k'\lambda}) \cdot \hat{n}' \right|^2 = k'_i k'_j (\delta_{ij} - n'_i n'_j)$$

# Assumptions and simplifications

- ◆ Evolution of  $J/\Psi$  only
- ◆ Initial condition : unpolarized  $J/\Psi$  produced by hard scattering
- ◆ Ignore regeneration, only dissociation
- ◆ Spin dependent damping rate in QGP leads to spin alignment

from particle effect

Vector meson field fluctuation

Glasma field fluctuation

Vorticity field

EM field

Fragmentation

from field fluctuation

from mean field

# Boltzmann equation in Bjorken flow

$$p^\mu \partial_\mu f_i = -C_i f_i \quad C_i = C^E + C_i^B$$

In Bjorken flow  $C^E = C^E(\tau, p), \quad C_i^B = C_i^B(\tau, p, n)$

Approx boost invariant solution  $E \rightarrow \infty$

$$f(\tau, \eta, y, p_T) = \frac{\tau_0}{\tau} \bar{f}(\tau, y, p_T) \delta(\eta - y) \quad \text{Zhu-Zhuang-Xu, PLB 2005}$$

$J/\Psi$  produced at collision point dissociation changes number, not momentum

$$\bar{f}(\tau, y, p_T) = \exp\left(-\int_{\tau_0}^{\tau} \frac{d\tau'}{\tau_R^i(\tau')}\right) \bar{f}_0(\tau_0, y, p_T) \quad \frac{1}{\tau_R^i} = \frac{C^E}{p \cdot u} + \frac{C_i^B}{p \cdot u}$$

# Spin alignment

$$f^i(\tau, y, p_T) \simeq \exp\left(-\int_{\tau_0}^{\tau} d\tau' \frac{C^E}{p \cdot u}\right) \exp\left(-\int_{\tau_0}^{\tau} d\tau' \frac{C_i^B}{p \cdot u}\right) \bar{f}_0(\tau_0, y, p_T)$$

$$\rho_{00} - \frac{1}{3} = \frac{f^0}{f^0 + f^- + f^+} - \frac{1}{3} \simeq -\frac{1}{3} \int_{\tau_0}^{\tau} \frac{C_0^B d\tau'}{p \cdot u} + \frac{1}{3} \int_{\tau_0}^{\tau} \frac{d\tau' \bar{C}^B}{p \cdot u}$$

Only chromo-magnetic damping factor survives

$$C_0^B \propto k'_i k'_j (\delta_{ij} - n'_i n'_j)$$

$$C_0^B + C_+^B + C_-^B \propto 2k'^2$$

isotropic  $k'_i k'_j \rightarrow \frac{1}{3} k'^2 \delta_{ij}$

alignment: anisotropic collision geometry

# Spin dependent damping: limit 1

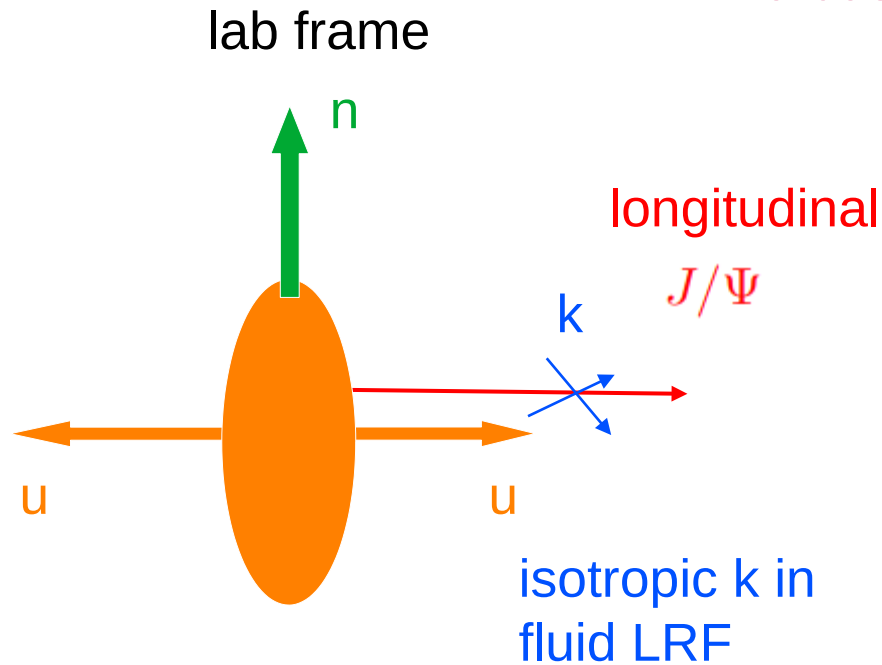
$$p^\mu \partial_\mu f_i = -C_i f_i$$

$$C_0^B \propto k'_i k'_j (\delta_{ij} - n'_i n'_j)$$

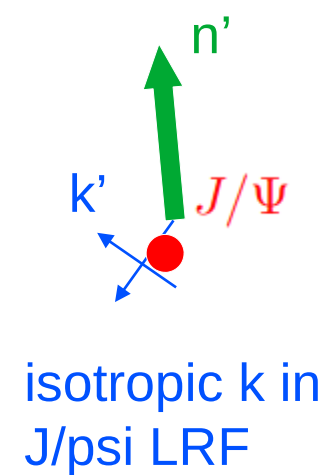
$$C_0^B + C_+^B + C_-^B \propto 2k'^2$$

$$p_T \rightarrow 0$$

No boost



$J/\Psi$  rest frame



$$k'_i k'_j \rightarrow \frac{1}{3} k'^2 \delta_{ij}$$

$$C_0^B \rightarrow \bar{C}^B$$

$$\rho_{00} \rightarrow \frac{1}{3}$$



# Spin dependent damping: limit 2

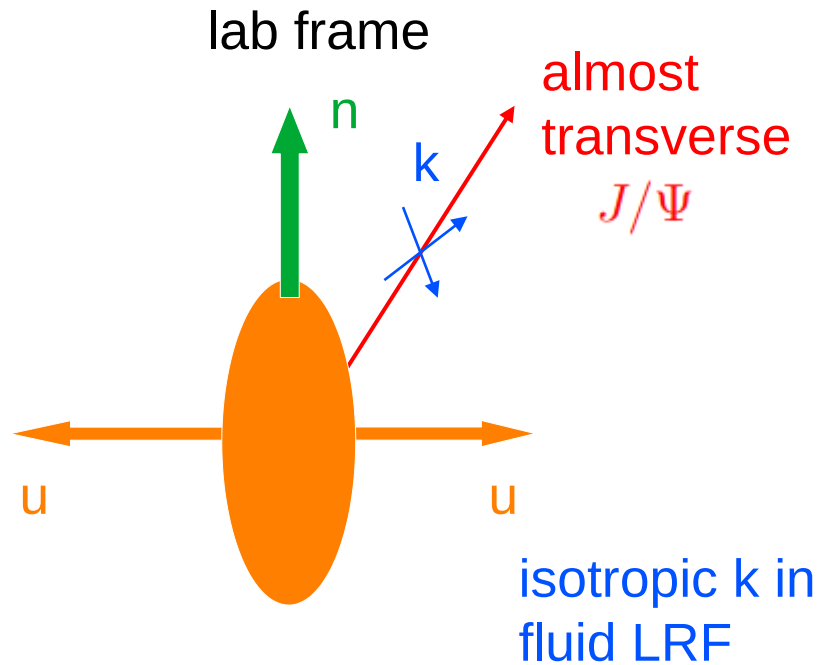
$$p^\mu \partial_\mu f_i = -C_i f_i$$

$$C_0^B \propto k'_i k'_j (\delta_{ij} - n'_i n'_j)$$

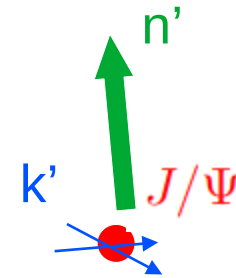
$$C_0^B + C_+^B + C_-^B \propto 2k'^2$$

$$p_T \rightarrow \infty$$

transverse boost



$J/\Psi$  rest frame



$$\langle k'_i k'_j \rangle_{\hat{p}} \rightarrow \frac{1}{2} k'^2 \delta_{ij}$$

$$C_0^B < \bar{C}^B$$

$$\rho_{00} > \frac{1}{3}$$

$k$  approx transverse in  $J/\psi$  LRF

# Frame & quantization axis

$$p^\mu \partial_\mu f_i = -C_i f_i$$

Lorentz invariant

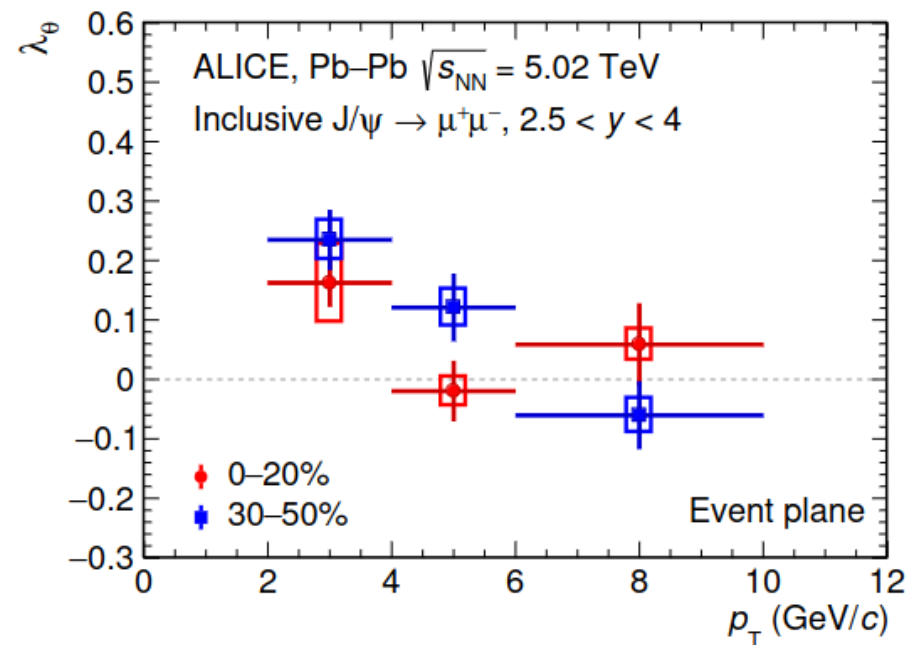
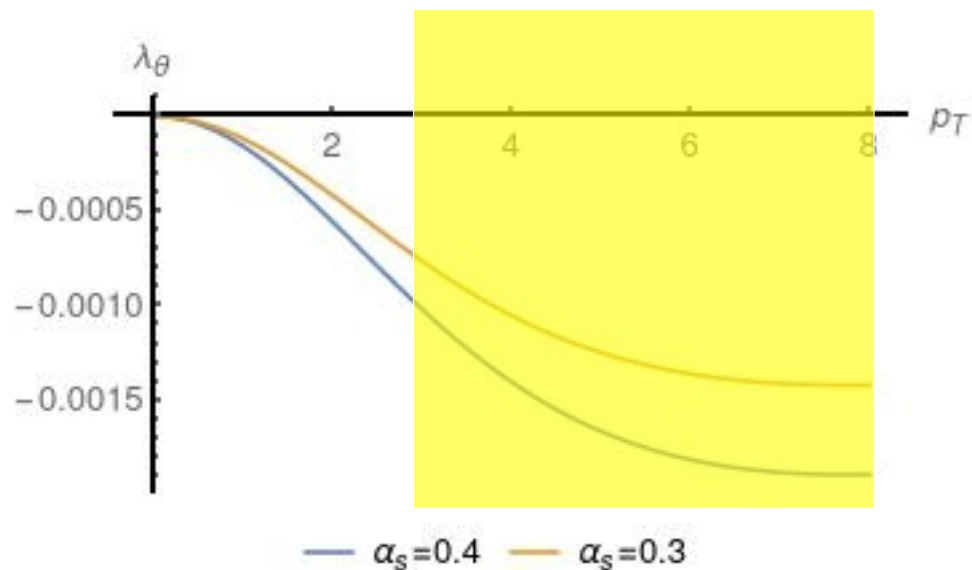
$$\rho_{00} - \frac{1}{3} = \frac{f^0}{f^0 + f^- + f^+} - \frac{1}{3}$$

frame independent  
quantization axis dependent

$$\rho_{00} - \frac{1}{3} = \frac{1}{3} A \left[ \frac{1}{3} + \frac{(-u \cdot n + \frac{p \cdot u}{m} \frac{p \cdot n}{m})^2}{(\frac{p \cdot n}{m})^2 + 1} - \frac{1}{3} \left( \frac{p \cdot u}{m} \right)^2 \right]$$

expressed in lab frame

# Spin alignment



- non-monotonic  $p_T$  dependence
- rapidity independent
- Coulombic binding

$$f(\tau, \eta, y, p_T) = \frac{\tau_0}{\tau} \bar{f}(\tau, y, p_T) \delta(\eta - y)$$

$$\frac{g^2 T_0^{1/2} \epsilon_B^{5/2}}{m_Q^2}$$

# Conclusion

- ◆ Possible mechanism of  $J/\Psi$  spin alignment from particle effect
- ◆ Interplay of spin-chromo-magnetic coupling and anisotropic flow leads to spin dependent damping
- ◆ Dissociation only gives  $\rho_{00} > \frac{1}{3}$

# Outlook

- ◆  $J/\Psi$  regeneration to give non-trivial momentum dependence
- ◆ QGP effect on formation of  $J/\Psi$
- ◆ Feed down from excited states

Thank you!